R4ds Chapter 5 Data Transformation Yuqing Xue Personal Note

Yuqing Xue

October 22, 2017

The following personal code and notes are based on the materials from Hadley Wickham's 'R for Data Science', Chapter 5. http://r4ds.had.co.nz/transform.html#introduction-2

- 5.1 Introduction
- 5.2 Filter
- 5.2.4 Exercises
- 5.3 Arrange
- 5.3.1 Exercises
- 5.4 Select
- 5.4.1 Exercises
- 5.5 Mutate
- 5.5.1 Useful Creation Functions
- 5.5.2 Exercises
- 5.6 Summarise
- 5.6.1 Combining multiple operations with the pipe
- 5.6.3 Counts
- 5.6.4 Useful Summary Functions
- 5.6.5 Grouping by multiple variables
- 5.6.6 Ungrouping

5.1 Introduction

nycflights13

```
## # A tibble: 336,776 x 19
       year month
                     day dep_time sched_dep_time dep_delay arr_time
##
      <int> <int> <int>
                                                       <dbl>
                            <int>
                                            <int>
                                                                <int>
       2013
## 1
                1
                       1
                              517
                                              515
                                                           2
                                                                  830
## 2
       2013
                1
                       1
                              533
                                              529
                                                           4
                                                                  850
       2013
                                                           2
## 3
                1
                       1
                              542
                                              540
                                                                  923
## 4
       2013
                1
                       1
                              544
                                              545
                                                          -1
                                                                 1004
```

```
## 5
       2013
                 1
                       1
                              554
                                               600
                                                          -6
                                                                   812
## 6
       2013
                       1
                              554
                                               558
                                                          -4
                                                                   740
                 1
## 7
       2013
                       1
                              555
                                               600
                                                          -5
                                                                   913
## 8
       2013
                                               600
                                                          -3
                                                                   709
                       1
                              557
                 1
## 9
       2013
                 1
                       1
                              557
                                               600
                                                          -3
                                                                   838
## 10 2013
                       1
                              558
                                               600
                                                          -2
                                                                   753
                 1
## # ... with 336,766 more rows, and 12 more variables: sched arr time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
## #
       origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>
5.2 Filter
Explore, try %in%
jan1 <- filter(flights, month == 1, day == 1)
nov_and_dec = filter(flights, month == 11 | month == 12)
## A useful short-hand for this problem is x %in% y. This will select every row where x is one of the v
nov_dec <- filter(flights, month %in% c(11, 12))</pre>
NYCtoSF <-
  flights %>%
    filter(dest %in% c("SFO", "OAK", "SJC")) %>%
      select(year, month, day, carrier, origin, dest, air_time)
## # A tibble: 13,972 x 7
##
       year month
                     day carrier origin dest air_time
##
      <int> <int> <int>
                           <chr>
                                  <chr> <chr>
                                                   <dbl>
## 1
       2013
                              UA
                                     EWR
                                           SFO
                                                     361
                 1
                       1
## 2
       2013
                 1
                       1
                              UA
                                     JFK
                                           SFO
                                                     366
## 3
       2013
                       1
                              DL
                                     JFK
                                           SFO
                                                     362
                 1
## 4
       2013
                 1
                       1
                              VX
                                     JFK
                                           SFO
                                                     356
       2013
## 5
                 1
                       1
                              В6
                                     JFK
                                           SFO
                                                     350
## 6
       2013
                 1
                       1
                              AA
                                     JFK
                                           SFO
                                                     378
## 7
                                                     373
       2013
                       1
                              UA
                                     EWR
                                           SFO
                 1
## 8
       2013
                                     JFK
                                           SFO
                                                     369
                 1
                       1
                              UA
## 9
       2013
                                     EWR
                                           SF<sub>0</sub>
                                                     357
                       1
                              UA
                 1
```

```
## # ... with 13,962 more rows

NYCtoSF2 <-
flights %>%
  filter(dest == "SFO" | dest == "OAK" | dest == "SJC") %>%
    select(year, month, day, carrier, origin, dest, air_time)

NYCtoSF2
```

389

SF₀

JFK

AA

```
## # A tibble: 13,972 x 7
       year month
                      day carrier origin dest air time
##
      <int> <int> <int>
                             <chr>
                                    <chr> <chr>
                                                     <dbl>
## 1
       2013
                  1
                        1
                                UA
                                       EWR
                                              SF<sub>0</sub>
                                                        361
## 2
       2013
                 1
                        1
                                UA
                                       JFK
                                             SFO
                                                       366
## 3
       2013
                  1
                        1
                                DL
                                       JFK
                                             SF0
                                                       362
## 4
       2013
                                VX
                                       JFK
                                             SFO
                                                       356
                        1
                  1
```

10 2013

1

1

```
350
## 5
        2013
                    1
                                    В6
                                            JFK
                                                   SFO
## 6
        2013
                           1
                                    AA
                                            JFK
                                                   SFO
                                                               378
                    1
## 7
        2013
                           1
                                    UA
                                            EWR
                                                   SF<sub>0</sub>
                                                               373
        2013
## 8
                           1
                                    UA
                                            JFK
                                                   SFO
                                                               369
                    1
## 9
        2013
                           1
                                    UA
                                            EWR
                                                   SFO
                                                               357
## 10 2013
                           1
                                                               389
                    1
                                    AA
                                            JFK
                                                   SF<sub>0</sub>
## # ... with 13,962 more rows
```

H.W. As well as & and |, R also has && and ||. Don't use them here! You'll learn when you should use

- 5.2.4 Exercises
- 1. Find all flights that
- 1.1 Had an arrival delay of two or more hours
- 1.2. Flew to Houston (IAH or HOU)
- 1.3. Were operated by United, American, or Delta
- 1.4. Departed in summer (July, August, and September)
- 1.5. Arrived more than two hours late, but didn't leave late
- 1.6. Were delayed by at least an hour, but made up over 30 minutes in flight
- 1.7. Departed between midnight and 6am (inclusive)

```
Ex1.1 <-
flights %>%
filter(arr_delay >= 120) %>%
    arrange(desc(arr_delay)) %>%
    select(month, day, carrier, origin, dest, dep_delay, arr_delay)
Ex1.1
```

```
## # A tibble: 10,200 x 7
##
      month
                day carrier origin dest dep_delay arr_delay
##
       <int> <int>
                      <chr>
                              <chr> <chr>
                                                 <dbl>
                                                            <dbl>
## 1
                                 JFK
                                       HNL
                                                  1301
                                                             1272
           1
                  9
                          HA
## 2
           6
                 15
                          MQ
                                 JFK
                                       CMH
                                                  1137
                                                             1127
## 3
           1
                 10
                          MQ
                                EWR
                                       ORD
                                                  1126
                                                             1109
## 4
           9
                 20
                          AA
                                 JFK
                                       SF<sub>0</sub>
                                                  1014
                                                             1007
## 5
           7
                 22
                                 JFK
                                       CVG
                          MQ
                                                  1005
                                                              989
## 6
           4
                 10
                          DL
                                 JFK
                                       TPA
                                                   960
                                                              931
           3
                 17
                                LGA
## 7
                          DL
                                       MSP
                                                   911
                                                              915
## 8
           7
                 22
                          DL
                                LGA
                                                   898
                                                              895
                                       ATL
## 9
          12
                  5
                          AA
                                EWR
                                       MIA
                                                   896
                                                              878
                                                   878
## 10
           5
                  3
                          MQ
                                 EWR
                                       ORD
                                                              875
## # ... with 10,190 more rows
```

```
Ex1.2 = filter(flights, dest %in% c("IAH","HOU"))
Ex1.3 = filter(flights, carrier %in% c("UA","AA","DL"))
Ex1.4 = filter(flights, month %in% c(7,8,9))

Ex1.5 = filter(flights, arr_delay >= 120 & dep_delay <= 0 )
Ex1.6 = filter(flights, dep_delay >= 60 & dep_delay - arr_delay >= 30)
Ex1.7 = filter(flights, dep_time <= 600)</pre>
```

2. Another useful dplyr filtering helper is between(). What does it do? Can you use it to simplify the code needed to answer the previous challenges?

```
?between
Ex1.4b = filter(flights, between(month, 7, 9))
```

3. How many flights have a missing dep_time? What other variables are missing? What might these rows represent?

```
sum(is.na(flights$dep_time)) # 8255
## [1] 8255
flights_missing_dep_time <- flights %>% filter(is.na(dep_time))
flights_missing_dep_time
## # A tibble: 8,255 x 19
##
       year month
                     day dep_time sched_dep_time dep_delay arr_time
      <int> <int> <int>
                                                      <dbl>
##
                            <int>
                                            <int>
                                                                <int>
## 1
       2013
                       1
                               NA
                                             1630
                                                         NA
                                                                   NA
                1
## 2
       2013
                1
                       1
                               NA
                                             1935
                                                         NA
                                                                   NA
## 3
       2013
                1
                       1
                               NA
                                             1500
                                                          NA
                                                                   NA
## 4
       2013
                1
                       1
                               NA
                                              600
                                                          NA
                                                                   NA
                       2
## 5
       2013
                                                          NA
                                                                   NA
                1
                               NA
                                             1540
       2013
                       2
## 6
                               NA
                                             1620
                                                          NA
                                                                   NA
                1
                       2
## 7
       2013
                1
                               NA
                                             1355
                                                          ΝA
                                                                   NA
                       2
## 8
       2013
                1
                               NA
                                             1420
                                                          NA
                                                                   NA
## 9
       2013
                       2
                1
                               NA
                                             1321
                                                          NA
                                                                   NA
## 10 2013
                       2
                               NA
                                             1545
                1
                                                         NA
                                                                   NA
## # ... with 8,245 more rows, and 12 more variables: sched_arr_time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
## #
       origin <chr>, dest <chr>, air time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>
flights_cancelled <- flights %>%
  filter(is.na(dep_time) & is.na(dep_delay) & is.na(arr_time) & is.na(arr_delay) & is.na(arr_time))
# same 8255 flights
```

Beside dep_time, dep_delay, arr_time, arr_delay and air_time are also missing, for all 8255 flights. One possible explanation for it is that those flights were cancelled.

- 4. Why is NA ^ 0 not missing? Why is NA | TRUE not missing? Why is FALSE & NA not missing? Can you figure out the general rule? (NA * 0 is a tricky counterexample!)
- NA ^ 0 returns 1. Any number to the power of 0 is 1, whether the number is missing or not does not matter.

NA | TRUE returns TRUE, since the | operator returns TRUE if either of the terms are TRUE. In this case, the right half is TRUE, so the whole expression will always return TRUE.

FALSE & NA returns FALSE, because operator & returns TRUE when both terms are true. The left half is FALSE, so the whole expression returns FALSE despite the NA on the right half.

```
NA * 0
```

[1] NA

NA * 0 returns 0, which may rendered the general rule we discovered from the previous not definite: if NA represent a value that is Inf, and we know Inf * 0 should not be a number, i.e., NaN.

5.3 Arrange

arrange() works similarly to filter() except that instead of selecting rows, it changes their order. It takes a data frame and a set of column names (or more complicated expressions) to order by. If you provide more than one column name, each additional column will be used to break ties in the values of preceding columns:

arrange(flights, year, month, day)

```
## # A tibble: 336,776 x 19
##
       year month
                     day dep_time sched_dep_time dep_delay arr_time
##
      <int> <int> <int>
                             <int>
                                             <int>
                                                        <dbl>
                                                                  <int>
## 1
       2013
                 1
                        1
                               517
                                                515
                                                             2
                                                                    830
##
       2013
                 1
                        1
                               533
                                                529
                                                             4
                                                                    850
## 3
                                                             2
       2013
                        1
                                                540
                 1
                               542
                                                                    923
## 4
       2013
                 1
                        1
                               544
                                                545
                                                            -1
                                                                   1004
       2013
## 5
                 1
                        1
                               554
                                                600
                                                            -6
                                                                    812
## 6
       2013
                 1
                        1
                               554
                                                558
                                                            -4
                                                                    740
## 7
       2013
                        1
                                                            -5
                 1
                               555
                                                600
                                                                    913
## 8
       2013
                        1
                               557
                                                600
                                                            -3
                                                                    709
                 1
## 9
       2013
                        1
                               557
                                                600
                                                            -3
                                                                    838
                 1
## 10
       2013
                 1
                        1
                               558
                                                600
                                                            -2
                                                                    753
## # ... with 336,766 more rows, and 12 more variables: sched_arr_time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
       origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>
arrange(flights, desc(arr_delay))
```

A tibble: 336.776 x 19

## # K CIDDIE. 550,776 X 15								
##		year	${\tt month}$	day	dep_time	${\tt sched_dep_time}$	<pre>dep_delay</pre>	arr_time
##		<int></int>	<int></int>	<int></int>	<int></int>	<int></int>	<dbl></dbl>	<int></int>
##	1	2013	1	9	641	900	1301	1242
##	2	2013	6	15	1432	1935	1137	1607
##	3	2013	1	10	1121	1635	1126	1239
##	4	2013	9	20	1139	1845	1014	1457
##	5	2013	7	22	845	1600	1005	1044
##	6	2013	4	10	1100	1900	960	1342
##	7	2013	3	17	2321	810	911	135
##	8	2013	7	22	2257	759	898	121
##	9	2013	12	5	756	1700	896	1058

```
878
## 10 2013
                5
                       3
                             1133
                                             2055
                                                                 1250
## # ... with 336,766 more rows, and 12 more variables: sched_arr_time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
       origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>,
       minute <dbl>, time_hour <dttm>
df \leftarrow tibble(x = c(5, 2, NA))
arrange(df, x)
## # A tibble: 3 x 1
##
##
     <dbl>
## 1
         2
## 2
         5
## 3
        NA
```

In this way, x then becomes the column name of the tibble df.

5.3.1 Exercise

1. How could you use arrange() to sort all missing values to the start? (Hint: use is.na()).

It seems that R recognized FALSE as 0 and TRUE as 1, which makes FALSE is less than TRUE, hence can be sorted to the start use arrange.

2. Sort flights to find the most delayed flights. Find the flights that left earliest.

```
colnames(flights)
```

```
[1] "year"
                          "month"
                                             "day"
                                                               "dep_time"
##
    [5] "sched_dep_time"
                          "dep_delay"
                                             "arr_time"
                                                               "sched_arr_time"
                           "carrier"
                                             "flight"
                                                               "tailnum"
   [9] "arr_delay"
## [13] "origin"
                          "dest"
                                             "air_time"
                                                               "distance"
## [17] "hour"
                          "minute"
                                             "time_hour"
flights %>%
  arrange(desc(arr_delay))
```

```
## # A tibble: 336,776 x 19
##
       year month
                     day dep_time sched_dep_time dep_delay arr_time
##
      <int> <int> <int>
                             <int>
                                             <int>
                                                        dbl>
## 1
       2013
                       9
                               641
                                               900
                                                         1301
                                                                  1242
                 1
## 2
       2013
                 6
                      15
                              1432
                                              1935
                                                         1137
                                                                  1607
## 3
       2013
                      10
                 1
                              1121
                                              1635
                                                         1126
                                                                  1239
## 4
       2013
                 9
                      20
                              1139
                                              1845
                                                         1014
                                                                  1457
                 7
## 5
       2013
                      22
                               845
                                              1600
                                                         1005
                                                                  1044
      2013
                              1100
## 6
                      10
                                              1900
                                                         960
                                                                  1342
```

```
## 7
       2013
                 3
                      17
                             2321
                                              810
                                                         911
                                                                   135
## 8
       2013
                7
                      22
                             2257
                                              759
                                                         898
                                                                   121
## 9
       2013
                12
                       5
                              756
                                             1700
                                                         896
                                                                 1058
                5
                       3
                                                                 1250
## 10 2013
                             1133
                                             2055
                                                         878
## # ... with 336,766 more rows, and 12 more variables: sched_arr_time <int>,
       arr delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
       origin <chr>, dest <chr>, air time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>
flights %>%
  arrange(dep_time)
```

```
## # A tibble: 336,776 x 19
##
                      day dep_time sched_dep_time dep_delay arr_time
       year month
##
      <int> <int> <int>
                              <int>
                                              <int>
                                                         <dbl>
                                                                   <int>
                                                            72
## 1
       2013
                       13
                                               2249
                                                                      108
                 1
                                  1
## 2
       2013
                 1
                       31
                                  1
                                               2100
                                                           181
                                                                      124
## 3
       2013
                       13
                                  1
                                               2359
                                                              2
                                                                     442
                11
                                                              2
## 4
       2013
                12
                       16
                                  1
                                               2359
                                                                     447
                                                              2
## 5
       2013
                       20
                12
                                  1
                                               2359
                                                                     430
                                                              2
## 6
       2013
                12
                       26
                                  1
                                               2359
                                                                     437
                                                              2
## 7
       2013
                12
                       30
                                  1
                                               2359
                                                                     441
## 8
       2013
                 2
                       11
                                  1
                                               2100
                                                            181
                                                                     111
## 9
       2013
                 2
                       24
                                  1
                                               2245
                                                            76
                                                                     121
## 10 2013
                 3
                        8
                                  1
                                               2355
                                                              6
                                                                     431
## # ... with 336,766 more rows, and 12 more variables: sched_arr_time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
       origin <chr>, dest <chr>, air time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>
```

which may lead to an idea to create a function:

idea: do all the common topRanking (smallest/largest, variable) and put it on Shiny

3. Sort flights to find the fastest flights.

1

2

EWR

EWR

BDL

BDL

time form needs to be clearer, answer not reliable

Idea: create a variable travelTime to measure the flight time (arr_time - dep_time. Noted that dep_time and arr_time are coded in a form that is intuitive to read and comprehend, but a little harder to make further calculation with, because they're not continuous. A more convenient representation of number of minutes since midnight are yet to be computed. So travelTime are neither real minutes nor hours and minutes like dep_time and arr_time. More details and discussion can be found in exersice 5.5.2 problem 2. http://r4ds.had.co.nz/transform.html#exercises-10).

Tricky: The way how dep_time and arr_time is coded needs a slightly modification.

```
## 5
         EWR
                BDL
                          722
                                          729
                                                    758
                                                                    830
                                                                                 36
                                          725
                                                                    822
                                                                                 36
## 6
         EWR
                BDL
                          718
                                                    754
## 7
         EWR
                BDL
                         1418
                                         1329
                                                   1455
                                                                   1426
                                                                                 37
## 8
                BDL
                                                                                 37
         EWR
                           16
                                         2159
                                                     53
                                                                   2304
## 9
                BDL
                                                                                 37
         EWR
                          717
                                          725
                                                    754
                                                                    822
## 10
         EWR
                BDL
                         1315
                                         1320
                                                   1353
                                                                   1419
                                                                                 38
## # ... with 336,766 more rows
# and the slowest flights
flights %>%
  mutate(travelTime = ifelse(arr_time - dep_time < 0, arr_time + 2400 - dep_time, arr_time - dep_time))</pre>
    select(origin, dest, dep_time, sched_dep_time, arr_time, sched_arr_time, travelTime) %>%
      arrange(desc(travelTime))
## # A tibble: 336,776 x 7
      origin dest dep_time sched_dep_time arr_time sched_arr_time travelTime
##
       <chr> <chr>
                        <int>
                                        <int>
                                                  <int>
                                                                  <int>
                                                                              <dbl>
## 1
         EWR
                ORD
                         1623
                                         1545
                                                   1148
                                                                   1710
                                                                               1925
## 2
         EWR
                DFW
                          959
                                          920
                                                   2129
                                                                   1240
                                                                               1170
## 3
         LGA
                ATL
                         1500
                                         1459
                                                    245
                                                                   1737
                                                                               1145
## 4
         EWR
                LAX
                         1259
                                         1300
                                                   2358
                                                                   1555
                                                                               1099
## 5
         JFK
                BOS
                         2313
                                         2050
                                                   1003
                                                                   2203
                                                                               1090
## 6
         EWR
                GSP
                          653
                                          659
                                                   1704
                                                                    857
                                                                               1051
## 7
         JFK
                          625
                                          630
                                                   1635
                                                                    922
                                                                               1010
                LAX
## 8
         LGA
                ATL
                         1415
                                         1355
                                                     18
                                                                   1617
                                                                               1003
## 9
                DEN
                                                                                982
         LGA
                          755
                                          800
                                                   1737
                                                                   1025
## 10
         JFK
                SLC
                          644
                                          655
                                                   1624
                                                                   1030
                                                                                980
## # ... with 336,766 more rows
flights_Testimate <- flights %>%
  mutate(travelTime = ifelse(arr_time - dep_time < 0, arr_time + 2400 - dep_time, arr_time - dep_time))
```

The most unexpected flights, like the one from EWR to ORD that took 19 hours 25 minutes, can be spotted and further investigated.

4. Which flights travelled the longest? Which travelled the shortest?

Idea: sort variable distance

3

4

EWR

EWR

BDL

BDL

1203

722

1153

730

1238

758

1250

830

35

36

```
# The longest flights
flights_Testimate %>%
    select(carrier:distance, travelTime) %>%
    arrange(desc(distance))

## # A tibble: 336,776 x 8
## carrier flight tailnum origin dest air_time distance travelTime
## <chr> <int> <chr> <chr> <chr> <chr> <chr> <chr> <dbl> <dbl> <dbl> <dbl>
```

```
## 8
           HA
                   51 N389HA
                                  JFK
                                         HNL
                                                  645
                                                           4983
                                                                        603
## 9
           HΑ
                   51 N384HA
                                  JFK
                                        HNL
                                                  640
                                                           4983
                                                                        601
## 10
           HA
                   51
                       N388HA
                                  JFK
                                        HNL
                                                  633
                                                           4983
                                                                        590
## # ... with 336,766 more rows
# The longest flight where destination is not HNL
flights Testimate %>%
  select(carrier:distance, travelTime) %>%
    filter(dest != 'HNL') %>%
      arrange(desc(distance))
## # A tibble: 336,069 x 8
      carrier flight tailnum origin dest air_time distance travelTime
##
##
        <chr> <int>
                        <chr>
                                <chr> <chr>
                                                <dbl>
                                                          <dbl>
                                                                      <dbl>
## 1
                                                                        325
           UA
                  887
                       N587UA
                                  EWR
                                         ANC
                                                  418
                                                           3370
## 2
                  887
                       N572UA
                                                           3370
                                                                        337
           UA
                                  EWR
                                         ANC
                                                  404
## 3
           UA
                  887
                      N567UA
                                  EWR
                                        ANC
                                                  418
                                                           3370
                                                                        385
## 4
                                        ANC
           UA
                  887 N559UA
                                  EWR
                                                  388
                                                           3370
                                                                        289
## 5
           UA
                  887 N572UA
                                  EWR
                                        ANC
                                                  434
                                                           3370
                                                                        388
## 6
           UA
                  887
                      N559UA
                                  EWR
                                        ANC
                                                  411
                                                           3370
                                                                        309
## 7
           UA
                  887 N528UA
                                  EWR
                                        ANC
                                                  404
                                                           3370
                                                                        302
## 8
           UA
                  887 N534UA
                                  EWR
                                        ANC
                                                  428
                                                           3370
                                                                        326
## 9
           UA
                  303 N532UA
                                  JFK
                                         SFO
                                                  366
                                                           2586
                                                                        334
## 10
           DI.
                 1865 N705TW
                                  JFK
                                        SFO
                                                  362
                                                           2586
                                                                        382
## # ... with 336,059 more rows
# Besides HNL and ANC
flights_Testimate %>%
  select(carrier:distance, travelTime) %>%
    filter(dest != 'HNL' & dest != "ANC") %>%
      arrange(desc(distance))
## # A tibble: 336,061 x 8
##
      carrier flight tailnum origin dest air time distance travelTime
##
        <chr>
               <int>
                        <chr>
                                                <dbl>
                                                                      <dbl>
                               <chr> <chr>
                                                          <dbl>
## 1
           UA
                  303 N532UA
                                  JFK
                                         SFO
                                                  366
                                                           2586
                                                                        334
                 1865 N705TW
## 2
           DL
                                  JFK
                                        SF<sub>0</sub>
                                                  362
                                                           2586
                                                                        382
## 3
           VX
                   11 N635VA
                                  JFK
                                         SF<sub>0</sub>
                                                  356
                                                           2586
                                                                        320
## 4
           В6
                                        SFO
                  643 N625JB
                                  JFK
                                                  350
                                                           2586
                                                                        313
## 5
           AA
                   59 N336AA
                                  JFK
                                        SFO
                                                  378
                                                           2586
                                                                        390
                  223 N510UA
## 6
           UA
                                  JFK
                                        SF0
                                                  369
                                                           2586
                                                                        329
## 7
                  179 N325AA
                                  JFK
                                        SF<sub>0</sub>
                                                  389
                                                           2586
                                                                        398
           AA
## 8
           VX
                   23 N625VA
                                  JFK
                                         SF<sub>0</sub>
                                                  363
                                                           2586
                                                                        322
## 9
           UA
                  285 N517UA
                                  JFK
                                         SF<sub>0</sub>
                                                  364
                                                           2586
                                                                        328
## 10
           В6
                  641 N590JB
                                  JFK
                                         SF<sub>0</sub>
                                                  349
                                                           2586
                                                                        311
## # ... with 336,051 more rows
# Besides HNL, ANC and JFK to SFO
flights_Testimate %>%
  select(carrier:distance, travelTime) %>%
    filter(dest != 'HNL' & dest != "ANC" & dest != "SFO") %>%
      arrange(desc(distance))
## # A tibble: 322,730 x 8
##
      carrier flight tailnum origin dest air_time distance travelTime
##
        <chr> <int> <chr> <chr> <chr>
                                                <dbl>
                                                          <dbl>
```

```
## 1
            B6
                    91
                        N523JB
                                    JFK
                                           OAK
                                                     330
                                                              2576
                                                                            312
                    91
## 2
                                           OAK
            B6
                        N646JB
                                    JFK
                                                     328
                                                              2576
                                                                            317
## 3
            B6
                    91
                        N636JB
                                    JFK
                                           OAK
                                                     319
                                                              2576
                                                                            278
## 4
                    91
                        N524JB
                                    JFK
                                           OAK
                                                     351
                                                              2576
                                                                            313
            B6
## 5
            B6
                    91
                        N659JB
                                    JFK
                                           OAK
                                                     351
                                                              2576
                                                                            320
## 6
            B6
                    91
                        N784JB
                                    JFK
                                           OAK
                                                     341
                                                              2576
                                                                            361
## 7
            B6
                    91
                        N517JB
                                    JFK
                                           OAK
                                                     345
                                                              2576
                                                                            358
## 8
            B6
                    91
                        N656JB
                                    JFK
                                           OAK
                                                     353
                                                              2576
                                                                            313
## 9
            B6
                    91
                        N563JB
                                    JFK
                                           OAK
                                                     364
                                                              2576
                                                                            333
## 10
            B6
                    91
                        N705JB
                                    JFK
                                           OAK
                                                     346
                                                              2576
                                                                            365
## # ... with 322,720 more rows
```

The second longest flight is from EWR to ANC. The third one is JFK to SFO, and the forth longest flight within United States is from JFK to OAK.

```
# The shortest flights
flights_Testimate %>%
  select(carrier:distance, travelTime) %>%
    arrange(distance)
## # A tibble: 336,776 x 8
##
      carrier flight tailnum origin
                                       dest air_time distance travelTime
##
        <chr>
                <int>
                        <chr>>
                                <chr>>
                                                <dbl>
                                                          <dbl>
                                                                      <dbl>
                                      <chr>
                          <NA>
## 1
           US
                 1632
                                  EWR
                                        LGA
                                                   NA
                                                             17
                                                                         NA
## 2
           ΕV
                 3833
                       N13989
                                  EWR
                                        PHL
                                                   30
                                                             80
                                                                         95
## 3
                       N14972
           ΕV
                 4193
                                  EWR
                                        PHL
                                                   30
                                                             80
                                                                         93
## 4
           ΕV
                 4502
                       N15983
                                  EWR
                                        PHL
                                                   28
                                                             80
                                                                        108
## 5
           ΕV
                 4645
                       N27962
                                  EWR
                                        PHL
                                                   32
                                                             80
                                                                         90
           ΕV
                 4193
                                                   29
## 6
                       N14902
                                  EWR
                                        PHL
                                                             80
                                                                         86
## 7
           ΕV
                 4619
                       N22909
                                  EWR
                                        PHL
                                                   22
                                                             80
                                                                         99
## 8
           ΕV
                 4619
                       N33182
                                  EWR
                                        PHL
                                                   25
                                                             80
                                                                         88
## 9
           ΕV
                 4619
                                  EWR
                                                   30
                       N11194
                                        PHL
                                                             80
                                                                        177
## 10
           E۷
                 4619
                       N17560
                                  EWR
                                        PHL
                                                   27
                                                             80
                                                                         91
## # ... with 336,766 more rows
flights_Testimate %>%
  filter(distance == 17)
## # A tibble: 1 x 20
##
      year month
                    day dep_time sched_dep_time dep_delay arr_time
##
     <int> <int> <int>
                            <int>
                                            <int>
                                                      <dbl>
                                                                <int>
      2013
                     27
                               NA
                                              106
                                                          NA
## # ... with 13 more variables: sched_arr_time <int>, arr_delay <dbl>,
       carrier <chr>, flight <int>, tailnum <chr>, origin <chr>, dest <chr>,
## #
       air_time <dbl>, distance <dbl>, hour <dbl>, minute <dbl>,
## #
       time_hour <dttm>, travelTime <dbl>
```

5.4 Select

select() can be used to rename variables, but it's rarely useful because it drops all of the variables not explicitly mentioned. Instead, use rename(), which is a variant of select() that keeps all the variables that aren't explicitly mentioned

```
# change tailnum to tail_num
```

```
flights %>%
  rename(tail_num = tailnum)
## # A tibble: 336,776 x 19
##
                     day dep_time sched_dep_time dep_delay arr_time
       year month
##
      <int> <int> <int>
                             <int>
                                             <int>
                                                        <dbl>
                                                                  <int>
## 1
       2013
                 1
                        1
                               517
                                               515
                                                             2
                                                                    830
                                               529
## 2
       2013
                               533
                                                             4
                                                                    850
                 1
                        1
       2013
                                                            2
## 3
                        1
                               542
                                               540
                                                                    923
                 1
## 4
       2013
                               544
                                               545
                                                                   1004
                 1
                        1
                                                            -1
## 5
       2013
                 1
                        1
                               554
                                               600
                                                            -6
                                                                    812
## 6
       2013
                 1
                        1
                               554
                                               558
                                                            -4
                                                                    740
## 7
       2013
                        1
                                               600
                                                            -5
                                                                    913
                 1
                               555
## 8
       2013
                 1
                        1
                               557
                                               600
                                                            -3
                                                                    709
## 9
       2013
                        1
                               557
                                               600
                                                            -3
                                                                    838
                 1
## 10 2013
                 1
                        1
                               558
                                               600
                                                            -2
                                                                    753
## # ... with 336,766 more rows, and 12 more variables: sched_arr_time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tail_num <chr>,
## #
       origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>
```

Nothing changes the original dataset flights_Testimate, which still has that variable named tailnum.

Another option is to use select() in conjunction with the everything() helper. This is useful if you have a handful of variables you'd like to move to the start of the data frame.

Move some main information to the start of the dataframe and keep the rest:

```
flights %>%
  select(carrier:dest, everything())
```

```
## # A tibble: 336,776 x 19
##
      carrier flight tailnum origin dest year month
                                                           day dep time
##
        <chr>
                <int>
                        <chr>>
                               <chr> <chr> <int> <int> <int>
                                                                   <int>
## 1
                 1545 N14228
                                             2013
           UA
                                  EWR
                                        IAH
                                                       1
                                                             1
                                                                     517
## 2
           UA
                1714 N24211
                                 LGA
                                        IAH
                                             2013
                                                             1
                                                                     533
                                                       1
## 3
           AA
                 1141
                      N619AA
                                  JFK
                                        MIA
                                             2013
                                                       1
                                                             1
                                                                     542
## 4
           B6
                 725 N804JB
                                  JFK
                                        BQN
                                             2013
                                                                     544
                                                       1
                                                             1
## 5
           DL
                  461 N668DN
                                 LGA
                                        ATL
                                             2013
                                                                     554
## 6
           UA
                 1696 N39463
                                  EWR
                                        ORD
                                             2013
                                                             1
                                                                     554
                                                       1
## 7
           B6
                  507
                       N516JB
                                  EWR
                                        FLL
                                             2013
                                                             1
                                                                     555
## 8
           ΕV
                 5708
                                                                     557
                       N829AS
                                  LGA
                                        IAD
                                             2013
                                                             1
                                                       1
## 9
           B6
                   79
                       N593JB
                                  JFK
                                        MCO
                                             2013
                                                             1
                                                                     557
## 10
           AA
                  301
                       N3ALAA
                                  LGA
                                        ORD
                                             2013
                                                       1
                                                             1
                                                                     558
     ... with 336,766 more rows, and 10 more variables: sched_dep_time <int>,
## #
       dep_delay <dbl>, arr_time <int>, sched_arr_time <int>,
       arr_delay <dbl>, air_time <dbl>, distance <dbl>, hour <dbl>,
       minute <dbl>, time_hour <dttm>
## #
```

5.4.1 Exercise

- 1.Brainstorm as many ways as possible to select dep_time, dep_delay, arr_time, and arr_delay from flights.
- 1.0. Just list all the variables to select

```
flights %>%
  select(dep_time, dep_delay, arr_time, arr_delay)
## # A tibble: 336,776 x 4
##
      dep_time dep_delay arr_time arr_delay
##
          <int>
                    <dbl>
                              <int>
                                         <dbl>
## 1
            517
                         2
                                830
                                            11
## 2
            533
                         4
                                850
                                            20
## 3
            542
                         2
                                923
                                            33
## 4
            544
                        -1
                               1004
                                           -18
## 5
            554
                        -6
                                812
                                           -25
## 6
            554
                        -4
                                740
                                            12
## 7
            555
                        -5
                                            19
                                913
## 8
            557
                        -3
                                709
                                           -14
## 9
            557
                        -3
                                            -8
                                838
## 10
            558
                        -2
                                753
                                             8
## # ... with 336,766 more rows
1.1. starts_with and ends_with
flights %>%
  select(starts_with("dep"), starts_with("arr"))
## # A tibble: 336,776 x 4
##
      dep_time dep_delay arr_time arr_delay
##
          <int>
                    <dbl>
                              <int>
                                         <dbl>
## 1
            517
                         2
                                830
                                            11
## 2
            533
                         4
                                850
                                            20
## 3
                         2
                                            33
            542
                                923
## 4
            544
                        -1
                               1004
                                           -18
## 5
                                812
                                           -25
            554
                        -6
## 6
            554
                        -4
                                740
                                            12
## 7
            555
                        -5
                                913
                                            19
## 8
            557
                        -3
                                709
                                           -14
## 9
                                            -8
            557
                        -3
                                838
## 10
            558
                        -2
                                753
                                             8
## # ... with 336,766 more rows
flights %>%
  select(ends_with("time"), ends_with("delay")) %>%
    select(-c(starts_with("sched"), starts_with("air")))
## # A tibble: 336,776 x 4
##
      dep_time arr_time dep_delay arr_delay
##
                              <dbl>
          <int>
                   <int>
                                         <dbl>
## 1
            517
                     830
                                   2
                                            11
## 2
                                            20
            533
                     850
                                   4
## 3
            542
                     923
                                   2
                                            33
## 4
            544
                    1004
                                           -18
                                  -1
## 5
            554
                     812
                                  -6
                                           -25
## 6
            554
                     740
                                  -4
                                            12
## 7
                                  -5
            555
                     913
                                            19
## 8
            557
                     709
                                  -3
                                           -14
## 9
            557
                     838
                                  -3
                                            -8
## 10
                                  -2
                                              8
            558
                     753
## # ... with 336,766 more rows
```

1.2. Fancier: contains

```
flights %>% select(dep_time:arr_delay, -c(contains("sched")))
```

```
## # A tibble: 336,776 x 4
##
      dep_time dep_delay arr_time arr_delay
##
          <int>
                     <dbl>
                               <int>
                                          <dbl>
## 1
            517
                         2
                                 830
                                             11
## 2
            533
                         4
                                 850
                                             20
## 3
            542
                         2
                                 923
                                             33
## 4
            544
                        -1
                                1004
                                            -18
## 5
            554
                        -6
                                 812
                                            -25
## 6
            554
                        -4
                                 740
                                             12
## 7
            555
                        -5
                                             19
                                 913
## 8
            557
                        -3
                                 709
                                            -14
## 9
                        -3
                                             -8
            557
                                 838
## 10
            558
                        -2
                                 753
                                              8
## # ... with 336,766 more rows
```

1.3. Start learning matches syntax

flights %>% select(matches("^dep|^arr"))

```
## # A tibble: 336,776 x 4
##
      dep_time dep_delay arr_time arr_delay
##
                     <dbl>
          <int>
                               <int>
                                          <dbl>
## 1
            517
                         2
                                 830
                                             11
## 2
            533
                         4
                                 850
                                             20
## 3
                         2
                                 923
                                             33
            542
## 4
            544
                        -1
                                1004
                                            -18
## 5
                                            -25
            554
                        -6
                                 812
## 6
                        -4
                                 740
                                             12
            554
## 7
            555
                        -5
                                 913
                                             19
## 8
            557
                        -3
                                 709
                                            -14
## 9
            557
                        -3
                                 838
                                             -8
## 10
                        -2
                                              8
            558
                                 753
## # ... with 336,766 more rows
```

2. What happens if you include the name of a variable multiple times in a select() call?

flights %>% select(dep_time, dep_time, dep_time)

```
## # A tibble: 336,776 x 1
##
      dep_time
##
         <int>
## 1
           517
## 2
           533
## 3
           542
## 4
           544
## 5
           554
## 6
           554
## 7
           555
## 8
           557
## 9
           557
## 10
           558
## # ... with 336,766 more rows
```

Just select the variable once despite multiple select call.

3. What does the one_of() function do? Why might it be helpful in conjunction with this vector? vars <- c("year", "month", "day", "dep_delay", "arr_delay")

```
vars <- c("year", "month", "day", "dep_delay", "arr_delay")</pre>
flights %>% select(one of(vars))
## # A tibble: 336,776 x 5
##
       year month
                      day dep_delay arr_delay
##
       <int> <int> <int>
                               <dbl>
                                           <dbl>
## 1
       2013
                                    2
                                              11
                  1
                        1
## 2
       2013
                  1
                        1
                                    4
                                              20
                                    2
                                              33
## 3
       2013
                  1
                        1
## 4
       2013
                  1
                        1
                                   -1
                                             -18
## 5
       2013
                                             -25
                  1
                        1
                                   -6
## 6
       2013
                        1
                                   -4
                                              12
## 7
       2013
                        1
                                   -5
                                              19
                  1
```

4. Does the result of running the following code surprise you? How do the select helpers deal with case by default? How can you change that default?

-14

-8

8

```
select(flights, contains("TIME"))
## # A tibble: 336,776 x 6
##
      dep_time sched_dep_time arr_time sched_arr_time air_time
##
         <int>
                          <int>
                                   <int>
                                                   <int>
                                                             <dbl>
## 1
           517
                            515
                                     830
                                                     819
                                                               227
## 2
           533
                            529
                                                               227
                                     850
                                                     830
## 3
           542
                            540
                                     923
                                                     850
                                                               160
## 4
           544
                            545
                                    1004
                                                     1022
                                                               183
## 5
           554
                            600
                                     812
                                                     837
                                                               116
## 6
           554
                            558
                                     740
                                                     728
                                                               150
## 7
           555
                            600
                                     913
                                                     854
                                                               158
## 8
           557
                            600
                                     709
                                                      723
                                                                53
## 9
           557
                            600
                                     838
                                                     846
                                                               140
## 10
           558
                            600
                                     753
                                                     745
                                                               138
## # ... with 336,766 more rows, and 1 more variables: time_hour <dttm>
select(flights, contains("TIME", ignore.case = FALSE))
```

-3

-3

-2

A tibble: 336,776 x 0

8

9

10

2013

2013

2013

1

1

1

... with 336,766 more rows

1

1

1

contains does not treat argument with case sensitive by default. Use ignore.case = FALSE to cange that setting.

5.5 Add new variables with mutate()

```
flights_sml <- select(flights,
    year:day,</pre>
```

```
ends_with("delay"),
  distance,
  air_time
)
mutate(flights_sml,
  gain = arr_delay - dep_delay,
  speed = distance / air_time * 60
)
## # A tibble: 336,776 x 9
##
       year month
                     day dep_delay arr_delay distance air_time
                                                                              speed
                                                                     gain
                               <dbl>
                                          <dbl>
                                                             <dbl> <dbl>
                                                                              <dbl>
##
      <int> <int> <int>
                                                   <dbl>
## 1
       2013
                 1
                        1
                                   2
                                             11
                                                     1400
                                                                227
                                                                        9 370.0441
## 2
       2013
                                   4
                                             20
                                                     1416
                                                                227
                                                                       16 374.2731
                 1
                        1
## 3
       2013
                        1
                                   2
                                             33
                                                     1089
                                                                160
                                                                       31 408.3750
                 1
                                            -18
## 4
       2013
                                                     1576
                                                                183
                                                                      -17 516.7213
                 1
                        1
                                  -1
## 5
       2013
                                  -6
                                            -25
                                                     762
                                                                      -19 394.1379
                 1
                        1
                                                                116
## 6
       2013
                 1
                        1
                                  -4
                                             12
                                                     719
                                                                150
                                                                       16 287.6000
## 7
       2013
                 1
                        1
                                  -5
                                             19
                                                     1065
                                                                158
                                                                       24 404.4304
                                  -3
## 8
       2013
                        1
                                            -14
                                                      229
                                                                      -11 259.2453
                 1
                                                                 53
## 9
       2013
                        1
                                  -3
                                             -8
                                                      944
                                                                140
                                                                       -5 404.5714
                 1
## 10 2013
                                  -2
                                              8
                                                      733
                                                                       10 318.6957
                 1
                        1
                                                                138
## # ... with 336,766 more rows
```

If you only want to keep the new variables, use transmute():

```
transmute(flights,
  gain = arr_delay - dep_delay,
  hours = air_time / 60,
  gain_per_hour = gain / hours # minutes gain per airtime hour
)
```

```
## # A tibble: 336,776 x 3
##
       gain
                hours gain_per_hour
##
      <dbl>
                 <dbl>
                               <dbl>
## 1
          9 3.7833333
                            2.378855
## 2
         16 3.7833333
                            4.229075
## 3
         31 2.6666667
                           11.625000
## 4
        -17 3.0500000
                           -5.573770
## 5
        -19 1.9333333
                           -9.827586
## 6
         16 2.5000000
                            6.400000
## 7
         24 2.6333333
                            9.113924
## 8
        -11 0.8833333
                          -12.452830
## 9
         -5 2.3333333
                           -2.142857
## 10
         10 2.3000000
                            4.347826
## # ... with 336,766 more rows
```

5.5.1 Useful creation functions

The key property is that the function mutate must be vectorised: it must take a vector of values as input, return a vector with the same number of values as output.

If one parameter is shorter than the other, it will be automatically extended to be the same length. This is most useful when one of the arguments is a single number: air time / 60, hours * 60 + minute, etc.

Ranking: The default gives smallest values the small ranks; use desc(x) to give the largest values the smallest ranks.

```
y <- c(70, 10, 10, NA, 30, 40)
min_rank(y)

## [1] 5 1 1 NA 3 4
min_rank(desc(y)) # order by value, more common

## [1] 1 4 4 NA 3 2</pre>
```

5.5.2 Exercises

1. Currently dep_time and sched_dep_time are convenient to look at, but hard to compute with because they're not really continuous numbers. Convert them to a more convenient representation of number of minutes since midnight.

```
Modular arithmetic: %/% (integer division) and %% (remainder), where x == y * (x %/% y) + (x %% y)

flights_5.5.2.1 = flights_Testimate %>%

mutate(dep_time_totalMinutes = dep_time %/% 100 * 60 + dep_time %% 100, sched_dep_time_totalMinutes

select(year:dep_delay,dep_time_totalMinutes,sched_dep_time_totalMinutes,arr_time:time_hour)
```

Use select to rearrange column orders.

2. Compare air_time with arr_time - dep_time. What do you expect to see? What do you see? What do you need to do to fix it?

```
flights_Testimate %>%
  mutate(arr_dep = arr_time - dep_time) %>%
  select(carrier:air_time, arr_dep)
```

```
## # A tibble: 336,776 x 7
##
      carrier flight tailnum origin dest air_time arr_dep
##
        <chr>
                <int>
                                <chr> <chr>
                                                <dbl>
                        <chr>>
                                                         <int>
## 1
           UA
                 1545 N14228
                                  EWR
                                        IAH
                                                  227
                                                           313
## 2
           UA
                 1714 N24211
                                  LGA
                                        IAH
                                                  227
                                                           317
## 3
           AA
                 1141 N619AA
                                  JFK
                                        MIA
                                                  160
                                                           381
## 4
           B6
                  725 N804JB
                                  JFK
                                        BQN
                                                           460
                                                  183
## 5
           DL
                  461
                       N668DN
                                  LGA
                                        ATL
                                                  116
                                                           258
## 6
           UA
                 1696 N39463
                                  EWR
                                        ORD
                                                  150
                                                           186
## 7
           B6
                  507
                       N516JB
                                  EWR
                                        FLL
                                                  158
                                                           358
                 5708 N829AS
## 8
           ΕV
                                  LGA
                                        IAD
                                                   53
                                                           152
## 9
           B6
                   79
                       N593JB
                                  JFK
                                        MCO
                                                  140
                                                           281
## 10
           AA
                  301
                       N3ALAA
                                  LGA
                                        ORD
                                                  138
                                                           195
## # ... with 336,766 more rows
```

We expect to see air_time equals arr_time - dep_time, however they are not remotely equal, and they shouldn't be, because as mentioned in problem 1, dep_time and arr_time (and their corresponding scheduked version) are not recorded in a manner that easy to add or substract. So a more convenient version of representation is preferred.

```
select(year:arr_delay,dep_time_totalMinutes, sched_dep_time_totalMinutes, arr_time_totalMinutes,
                     sched_arr_time_totalMinutes, air_time, carrier:travelTime)
flights_Testimate %>%
    mutate(air_time_minutes = arr_time_totalMinutes - dep_time_totalMinutes) %>%
        select(carrier:distance, sched_dep_time_totalMinutes, sched_arr_time_totalMinutes, dep_time_totalMinutes, dep_time
## # A tibble: 336,776 x 12
             carrier flight tailnum origin dest distance
##
##
                 <chr>
                               <int>
                                                <chr>
                                                               <chr> <chr>
                                                                                               <dbl>
## 1
                       UA
                                 1545 N14228
                                                                   EWR
                                                                                IAH
                                                                                                 1400
## 2
                       UA
                                 1714 N24211
                                                                   LGA
                                                                                IAH
                                                                                                 1416
## 3
                       AA
                                 1141 N619AA
                                                                   JFK
                                                                               MIA
                                                                                                 1089
## 4
                       В6
                                   725 N804JB
                                                                   JFK
                                                                               BQN
                                                                                                 1576
## 5
                       DL
                                   461 N668DN
                                                                   LGA
                                                                                ATL
                                                                                                   762
## 6
                       UA
                                 1696 N39463
                                                                   EWR
                                                                                ORD
                                                                                                   719
## 7
                       В6
                                  507 N516JB
                                                                   EWR
                                                                               FLL
                                                                                                 1065
                       ΕV
## 8
                                 5708 N829AS
                                                                   LGA
                                                                                IAD
                                                                                                   229
## 9
                       B6
                                     79 N593JB
                                                                   JFK
                                                                                MCO
                                                                                                   944
## 10
                       AA
                                    301 N3ALAA
                                                                   LGA
                                                                                ORD
                                                                                                   733
## # ... with 336,766 more rows, and 6 more variables:
              sched_dep_time_totalMinutes <dbl>, sched_arr_time_totalMinutes <dbl>,
## #
              dep_time_totalMinutes <dbl>, arr_time_totalMinutes <dbl>,
## #
              air_time_minutes <dbl>, air_time <dbl>
    3. Compare dep_time, sched_dep_time, and dep_delay. How would you expect those three numbers to
          be related?
flights_Testimate %>%
    mutate(dep_delay_copy = dep_time - sched_dep_time) %>%
        select(dep_time, sched_dep_time, dep_delay_copy, dep_delay)
## # A tibble: 336,776 x 4
            dep_time sched_dep_time dep_delay_copy dep_delay
##
##
                   <int>
                                                   <int>
                                                                                   <int>
                                                                                                        <dbl>
## 1
                       517
                                                       515
                                                                                          2
                                                                                                                2
                                                                                          4
## 2
                       533
                                                       529
                                                                                                                4
                                                                                           2
## 3
                                                                                                                2
                       542
                                                       540
## 4
                                                       545
                                                                                        -1
                       544
                                                                                                              -1
## 5
                       554
                                                       600
                                                                                      -46
                                                                                                              -6
                                                                                        -4
                                                                                                              -4
## 6
                       554
                                                       558
## 7
                       555
                                                       600
                                                                                      -45
                                                                                                              -5
## 8
                                                       600
                                                                                      -43
                                                                                                              -3
                       557
## 9
                       557
                                                       600
                                                                                      -43
                                                                                                              -3
                       558
                                                                                      -42
                                                                                                              -2
## 10
                                                       600
## # ... with 336,766 more rows
flights Testimate %>%
    mutate(dep_delay_copy = dep_time_totalMinutes - sched_dep_time_totalMinutes) %>%
        select(dep_time, sched_dep_time, dep_delay_copy, dep_delay)
## # A tibble: 336,776 x 4
##
            dep_time sched_dep_time dep_delay_copy dep_delay
##
                   <int>
                                                   <int>
                                                                                   <dbl>
                                                                                                        <dbl>
## 1
                       517
                                                       515
                                                                                          2
                                                                                                                2
## 2
                       533
                                                       529
                                                                                           4
                                                                                                                4
```

```
## 3
            542
                              540
                                                  2
                                                             2
## 4
            544
                              545
                                                 -1
                                                             -1
## 5
            554
                              600
                                                 -6
                                                            -6
                              558
                                                 -4
                                                            -4
## 6
            554
## 7
            555
                              600
                                                 -5
                                                             -5
## 8
                              600
                                                 -3
                                                            -3
            557
## 9
                              600
                                                 -3
                                                            -3
            557
## 10
                                                 -2
                                                            -2
            558
                              600
## # ... with 336,766 more rows
```

4. Find the 10 most delayed flights using a ranking function. How do you want to handle ties? Carefully read the documentation for min_rank().

My first answer: arr_delay

```
flights_Testimate %>%
  mutate(delay_rank = min_rank(desc(arr_delay))) %>%
  select(carrier:dest, arr_delay, delay_rank) %>%
    arrange(delay_rank)
```

```
## # A tibble: 336,776 x 7
##
      carrier flight tailnum origin dest arr_delay delay_rank
##
         <chr>
                 <int>
                          <chr>
                                 <chr> <chr>
                                                    <dbl>
                                                                <int>
## 1
            HA
                    51
                        N384HA
                                    JFK
                                          HNL
                                                     1272
                                                                     1
## 2
            MQ
                  3535
                        N504MQ
                                    JFK
                                          CMH
                                                     1127
                                                                     2
                 3695
                                                                    3
## 3
            MQ
                        N517MQ
                                    EWR
                                          ORD
                                                     1109
                                                                     4
                   177
                        N338AA
## 4
            AA
                                    JFK
                                          SF<sub>0</sub>
                                                     1007
                                                                    5
## 5
            MQ
                 3075
                        N665MQ
                                    JFK
                                          CVG
                                                      989
## 6
            DL
                 2391
                        N959DL
                                    JFK
                                          TPA
                                                      931
                                                                     6
## 7
            DL
                  2119
                        N927DA
                                   LGA
                                          MSP
                                                                     7
                                                      915
## 8
            DL
                  2047
                        N6716C
                                    LGA
                                          ATL
                                                      895
                                                                    8
## 9
                                                                    9
            AA
                   172
                        N5DMAA
                                    EWR
                                          MIA
                                                      878
## 10
            MQ
                  3744
                        N523MQ
                                    EWR
                                          ORD
                                                      875
                                                                   10
## # ... with 336,766 more rows
```

Improved version (without having to create a new variable)

```
flights_Testimate %>%
  filter(min_rank(desc(arr_delay)) <= 10) %>%
  select(carrier:dest, arr_delay) %>%
    arrange(desc(arr_delay))
```

```
## # A tibble: 10 x 6
##
       carrier flight tailnum origin
                                         dest arr_delay
##
         <chr>>
                 <int>
                          <chr>>
                                  <chr>
                                        <chr>
                                                    <dbl>
## 1
            HA
                    51
                        N384HA
                                    JFK
                                           HNL
                                                     1272
## 2
            MQ
                  3535
                        N504MQ
                                    JFK
                                           CMH
                                                     1127
## 3
            MQ
                  3695
                        N517MQ
                                    EWR
                                           ORD
                                                     1109
                        N338AA
## 4
            AA
                   177
                                    JFK
                                           SF<sub>0</sub>
                                                     1007
## 5
            MQ
                  3075
                        N665MQ
                                    JFK
                                           CVG
                                                      989
## 6
            DL
                  2391
                        N959DL
                                    JFK
                                           TPA
                                                      931
## 7
            DL
                  2119
                        N927DA
                                    LGA
                                           MSP
                                                      915
## 8
            DL
                  2047
                        N6716C
                                    LGA
                                           ATL
                                                      895
                   172
## 9
                                    EWR
                                                      878
            AA
                        N5DMAA
                                           MIA
## 10
            MQ
                  3744
                        N523MQ
                                    EWR
                                           ORD
                                                      875
```

5. What does 1:3 + 1:10 return? Why?

```
1:3 + 1:10
```

```
## Warning in 1:3 + 1:10: longer object length is not a multiple of shorter ## object length ## [1] 2 4 6 5 7 9 8 10 12 11
```

It returns a 10 dimensional vector along with a warning message. Looks like the shorter vector 1:3 is repeated out to the length of the longer 1:10 one.

5.6 Grouped summaries with summarise

It collapses a data frame to a single row.

summarise() is not terribly useful unless we pair it with group_by()

```
by_day <- group_by(flights, year, month, day)
summarise(by_day, delay = mean(dep_delay, na.rm = TRUE))</pre>
```

```
## Source: local data frame [365 x 4]
## Groups: year, month [?]
##
##
       year month
                    day
                             delay
##
      <int> <int> <int>
                             <dbl>
       2013
## 1
                1
                      1 11.548926
## 2
       2013
                1
                      2 13.858824
## 3
       2013
                1
                      3 10.987832
## 4
       2013
                      4 8.951595
                1
## 5
       2013
                1
                      5 5.732218
                      6 7.148014
       2013
## 6
                1
## 7
       2013
                1
                      7
                         5.417204
## 8
       2013
                1
                      8 2.553073
## 9
       2013
                      9 2.276477
## 10 2013
                      10 2.844995
                1
## # ... with 355 more rows
```

5.6.1 Combining multiple operations with the pipe

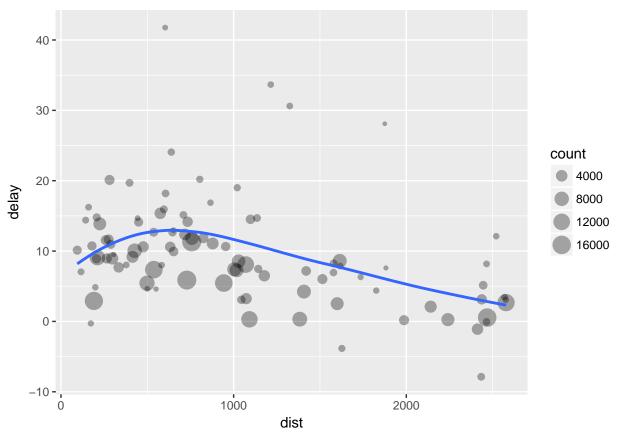
Imagine that we want to explore the relationship between the distance and average delay for each location. Using what you know about dplyr, you might write code like this:

```
delays <- flights %>%
  group_by(dest) %>%
  summarise(
    count = n(),
    dist = mean(distance, na.rm = TRUE),
    delay = mean(arr_delay, na.rm = TRUE)
) %>%
  filter(count > 20, dest != "HNL")

# It looks like delays increase with distance up to ~750 miles and then decrease. Maybe as flights get
ggplot(data = delays, mapping = aes(x = dist, y = delay)) +
```

```
geom_point(aes(size = count), alpha = 1/3) +
geom_smooth(se = FALSE)
```

`geom_smooth()` using method = 'loess'



```
#> `geom_smooth()` using method = 'loess'
```

There are three steps to prepare this data:

Group flights by destination.

Summarise to compute distance, average delay, and number of flights.

Filter to remove noisy points and Honolulu airport, which is almost twice as far away as the next closest airport.

This code is a little frustrating to write because we have to give each intermediate data frame a name, even though we don't care about it. Naming things is hard, so this slows down our analysis.

5.6.2 Missing Values

Naive failure try:

```
flights %>%
  group_by(year, month, day) %>%
  summarise(mean = mean(dep_delay))

## Source: local data frame [365 x 4]
## Groups: year, month [?]
##
```

```
##
       year month
                     day mean
##
      <int> <int> <int> <dbl>
## 1
       2013
                 1
                       1
                             NA
## 2
       2013
                       2
                             NA
                 1
## 3
       2013
                 1
                       3
                             NA
## 4
       2013
                       4
                             NA
                 1
## 5
       2013
                       5
                 1
                            NA
## 6
       2013
                 1
                       6
                            NA
## 7
       2013
                 1
                       7
                             NA
## 8
       2013
                 1
                       8
                             NA
## 9
       2013
                 1
                       9
                             NA
## 10 2013
                      10
                             NA
                 1
## # ... with 355 more rows
All aggregation functions have an na.rm argument which removes the missing values prior to computation:
flights %>%
  group_by(year, month, day) %>%
  summarise(mean = mean(dep_delay, na.rm = TRUE))
## Source: local data frame [365 x 4]
## Groups: year, month [?]
##
##
       year month
                     day
                               mean
##
      <int> <int> <int>
                              <dbl>
       2013
## 1
                 1
                       1 11.548926
## 2
       2013
                 1
                       2 13.858824
## 3
       2013
                       3 10.987832
                 1
## 4
       2013
                       4
                          8.951595
                 1
## 5
       2013
                       5
                          5.732218
                 1
## 6
       2013
                 1
                       6
                          7.148014
## 7
       2013
                       7
                          5.417204
                 1
## 8
       2013
                 1
                       8
                          2.553073
## 9
       2013
                       9
                          2.276477
                 1
## 10 2013
                 1
                      10 2.844995
## # ... with 355 more rows
Departure delay by day:
not_cancelled <- flights %>%
  filter(!is.na(dep_delay), !is.na(arr_delay))
not_cancelled %>%
  group_by(year, month, day) %>%
  summarise(mean = mean(dep_delay))
## Source: local data frame [365 x 4]
## Groups: year, month [?]
##
##
       year month
                     day
                               mean
      <int> <int> <int>
##
                              <dbl>
## 1
       2013
                 1
                       1 11.435620
## 2
       2013
                 1
                       2 13.677802
## 3
       2013
                       3 10.907778
                 1
       2013
## 4
                       4
                          8.965859
                 1
## 5
                       5
                         5.732218
       2013
                 1
```

```
2013
## 6
               1
                      6 7.145959
## 7
      2013
                      7
                        5.417204
                1
## 8
      2013
                      8
                         2.558296
## 9
      2013
                      9 2.301232
                1
## 10 2013
                1
                     10
                         2.844995
## # ... with 355 more rows
```

Useful tool alert!

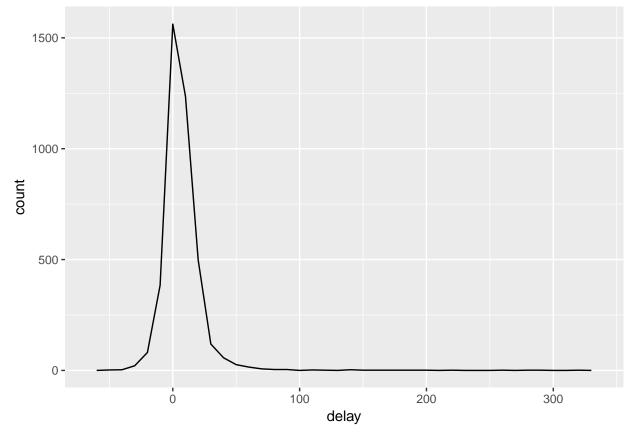
5.6.3 Counts

Whenever you do any aggregation, it's always a good idea to include either a count n(), or a count of non-missing values (sum(!is.na(x))). That way you can check that you're not drawing conclusions based on very small amounts of data. For example, let's look at the planes (identified by their tail number) that have the highest average delays:

planes identified by their tail number

```
delays <- not_cancelled %>%
  group_by(tailnum) %>%
  summarise(
   delay = mean(arr_delay)
)

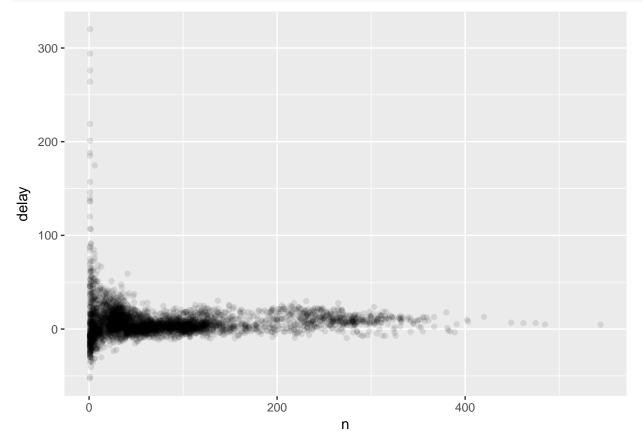
ggplot(data = delays, mapping = aes(x = delay)) +
  geom_freqpoly(binwidth = 10)
```



There are some planes that have an average delay of 5 hours (300 minutes), but the story is actually a little more nuanced. We can get more insight if we draw a scatterplot of number of flights vs. average delay:

```
delays <- not_cancelled %>%
  group_by(tailnum) %>%
  summarise(
   delay = mean(arr_delay, na.rm = TRUE),
   n = n() # preparation for 2 uses: 1. as x axis when calling in ggplot
)

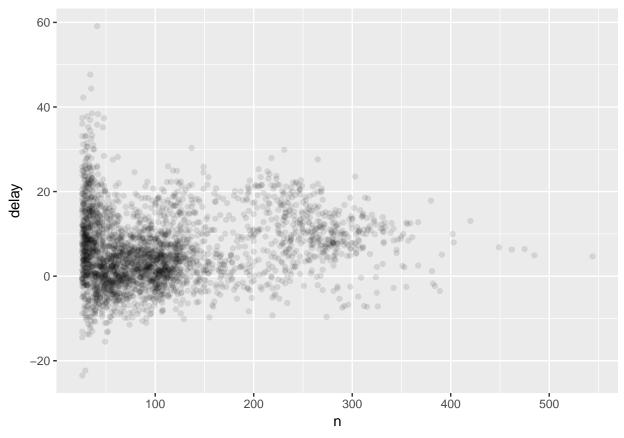
ggplot(data = delays, mapping = aes(x = n, y = delay)) +
  geom_point(alpha = 1/10)
```



Not surprisingly, there is much greater variation in the average delay when there are few flights. The shape of this plot is very characteristic: whenever you plot a mean (or other summary) vs. group size, you'll see that the variation decreases as the sample size increases.

When looking at this sort of plot, it's often useful to filter out the groups with the smallest numbers of observations, so you can see more of the pattern and less of the extreme variation in the smallest groups.

```
delays %>%
  filter(n > 25) %>% # 2. n = n() can be used later if data needs to be filtered
  ggplot(mapping = aes(x = n, y = delay)) +
    geom_point(alpha = 1/10)
```



RStudio tip: a useful keyboard shortcut is $\operatorname{Cmd}/\operatorname{Ctrl} + \operatorname{Shift} + \operatorname{P}$. This resends the previously sent chunk from the editor to the console. This is very convenient when you're (e.g.) exploring the value of n in the example above. You send the whole block once with $\operatorname{Cmd}/\operatorname{Ctrl} + \operatorname{Enter}$, then you modify the value of n and press $\operatorname{Cmd}/\operatorname{Ctrl} + \operatorname{Shift} + \operatorname{P}$ to resend the complete block.

Baseball performance

Here I use data from the Lahman package to compute the batting average (number of hits / number of attempts) of every major league baseball player.

```
# Convert to a tibble so it prints nicely
library(Lahman)

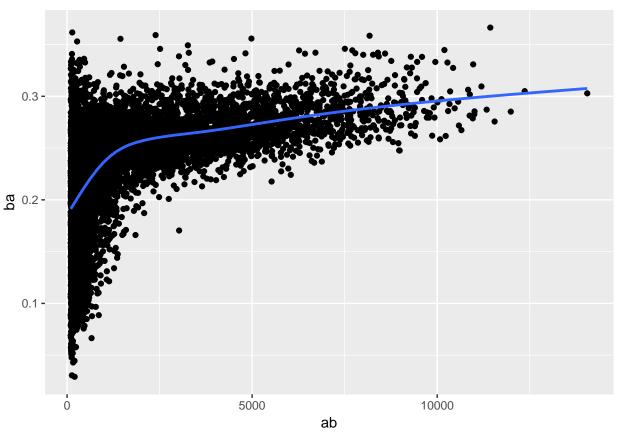
## Warning: package 'Lahman' was built under R version 3.3.2
batting <- as_tibble(Lahman::Batting)

batters <- batting %>%
```

```
group_by(playerID) %>%
summarise(
  ba = sum(H, na.rm = TRUE) / sum(AB, na.rm = TRUE),
  ab = sum(AB, na.rm = TRUE)
)
batters %>%
filter(ab > 100) %>%
ggplot(mapping = aes(x = ab, y = ba)) +
```

```
geom_point() +
geom_smooth(se = FALSE)
```

`geom_smooth()` using method = 'gam'



#> `geom_smooth()` using method = 'gam'

you see two patterns:

##

- 1. As above, the variation in our aggregate decreases as we get more data points.
- 2. There's a positive correlation between skill (ba) and opportunities to hit the ball (ab). This is because teams control who gets to play, and obviously they'll pick their best players.

5.6.4 Useful Summary Functions

It's sometimes useful to combine aggregation with logical subsetting.

Problem: Calculate the average postice delay

```
not_cancelled %>%
  group_by(year, month, day) %>%
  summarise(
    avg_delay1 = mean(arr_delay),
    avg_delay2 = mean(arr_delay[arr_delay > 0]) # the average positive delay
)

## Source: local data frame [365 x 5]
## Groups: year, month [?]
```

```
##
                     day avg_delay1 avg_delay2
       year month
##
      <int> <int> <int>
                               <dbl>
                                           <dbl>
## 1
       2013
                 1
                        1 12.6510229
                                        32.48156
       2013
## 2
                        2 12.6928879
                                        32.02991
                 1
## 3
       2013
                 1
                       3
                           5.7333333
                                        27.66087
## 4
       2013
                                        28.30976
                        4 -1.9328194
                 1
## 5
                                        22.55882
       2013
                 1
                       5 -1.5258020
## 6
       2013
                 1
                       6
                          4.2364294
                                        24.37270
## 7
       2013
                 1
                       7 -4.9473118
                                        27.76132
## 8
       2013
                 1
                       8 -3.2275785
                                        20.78909
## 9
       2013
                        9 -0.2642777
                                        25.63415
                 1
## 10
       2013
                      10 -5.8988159
                                        27.34545
                 1
## # ... with 355 more rows
```

Measures of Position

first(x), nth(x, 2), last(x). These work similarly to x[1], x[2], and x[length(x)] but let you set a default value if that position does not exist (i.e. you're trying to get the 3rd element from a group that only has two elements). For example, we can find the first and last departure for each day:

```
not_cancelled %>%
  group_by(year, month, day) %>%
  summarise(
    first dep = first(dep time),
    last_dep = last(dep_time)
## Source: local data frame [365 x 5]
## Groups: year, month [?]
##
##
                      day first_dep last_dep
       year month
##
      <int> <int>
                   <int>
                               <int>
                                         <int>
       2013
## 1
                 1
                        1
                                 517
                                          2356
## 2
       2013
                        2
                                  42
                                          2354
                 1
## 3
       2013
                        3
                                  32
                                          2349
## 4
       2013
                        4
                                  25
                                          2358
                 1
                        5
## 5
       2013
                 1
                                  14
                                          2357
## 6
       2013
                 1
                        6
                                  16
                                          2355
                        7
## 7
       2013
                                  49
                                          2359
       2013
                        8
                                          2351
## 8
                 1
                                 454
## 9
       2013
                 1
                        9
                                   2
                                          2252
## 10
       2013
                       10
                                   3
                                          2320
                 1
## # ... with 355 more rows
```

These functions are complementary to filtering on ranks. Filtering gives you all variables, with each observation in a separate row

Testimate Smart: first and last - filter(r %in% range(r))

min_rank

```
not_cancelled %>%
  group_by(year, month, day) %>%
  mutate(r = min_rank(desc(dep_time))) %>%
  filter(r %in% range(r))
```

```
## Source: local data frame [770 x 20]
## Groups: year, month, day [365]
##
##
                     day dep_time sched_dep_time dep_delay arr_time
       year month
##
      <int> <int> <int>
                            <int>
                                             <int>
                                                       <dbl>
                                                                 <int>
## 1
       2013
                               517
                                               515
                                                            2
                                                                   830
                 1
                       1
## 2
       2013
                 1
                       1
                              2356
                                              2359
                                                           -3
                                                                   425
## 3
       2013
                       2
                                              2359
                 1
                                42
                                                           43
                                                                   518
## 4
       2013
                 1
                       2
                              2354
                                              2359
                                                           -5
                                                                   413
## 5
       2013
                       3
                                                                   504
                 1
                                32
                                              2359
                                                           33
## 6
       2013
                 1
                       3
                              2349
                                              2359
                                                          -10
                                                                   434
## 7
       2013
                       4
                                25
                                              2359
                                                           26
                                                                   505
                 1
## 8
                       4
       2013
                 1
                              2358
                                              2359
                                                           -1
                                                                   429
## 9
       2013
                       4
                              2358
                                                           -1
                                                                   436
                 1
                                              2359
## 10 2013
                       5
                                14
                                              2359
                                                           15
                                                                   503
                 1
## # ... with 760 more rows, and 13 more variables: sched_arr_time <int>,
       arr_delay <dbl>, carrier <chr>, flight <int>, tailnum <chr>,
## #
       origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>,
## #
       minute <dbl>, time_hour <dttm>, r <int>
```

Counts: To count the number of non-missing values, use sum(!is.na(x)). To count the number of distinct (unique) values, use n_distinct(x). For example:

Which destinations have the most carriers?

```
not_cancelled %>%
  group by(dest) %>%
  summarise(carriers = n_distinct(carrier)) %>%
  arrange(desc(carriers))
## # A tibble: 104 x 2
##
       dest carriers
##
      <chr>
                <int>
## 1
        ATL
                    7
## 2
        BOS
                    7
                    7
## 3
        CLT
## 4
        ORD
                    7
                    7
## 5
        TPA
## 6
        AUS
                    6
## 7
        DCA
## 8
        DTW
                    6
## 9
                    6
        IAD
        MSP
                    6
## 10
## # ... with 94 more rows
not_cancelled %>%
  count(dest)
```

```
## # A tibble: 104 x 2
##
       dest
                 n
##
      <chr> <int>
## 1
        ABQ
               254
## 2
        ACK
               264
## 3
        ALB
               418
## 4
        ANC
                 8
## 5
        ATL 16837
```

```
## 6
        AUS 2411
## 7
        AVL
               261
## 8
        BDL
               412
## 9
               358
        BGR
## 10
        BHM
               269
## # ... with 94 more rows
```

Testimate: similar to table(), with even straightforward command.

You can optionally provide a weight variable. For example, you could use this to "count" (sum) the total number of miles a plane flew:

```
not_cancelled %>%
  count(tailnum, wt = distance)
## # A tibble: 4,037 x 2
##
      tailnum
                   n
##
               <dbl>
        <chr>
## 1
       D942DN
                3418
## 2
       NOEGMQ 239143
## 3
       N10156 109664
## 4
       N102UW 25722
## 5
      N103US
               24619
## 6
       N104UW
               24616
## 7
       N10575 139903
## 8
       N105UW 23618
## 9
       N107US
               21677
## 10 N108UW
               32070
## # ... with 4,027 more rows
To verify, we may simply calculate / observe like this:
```

```
not_cancelled %>%
  filter(tailnum == "D942DN") %>%
    select(tailnum, distance)
```

```
## # A tibble: 4 x 2
##
     tailnum distance
##
       <chr>>
                <dbl>
                  762
## 1 D942DN
## 2
     D942DN
                  950
## 3 D942DN
                  944
## 4 D942DN
                  762
```

Counts and proportions of logical values: sum(x) gives the number of TRUEs in x, and mean(x) gives the proportion.

```
# How many flights left before 5am? (these usually indicate delayed
# flights from the previous day)
not_cancelled %>%
  group_by(year, month, day) %>%
  summarize(n_early = sum(dep_time < 500))</pre>
## Source: local data frame [365 x 4]
```

```
## Groups: year, month [?]
##
##
       year month
                    day n_early
```

```
##
      <int> <int> <int>
                            <int>
## 1
       2013
                        1
                                0
                 1
       2013
                        2
                                3
## 2
                 1
## 3
       2013
                        3
                                4
                 1
## 4
       2013
                 1
                        4
                                3
## 5
       2013
                        5
                                3
                 1
## 6
       2013
                        6
                                2
                 1
## 7
       2013
                        7
                                2
                 1
## 8
       2013
                 1
                        8
                                1
## 9
       2013
                        9
                 1
                                3
## 10 2013
                 1
                       10
                                3
## # ... with 355 more rows
# What proportion of flights are delayed by more than an hour?
not_cancelled %>%
  group_by(year, month, day) %>%
  summarise(hour_perc = round(mean(arr_delay > 60), digit = 3))
## Source: local data frame [365 x 4]
## Groups: year, month [?]
##
##
       year month
                     day hour_perc
##
      <int> <int> <int>
                              <dbl>
## 1
       2013
                 1
                        1
                              0.072
## 2
       2013
                 1
                        2
                              0.085
## 3
       2013
                       3
                              0.057
                 1
## 4
       2013
                 1
                        4
                              0.040
## 5
       2013
                        5
                              0.035
                 1
## 6
       2013
                 1
                        6
                              0.047
## 7
       2013
                        7
                              0.033
                 1
## 8
       2013
                        8
                              0.021
                 1
## 9
       2013
                        9
                 1
                              0.020
                              0.018
## 10 2013
                 1
                      10
## # ... with 355 more rows
```

5.6.5 Grouping by multiple variables

When you group by multiple variables, each summary peels off one level of the grouping. That makes it easy to progressively roll up a dataset:

```
daily <- group_by(flights, year, month, day)</pre>
(per_day <- summarise(daily, flights = n()))</pre>
## Source: local data frame [365 x 4]
## Groups: year, month [?]
##
##
       year month
                      day flights
##
      <int> <int> <int>
                             <int>
## 1
       2013
                 1
                        1
                               842
## 2
       2013
                 1
                        2
                               943
## 3
       2013
                 1
                        3
                               914
                        4
## 4
       2013
                               915
                 1
## 5
       2013
                 1
                        5
                               720
                        6
                               832
## 6
       2013
                 1
## 7
       2013
                        7
                               933
```

```
## 8
       2013
                 1
                       8
                              899
## 9
       2013
                 1
                       9
                              902
## 10 2013
                 1
                      10
                              932
## # ... with 355 more rows
(per_month <- summarise(per_day, flights = sum(flights)))</pre>
## Source: local data frame [12 x 3]
## Groups: year [?]
##
##
       year month flights
##
      <int> <int>
                     <int>
## 1
       2013
                     27004
       2013
## 2
                 2
                     24951
## 3
       2013
                 3
                     28834
## 4
       2013
                 4
                     28330
## 5
       2013
                 5
                     28796
## 6
       2013
                 6
                     28243
## 7
       2013
                 7
                     29425
## 8
       2013
                 8
                     29327
## 9
       2013
                 9
                     27574
## 10
       2013
                10
                     28889
## 11
       2013
                11
                     27268
## 12
       2013
                12
                     28135
          <- summarise(per_month, flights = sum(flights)))
## # A tibble: 1 x 2
##
      year flights
##
     <int>
              <int>
     2013
            336776
```

Be careful when progressively rolling up summaries: it's OK for sums and counts, but you need to think about weighting means and variances, and it's not possible to do it exactly for rank-based statistics like the median. In other words, the sum of groupwise sums is the overall sum, but the median of groupwise medians is not the overall median.

5.6.6 Ungrouping