

Homework 5

Questions No.	1	2	3	Total
Score	30%	40%	30%	100%

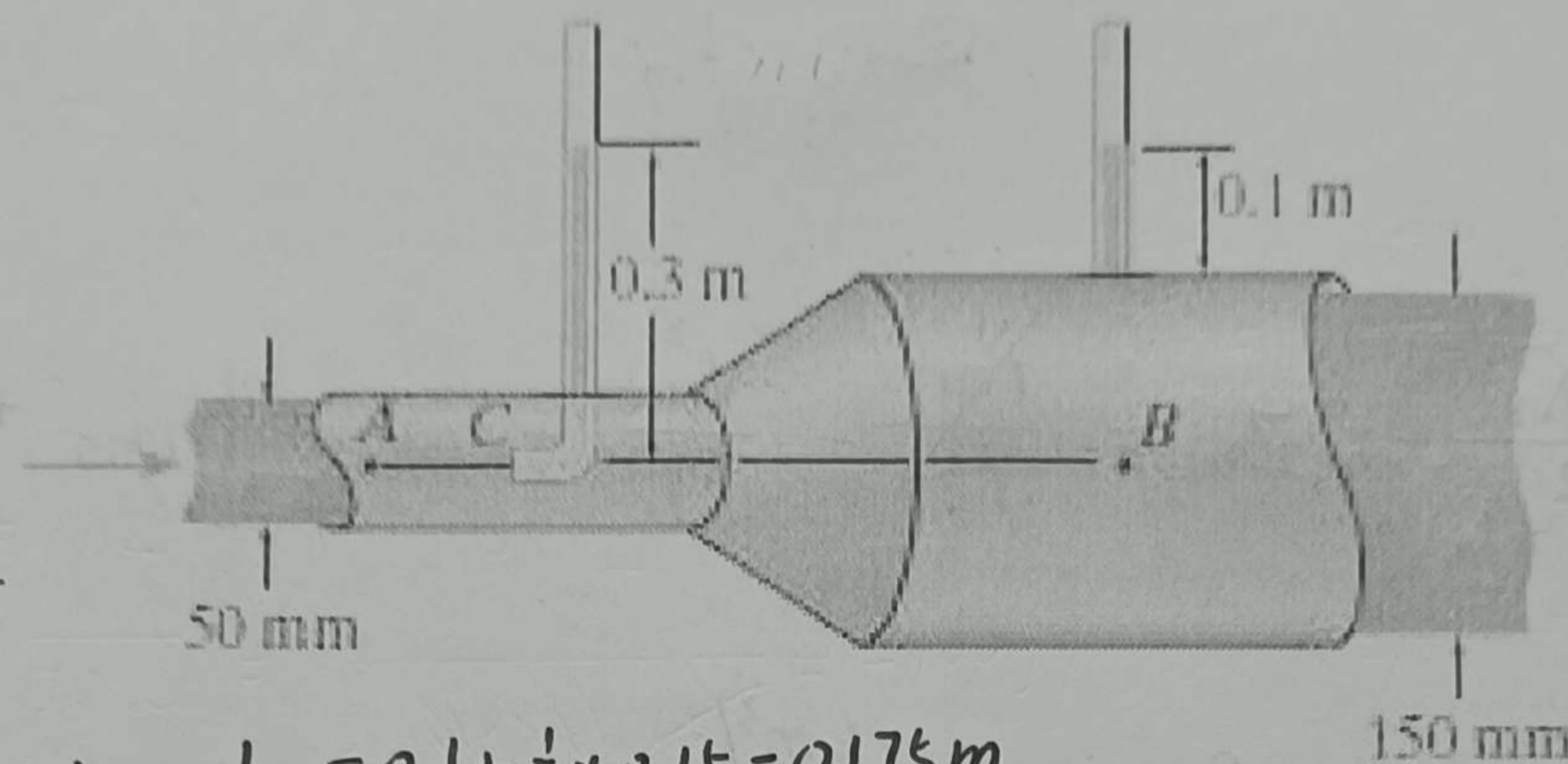
Q5.1 Determine the (volumetric flow) and the pressure in the pipe at A if the height of the (water) column in the Pitot tube is 0.3 m and the height in the piezometer is 0.1 m.

解:

$$\frac{P}{\rho} + \frac{1}{2}v^2 + gz = \text{Const}$$

set reference z : ABC.

$$\frac{P_A}{\rho} + \frac{1}{2}V_A^2 = \frac{P_C}{\rho} + 0 = \frac{P_B}{\rho} + \frac{1}{2}V_B^2$$



$$P_C = \rho g h_C, P_B = \rho g h_B, h_C = 0.3 \text{ m}, h_B = 0.1 + \frac{1}{2} \times 0.15 = 0.175 \text{ m}$$

$$V_A \cdot \pi \left(\frac{d_A}{2}\right)^2 = V_B \cdot \pi \left(\frac{d_B}{2}\right)^2$$

Solve and get: $P_A = -96.32 \text{ kPa}$, $V_A = 14.09 \text{ m/s}$, $V_B = 1.566 \text{ m/s}$, volumetric flow $Q_A = \pi \left(\frac{d_A}{2}\right)^2 \cdot V_A = 2.767 \times 10^{-2} \text{ m}^3/\text{s}$

Q5.2 Oil flows through the [constant-diameter pipe] such that at A the pressure is 50 kPa, and the velocity is 2 m/s. Plot the (pressure head) and the (gravitational head) for AB using a datum at (B). Take $\rho_o = 900 \text{ kg/m}^3$. Assume oil flow is compressible which is a reasonable assumption.

Since constant-diameter

$$V_{AB} \cdot A_{AB} = V_A \cdot A_{AB}$$

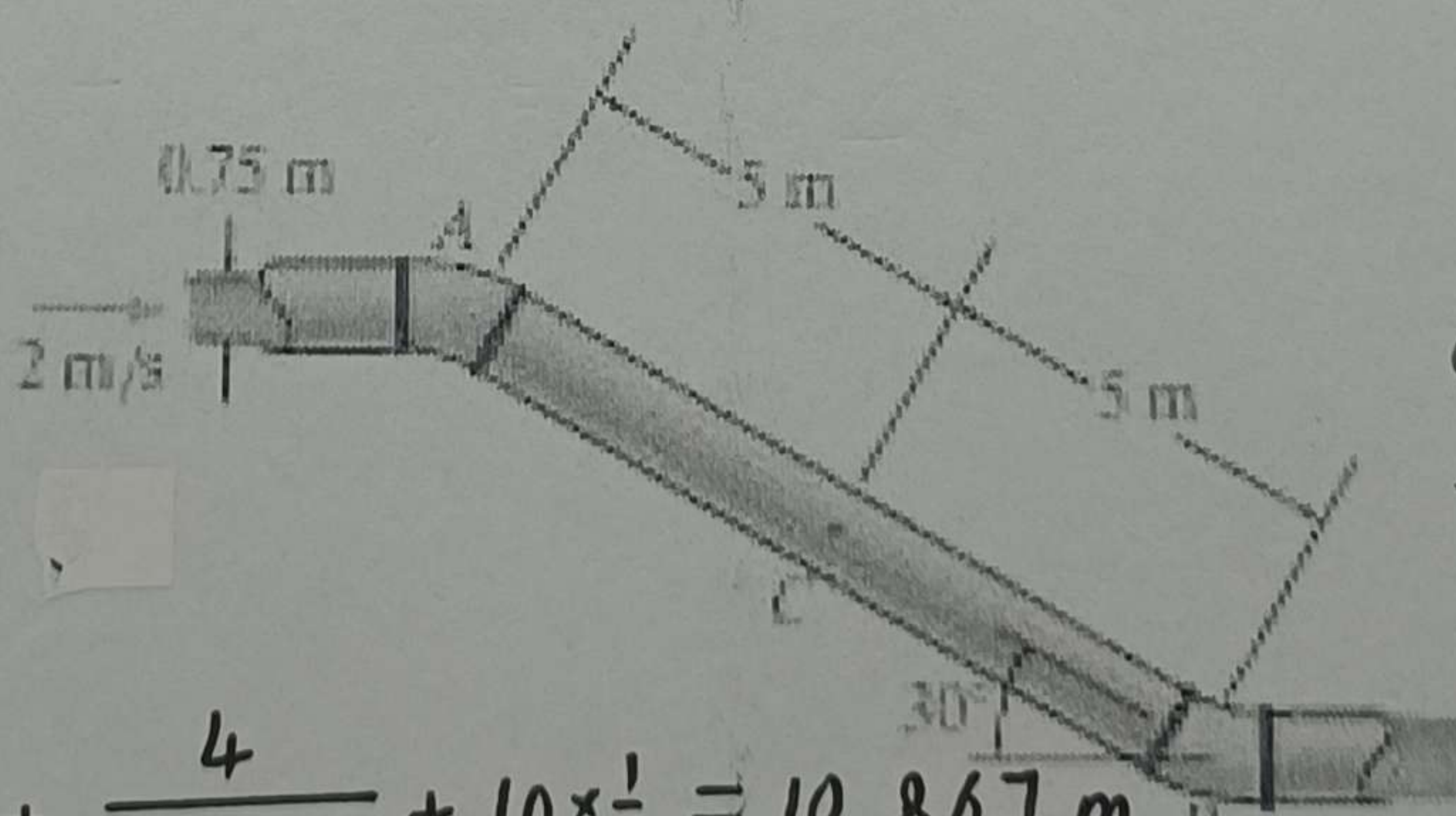
$$V_{AB} = V_A = 2 \text{ m/s}$$

解: $\frac{P}{\rho} + \frac{1}{2}v^2 + gz = \text{Const}$

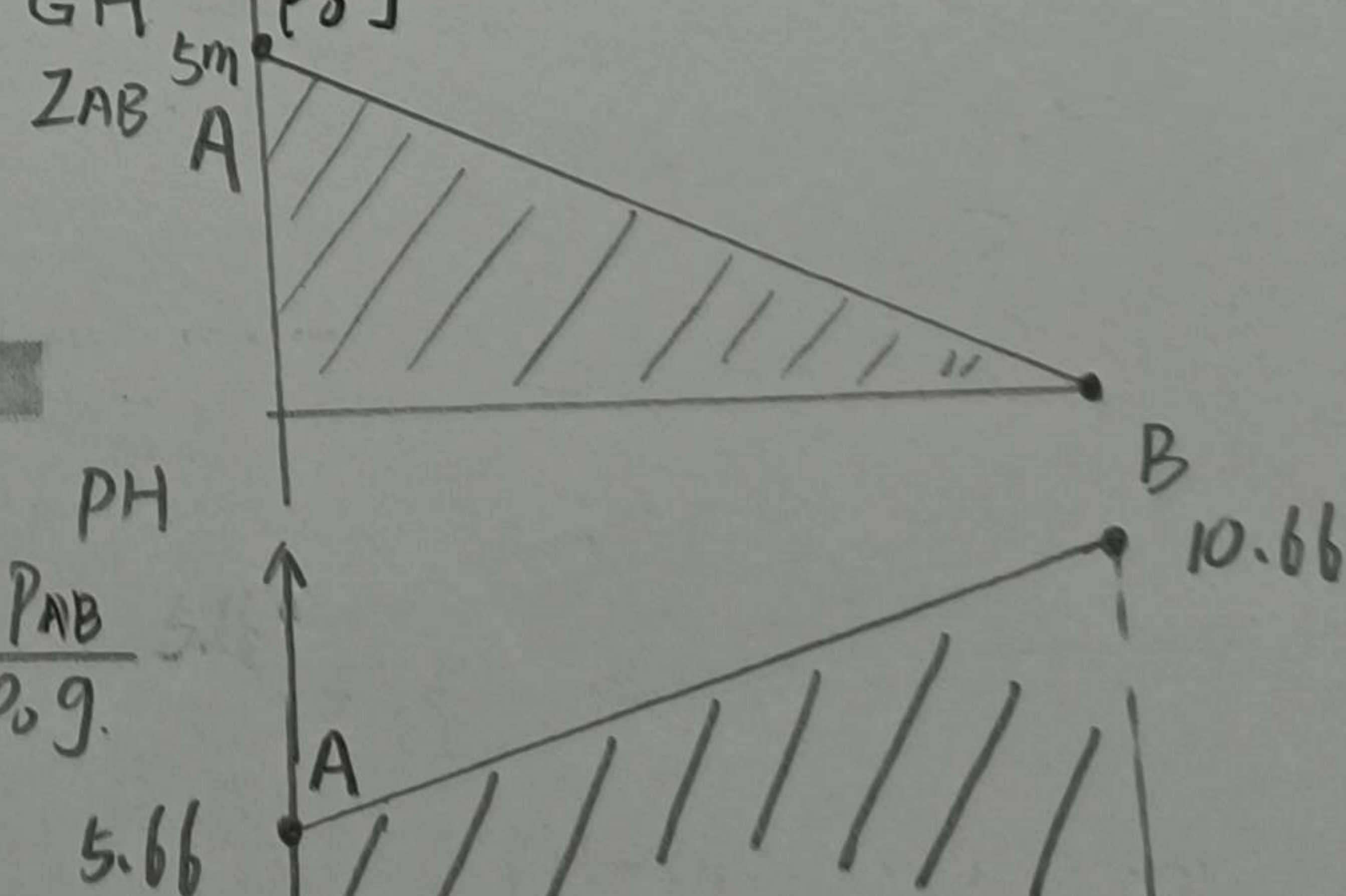
$$\frac{P}{\rho g} + \frac{V^2}{2g} + z = \text{Const}$$

Point A: $\frac{P_A}{\rho_o g} + \frac{V_A^2}{2g} + z_A = \text{Const}$

$$= \frac{50 \times 10^3}{900 \times 9.81} + \frac{4}{2 \times 9.81} + 10 \times \frac{1}{2} = 10.867 \text{ m}$$



$$\frac{P_{AB}}{\rho_o g} + z_{AB} = 10.867 - \frac{4}{2 \times 9.81} = 10.66 \text{ m}$$



for AB: $\frac{P_{AB}}{\rho_o g} + \frac{V_{AB}^2}{2g} + z_{AB} = 10.867 \text{ m}$

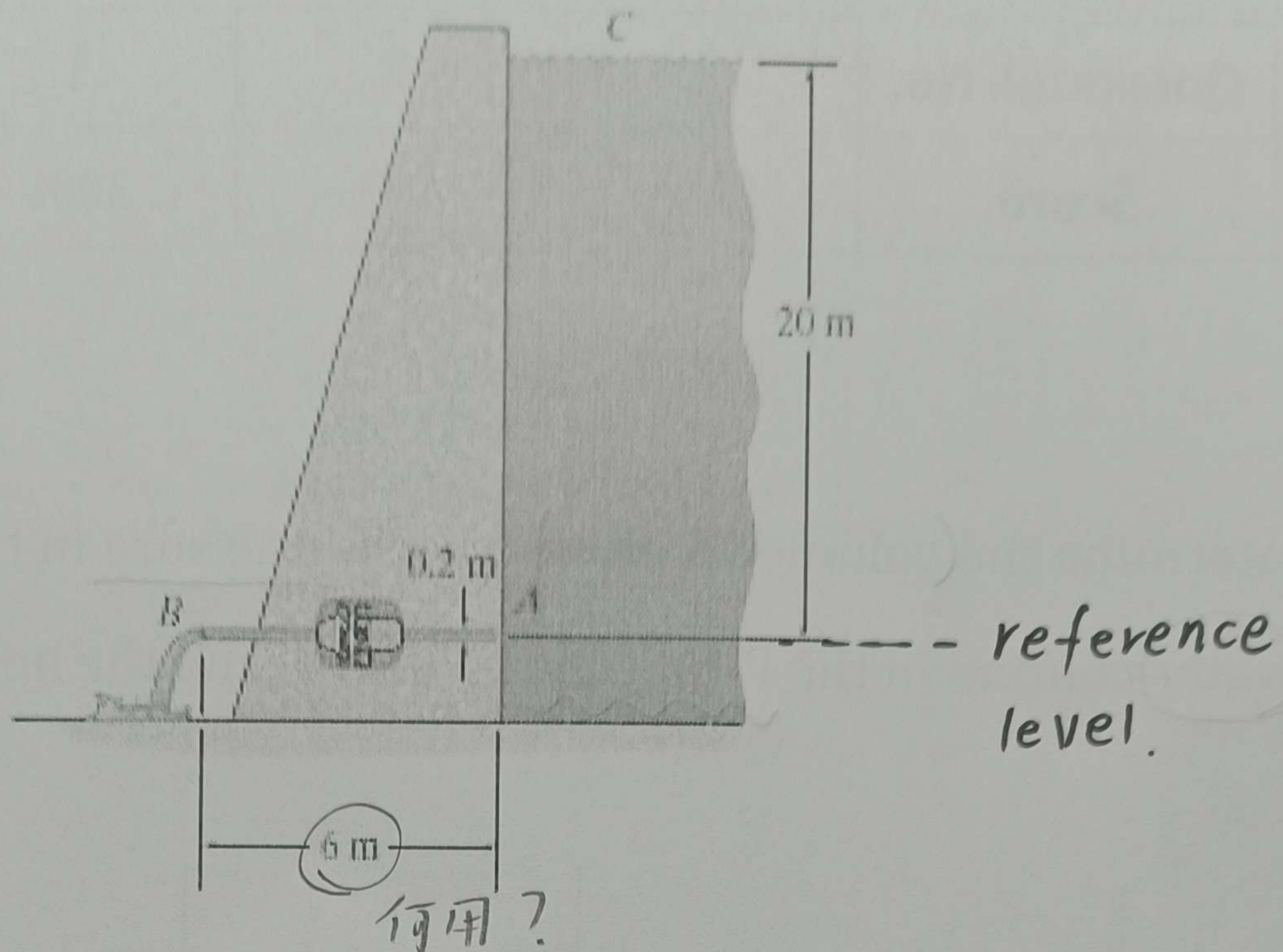
$\frac{P_{AB}}{\rho_o g}$ (PH) $\frac{V_{AB}^2}{2g}$ z_{AB} (GH)

Q5.3 Water in the reservoir flows through the 0.2-m-diameter pipe at A into the turbine. If the discharge at B is $(0.5 \text{ m}^3/\text{s})$ determine the power output of the turbine. Assume the turbine (runs with) an efficiency of 65%, and there is a head

$$\eta = 65\%$$

$$\eta = \frac{h_{\text{turbine, actual}}}{h_{\text{turbine, ideal}}}$$

loss of 0.5m through the pipe.



DDL:2021/05/09

解: $\frac{P_{in}}{\rho g} + \frac{V_{in}^2}{2g} + Z_{in} = \frac{P_{out}}{\rho g} + \frac{V_{out}^2}{2g} + Z_{out} + h_{loss} + h_{turbine, ideal}$

$$P_{in} = P_{out}$$

$$V_{in} = 0, V_{out} = \frac{Q_{out}}{A_{out}} = \frac{0.5 \text{ m}^3/\text{s}}{\pi \times 0.1^2} = 15.92 \text{ m/s}$$

$$Z_{in} = 20 \text{ m}, Z_{out} = 0 \text{ m}$$

$$h_{loss} = 0.5 \text{ m}$$

$$\Rightarrow h_{turbine, ideal} = \left(\frac{15.92^2}{2 \times 9.81} + 0 + 0.5 - 20 \right) = +6.582 \text{ m}$$

$$P_{turbine, out} = \eta \cdot \dot{m} g \cdot h_{turbine, ideal} = 65\% \times \rho \times 0.5 \times 9.81 \times 6.582 = 20.99 \text{ kW}$$