

Preferential Voting Tools

pref_voting

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October 18, 2024

Preferential Voting Tools (pref_voting)

A Python library that can be used to study and run elections with different preferential voting methods (graded voting methods and cardinal voting methods are also included for comparison).

<https://pref-voting.readthedocs.io/>

The screenshot shows a web browser displaying the documentation for the `pref_voting` Python library. The URL in the address bar is `pref-voting.readthedocs.io/en/latest/index.html`. The page title is "Prefential Voting Tools". On the left sidebar, there is a search bar and links to "Introduction", "Installation", "ELECTIONS", "Overview", and "Ballots". The main content area features a large heading "Introduction". Below it, the text explains what the library does: "Prefential Voting Tools (`pref_voting`) is a Python library that can be used to study different preferential voting methods. In a preferential voting election, each voter submits a *ranking* of the candidates, and the winners are determined based on the submitted rankings. The rankings may include ties between candidates, and some candidates may be left off the ranking." It also states the main objective: "The main objective is to create a set of tools that can be used by teachers and researchers to study voting methods. Use the following website to run an election using the preferential voting method Stable Voting: <https://stablevoting.org/>". At the bottom, it credits the developers: "The library is developed by Wes Holliday (<http://wesholliday.net>) and Eric Pacuit (<https://pacuit.org>)."

Notebook Available on Colab

[https://colab.research.google.com/drive/
1QcmITfZEuRv7N2cyeqRbsZk3XZRjr0dd?usp=sharing](https://colab.research.google.com/drive/1QcmITfZEuRv7N2cyeqRbsZk3XZRjr0dd?usp=sharing)



Election Data

- ▶ **Profile:** each voter linearly orders the candidates;
- ▶ **ProfileWithTies:** each voter ranks the candidates, allowing ties and omissions of candidates;
- ▶ **GradeProfile:** each voter assigns grades from some finite list of grades to selected candidates (with approval ballots as a special case);
- ▶ **UtilityProfile:** each voter assigns a real number to each candidate;
- ▶ **SpatialProfile:** each voter and each candidate is placed in a multi-dimensional space;
- ▶ **MajorityGraph:** an edge from candidate A to candidate B represents that more voters rank A above B than vice versa;
- ▶ **MarginGraph:** a weighted version of a MajorityGraph, where the weight on an edge represents the margin of victory.

Election Data

- ▶ Profile: each voter linearly orders the candidates;

```
▶ from pref_voting.profiles import Profile

prof = Profile(
    [[2, 1, 0, 3], [3, 2, 0, 1], [3, 1, 0, 2]], # linear rankings
    rcounts=[2, 1, 3], # number of voters for each ranking
    cmap={0: 'a', 1: 'b', 2: 'c', 3: 'd'} # candidate mapping
)

prof.display()
[15] ✓ 0.0s
...
... +---+---+---+
| 2 | 1 | 3 |
+---+---+---+
| c | d | d |
| b | c | b |
| a | a | a |
| d | b | c |
+---+---+---+
```

Election Data

- ▶ ProfileWithTies: each voter ranks the candidates, allowing ties and omissions of candidates;

```
from pref_voting.profiles_with_ties import ProfileWithTies

prof = ProfileWithTies(
    [{0:1, 1:1}, {0:1, 1:1, 2:2}, {0:3, 1:1, 2:2}, {0:1, 3:0, 2:1}], # rankings with ties
    rcounts=[2, 2, 1, 3], # number of voters for each ranking
    candidates=[0, 1, 2, 3], # candidates in the election
    cmap={0: 'a', 1: 'b', 2: 'c', 3: 'd'} # candidate map
)

prof.display()

[16] ✓ 0.0s
...
+---+---+---+---+
| 2 | 2 | 1 | 3 |
+---+---+---+---+
| a b | a b | b | d |
|     |   c | c | a c |
|     |     | a |   |
|     |     |   |   |
+---+---+---+---+
```

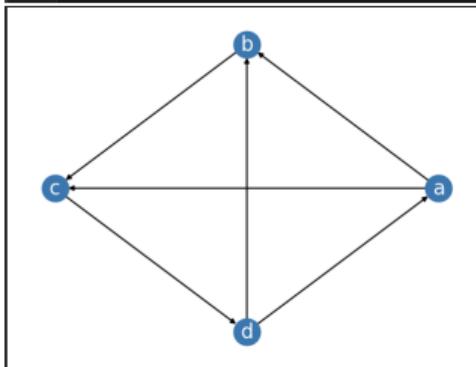
Election Data

- ▶ MajorityGraph: an edge from candidate A to candidate B represents that more voters rank A above B than vice versa;

```
from pref_voting.weighted_majority_graphs import MajorityGraph

mg = MajorityGraph(
    [0, 1, 2, 3], # candidates in the election
    [(0, 1), (1, 2), (0, 2), (3, 0), (3, 1), (2, 3)], # edges in the majority graph
    ...cmap={0: 'a', 1: 'b', 2: 'c', 3: 'd'} # candidate mapping
)

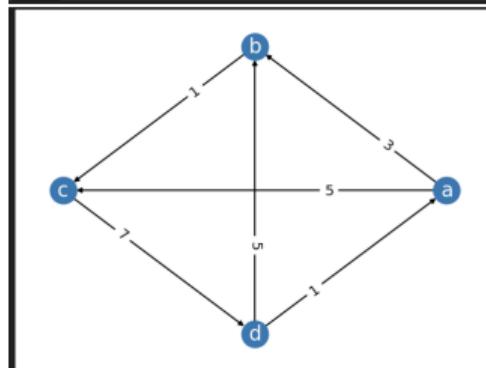
mg.display()
```



Election Data

- ▶ MarginGraph: a weighted version of a MajorityGraph, where the weight on an edge represents the margin of victory.

```
from pref_voting.weighted_majority_graphs import MarginGraph
mg = MarginGraph(
    [0, 1, 2, 3], # candidates in the election
    [(0, 1, 3), (1, 2, 1), (0, 2, 5), (3, 0, 1), (3, 1, 5), (2, 3, 7)], # weighted edges in the
    margin graph
    cmap={0: 'a', 1: 'b', 2: 'c', 3: 'd'} # candidate mapping
)
mg.display()
```



Election Data

- ▶ UtilityProfile: each voter assigns a real number to each candidate;

```
from pref_voting.utility_profiles import UtilityProfile

uprof = UtilityProfile([
    {0:1.0, 1: 0.5, 2: 1.25}, # utilities for each candidate
    {0:-0.5, 1: 9.5, 2: 1.05},
    {0:3.0, 1: -2.0, 2: 1.0},
    {0:0.5, 1: 0.0, 2: 3.0}
])

uprof.display()
```

[22] ✓ 0.0s

...	Voter	0	1	2
-----	---	----	----	-----
1	1	0.5	1.25	
2	-0.5	9.5	1.05	
3	3	-2	1	
4	0.5	0	3	

Election Data

- ▶ GradeProfile: each voter assigns grades from some finite list of grades to selected candidates (with approval ballots as a special case);

```
from pref_voting.grade_profiles import GradeProfile

gprof = GradeProfile([
    {0:1, 1:3, 2:3}, # grades for each candidate
    {0:3, 1:2, 2:1},
    {0:1, 1:1, 2:1},
],
gcnts=[1, 2, 1], # number of voters for each grade assignment
grades=[0, 1, 2, 3], # the grades in the profile
cmap = {0: 'a', 1: 'b', 2: 'c'} # candidate mapping
)

gprof.display(show_totals=True)
```

[24] ✓ 0.0s

...	1	2	1	Sum	Median
a	1	3	1	8	1
b	3	2	1	8	2
c	3	1	1	6	1

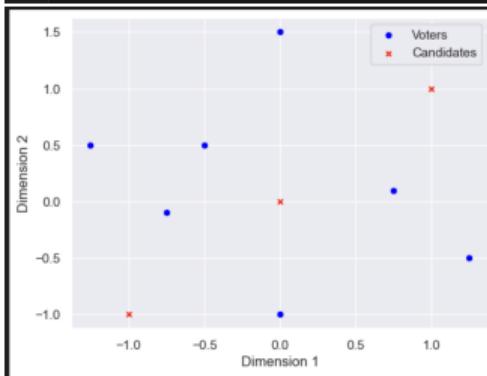
Election Data

- ▶ **SpatialProfile:** each voter and each candidate is placed in a multi-dimensional space;

```
from pref_voting.spatial_profiles import SpatialProfile

sprof = SpatialProfile(
    cand_pos={0:(0, 0), 1: (1, 1), 2:(-1, -1)}, # candidate positions
    voter_pos={0:(0, 1.5), 1:(-1.25, 0.5), 2:(0.75, 0.1), 3:(0, -1), 4:(1.25, -0.5), 5:(-0.75,
-0.1), 6:(-0.5, 0.5)}, # voter positions
    candidate_types={0:'L', 1:'L', 2:'C' }) # assignment of candidates to types (or parties)

# sprof.display() # display the spatial profile
sprof.view()
```



to_latex()

```
▷ ▾
  ∵ prof = Profile(
    [[0, 1, 2], [2, 1, 0], [1, 2, 0]],
    rcounts=[2, 1, 4],
    cmap={0: 'a', 1: 'b', 2: 'c'})

  print(prof.to_latex())
[36] ✓ 0.0s
...
... \begin{tabular}{ccc}
$2$ & $1$ & $4$\\ \hline
$a$ & $c$ & $b$\\
$b$ & $b$ & $c$\\
$c$ & $a$ & $a$\\
\end{tabular}
```

2	1	4
<i>a</i>	<i>c</i>	<i>b</i>
<i>b</i>	<i>b</i>	<i>c</i>
<i>c</i>	<i>a</i>	<i>a</i>

Properties of Profiles

```
prof = Profile([
    [2, 1, 0, 3],
    [3, 2, 0, 1],
    [3, 1, 0, 2]],
    rcounts=[2, 2, 3])

prof.display()

print(f"The margin of 1 over 3 is {prof.margin(1, 3)}")
print(f"The Plurality scores are {prof.plurality_scores()}")
print(f"The Copeland scores are {prof.copeland_scores()}")
print(f"The Borda scores are {prof.borda_scores()}")
print(f"The Condorcet winner is {prof.condorcet_winner()}")
print(f"The weak Condorcet winner is {prof.weak_condorcet_winner()}")
print(f"The Condorcet loser is {prof.condorcet_loser()}")
print(f"The profile is uniquely weighted: {prof.is_uniquely_weighted()}")
```

<https://pref-voting.readthedocs.io/en/latest/profiles.html>

Properties of Profiles

```
... +---+---+---+
| 2 | 2 | 3 |
+---+---+---+
| 2 | 3 | 3 |
| 1 | 2 | 1 |
| 0 | 0 | 0 |
| 3 | 1 | 2 |
+---+---+---+
The margin of 1 over 3 is -3
The Plurality scores are {0: 0, 1: 0, 2: 2, 3: 5}
The Copeland scores are {0: -3.0, 1: -1.0, 2: 1.0, 3: 3.0}
The Borda scores are {0: 7, 1: 10, 2: 10, 3: 15}
The Condorcet winner is 3
The weak Condorcet winner is [3]
The Condorcet loser is 0
The profile is uniquely weighted: False
```

<https://pref-voting.readthedocs.io/en/latest/profiles.html>

Transforming Between Election Data

Object	Method	Output
Profile/ProfileWithTies	majority_graph()	MajorityGraph
Profile/ProfileWithTies	margin_graph()	MarginGraph

Transforming Between Election Data

Object	Method	Output
Profile/ProfileWithTies	majority_graph()	MajorityGraph
Profile/ProfileWithTies	margin_graph()	MarginGraph
Profile	to_profile_with_ties()	ProfileWithTies
Profile	randomly_truncate()	ProfileWithTies
ProfileWithTies	to_linear_profile()	Profile

Transforming Between Election Data

Object	Method	Output
Profile/ProfileWithTies	majority_graph()	MajorityGraph
Profile/ProfileWithTies	margin_graph()	MarginGraph
Profile	to_profile_with_ties()	ProfileWithTies
Profile	randomly_truncate()	ProfileWithTies
ProfileWithTies	to_linear_profile()	Profile
MarginGraph	debord_profile()	Profile
MarginGraph	minimal_profile()	Profile

Transforming Between Election Data

Object	Method	Output
Profile/ProfileWithTies	majority_graph()	MajorityGraph
Profile/ProfileWithTies	margin_graph()	MarginGraph
Profile	to_profile_with_ties()	ProfileWithTies
Profile	randomly_truncate()	ProfileWithTies
ProfileWithTies	to_linear_profile()	Profile
MarginGraph	debord_profile()	Profile
MarginGraph	minimal_profile()	Profile
UtilityProfile	to_ranking_profile()	ProfileWithTies
GradeProfile	to_ranking_profile()	ProfileWithTies

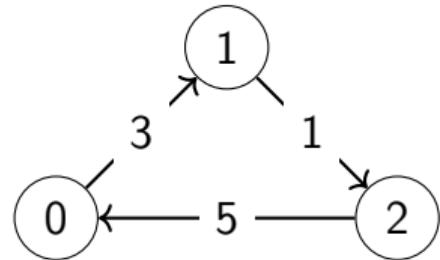
Transforming Between Election Data

Object	Method	Output
Profile/ProfileWithTies	majority_graph()	MajorityGraph
Profile/ProfileWithTies	margin_graph()	MarginGraph
Profile	to_profile_with_ties()	ProfileWithTies
Profile	randomly_truncate()	ProfileWithTies
ProfileWithTies	to_linear_profile()	Profile
MarginGraph	debord_profile()	Profile
MarginGraph	minimal_profile()	Profile
UtilityProfile	to_ranking_profile()	ProfileWithTies
GradeProfile	to_ranking_profile()	ProfileWithTies
UtilityProfile	to_approval_profile()	GradeProfile
UtilityProfile	to_k_approval_profile()	GradeProfile

Transforming Between Election Data

Object	Method	Output
Profile/ProfileWithTies	majority_graph()	MajorityGraph
Profile/ProfileWithTies	margin_graph()	MarginGraph
Profile	to_profile_with_ties()	ProfileWithTies
Profile	randomly_truncate()	ProfileWithTies
ProfileWithTies	to_linear_profile()	Profile
MarginGraph	debord_profile()	Profile
MarginGraph	minimal_profile()	Profile
UtilityProfile	to_ranking_profile()	ProfileWithTies
GradeProfile	to_ranking_profile()	ProfileWithTies
UtilityProfile	to_approval_profile()	GradeProfile
UtilityProfile	to_k_approval_profile()	GradeProfile
SpatialProfile	to_utility_profile()	UtilityProfile

MarginGraph to Profile



```
mg = MarginGraph([0, 1, 2], [(0, 1, 3), (1, 2, 1), (2, 0, 5)])  
debord_prof = mg.debord_profile()  
debord_prof.display()  
  
min_prof = mg.minimal_profile()  
min_prof.display()  
  
[45] ✓ 0.0s  
...  
+---+---+---+---+---+  
| 1 | 1 | 3 | 3 | 1 |  
+---+---+---+---+  
| 0 | 2 | 2 | 1 | 0 |  
| 1 | 0 | 0 | 2 | 1 |  
| 2 | 1 | 1 | 0 | 2 |  
+---+---+---+---+  
+---+---+---+  
| 2 | 3 | 4 |  
+---+---+---+  
| 0 | 1 | 2 |  
| 1 | 2 | 0 |  
| 2 | 0 | 1 |  
+---+---+---+
```

SpatialProfile to UtilityProfile

https://pref-voting.readthedocs.io/en/latest/spatial_profiles.html#utility-functions

```
from pref_voting.utility_functions import *

uprof = sprof.to_utility_profile(utility_function=linear_utility)

uprof = sprof.to_utility_profile(utility_function=quadratic_utility)

uprof = sprof.to_utility_profile(utility_function=rm_utility)

uprof = sprof.to_utility_profile(utility_function=mixed_rm_utility)

uprof = sprof.to_utility_profile(utility_function=matthews_utility)

uprof = sprof.to_utility_profile(utility_function=shepsle_utility)

uprof = sprof.to_utility_profile(utility_function=city_block_utility)
```

Generating Elections - Profile

- ▶ `generate_profile`
 - ▶ Wrapper function that uses the `prefsampling` package to generate profiles using standard probability models:
<https://comsoc-community.github.io/prefsampling/index.html>.
- ▶ Enumerating Profile objects
 - ▶ `enumerate_anon_profile`

Generating a Profile

```
▶ ▾ from pref_voting.generate_profiles import generate_profile

prof = generate_profile(3, 11) # default is the impartial culture

prof = generate_profile(3, 11, prob_model="IAC") # impartial anonymous culture

prof = generate_profile(3, 11, prob_model="mallows", phi=0.8, normalize_phi=True)

prof = generate_profile(3, 11, prob_model="urn", alpha=3)

prof = generate_profile(3, 11, prob_model="euclidean", num_dims=5)

prof = generate_profile(3, 11, prob_model="single_peaked_conitzer", num_dims=5)

prof = generate_profile(3, 11, prob_model="plackett_luce", alphas=[3, 1, 1])
```

Generating Elections - SpatialProfile

- ▶ generate_spatial_profile
- ▶ generate_spatial_profile_polarized
- ▶ generate_spatial_profile_polarized_cands_randomly_polarized_voters

Generating a SpatialProfile

```
from pref_voting.generate_spatial_profiles import generate_spatial_profile, generate_spatial_profile_polarized,  
generate_spatial_profile_polarized_cands_randomly_polarized_voters, generate_covariance  
  
sprof = generate_spatial_profile(3, 100, num_dims=3) # 3 candidates, 100 voters, 3 dimensions  
  
sprof = generate_spatial_profile_polarized(  
    [((-1, 0), generate_covariance(2, 0.1, 0), 2), # 2 candidates in this cluster  
     ((1, 0), generate_covariance(2, 0.1, 0), 2), # 2 candidates in this cluster  
    ],  
    [((-1, 0), generate_covariance(2, 0.25, 0), 100), # 100 voters in this cluster  
     ((1, 0), generate_covariance(2, 0.25, 0), 100), # 100 voters in this cluster  
    ],  
)  
  
sprof = generate_spatial_profile_polarized_cands_randomly_polarized_voters(  
    [((-1, 0), generate_covariance(2, 0.1, 0), 2), # 2 candidates in this cluster  
     ((1, 0), generate_covariance(2, 0.1, 0), 2), # 2 candidates in this cluster  
    ],  
    1000, # number of voters  
    [((-1, 0), generate_covariance(2, 0.25, 0), 0.6), # 60% of voters in this cluster  
     ((1, 0), generate_covariance(2, 0.25, 0), 0.4)], # 40% of voters in this cluster],  
)
```

Other Tools

- ▶ Generating a MarginGraph
 - ▶ `generate_margin_graph`
 - ▶ `generate_margin_graph_bradley_terry`

Other Tools

- ▶ Generating a MarginGraph
 - ▶ generate_margin_graph
 - ▶ generate_margin_graph_bradley_terry
- ▶ Generating *edge ordered* tournaments:
 - ▶ generate_edge_ordered_tournament
 - ▶ generate_edge_ordered_tournament_infinite_limit

Other Tools

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- ▶ Enumerating MarginGraph objects
 - ▶ `enumerate_canonical_edge_ordered_tournaments`
 - ▶ `enumerate_uniquely_weighted_margin_graphs`

Other Tools

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- ▶ Enumerating MarginGraph objects
 - ▶ `enumerate_canonical_edge_ordered_tournaments`
 - ▶ `enumerate_uniquely_weighted_margin_graphs`
- ▶ Generating a UtilityProfile
 - ▶ `generate_utility_profile_uniform`
 - ▶ `generate_utility_profile_normal`

Collective Decision Methods

- ▶ VotingMethod: given *edata*, outputs a list of candidates, representing tied winners;
- ▶ ProbVotingMethod: given *edata*, outputs a dictionary whose keys are candidates and whose values are probabilities;
- ▶ SocialWelfareFunction: given *edata*, outputs a ranking of the candidates.

Voting Methods

Currently, there are 79 voting methods that are implemented.

- ▶ Scoring Rules:

pref-voting.readthedocs.io/en/latest/scoring_methods.html

- ▶ Iterative Methods:

pref-voting.readthedocs.io/en/latest/iterative_methods.html

- ▶ C1 Methods

pref-voting.readthedocs.io/en/latest/c1_methods.html

- ▶ Margin Based Methods

pref-voting.readthedocs.io/en/latest/margin_based_methods.html

- ▶ Combined Methods

pref-voting.readthedocs.io/en/latest/combined_methods.html

- ▶ Other Methods

pref-voting.readthedocs.io/en/latest/other_methods.html

Voting Methods

```
from pref_voting.voting_methods import *
from pref_voting.generate_profiles import generate_profile

prof = generate_profile(4, 1000)
vms = [plurality, borda, instant_runoff, instant_runoff_put, minimax, split_cycle, ranked_pairs, river]
for vm in vms:
    print(f"The {vm.name} winners: {vm(prof)}")
    print(f"\trestricted to the candidates [1, 2, 3]: {vm(prof, curr_cands=[1, 2, 3])}")

[103] ✓ 0.0s
...
The Plurality winners: [3]
    restricted to the candidates [1, 2, 3]: [3]
The Borda winners: [3]
    restricted to the candidates [1, 2, 3]: [3]
The Instant Runoff winners: [0]
    restricted to the candidates [1, 2, 3]: [3]
The Instant Runoff PUT winners: [0]
    restricted to the candidates [1, 2, 3]: [3]
The Minimax winners: [0]
    restricted to the candidates [1, 2, 3]: [3]
The Split Cycle winners: [0]
    restricted to the candidates [1, 2, 3]: [3]
The Ranked Pairs winners: [0]
    restricted to the candidates [1, 2, 3]: [3]
The River winners: [0]
    restricted to the candidates [1, 2, 3]: [3]
```

Axioms

The Axiom objects include functions that check whether a collective decision procedure satisfies a given axiom with respect to some *edata*:

- ▶ `hasViolation`: check whether there is at least one violation of the axiom by the procedure for the given *edata*
- ▶ `findAllViolations`: enumerate all violations together with relevant data.

Axioms

- ▶ dominance axioms
pref-voting.readthedocs.io/en/latest/dominance_axioms.html
- ▶ invariance axioms
pref-voting.readthedocs.io/en/latest/invariance_axioms.html
- ▶ monotonicity axioms
pref-voting.readthedocs.io/en/latest/monotonicity_axioms.html
- ▶ strategic axioms
pref-voting.readthedocs.io/en/latest/strategic_axioms.html
- ▶ variable voter axioms
pref-voting.readthedocs.io/en/latest/variable_voter_axioms.html
- ▶ variable candidate axioms
pref-voting.readthedocs.io/en/latest/variable_candidate_axioms.html
- ▶ SWF axioms
pref-voting.readthedocs.io/en/latest/swf_axioms.html

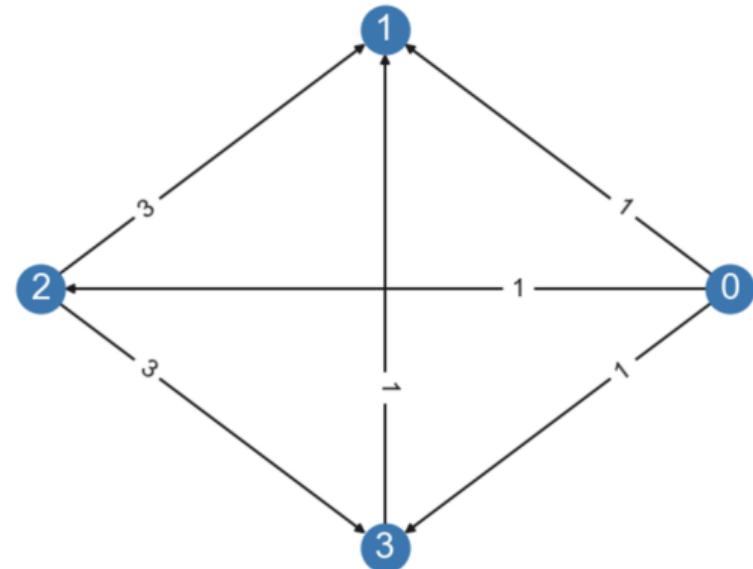
Condorcet Winner

```
▶ ^ from pref_voting.dominance_axioms import *

vm = borda
num_cands = 4
num_voters = 3
num_trials = 1000

for t in range(num_trials):
    prof = generate_profile(num_cands, num_voters)
    if condorcet_winner.hasViolation(prof, vm, only_resolute=True, verbose=True):
        break
```

Condorcet Winner



```
Profile([[0, 2, 3, 1], [2, 3, 1, 0], [0, 2, 1, 3]], rcounts=[1, 1, 1], cmap={0: '0', 1: '1', 2: '2', 3: '3'})  
The Condorcet winner 0 is not the unique winner:  
Borda winner is {2}
```

Immunity to Spoilers

```
from pref_voting.variable_candidate_axioms import *

vm = borda
num_cands = 4
num_voters = 3
num_trials = 1000

for t in range(num_trials):
    prof = generate_profile(num_cands, num_voters)
    if immunity_to_spoilers.hasViolation(prof, vm, verbose=True):
        break
```

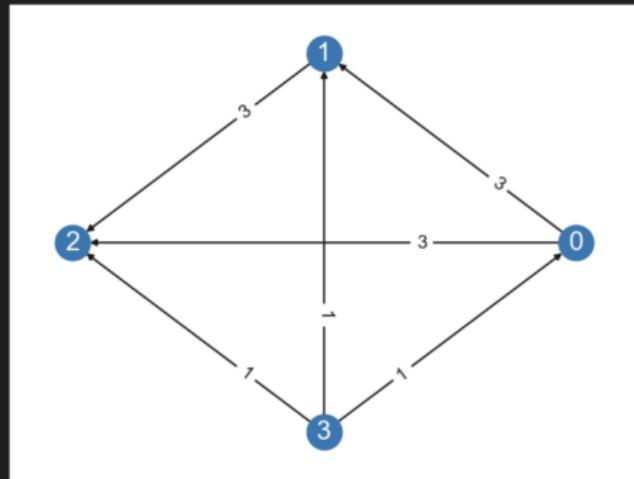
Immunity to Spoilers

Immunity to Spoilers violation for Borda.

3 wins without 1 in the election and is majority preferred to 1 but both lose when 1 is included:

+	-	-	-	+
	1		1	
+	-	-	-	+
	3		3	
	0		0	
	1		1	
	2		2	
+	-	-	-	+
	2		2	
+	-	-	-	+
	3		0	
	0		1	
	1		2	
	2		3	
+	-	-	-	+

Profile([[3, 0, 1, 2], [3, 0, 1, 2], [0, 1, 2, 3]], rcounts=[1, 1, 1], cmap={0: '0', 1: '1', 2: '2', 3: '3'})



Winners in full election: [0]

Winners in election without 1: [0, 3]

Calculating Condorcet Efficiency - 1

```
from pref_voting.analysis import binomial_confidence_interval

min_error = 0.05
min_num_samples = 1000
max_num_samples = 100_000

voting_methods = [plurality, borda, instant_runoff]

num_candidates = 4
num_voters = 11

has_condorcet_winner = []
elect_condorcet_winner = {vm.name: [] for vm in voting_methods}

num_samples = 0
error_ranges = []
```

Calculating Condorcet Efficiency - 2

```
while num_samples < min_num_samples or (any([(err[1] - err[0]) > min_error for err in error_ranges]) and num_samples < max_num_samples):

    num_samples += 1
    prof = generate_profile(num_candidates, num_voters)
    cw = prof.condorcet_winner()

    has_condorcet_winner.append(cw is not None)
    for vm in voting_methods:
        if cw is not None:
            elect_condorcet_winner[vm.name].append(vm(prof) == [cw])

    error_ranges = [binomial_confidence_interval(elect_condorcet_winner[vm.name])
                    if len(elect_condorcet_winner[vm.name]) > 0 else (0, np.inf)
                    for vm in voting_methods]
```

Calculating Condorcet Efficiency - 3

```
print(f"For {num_samples} samples:\n")
print(f"The percentage of profiles with a Condorcet winner is {np.mean
(has_condorcet_winner)}")
err = binomial_confidence_interval(has_condorcet_winner)
print(f"\tError: {err[1]-err[0]}")

print()
for vm in voting_methods:
    print(f"The Condorcet efficiency of {vm.name} is {np.mean(elect_condorcet_winner[vm.
name])}")
    err = binomial_confidence_interval(elect_condorcet_winner[vm.name])
    print(f"\tError: {err[1]-err[0]}")
```

Calculating Condorcet Efficiency - Output

```
... For 1764 samples:
```

```
The percentage of profiles with a Condorcet winner is 0.8378684807256236  
Error: 0.03495235683503972
```

```
The Condorcet efficiency of Plurality is 0.6258457374830853  
Error: 0.04997642712974326
```

```
The Condorcet efficiency of Borda is 0.8640054127198917  
Error: 0.03561495608588128
```

```
The Condorcet efficiency of Instant Runoff is 0.9242219215155616  
Error: 0.027667207860292087
```

pref_voting.analysis.condorcet_efficiency_data

```
▶ from pref_voting.analysis import condorcet_efficiency_data

prob_models = {
    "Impartial Culture": lambda nc, nv: generate_profile(nc, nv),
    "Mallows": lambda nc, nv: generate_profile(nc, nv, probmodel="mallows", phi=0.8,
                                                normalise_phi=True),
    "Urn": lambda nc, nv: generate_profile(nc, nv, probmodel="urn", alpha=5),
    "Spatial": lambda nc, nv: generate_spatial_profile(nc, nv, 3).to_utility_profile().
        to_ranking_profile().to_linear_profile()
}

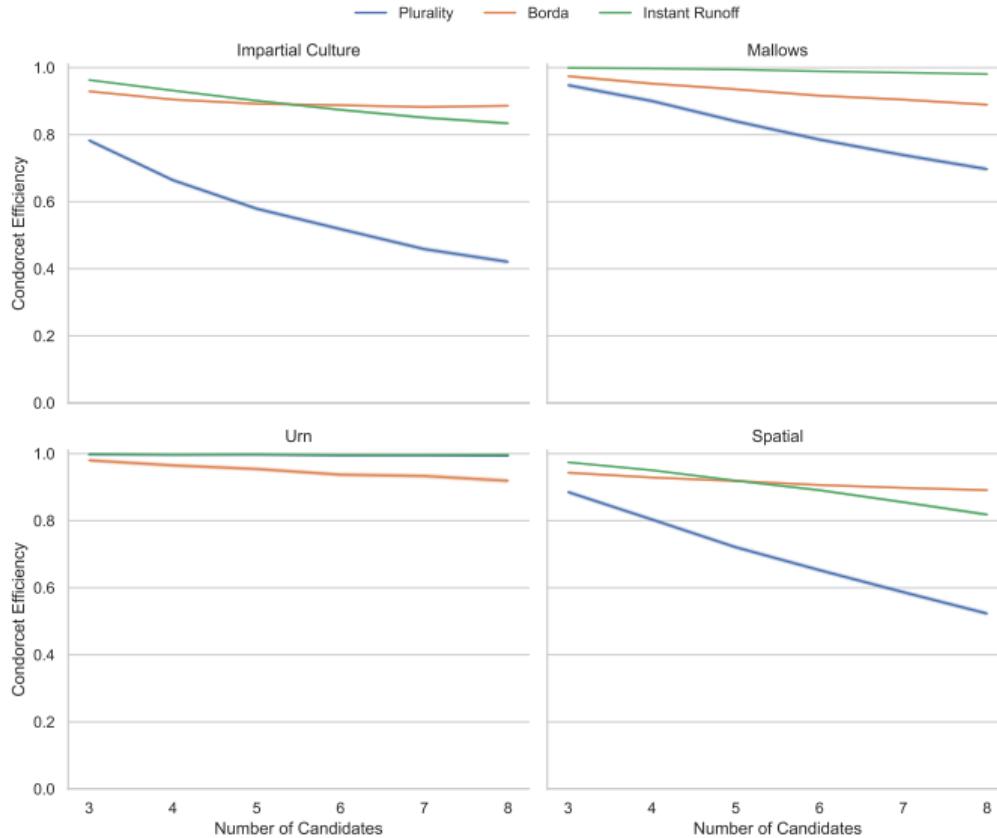
df = condorcet_efficiency_data(
    [plurality, borda, instant_runoff], # voting methods to evaluate
    numbers_of_candidates=[3, 4, 5, 6, 7, 8], # numbers of candidates to check
    numbers_of_voters=[100], # numbers of voters to check
    prob_models=prob_models, # dictionary of the probability models to use
    min_num_samples=1000, # minimum number of samples
    max_num_samples=100_000, # maximum number of samples
    min_error=0.01, # the minimum error
    use_parallel=True, # use parallel processing
    num_cpus=12) # number of cpus to use when doing parallel processing
```

[114]

✓

5m 25.6s

pref_voting.analysis.condorcet_efficiency_data



Percentage of Violations: Immunity to Spoilers - 1

```
from pref_voting.analysis import binomial_confidence_interval
from pref_voting.variable_candidate_axioms import immunity_to_spoilers

min_error = 0.01
min_num_samples = 1000
max_num_samples = 100_000

axiom = immunity_to_spoilers
voting_methods = [plurality, borda, instant_runoff]

num_candidates = 4
num_voters = 11

hasViolation = {vm.name: [] for vm in voting_methods}
num_samples = 0
error_ranges = []
```

Percentage of Violations: Immunity to Spoilers - 2

```
while num_samples < min_num_samples or (any([(err[1] - err[0]) > min_error for err in error_ranges])
and num_samples < max_num_samples):

    num_samples += 1
    prof = generate_profile(num_candidates, num_voters)

    for vm in voting_methods:
        hasViolation[vm.name].append(axiom.hasViolation(prof, vm))

    error_ranges = [binomial_confidence_interval(hasViolation[vm.name])
                    if len(hasViolation[vm.name]) > 0 else (0, np.inf)
                    for vm in voting_methods]

print(f"For {num_samples} samples:\n")

for vm in voting_methods:
    print(f"The percentage of violations of {axiom.name} for {vm.name} is {np.mean
(elect_condorcet_winner[vm.name])}")
    err = binomial_confidence_interval(elect_condorcet_winner[vm.name])
    print(f"\tError: {err[1]-err[0]}")
```

Percentage of Violations: Immunity to Spoilers - Output

```
[131] ✓ 2m 30.6s
...
For 28445 samples:

The percentage of violations of Immunity to Spoilers for Plurality is 0.6258457374830853
Error: 0.04997642712974326
The percentage of violations of Immunity to Spoilers for Borda is 0.8640054127198917
Error: 0.03561495608588128
The percentage of violations of Immunity to Spoilers for Instant Runoff is 0.9242219215155616
Error: 0.027667207860292087
```

Thank you!

<https://pref-voting.readthedocs.io/>

<https://pypi.org/project/pref-voting/>

https://github.com/voting-tools/pref_voting/tree/main/howto

https://pref.tools/pref_voting/