

## Upwind finite difference scheme

### MA573 homework 12

(4) Write a pseudo code for value iteration.

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**Algorithm 1** Value iteration to solve the BVP:  $VI(\hat{\epsilon}, \hat{n})$

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1: Initialize  $\hat{\epsilon}, \hat{n}$ 
2: Initial guess:  $\{v(x) : x \in O^h\}$ 
3:  $flag \leftarrow 1, n \leftarrow 0$ 
4: while  $flag$  do
5:    $\epsilon \leftarrow 0; n \leftarrow n + 1$ 
6:   for  $x \in O^h$  do
7:      $u(x) \leftarrow v(x)$ 
8:      $v(x) \leftarrow F^h u(x)$ 
9:      $\epsilon \leftarrow \max\{\epsilon, |u(x) - v(x)|\}$ 
10:   if  $\epsilon < \hat{\epsilon}$  then
11:      $flag = 0$ 
12:   end if
13: end for
14: end while
15: return  $\{v(x) : x \in O^h\}$ 

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(5) Write a pseudo code for first visit Monte-Carlo method.

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**Algorithm 2** First visit Monte-Carlo method:  $MC(n)$

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1: Initialize  $Tol = 0$ 
2: for  $x \in O^h$  do
3:   for  $i = 1, 2, \dots, n$  do
4:     Generate  $w_i = \{S_0 = x, R_1, S_1, \dots, R_T, S_T, R_{T+1}\}$ 
5:     Compute  $G \leftarrow \sum_{i=1}^{T+1} r^{i-1} R_i$ 
6:      $Tol \leftarrow Tol + G$ 
7:   end for
8:   return  $v(x) \leftarrow \frac{Tol}{n}$ 
9: end for
10: return  $\{v(x) : x \in O^h\}$ 

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