1 Field Variables

| Symbol | SILO variable name | description |
|---------|---------------------------|--|
| $ ho_i$ | rho_1, rho_2, rho_3, etc. | ith density fraction. |
| s_i | sx, sy, sz | inertial frame momentum |
| z_i | zx, zy, zz | inertial frame spin momentum relative to cell center |
| g_i | gx, gy, gz | gravitational acceleration |
| ϕ | phi | gravitational acceleration |
| E | egas | kinetic + internal energy density |
| τ | tau | entropy tracer |

2 Other Variable

| Symbol | SILO variable name | description |
|---------|--------------------|------------------------------------|
| μ_i | A[i-1] | atomic mass number of ith fraction |
| Z_i | Z[i-1] | electron number of ith fraction |
| Ω | omega | rotation frequency of the grid |

3 Derived Expressions

total mass density

$$\rho := \sum_{i=1}^{N} \rho_i \tag{1}$$

x - velocity relative to grid

$$v_x := \frac{s_x}{\rho} + y\Omega \tag{2}$$

y - velocity relative to grid

$$v_y := \frac{s_y}{\rho} - x\Omega \tag{3}$$

z - velocity relative to grid

$$v_z := \frac{s_z}{\rho} \tag{4}$$

internal gas energy density

$$e := \begin{cases} E - \frac{1}{2} \frac{s^2}{rho} & \text{if } E - \frac{1}{2} \frac{s^2}{rho} > 0.001E \\ \tau^{\gamma} & \text{else} \end{cases}$$
 (5)

number density of ith fraction (ions + electrons)

$$n_i := \frac{\rho_i}{\mu_i m_H} \left(1 + Z_i \right) \tag{6}$$

total number density

$$n := \sum_{i=1}^{N} \tag{7}$$

temperature

$$T := \frac{1}{\gamma - 1} \frac{e}{n} \tag{8}$$

pressure

$$P := (\gamma - 1) e \tag{9}$$