Data Analytics and Machine Learning PS4

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Question 1: Automatic Stock Picking Algorithm

a. Download the data. The firm???level characteristics you will use are lnIssue, lnProf, lnInv, and lnME. For each of these four characteristics, create new, additional characteristics as the squared value of the original characteristic. Name the new characteristics the same as the original, but with a "2" at the end. For instance, for lnProf, the squared value should be lnProf2. Further, create additional characteristics by multiplying each characteristic with lnME (except for lnME itself, which you already have squared). To name these, add _ME at the end. Thus, lnProf interacted with lnME is named lnProf ME. You should have now gone from 4 to 11 characteristics.

library(foreign)

```
## Warning: package 'foreign' was built under R version 3.4.4
library(ggplot2)
## Warning: package 'ggplot2' was built under R version 3.4.4
library(data.table)
## Warning: package 'data.table' was built under R version 3.4.4
setwd("/Users/jiaminghuang/Downloads")
loan <- as.data.table(read.dta("StockRetAcct_insample.dta"))</pre>
loan[,Excess_Ret := exp(lnAnnRet)-exp(lnRf)]
loan1 <- loan[,c("FirmID","year","Excess_Ret","lnIssue","lnProf","lnInv","lnME")]</pre>
loan1[,lnIssue2 := lnIssue^2]
loan1[,lnProf2 := lnProf^2]
loan1[,lnInv2 := lnInv^2]
loan1[,lnME2 := lnME^2]
loan1[,lnIssue_ME := lnIssue * lnME]
loan1[,lnProf_ME := lnProf * lnME]
loan1[,lnInv_ME := lnInv * lnME]
loan1
##
          FirmID year Excess Ret
                                       lnIssue
                                                    lnProf
                                                                 lnInv
##
               6 1980 0.35639972
                                   0.03134417
                                                0.20176707
                                                            0.09362611
       1:
##
                                   0.04421350
               6 1981 -0.39109730
                                                0.21566088
                                                            0.08724214
       3:
##
               6 1982
                       0.06555250 -0.06819496
                                                0.18408749
                                                            0.11166344
##
               6 1983
                       0.53803206 -0.07177968
                                                0.16553123 -0.03311720
##
       5:
              10 1991 -0.46143337 0.11520413
                                                0.23978782
                                                            0.30005118
##
## 70752:
           20314 2010
                       0.21933699
                                                                     NA
                                            NA
                                                        NA
## 70753:
           20314 2011
                       0.07226863
                                            NA -0.89174885
                                                            1.05899596
## 70754:
           20314 2012 2.42904238
                                   0.21500303 -1.26431298
                                                            0.61405981
## 70755:
           20314 2013 1.23447438
                                    0.26048917 -1.16386342
                                                            0.44577339
```

lnProf2

0.18348676 0.03606884

lnInv2

0.77437043

lnME2 lnIssue_ME

70756:

##

20314 2014

lnME

0.11629506

lnIssue2

```
##
       1: 12.58147 0.0009824569 0.040709951 0.008765849 158.2934
##
       2: 12.90800 0.0019548332 0.046509617 0.007611191 166.6164 0.5707076
##
       3: 12.55777 0.0046505530 0.033888202 0.012468723 157.6977 -0.8563770
       4: 12.56195 0.0051523219 0.027400589 0.001096749 157.8027 -0.9016930
##
##
       5: 11.56583 0.0132719906 0.057498197 0.090030712 133.7685
##
## 70752: 14.61343
                             NΑ
                                          NA
                                                      NA 213.5523
                                                                          NA
## 70753: 14.92373
                             NA 0.795216004 1.121472448 222.7178
                                                                          NA
  70754: 15.00809 0.0462263023 1.598487318 0.377069445 225.2426
                                                                   3.2267838
  70755: 16.38328 0.0678546055 1.354578062 0.198713918 268.4119
                                                                   4.2676674
   70756: 17.21366 0.0336673910 0.001300961 0.599649566 296.3099
                                                                   3.1584779
##
            lnProf ME
                        lnInv_ME
##
            2.5385268
                       1.1779543
       1:
       2:
            2.7837499
##
                      1.1261212
##
       3:
            2.3117291
                      1.4022443
##
       4:
            2.0793957 -0.4160168
##
            2.7733454 3.4703413
       5:
##
## 70752:
                   NA
                              NΑ
## 70753: -13.3082206 15.8041717
## 70754: -18.9749170 9.2158619
## 70755: -19.0679023 7.3032311
## 70756:
            0.6208766 13.3297458
```

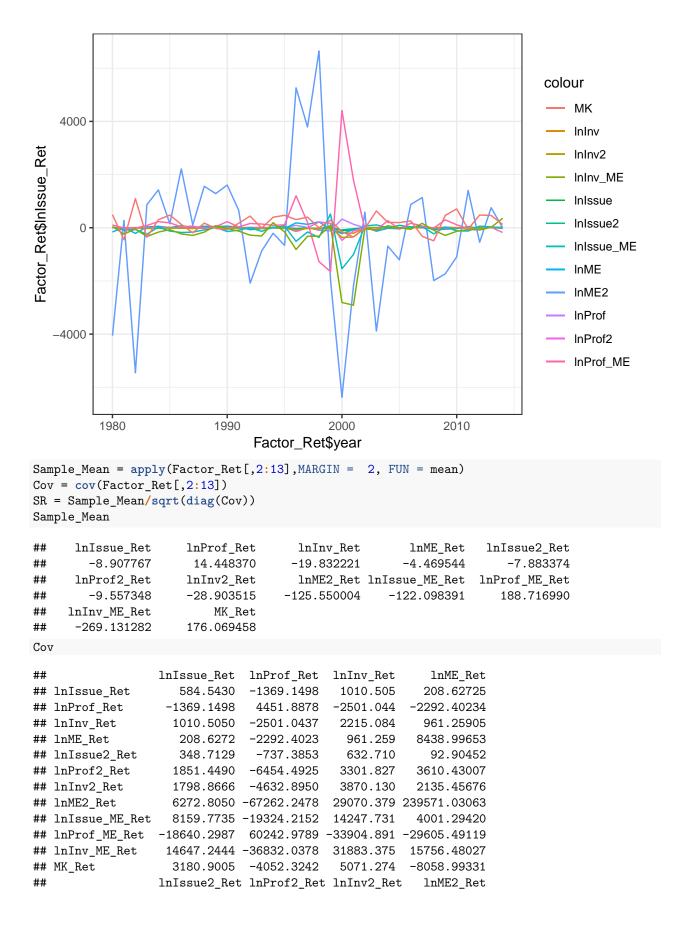
(i) For each year in the sample, cross???sectionally demean each of the 11 characteristics. That is, for each characteristic and each year subtract the average value of that characteristic across stocks. Then add as final characteristic a column of 1's to the dataset. This effectively inserts an intercept in the relation between the MVE portfolio weight and the characteristics.

Next calculate the factor portfolio returns corresponding to each of these 12 characteristics, as explained at the end of the Topic 4 note. Note that the factor corresponding to the constant is simply an equal???weighted portfolio of all stocks (the "market"). The overall idea is that with this approach you have a market factor and long???short characteristics factors. We do not normalize characteristics to have unit variance, as (as an empirical observation) the magnitude of the spread in characteristics across stocks is informative for the portfolio weights. Calculate and report the factor sample means and sample variance???covariance matrix

Calculate and report the factor sample means and sample variance????covariance matrix for these 12 annual factor returns, as well as the factors' sample Sharpe ratios.

```
##demean process
loan1[,lnIssue := ( lnIssue - mean(lnIssue,na.rm = TRUE)), by = year]
loan1[,lnProf := ( lnProf - mean(lnProf,na.rm = TRUE)), by = year]
loan1[,lnInv := ( lnInv - mean(lnInv,na.rm = TRUE)), by = year]
loan1[,lnME := ( lnME - mean(lnME,na.rm = TRUE)), by = year]
loan1[,lnIssue2 := ( lnIssue2 - mean(lnIssue2,na.rm = TRUE)), by = year]
loan1[,lnProf2 := ( lnProf2 - mean(lnProf2,na.rm = TRUE)), by = year]
loan1[,lnInv2 := ( lnInv2 - mean(lnInv2,na.rm = TRUE)), by = year]
loan1[,lnME2 := ( lnME2 - mean(lnME2,na.rm = TRUE)), by = year]
loan1[,lnIssue_ME := ( lnIssue_ME - mean(lnIssue_ME,na.rm = TRUE)), by = year]
loan1[,lnProf_ME := ( lnProf_ME - mean(lnProf_ME,na.rm = TRUE)), by = year]
loan1[,lnInv_ME := ( lnInv_ME - mean(lnInv_ME,na.rm = TRUE)), by = year]
loan1[,Intercept:=1]
# calculate factor return
lnIssue_Ret = loan1[,.(lnIssue_Ret = sum(Excess_Ret*lnIssue,na.rm = TRUE)),by = year]
lnProf_Ret = loan1[,.(lnProf_Ret = sum(Excess_Ret*lnProf,na.rm = TRUE)),by = year]
```

```
lnInv_Ret = loan1[,.(lnInv_Ret = sum(Excess_Ret*lnInv,na.rm = TRUE)),by = year]
lnME_Ret = loan1[,.(lnME_Ret = sum(Excess_Ret*lnME,na.rm = TRUE)),by = year]
lnIssue2_Ret = loan1[,.(lnIssue2_Ret = sum(Excess_Ret*lnIssue2,na.rm = TRUE)),by = year]
lnProf2 Ret = loan1[,.(lnProf2 Ret = sum(Excess Ret*lnProf2,na.rm = TRUE)),by = year]
lnInv2_Ret = loan1[,.(lnInv2_Ret = sum(Excess_Ret*lnInv2,na.rm = TRUE)),by = year]
lnME2_Ret = loan1[,.(lnME2_Ret = sum(Excess_Ret*lnME2,na.rm = TRUE)),by = year]
lnIssue_ME_Ret = loan1[,.(lnIssue_ME_Ret = sum(Excess_Ret*lnIssue_ME,na.rm = TRUE)),by = year]
lnProf ME Ret = loan1[,.(lnProf ME Ret = sum(Excess Ret*lnProf ME,na.rm = TRUE)),by = year]
lnInv ME Ret = loan1[,.(lnInv ME Ret = sum(Excess Ret*lnInv ME,na.rm = TRUE)),by = year]
MK Ret = loan1[,.(MK Ret = sum(Excess Ret*Intercept,na.rm = TRUE)),by = year]
Factor Ret = merge(lnIssue Ret,lnProf Ret,by = "year")
Factor Ret = merge(Factor Ret,lnInv Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnME_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnIssue2_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnProf2_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnInv2_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnME2_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnIssue_ME_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnProf_ME_Ret, by = "year")
Factor_Ret = merge(Factor_Ret,lnInv_ME_Ret, by = "year")
Factor_Ret = merge(Factor_Ret, MK_Ret, by = "year")
ggplot(Factor_Ret,aes(Factor_Ret$year))+
  geom line(aes(y = Factor Ret$lnIssue Ret, col = "lnIssue"))+
  geom_line(aes(y = Factor_Ret$lnProf_Ret, col = "lnProf"))+
  geom line(aes(y = Factor Ret$lnInv Ret, col = "lnInv"))+
  geom line(aes(y = Factor Ret$lnME Ret, col = "lnME"))+
  geom line(aes(y = Factor Ret$lnIssue2 Ret, col = "lnIssue2"))+
  geom_line(aes(y = Factor_Ret$lnProf2_Ret, col = "lnProf2"))+
  geom_line(aes(y = Factor_Ret$lnInv2_Ret, col = "lnInv2"))+
  geom_line(aes(y = Factor_Ret$lnME2_Ret, col = "lnME2"))+
  geom_line(aes(y = Factor_Ret$lnIssue_ME_Ret, col = "lnIssue_ME"))+
  geom_line(aes(y = Factor_Ret$lnProf_ME_Ret, col = "lnProf_ME"))+
  geom_line(aes(y = Factor_Ret$lnInv_ME_Ret, col = "lnInv_ME"))+
  geom_line(aes(y = Factor_Ret$MK_Ret, col = "MK"))+
  theme_bw()
```



```
## lnIssue Ret
                      348.71294
                                   1851.4490
                                                1798.867
                                                            6272.805
## lnProf Ret
                     -737.38527
                                  -6454.4925
                                              -4632.895
                                                          -67262.248
## lnInv Ret
                      632.70999
                                   3301.8273
                                                3870.130
                                                           29070.379
## lnME_Ret
                       92.90452
                                   3610.4301
                                                2135.457
                                                          239571.031
## lnIssue2 Ret
                      271.96691
                                    977.3913
                                                1145.608
                                                            2991.992
## lnProf2 Ret
                      977.39127
                                   9751.0286
                                                6160.744
                                                          106327.184
                     1145.60846
## lnInv2 Ret
                                   6160.7437
                                                6947.559
                                                           63671.966
## lnME2 Ret
                     2991.99186 106327.1842
                                              63671.966 6825870.842
## lnIssue ME Ret
                     4859.52613
                                  26133.5053
                                              25457.156
                                                          118455.413
## lnProf_ME_Ret
                   -10006.52065
                                 -87270.4579
                                              -62772.280
                                                         -870662.459
## lnInv_ME_Ret
                     9113.90652
                                  48836.3567
                                              56017.864
                                                          472514.913
## MK_Ret
                     2084.03573
                                   5400.6552
                                                9086.558 -212268.317
##
                   lnIssue_ME_Ret lnProf_ME_Ret lnInv_ME_Ret
                                                                     MK_Ret
                                       -18640.30
## lnIssue_Ret
                         8159.773
                                                     14647.244
                                                                   3180.901
## lnProf_Ret
                                        60242.98
                                                    -36832.038
                                                                  -4052.324
                       -19324.215
## lnInv_Ret
                        14247.731
                                       -33904.89
                                                     31883.375
                                                                   5071.274
## lnME_Ret
                         4001.294
                                       -29605.49
                                                     15756.480
                                                                  -8058.993
## lnIssue2 Ret
                         4859.526
                                       -10006.52
                                                      9113.907
                                                                   2084.036
## lnProf2 Ret
                        26133.505
                                       -87270.46
                                                     48836.357
                                                                   5400.655
## lnInv2 Ret
                        25457.156
                                       -62772.28
                                                     56017.864
                                                                   9086.558
## lnME2_Ret
                       118455.413
                                      -870662.46
                                                    472514.913
                                                               -212268.317
## lnIssue ME Ret
                       114166.371
                                      -262950.59
                                                    206840.728
                                                                  43510.896
## lnProf_ME_Ret
                      -262950.592
                                       815691.20
                                                   -499162.398
                                                                 -58455.207
## lnInv ME Ret
                       206840.728
                                      -499162.40
                                                    459968.732
                                                                  71918.981
## MK Ret
                        43510.896
                                       -58455.21
                                                     71918.981
                                                                 124932.566
SR
##
                                                                     lnIssue2_Ret
      lnIssue_Ret
                       lnProf_Ret
                                        lnInv_Ret
                                                         lnME_Ret
##
      -0.36843479
                       0.21654430
                                      -0.42138229
                                                      -0.04865391
                                                                      -0.47802881
##
      lnProf2_Ret
                       lnInv2_Ret
                                        lnME2_Ret lnIssue_ME_Ret
                                                                    lnProf_ME_Ret
##
      -0.09678592
                      -0.34676444
                                      -0.04805490
                                                      -0.36136064
                                                                       0.20895276
##
     lnInv_ME_Ret
                           MK_Ret
      -0.39682591
                       0.49813401
##
```

(ii) Next, you are to use the Elastic Net procedure (alpha = 0.5 in glmnet) to estimate the b coefficients. Here, we cannot use the pre???programmed cross???validation procedure in cv.glmnet. The reason is that the right and left hand side variables depend on the sample. You are to run a cross???sectional regression of average returns to the factors on the covariances of each factor with itself and the other factors (see slide 48 in Topic 4). A 5???fold cross???validation would tell you to first find the sample factor averages and sample factor covariance matrix in a 20???year subperiod, and then see how well the estimated b coefficients do in the 5???year out of sample period. In the out of sample

period, the average returns are the 5??? year average factor returns for this period and the covariances are the 5??? year covariances in this period. Thus, due to the combination of time series info (average returns and sample covariance matrix) and the cross??? sectional regression, our setting is a little more complicated than the standard cv.glmnet code.

So, to be clear: first, find sample average factor returns and covariance matrix from 1980???1999. Estimate the Elastic Net using the glmnet procedure (use family = 'Gaussian', alpha = 0.5). This gives you a matrix of b coefficients as a function of lambda. For each of these sets of b coefficients (each vector of b's correspond to a particular lambda), calculate the mean squared error in the out of sample period 2000???2004. Now you have MSE as a function of lambda for one 5???year fold. Then repeat using as in???sample data the 1980???1984 and 1990???2004 period. The out of

sample data is then the 1985???1989 period. Get the MSEs as a function of lambda and save. Repeat until you have done all 5 folds. Then take the average MSE for each value of lambda. Pick the lambda that gives the smallest average MSE. Finally, estimate the elastic net on the full 1980???2004 sample period. Pick the b???coefficient that corresponds to the value of lambda you have chosen.

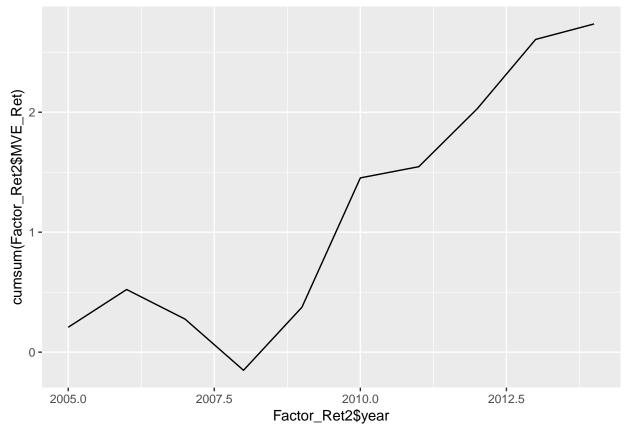
```
library(glmnet)
```

```
## Warning: package 'glmnet' was built under R version 3.4.4
## Loading required package: Matrix
## Loading required package: foreach
## Warning: package 'foreach' was built under R version 3.4.3
## Loaded glmnet 2.0-16
Factor_Ret1 = Factor_Ret
Factor_Ret = Factor_Ret[between(year,1980,2004)]
five_years = c(1980, 1985, 1990, 1995, 2000)
MSEs = NULL
count = 1
for (five_year in five_years) {
  test_sample = Factor_Ret[year >= five_year & year <= five_year+4]</pre>
  train_sample = Factor_Ret[!(year >= five_year & year <= five_year+4)]</pre>
  train_mean = apply(train_sample[,2:13],MARGIN = 2, FUN = mean)
  train_cov = cov(train_sample[,2:13])
  test_mean = apply(test_sample[,2:13],MARGIN = 2, FUN = mean)
  test_cov = cov(test_sample[,2:13])
  out = glmnet(x = train_cov,y = train_mean,family = "gaussian",alpha = 0.5,lambda = seq(300,0,-.1),int
  lambda = out$lambda
  beta = as.matrix(out$beta)
  out = predict(out,newx = test_cov)
  out_sample = data.table(
   lambda = lambda,
   lnIssue_Ret = out[1,],
   lnProf_Ret = out[2,],
   lnInv_Ret = out[3,],
   lnME_Ret = out[4,],
   lnIssue2_Ret = out[5,],
   lnProf2_Ret = out[6,],
   lnInv2_Ret = out[7,],
   lnME2_Ret = out[8,],
   lnIssue_ME_Ret = out[9,],
   lnProf_ME_Ret = out[10,],
   lnInv_ME_Ret = out[11,],
   MK_Ret = out[12,]
  test_pred = as.matrix(out_sample)
  MSE = (test_mean["lnIssue_Ret"]-test_pred[,"lnIssue_Ret"])^2+(test_mean["lnProf_Ret"]-test_pred[,"lnP
             (test_mean["lnInv_Ret"]-test_pred[,"lnInv_Ret"])^2+(test_mean["lnME_Ret"]-test_pred[,"lnME
             (test_mean["lnIssue2_Ret"]-test_pred[,"lnIssue2_Ret"])^2+(test_mean["lnProf2_Ret"]-test_pr
             (test_mean["lnInv2_Ret"]-test_pred[,"lnInv2_Ret"])^2+(test_mean["lnME2_Ret"]-test_pred[,"lnInv2_Ret"]
             (test_mean["lnIssue_ME_Ret"]-test_pred[,"lnIssue_ME_Ret"])^2+(test_mean["lnProf_ME_Ret"]-t
             (test_mean["lnInv_ME_Ret"]-test_pred[,"lnInv_ME_Ret"])^2+(test_mean["MK_Ret"]-test_pred[,":
```

```
MSE = MSE/12
  DT = data.table(
   lambda = lambda,
   MSE = MSE
  )
  colnames(DT) <- c("lambda",five_year)</pre>
  if (count == 1){
   MSEs = DT
  }
  else{
   MSEs = merge(MSEs,DT,by = "lambda")
  count = count + 1
MSE_min = c(min(MSEs$`1980`,na.rm = TRUE),min(MSEs$`1985`,na.rm = TRUE),min(MSEs$`1990`,na.rm = TRUE),m
lambda_min = c(MSEs[MSEs$\)1980\ == min(MSEs$\)1980\,na.rm = TRUE),]$lambda,MSEs[MSEs$\)1985\ == min(MSEs$
lambda_fin = lambda_min[which.min(MSE_min)]
whole_mean = apply(Factor_Ret[,2:13],MARGIN = 2, FUN = mean)
whole_cov = cov(Factor_Ret[,2:13])
out1 = glmnet(x = whole_cov,y = whole_mean,family = "gaussian",alpha = 0.5,intercept = FALSE,lambda = s
beta = out1$beta[,2962]
beta
##
                      lnProf_Ret
                                                      lnME_Ret
     lnIssue_Ret
                                      lnInv_Ret
                                                                 lnIssue2_Ret
   -4.435128e-04
                   0.000000e+00 -2.741984e-03
                                                  6.350011e-04 -2.571694e-02
##
##
     lnProf2_Ret
                      lnInv2_Ret
                                      lnME2_Ret lnIssue_ME_Ret lnProf_ME_Ret
##
    6.153037e-04
                    0.000000e+00
                                   2.484632e-05
                                                  0.000000e+00
                                                                 0.000000e+00
##
    lnInv_ME_Ret
                          MK_Ret
## -7.579993e-05
                    1.244093e-03
out1$lambda[2962]
```

[1] 3.9

(iii) With the final b???vector in hand, calculate the out???of???sample average return, standard deviation, and Sharpe ratio for the corresponding estimated "ex ante" MVE portfolio with return b'F t in the period 2005???2014.



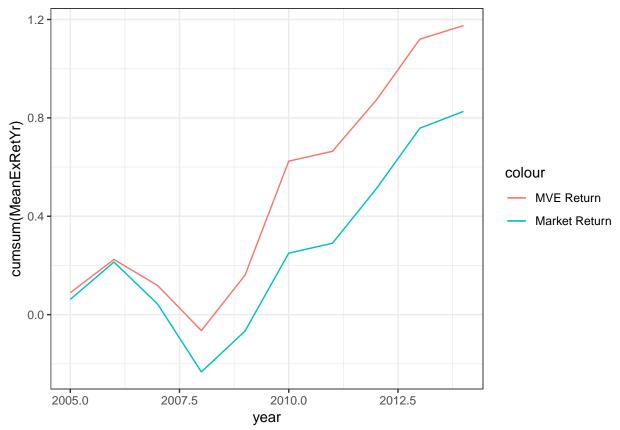
```
average_ret = mean(Factor_Ret2$MVE_Ret)
std_ret = sd(Factor_Ret2$MVE_Ret)
sr_ret = average_ret/std_ret
stat = data.table(
    Mean = average_ret,
    STD = std_ret,
    SR = sr_ret
)
stat
```

Mean STD SR ## 1: 0.2735894 0.4305522 0.6354384

(iv) Plot the cumulative return on this portfolio relative to that on the market (get market return using the value???weights in the sample, MEwt) over the 2005???2014 period, where you normalize the "MVE" portfolio's standard deviation to be the same as the market over this period. Compare. Note that one should really redo the estimation each year to get proper out of sample results that would mimic what you would do in the real world. Also, you could experiment in the in???sample cross???validation with different values for alpha to see what works best.

```
setwd("/Users/jiaminghuang/Downloads")
stockdata <- as.data.table(read.dta("StockRetAcct_insample.dta"))
stockdata[,ExRet:=exp(lnAnnRet) - exp(lnRf)]
setkey(stockdata, year)
vwretd <- stockdata[, list(MeanExRetYr = weighted.mean(ExRet, MEwt, na.rm = T)), by = year]
vwretd = vwretd[between(year,2005,2014)]
multi = sd(vwretd$MeanExRetYr)/std_ret</pre>
```

```
result4 = merge(vwretd,Factor_Ret2[,list(year,MVE_Ret)],by = "year")
result4$MVE_Ret = multi*result4$MVE_Ret
ggplot(data = result4,aes(year))+
  geom_line(aes(y = cumsum(MeanExRetYr),col="Market Return"))+
  geom_line(aes(y = cumsum(MVE_Ret),col = "MVE Return"))+
  theme_bw()
```

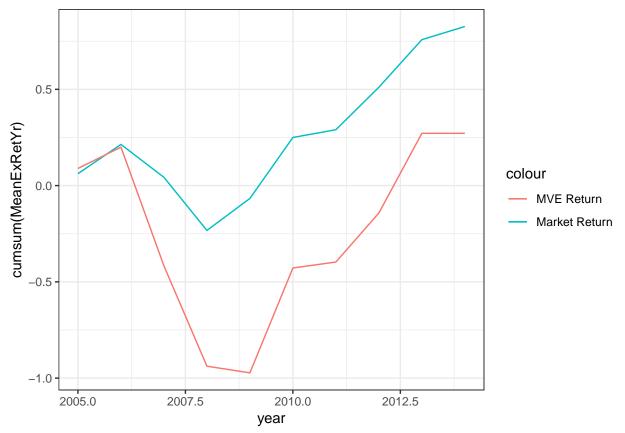


The graph above is the result we redo the estimation every twenty years and hold this bate estimation. We can see the MVE portfolio is better than market.

```
test_year = vwretd$year
for (y in test_year) {
  Factor_test = Factor_Ret1[year == y]
  Factor_train = Factor_Ret1[between(year,y-25,y-1)]
  five_years = c(y-25, y-20, y-15, y-10, y-5)
 MSEs = NULL
  count = 1
  for (five_year in five_years) {
    test_sample = Factor_train[year >= five_year & year <= five_year+4]</pre>
    train_sample = Factor_train[!(year >= five_year & year <= five_year+4)]</pre>
    train_mean = apply(train_sample[,2:13],MARGIN = 2, FUN = mean)
    train_cov = cov(train_sample[,2:13])
    test_mean = apply(test_sample[,2:13],MARGIN = 2, FUN = mean)
    test_cov = cov(test_sample[,2:13])
    out = glmnet(x = train_cov,y = train_mean,family = "gaussian",alpha = 0.5,lambda
                 = seq(300,0,-.1), intercept = FALSE)
    lambda = out$lambda
```

```
beta = as.matrix(out$beta)
    out = predict(out,newx = test_cov)
    out_sample = data.table(
        lambda = lambda,
        lnIssue_Ret = out[1,],
        lnProf_Ret = out[2,],
        lnInv_Ret = out[3,],
        lnME_Ret = out[4,],
        lnIssue2_Ret = out[5,],
        lnProf2_Ret = out[6,],
        lnInv2_Ret = out[7,],
        lnME2_Ret = out[8,],
        lnIssue_ME_Ret = out[9,],
        lnProf_ME_Ret = out[10,],
        lnInv_ME_Ret = out[11,],
       MK_Ret = out[12,]
   test_pred = as.matrix(out_sample)
   MSE = (test_mean["lnIssue_Ret"]-test_pred[,"lnIssue_Ret"])^2+(test_mean["lnProf_Ret"]-test_pred[,"li
                        (test_mean["lnInv_Ret"]-test_pred[,"lnInv_Ret"])^2+(test_mean["lnME_Ret"]-test_pred[,"lnME
                       (\texttt{test\_mean["lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"])^2+}(\texttt{test\_mean["lnProf2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIssue2\_Ret"]-test\_pred[,"lnIs
                        (test_mean["lnInv2_Ret"]-test_pred[,"lnInv2_Ret"])^2+(test_mean["lnME2_Ret"]-test_pred[,"lnInv2_Ret"]
                        (test_mean["lnIssue_ME_Ret"]-test_pred[,"lnIssue_ME_Ret"])^2+(test_mean["lnProf_ME_Ret"]-t
                        (test_mean["lnInv_ME_Ret"]-test_pred[,"lnInv_ME_Ret"])^2+(test_mean["MK_Ret"]-test_pred[,"
   MSE = MSE/12
   DT = data.table(
        lambda = lambda,
        MSE = MSE
   )
   colnames(DT) <- c("lambda",five_year)</pre>
   if (count == 1){
        MSEs = DT
   }
   else{
        MSEs = merge(MSEs,DT,by = "lambda")
    count = count + 1
colnames(MSEs) = c("lambda","1980","1985","1990","1995","2000")
MSE_min = c(min(MSEs$\`1980\`,na.rm = TRUE),min(MSEs$\`1985\`,na.rm =TRUE),min(MSEs$\`1990\`,na.rm = TRUE),
lambda_min = c(MSEs[which.min(MSEs$\cdot1980\),]\$lambda,MSEs[which.min(MSEs\cdot\),]\$lambda,MSEs[which.m
lambda_fin = lambda_min[which.min(MSE_min)]
whole_mean = apply(Factor_train[,2:13],MARGIN = 2, FUN = mean)
whole_cov = cov(Factor_train[,2:13])
out1 = glmnet(x = whole_cov,y = whole_mean,family = "gaussian",alpha = 0.5,intercept = FALSE,lambda =
beta = out1\theta,(300-lambda_fin)*10+1
Factor_Ret2[year == y,MVE_Ret:=beta["lnIssue_Ret"]*lnIssue_Ret+beta["lnProf_Ret"]*lnProf_Ret+beta["ln
                         beta["lnIssue2_Ret"]*lnIssue2_Ret+beta["lnProf2_Ret"]*lnProf2_Ret+beta["lnInv2_Ret"]*lnIn
                         beta["lnIssue_ME_Ret"]*lnIssue_ME_Ret+beta["lnProf_ME_Ret"]*lnProf_ME_Ret+beta["lnInv_ME_
```

```
result4 = merge(vwretd,Factor_Ret2[,list(year,MVE_Ret)],by = "year")
result4$MVE_Ret = multi*result4$MVE_Ret
ggplot(data = result4,aes(year))+
  geom_line(aes(y = cumsum(MeanExRetYr),col="Market Return"))+
  geom_line(aes(y = cumsum(MVE_Ret),col = "MVE Return"))+
  theme_bw()
```



The graph above is the result of redoing the estimation every year. We can see that if we redo the estimation each year, the MVE portfolio is not as good as market.

```
alphas = seq(0,1,0.1)
resultn = NULL
for (alpha in alphas) {
  five_years = c(1980, 1985, 1990, 1995, 2000)
MSEs = NULL
count = 1
for (five_year in five_years) {
  test_sample = Factor_Ret[year >= five_year & year <= five_year+4]</pre>
  train_sample = Factor_Ret[!(year >= five_year & year <= five_year+4)]</pre>
  train_mean = apply(train_sample[,2:13],MARGIN = 2, FUN = mean)
  train_cov = cov(train_sample[,2:13])
  test_mean = apply(test_sample[,2:13],MARGIN = 2, FUN = mean)
  test_cov = cov(test_sample[,2:13])
  out = glmnet(x = train_cov,y = train_mean,family = "gaussian",alpha = alpha,lambda = seq(300,0,-.1),i
  lambda = out$lambda
  beta = as.matrix(out$beta)
```

```
out = predict(out,newx = test_cov)
  out_sample = data.table(
   lambda = lambda,
   lnIssue_Ret = out[1,],
   lnProf_Ret = out[2,],
   lnInv_Ret = out[3,],
   lnME_Ret = out[4,],
   lnIssue2_Ret = out[5,],
   lnProf2_Ret = out[6,],
   lnInv2_Ret = out[7,],
   lnME2_Ret = out[8,],
   lnIssue_ME_Ret = out[9,],
   lnProf_ME_Ret = out[10,],
   lnInv_ME_Ret = out[11,],
   MK_Ret = out[12,]
  test_pred = as.matrix(out_sample)
  MSE = (test_mean["lnIssue_Ret"]-test_pred[,"lnIssue_Ret"])^2+(test_mean["lnProf_Ret"]-test_pred[,"lnP
             (test_mean["lnInv_Ret"]-test_pred[,"lnInv_Ret"])^2+(test_mean["lnME_Ret"]-test_pred[,"lnME
             (test_mean["lnIssue2_Ret"]-test_pred[,"lnIssue2_Ret"])^2+(test_mean["lnProf2_Ret"]-test_pr
             (test_mean["lnInv2_Ret"] -test_pred[,"lnInv2_Ret"])^2+(test_mean["lnME2_Ret"] -test_pred[,"lnInv2_Ret"])
             (test_mean["lnIssue_ME_Ret"]-test_pred[,"lnIssue_ME_Ret"])^2+(test_mean["lnProf_ME_Ret"]-t
             (test_mean["lnInv_ME_Ret"]-test_pred[,"lnInv_ME_Ret"])^2+(test_mean["MK_Ret"]-test_pred[,":
  MSE = MSE/12
  DT = data.table(
   lambda = lambda,
   MSE = MSE
  colnames(DT) <- c("lambda",five_year)</pre>
  if (count == 1){
   MSEs = DT
  }
  else{
   MSEs = merge(MSEs,DT,by = "lambda")
  count = count + 1
MSE_min = c(min(MSEs$`1980`,na.rm = TRUE),min(MSEs$`1985`,na.rm = TRUE),min(MSEs$`1990`,na.rm = TRUE),m
  lambda_min = c(MSEs[which.min(MSEs$\cdot1980\),]\$lambda,MSEs[which.min(MSEs\cdot\),]\$lambda,MSEs[which.m
lambda_fin = lambda_min[which.min(MSE_min)]
whole_mean = apply(Factor_Ret[,2:13],MARGIN = 2, FUN = mean)
whole_cov = cov(Factor_Ret[,2:13])
out1 = glmnet(x = whole_cov,y = whole_mean,family = "gaussian",alpha = alpha,intercept = FALSE,lambda =
beta = out1\theta,(300-lambda_fin)*10+1
Factor_Ret2[,MVE_Ret:=beta["lnIssue_Ret"]*lnIssue_Ret+beta["lnProf_Ret"]*lnProf_Ret+beta["lnInv_Ret"]*l
              beta["lnIssue2_Ret"]*lnIssue2_Ret+beta["lnProf2_Ret"]*lnProf2_Ret+beta["lnInv2_Ret"]*lnIn
              beta["lnIssue_ME_Ret"]*lnIssue_ME_Ret+beta["lnProf_ME_Ret"]*lnProf_ME_Ret+beta["lnInv_ME_
temp = Factor_Ret2[,list(year,MVE_Ret)]
```

```
colnames(temp) = c("year",alpha)
if(is.null(resultn)){
  resultn = temp
}
else{
  resultn = merge(resultn,temp, by = "year")
}
}
colnames(resultn) = c("year", "alpha1", "alpha2", "alpha3", "alpha4", "alpha5", "alpha6"
                       ,"alpha7","alpha8","alpha9","alpha10","alpha11")
ggplot(data = resultn,aes(year))+
  geom_line(aes(y = cumsum(alpha1*multi),col = "alpha=0"))+
  geom_line(aes(y = cumsum(alpha2*multi),col = "alpha=0.1"))+
  geom_line(aes(y = cumsum(alpha3*multi),col = "alpha=0.2"))+
  geom_line(aes(y = cumsum(alpha4*multi),col = "alpha=0.3"))+
  geom line(aes(y = cumsum(alpha5*multi),col = "alpha=0.4"))+
  geom_line(aes(y = cumsum(alpha6*multi),col = "alpha=0.5"))+
  geom_line(aes(y = cumsum(alpha7*multi),col = "alpha=0.6"))+
  geom_line(aes(y = cumsum(alpha8*multi),col = "alpha=0.7"))+
  geom_line(aes(y = cumsum(alpha9*multi),col = "alpha=0.8"))+
  geom_line(aes(y = cumsum(alpha10*multi),col = "alpha=0.9"))+
  geom_line(aes(y = cumsum(alpha11*multi),col = "alpha=1"))+
  theme_bw()+xlim(2005,2014)
   1.5
                                                                                colour
                                                                                    alpha=0
                                                                                    alpha=0.1
cumsum(alpha1 * multi)
                                                                                    alpha=0.2
   1.0
                                                                                    alpha=0.3
                                                                                    alpha=0.4
                                                                                    alpha=0.5
                                                                                    alpha=0.6
   0.5
                                                                                    alpha=0.7
                                                                                    alpha=0.8
                                                                                    alpha=0.9
                                                                                    alpha=1
   0.0
       2005.0
                         2007.5
                                          2010.0
                                                            2012.5
                                       year
```

From the graph above, we know that the out of sample estimation will be better with larger alpha.