

4.4

解:

$$\tau = \frac{q}{t}$$

$$\tau_1 = \frac{q_1}{2t} = \frac{3}{5} G a \alpha$$

$$\tau_2 = \frac{q_2}{2t} = \frac{7}{5} G a \alpha \quad \frac{7}{10} G a \alpha$$

$$\tau_3 = \frac{q_1 - q_2}{t} = -\frac{1}{5} G a \alpha$$

$$\tau_{\max} = \tau_2 = \frac{7}{5} G a \alpha$$

$$= \frac{7}{5} \times 20 \times 10^9 \times 0.1 \times \frac{5}{180} \times \pi$$

$$= 244.34 \text{ MPa} \times \frac{1}{2}$$

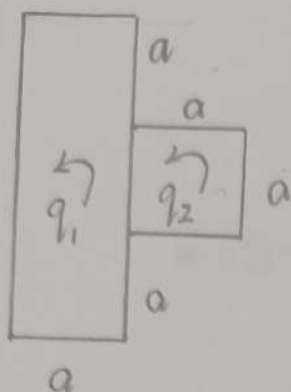
$$= 122.17 \text{ MPa}$$

4.6

10

解:

4.7
解:



$$T = 2A_1 q_1 + 2A_2 q_2$$

$$2GA_1 \alpha = q_1 \cdot \frac{7a}{t} + (q_1 - q_2) \cdot \frac{a}{t}$$

$$2GA_2 \alpha = q_2 \cdot \frac{3a}{t} + (q_2 - q_1) \cdot \frac{a}{t}$$

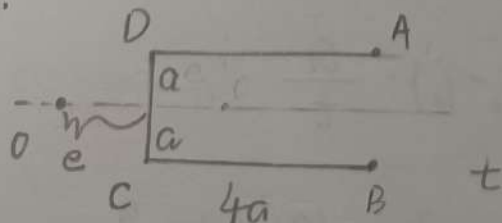
$$A_1 = 3a^2, \quad A_2 = a^2$$

$$\Rightarrow q_1 = \frac{26}{31} a G \alpha t = \frac{13T}{48 a^2} = \frac{13 \times 100}{48 \times 0.1^2} = 2708.3 \text{ N/m}$$

$$q_2 = \frac{22}{31} a G \alpha t = \frac{11T}{48 a^2} = \frac{11 \times 100}{48 \times 0.1^2} = 2291.7 \text{ N/m}$$

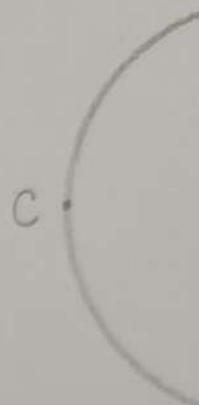
$$\alpha = \frac{31T}{200 G t a^3} = \frac{31 \times 100}{200 \times 20 \times 10^9 \times 5 \times 10^{-3} \times 0.1^3} = 1.55 \times 10^{-4} \text{ rad/m}$$

4.9
解:



$$w_A - w_B = -2\alpha A_s$$

4.12
解:



$$w(s) - w_0 = \frac{1}{2} \alpha s^2$$

$$A = \pi R^2 + 2R^2$$

$$\delta_s = \int_0^s \frac{ds}{t}$$

from A to E:

$$\delta_s = \frac{R \cdot \alpha}{t}$$

$$A_s = \frac{1}{2} \alpha R^2 + \frac{R}{2}$$

where: $\sin(\alpha - \theta)$

$$A \delta_s - A_s \delta =$$

$$= \frac{R}{t}$$

$$= \frac{R}{t}$$

$$f(\alpha) = \alpha - \frac{1}{2} \sin \alpha$$

$$f'(\alpha) = 1 - \frac{1}{2} \cos \alpha$$