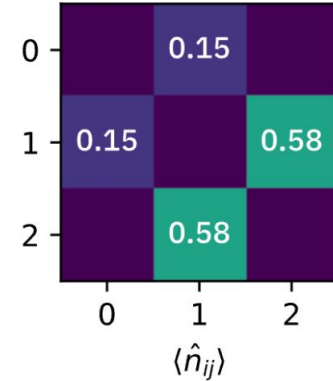
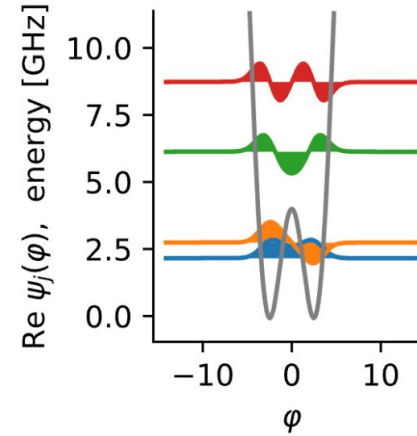


# Leakage Detection in Integer Fluxonium Qubits

**Jiakai Wang**, Vlad Manucharyan, Maxim Vavilov

# Property of fluxoniums

	Long coherence qubit?
half integer fluxonium, $ge$	✓



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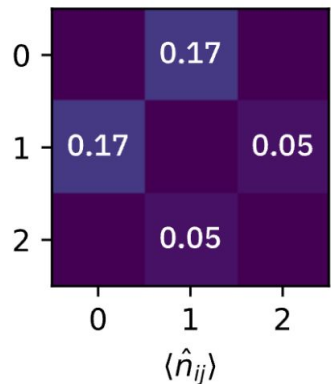
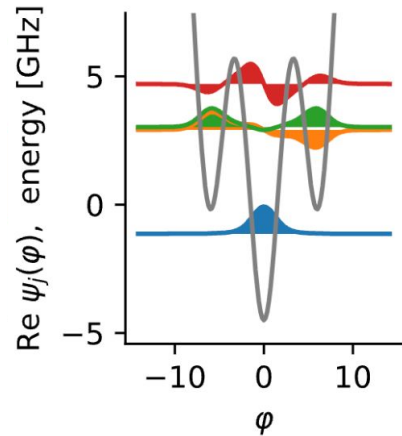
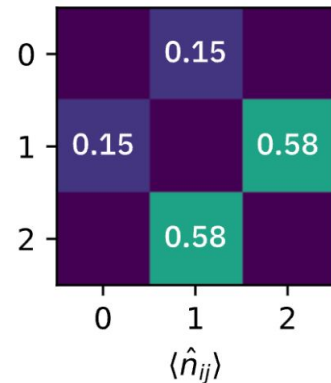
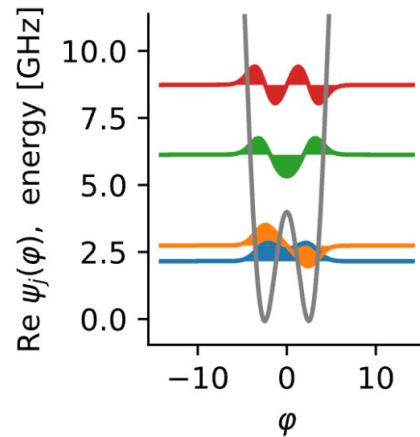
### Millisecond Coherence in a Superconducting Qubit

Aaron Somoroff, Quentin Ficheux, Raymond A. Mencia, Haonan Xiong, Roman Kuzmin, and Vladimir E. Manucharyan

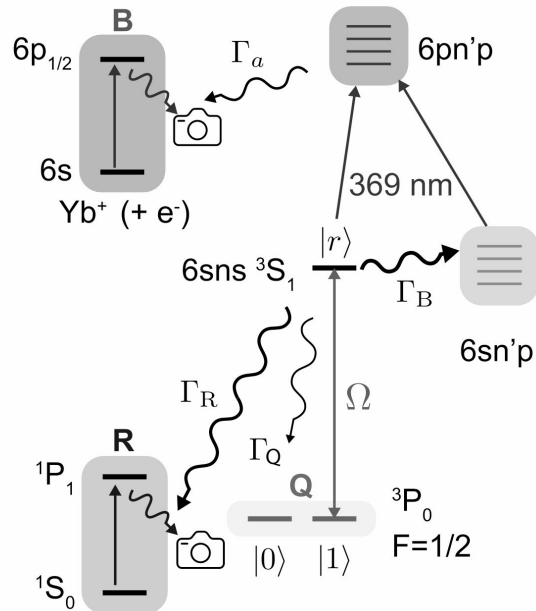
Phys. Rev. Lett. **130**, 267001 – Published 29 June 2023

# Property of fluxoniums

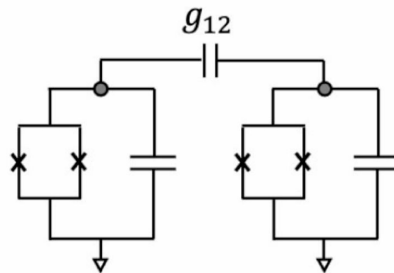
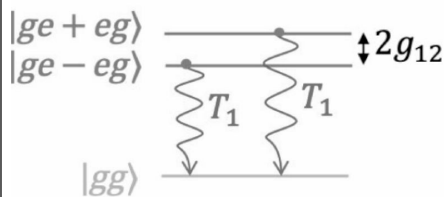
	Long coherence qubit?
half integer fluxonium, ge	✓
integer fluxonium, ge	✓ (preliminary data)
integer fluxonium, ef	✓



# Similarity in error structure



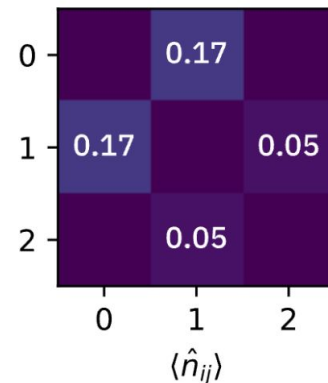
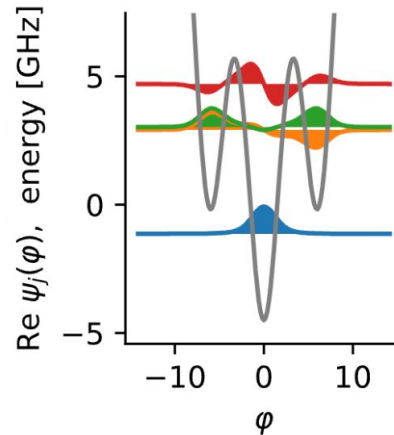
Nature Commun volume 13, 4657 (2022)



Phys. Rev. X **13**, 041022 (2023)

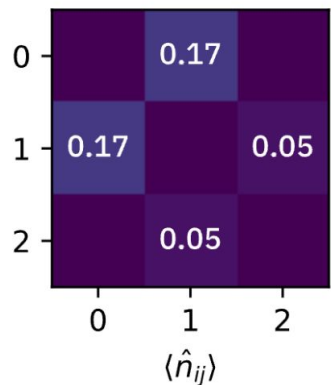
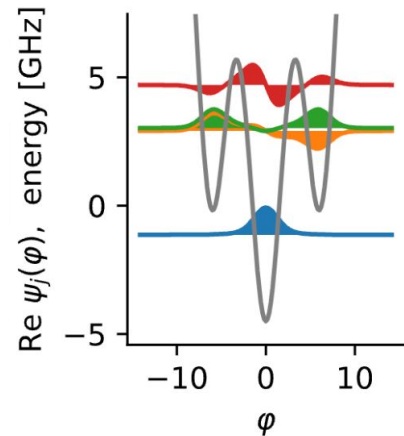
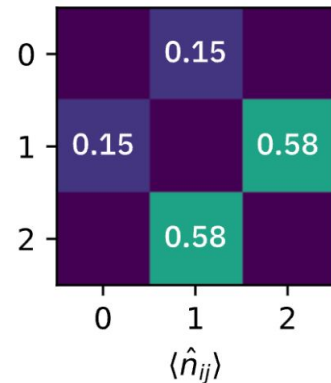
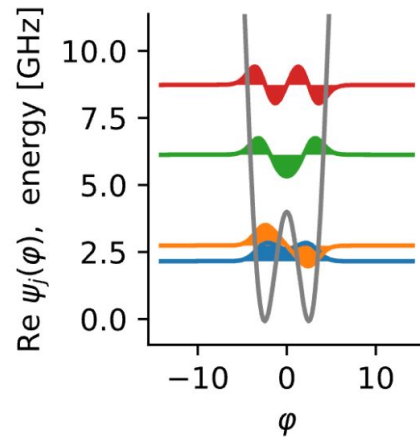
- 1) Highly coherent computational subspace
- 2) Convert most of the leakage to erasure error

(Note that we are not claiming to have a high erasure ratio  $Re = P(\text{erasure})/P(\text{total})$ .)

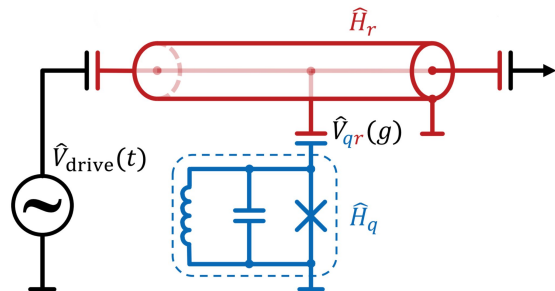


# Property of fluxoniums

	Long coherence qubit?	Potential for erasure conversion?
half integer fluxonium, $g_e$	✓	
integer fluxonium, $g_e$	✓	
integer fluxonium, $e\phi$	✓	✓



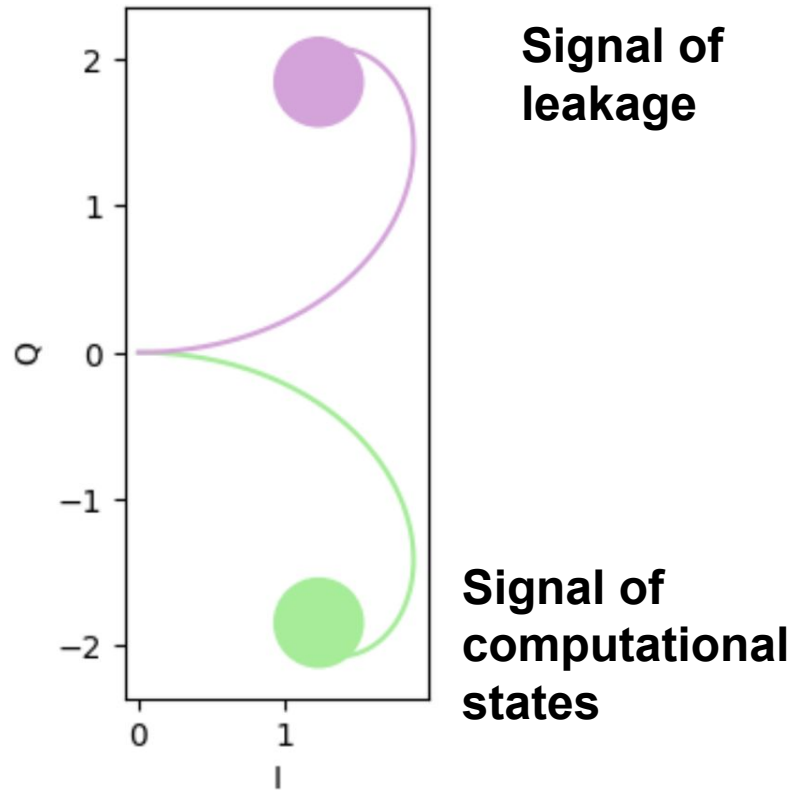
# Minimal cQED readout model



Plot credit : arXiv:2402.07360

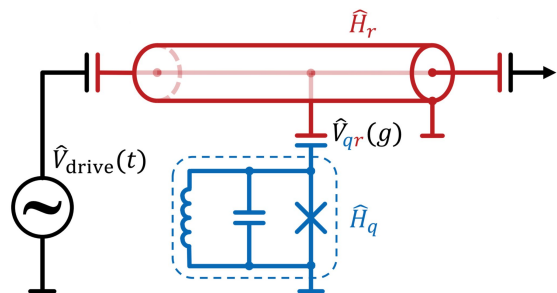
$$\mathcal{H} = \mathcal{H}_r + \mathcal{H}_q + \mathcal{H}_{\text{interaction}}$$

$$\mathcal{H}_{\text{interaction}} = g\hat{n}_r\hat{n}_q$$



We want  $\chi_1, \chi_2$  the same but distinguishable to  $\chi_0$

# Tuning $\omega_{\text{resonator}}$

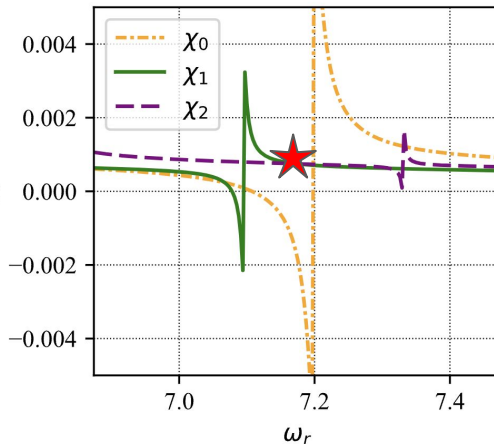
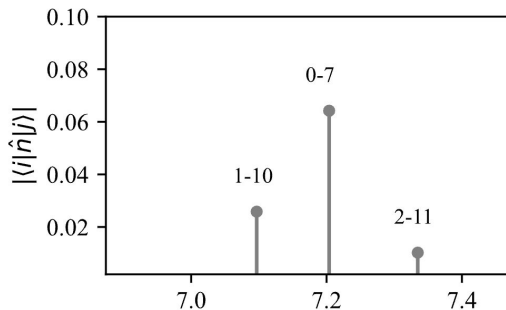


Plot credit : arXiv:2402.07360

$$\mathcal{H} = \mathcal{H}_r + \mathcal{H}_q + \mathcal{H}_{\text{interaction}}$$

Contribution to resonator frequency shift in approximation:

$$|\langle i | \hat{n} | j \rangle|^2 / \Delta_{ij}$$



$$\frac{8.538}{8.538} \frac{|1, 1\rangle}{|1, 1\rangle} \frac{8.560}{8.560} \frac{|2, 1\rangle}{|2, 1\rangle}$$

$$\frac{6.185}{6.184} \frac{|0, 1\rangle}{|0, 1\rangle}$$

$$\frac{1.373}{1.373} \frac{|1, 0\rangle}{|1, 0\rangle} \frac{1.394}{1.394} \frac{|2, 0\rangle}{|2, 0\rangle}$$

$$\frac{-0.981}{-0.981} \frac{|0, 0\rangle}{|0, 0\rangle}$$

(Coupling strength  $g \approx 100\text{MHz}$ )

# Simulation results

$$\mathcal{H} = \mathcal{H}_r + \mathcal{H}_q + \mathcal{H}_{\text{interaction}} + \mathcal{H}_{\text{drive}}$$

$$\mathcal{H}_{\text{drive}} = \Omega(t)(\hat{a} + \hat{a}^\dagger)$$

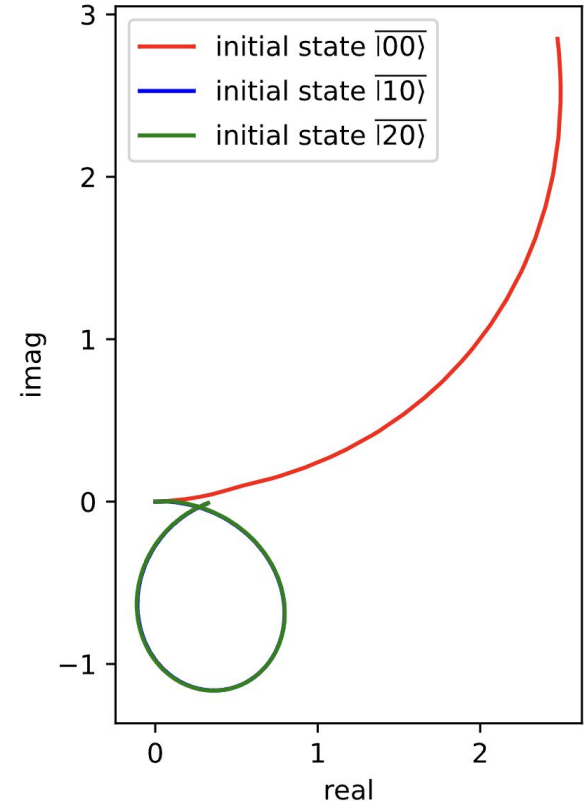
$$\mathcal{D}[\hat{a}]\rho = \kappa \left( \hat{a}\rho\hat{a}^\dagger - \frac{1}{2}\hat{a}^\dagger\hat{a}\rho - \frac{1}{2}\rho\hat{a}^\dagger\hat{a} \right)$$

Criterion for good distinguishability:

$$\sqrt{\kappa} \int_{t_0}^{t_{\text{stop}}} dt' |\langle \hat{\alpha}^l \rangle - \langle \hat{\alpha}^{1,2} \rangle|^2 \gg 1$$



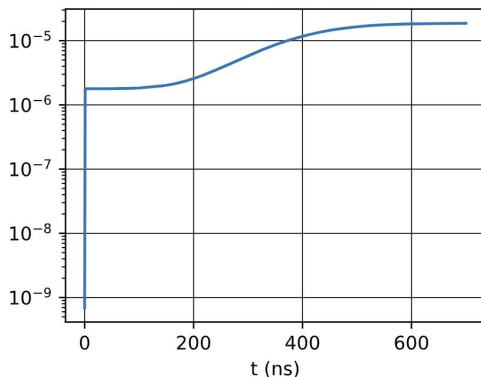
coherent state evolution with  $\kappa = 10^{-3}$  GHz



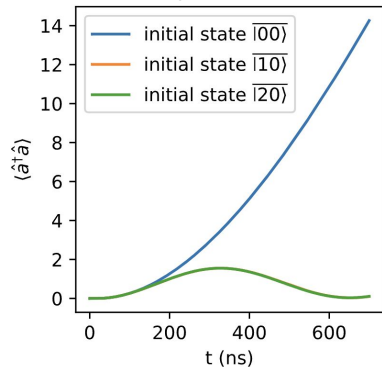


# Photon shot dephasing on computational subspace

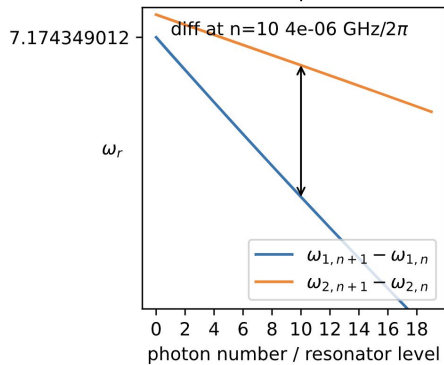
averaged infidelity of computational subspace  
with  $\kappa = 10^{-3}$  GHz



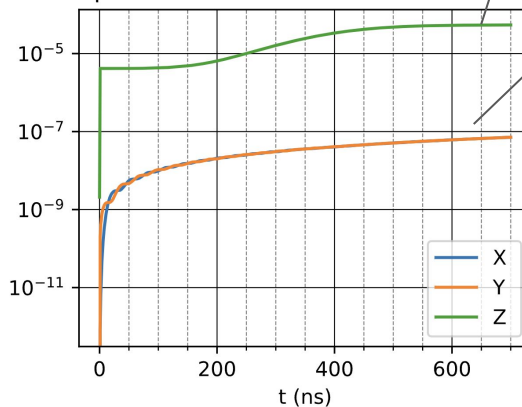
photon number expectation with  $\kappa = 10^{-3}$  GHz



ac-stark shift on computational subspace



pauli error rates with  $\kappa = 10^{-3}$  GHz



Photon shot  
dephasing

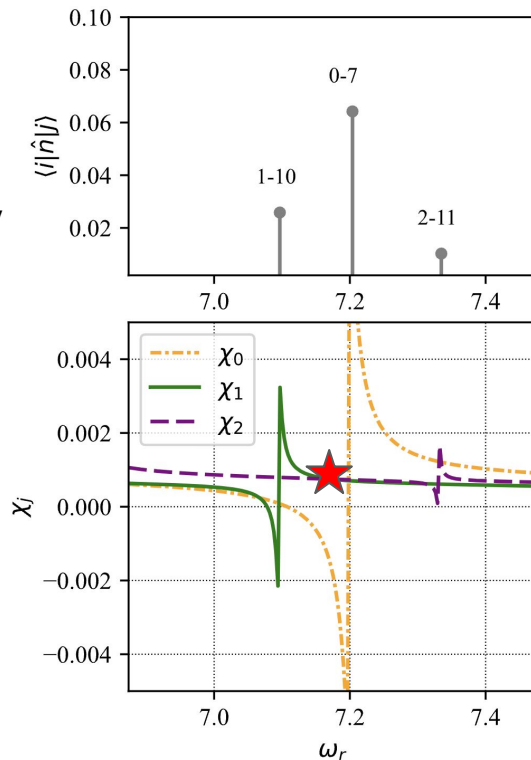
Purcell decay,  
non-dispersive  
contribution  
beyond linear  
resonator  
response

A short note on effective  
Pauli noise models  
Michael A. Perlin  
arXiv:2311.09129

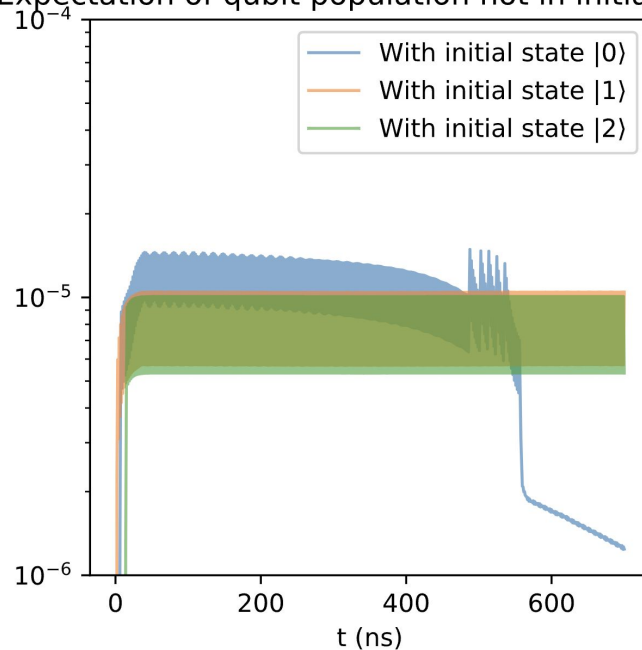
# Leakage to higher levels

Minimal additional leakage,

May be handled by QEC decoder



Expectation of qubit population not in initial state



# Is the detection worth it?

Assume a g-e  $T_1$  of  $300\mu\text{s}$  (preliminary data), then 300 ns would accumulate leakage on the order of  $10^{-3}$ ,

A  $10^{-5}$  fidelity cost of leakage detection is worth doing to remove that  $10^{-3}$  leakage population

# Conclusion

- 1) We propose e-f Integer Fluxonium Qubit with highly coherent computational subspace
- 2) The dominant leakage population can be converted into biased erasure, via high-accuracy, high fidelity dispersive detection

# Outlook

- 1) Experimentally calibrate the lifetime of e-f subspace of Integer Fluxonium,
- 2) Demonstrate the dispersive leakage detection
- 3) Explore architectural design space of this qubit