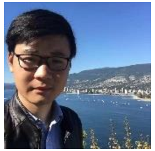
深蓝学院
shenlanxueyuan.com

Lecture 2

SEARCH-BASED PATH FINDING



主讲人 Fei Gao

Ph.D. in Robotics
Hong Kong University of Science and Technology
Assistant Professor，Zhejiang University

Outline

1. Graph Search Basis
2. Dijkstra and A*
3. Jump Point Search
4. Homework

Graph Search Basis

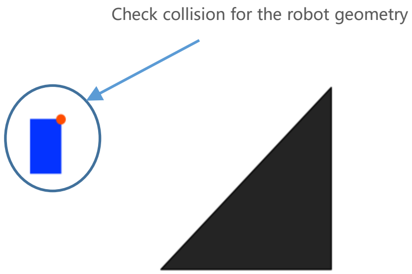
Configuration Space

Configuration Space

- **Robot configuration:** a specification of the positions of all points of the robot
- **Robot degree of freedom (DOF):** The minimum number n of real-valued coordinates needed to represent the robot configuration
- **Robot configuration space:** a n-dim space containing all possible robot configurations, denoted as C-space
- **Each robot pose is a point in the C-space**

Configuration Space Obstacle

- Planning in workspace
  - Robot has different shape and size
  - Collision detection requires knowing the robot geometry - time consuming and hard

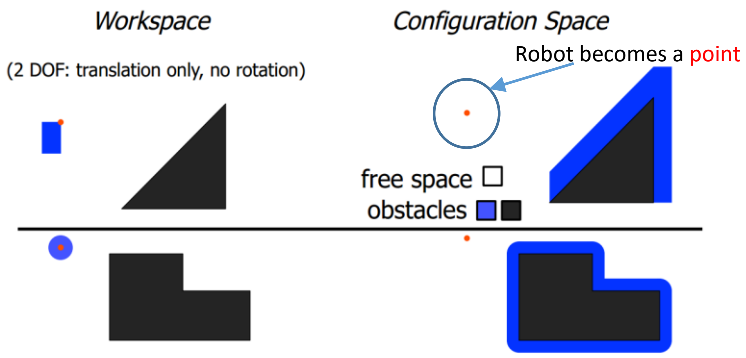


(1) Rectangular mobile robot

(2) Circular mobile robot

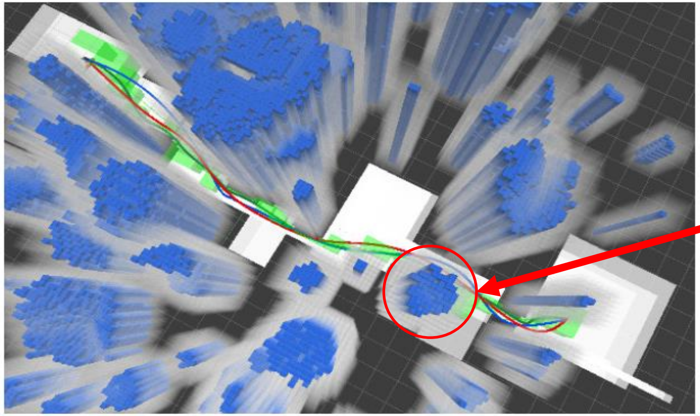
Configuration Space Obstacle

- Planning in configuration space
  - Robot is represented by a point in C-space, e.g. position (a point in R^3), pose (a point in $SO(3)$),etc.
  - Obstacles need to be represented in configuration space (one-time work prior to motion planning), called configuration space obstacle, or C-obstacle
  - C-space = (C-obstacle) ∪ (C-free)
  - The path planning is finding a path between start point q_{start} and goal point q_{goal} within C-free



Workspace and Configuration Space Obstacle

- In workspace
  - Robot has shape and size (i.e. hard for motion planning)
- In configuration space: C-space
  - Robot is a point (i.e. easy for motion planning)
  - Obstacle are represented in C-space prior to motion planning
- Representing an obstacle in C-space can be extremely complicated. So approximated (but more conservative) representations are used in practice.



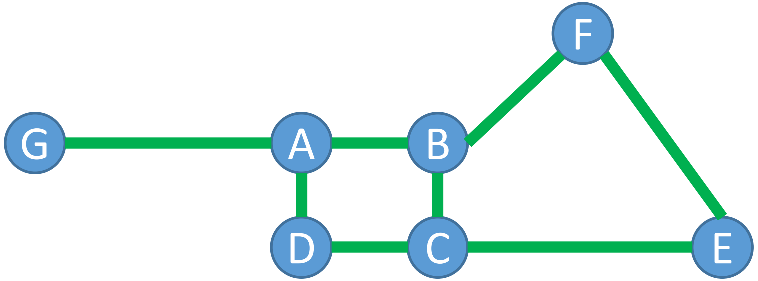
If we model the robot conservatively as a ball with radius δ_r, then the C-space can be constructed by inflating obstacle at all directions by δ_r.

Graph and Search Method

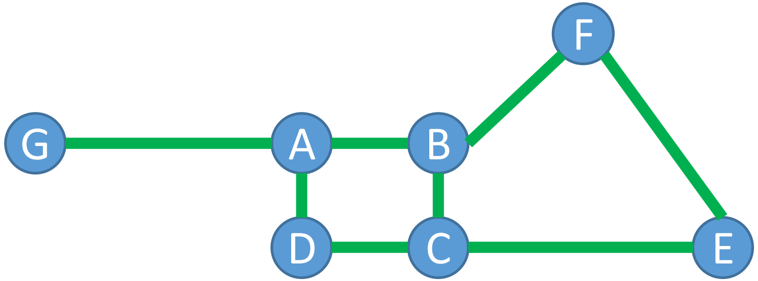
Search-based Method

Graphs

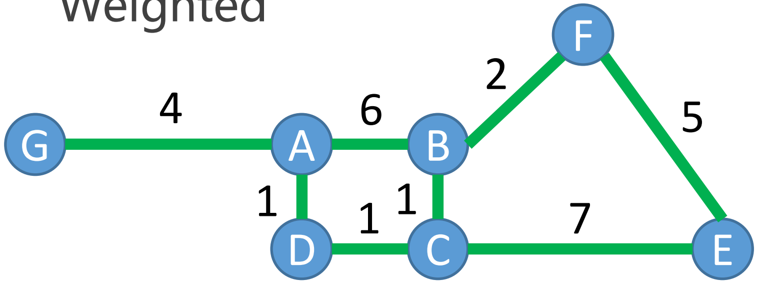
Graphs have nodes and edges



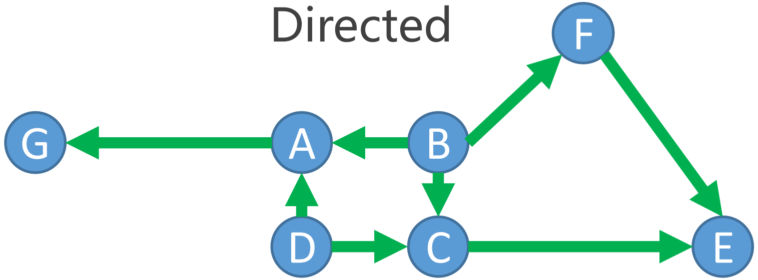
Undirected



Weighted

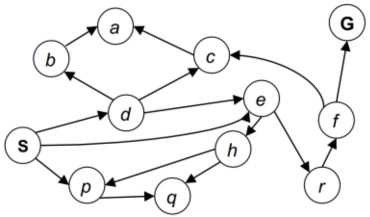


Directed

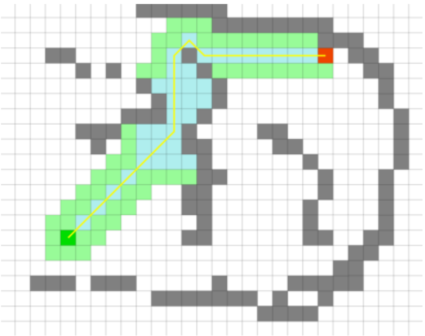


Search-based Method

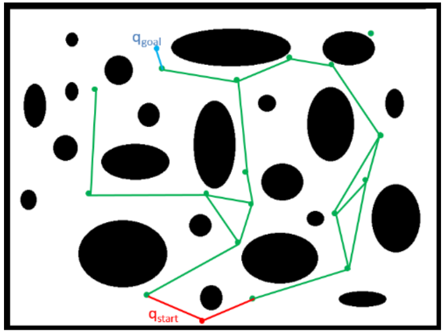
- State space graph: a mathematical representation of a search algorithm
  - For every search problem, there's a corresponding state space graph
  - Connectivity between nodes in the graph is represented by (directed or undirected) edges



Ridiculously tiny search graph for a tiny search problem



Grid-based graph: use grid as vertices and grid connections as edges

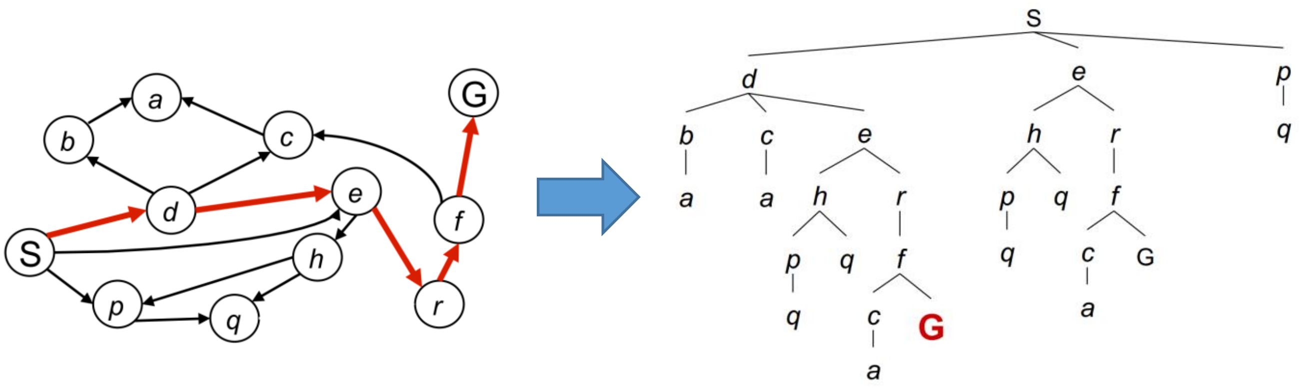


The graph generated by probabilistic roadmap (PRM)

Graph Search Overview

- The search always start from start state X_S
  - Searching the graph produces a search tree
  - Back-tracing a node in the search tree gives us a path from the start state to that node
  - For many problems we can never actually build the whole tree, too large or inefficient – we only want to reach the goal node asap.

生成树：再回溯
代价大 不推荐



Graph Search Overview

- Maintain a container to store all the nodes to be visited
- The container is initialized with the start state X_S
- Loop
  - Remove a node from the container according to some pre-defined score function
    - Visit a node 访问一个节点（弹出一个
  - Expansion: Obtain all neighbors of the node
    - Discover all its neighbors 发现新的邻居节点（以后可能会访问
  - Push them (neighbors) into the container

    新发现的放入container
- End Loop

  找到goal/container没有任何节点，循环结束

Graph Search Overview

- Question 1: When to end the loop?
  - Possible option: End the loop when the container is empty

定义循环结束的条件：找到goal，需要访问的container空

- Question 2: What if the graph is cyclic?
  - When a node is removed from the container (expanded / visited), it should never be added back to the container again

避免图是回环的： 另一个container只进不出保存visited过的

- Question 3: In what way to remove the right node such that the goal state can be reached as soon as possible, which results in less expansion of the graph node.

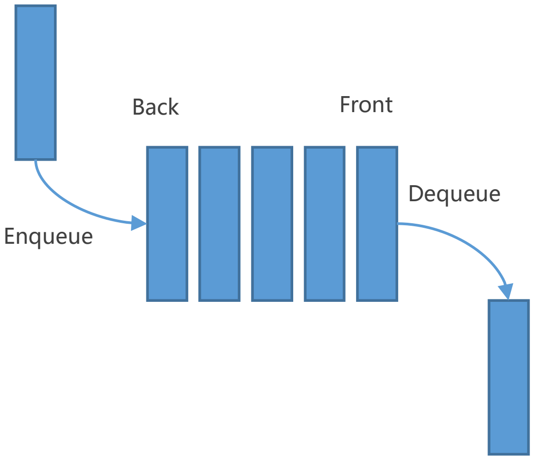
尽可能快

Graph Traversal

图的遍历

- Breadth First Search (BFS) vs. Depth First Search (DFS)

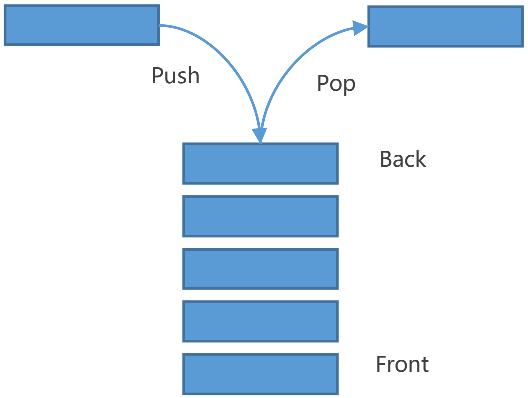
BFS uses “first in first out”



This is a queue

广度优先：用队列，先进先出

DFS uses “last in first out”



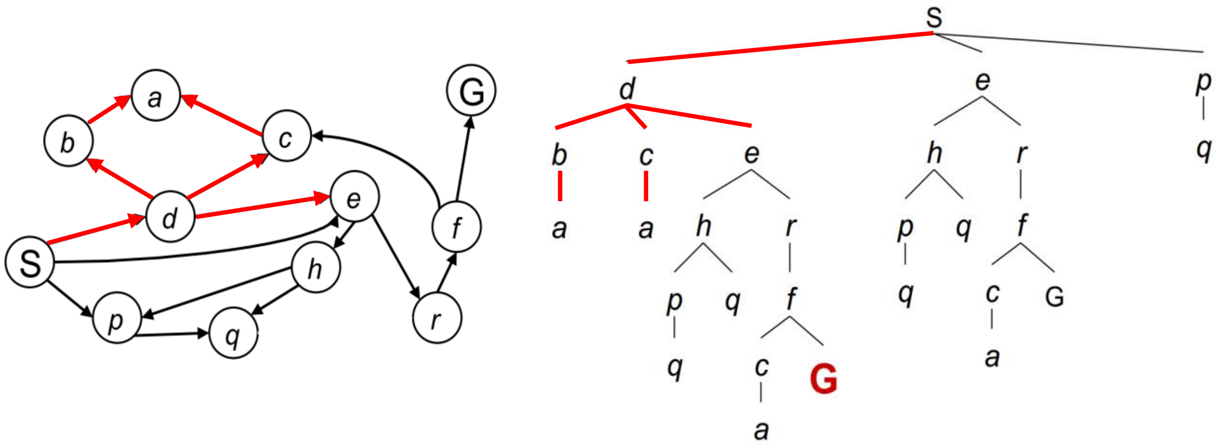
This is a stack

深度优先：堆栈，后进先出

Depth First Search (DFS)

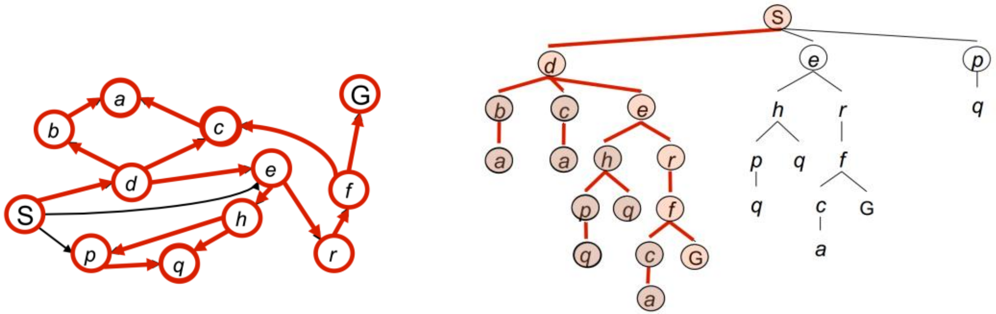
每次弹出的（访问）都是已有的最深层级的节点--将一个分支走到底

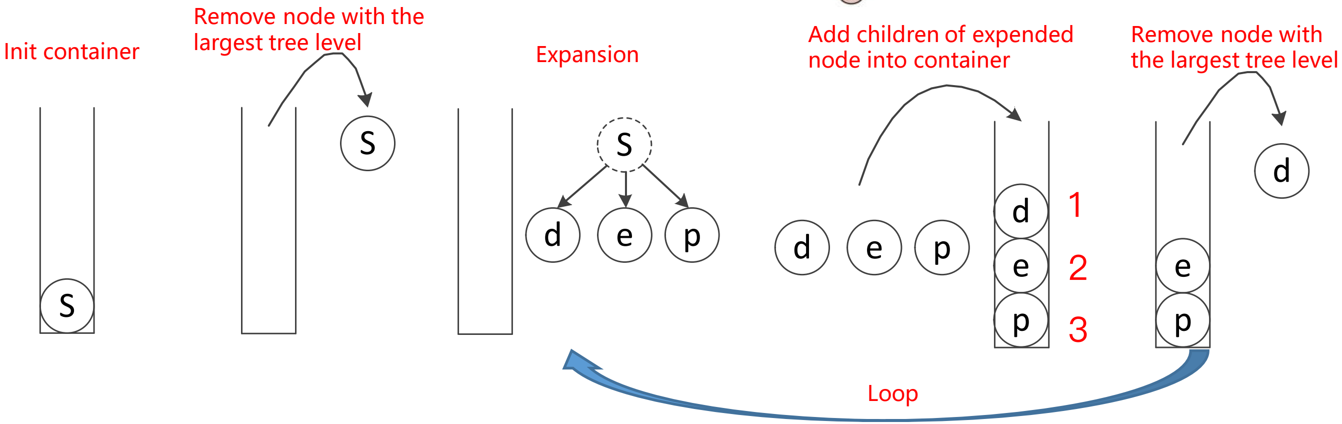
- Strategy: remove / expand the deepest node in the container



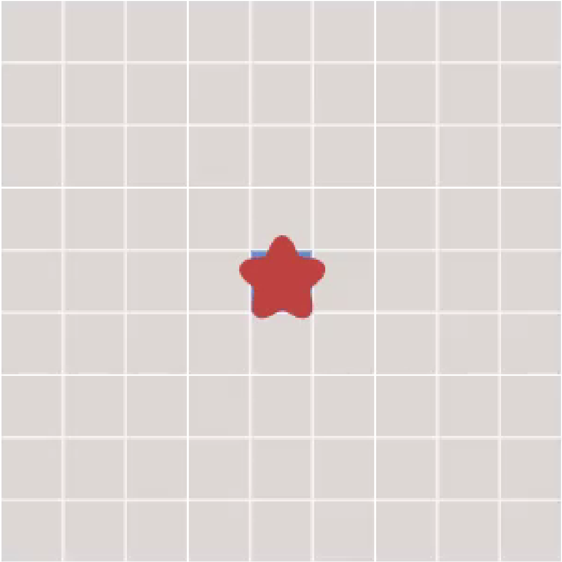
Depth First Search (DFS)

- Implementation: maintain a last in first out (LIFO) container (i.e. stack)





Depth First Search (DFS)

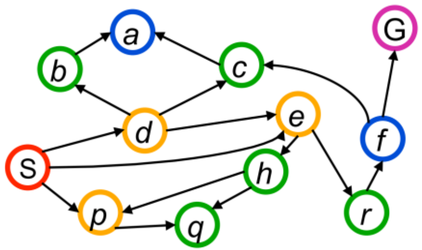


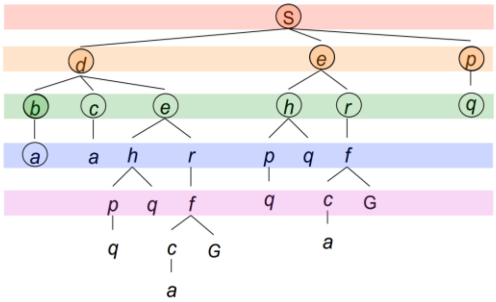
Courtesy: Amit Patel's Introduction to A*, Stanford

Breadth First Search (BFS)

优先弹出层级最浅的节点

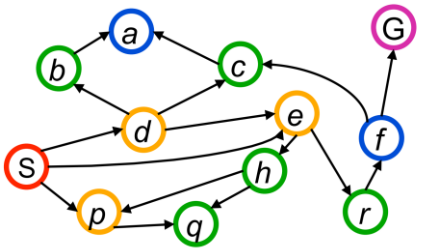
- Strategy: remove / expand the shallowest node in the container

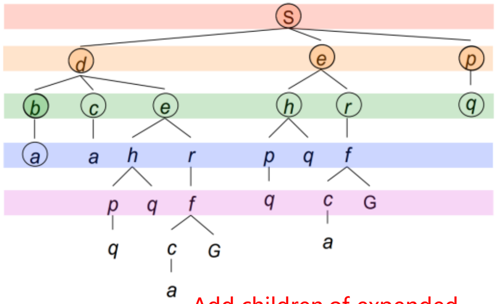


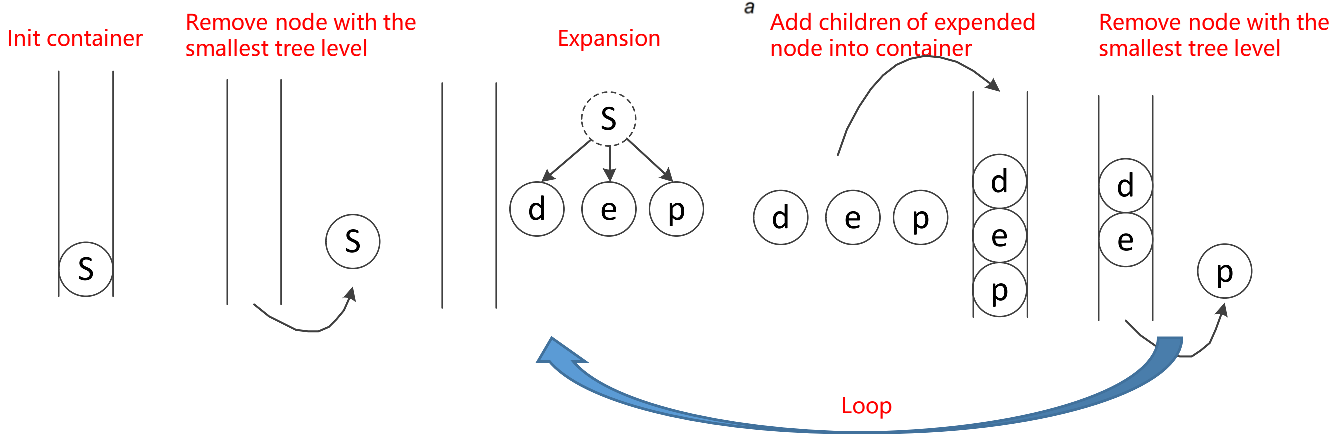


Breadth First Search (BFS)

- Implementation: maintain a first in first out (FIFO) container (i.e. queue)

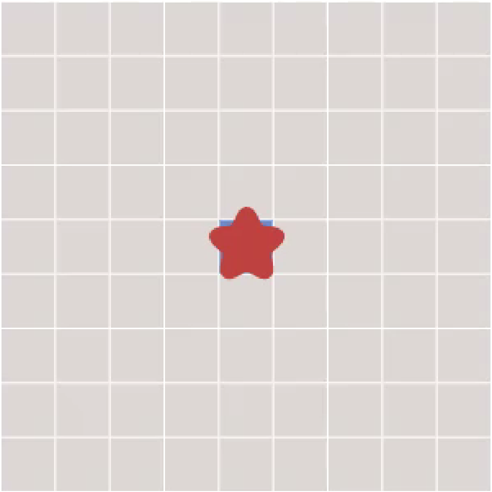






Breadth First Search (BFS)

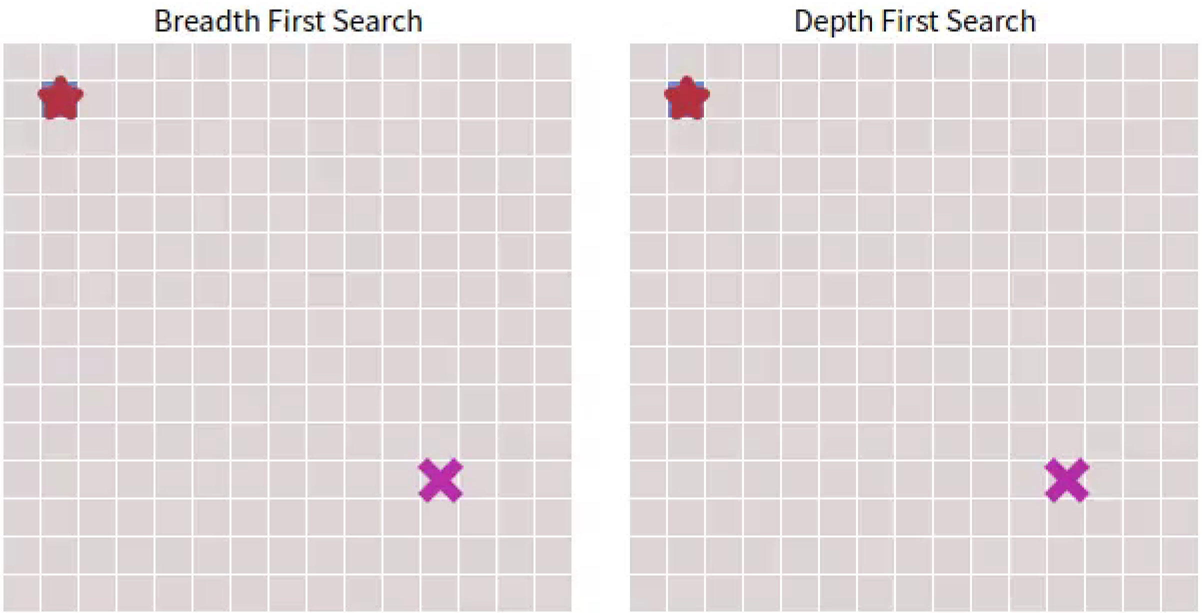
不断扩展前线frontier



Courtesy: Amit Patel's Introduction to A*, Stanford

BFS vs. DFS: which one is useful?

BFS更适合找最短路径



Remember BFS.

Heuristic search

启发式搜索算法

Greedy Best First Search

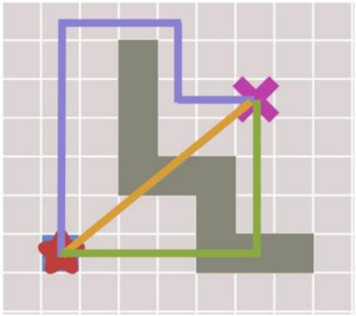
BFS：下一个需要访问的节点是最浅的， queue 先入先出
DFS： 下一个需要访问的节点最深的， stack 后入先出

- BFS and DFS pick the next node off the frontiers based on which was “first in” or “last in”.
- Greedy Best First picks the “best” node according to some rule, called a heuristic. 贪心算法：根据制定的heuristic启发

- Definition: A heuristic is a guess of how close you are to the target.

- A heuristic guides you in the right direction.
- A heuristic should be easy to compute.

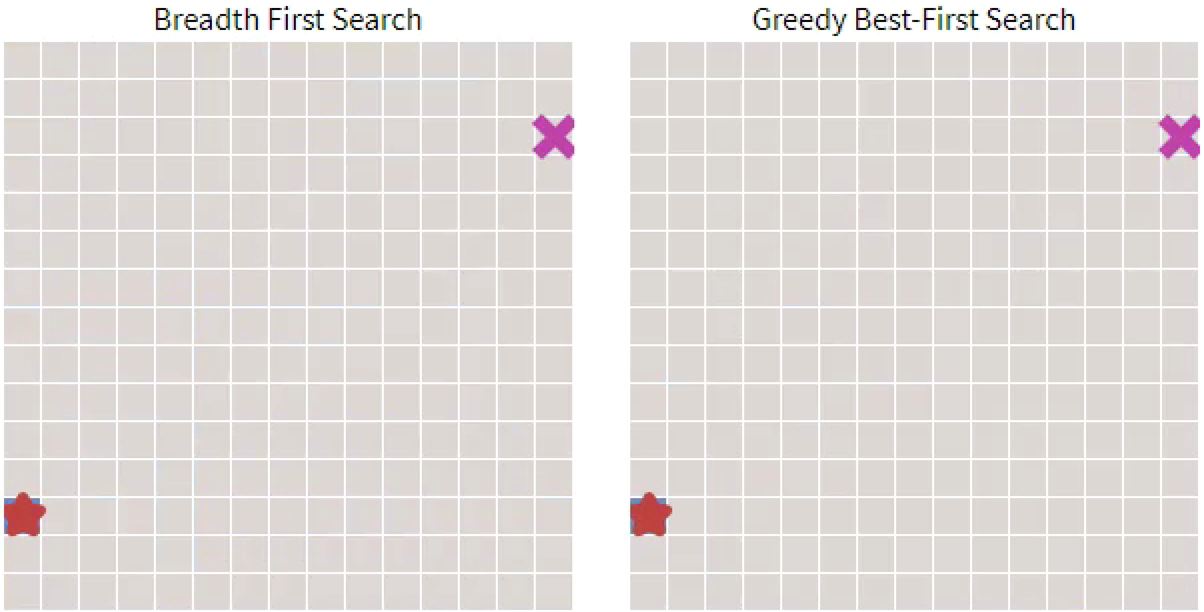
搜索过程中无法得知离target多近，所以使用猜测指引扩展方向，常用猜测方法：
欧式距离：忽略障碍两点连线
曼哈顿距离：忽略障碍x+y轴距离



- Euclidean Distance
- Manhattan Distance

Both are approximations for the actual shortest path.

Greedy Best First Search



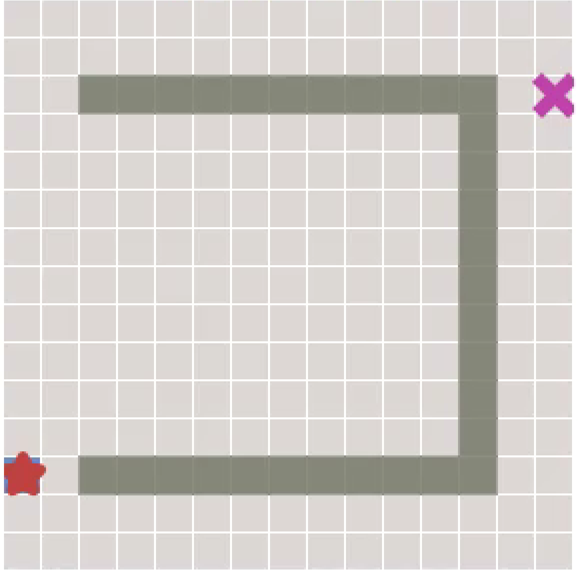
Looks pretty good.

Courtesy: Amit Patel's Introduction to A*, Stanford

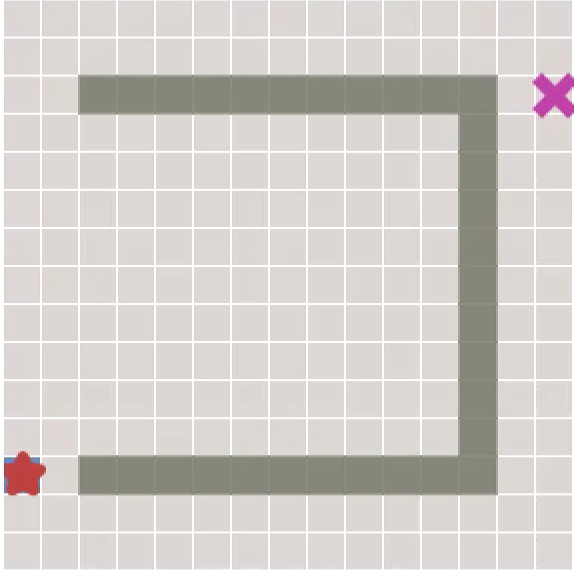
Greedy Best First Search

有障碍物时会陷入局部最优：因为猜测节点到终点有多近的时候是忽略障碍物的

Breadth First Search



Greedy Best-First Search



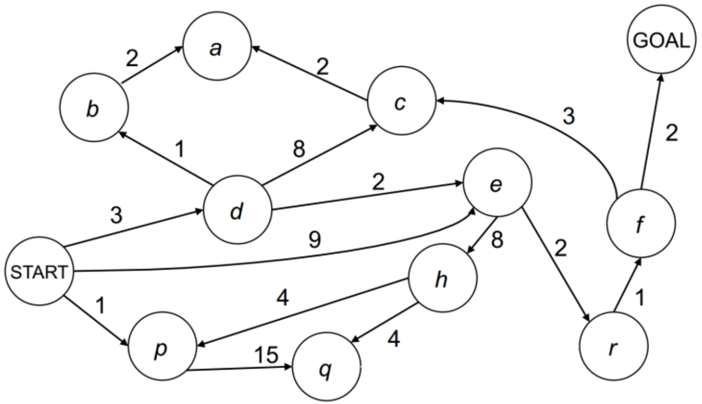
But with obstacles ...

Courtesy: Amit Patel's Introduction to A*, Stanford

Costs on Actions

前面BFS，DFS没有考虑cost，在权重都为1时BFS更优

- A practical search problem has a cost "C" from a node to its neighbor
  - Length, time, energy, etc.
- When all weight are 1, BFS finds the optimal solution
- For general cases, how to find the least-cost path as soon as possible?

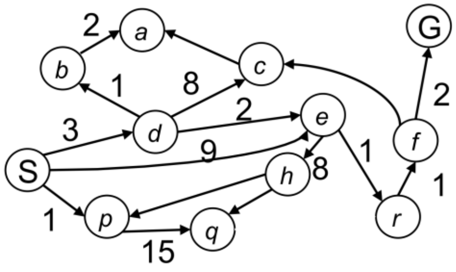


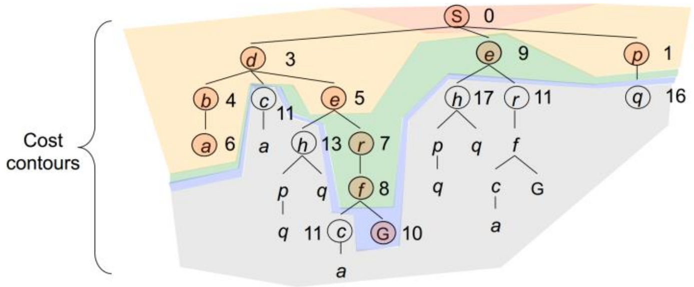
Dijkstra and A*

Algorithm Workflow

Dijkstra's Algorithm

- Strategy: expand/visit the node with cheapest accumulated cost g(n)
  - g(n): The current best estimates of the accumulated cost from the start state to node "n" g(n):起点到n的累积cost估计
  - Update the accumulated costs g(m) for all unexpanded neighbors "m" of node "n" 如果g(m)>g(n)+c(n->m),更新g(m)
  - A node that has been expanded/visited is guaranteed to have the smallest cost from the start state expended/visited可以保证最优性



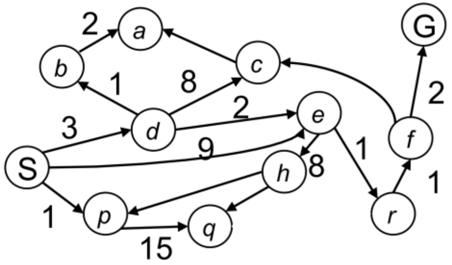


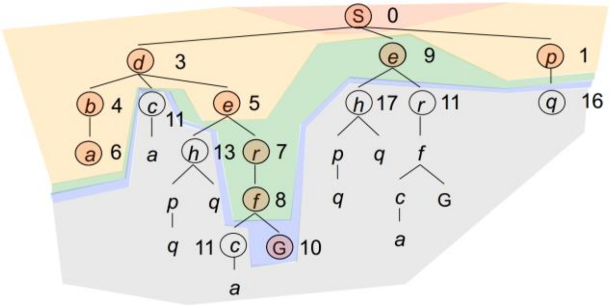
Dijkstra's Algorithm

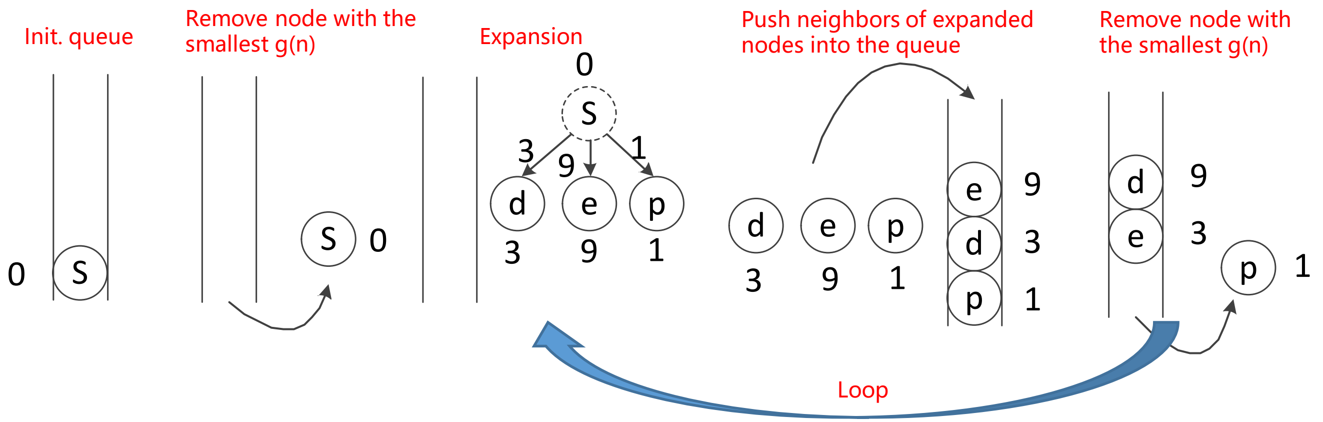
优先级队列，不是普通queue， 根据g(n):从小到大排列

- Maintain a priority queue to store all the nodes to be expanded
- The priority queue is initialized with the start state X_S
- Assign $g(X_S)=0$, and $g(n)$=infinite for all other nodes in the graph
- Loop
  - If the queue is empty, return FALSE; break;
  - Remove the node "n" with the lowest g(n) from the priority queue =open list
  - Mark node "n" as expanded = close list
  - If the node "n" is the goal state, return TRUE; break;
  - For all unexpanded neighbors "m" of node "n"
    - If g(m) = infinite
      - g(m)= g(n) + Cnm
      - Push node "m" into the queue
    - If $g(m) > g(n) + C_{nm}$
      - $g(m)= g(n) + C_{nm}$
  - end
- End Loop

Dijkstra’ s Algorithm







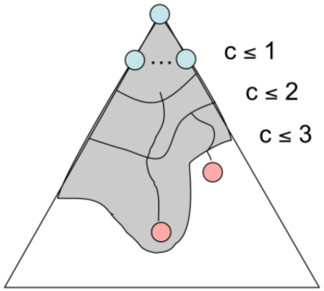
Pros and Cons of Dijkstra’s Algorithm

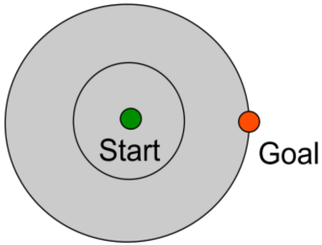
- The good:
  - Complete and optimal

优点：完备且最优（解存在的话

缺点：all direction exploring with different weights,如果weight all 1和BFS一样；没有终点信息盲目从各个方向扩展（穷举搜索

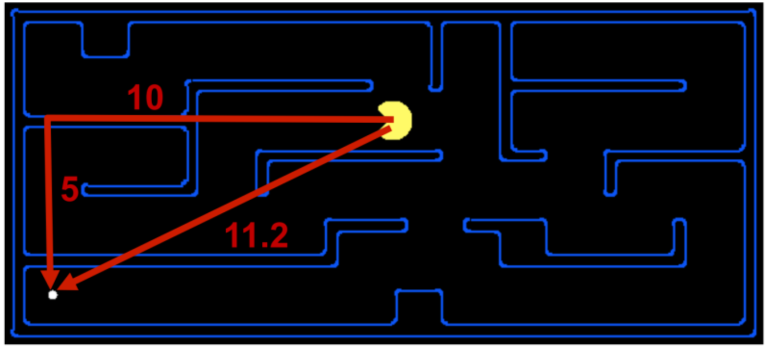
- The bad:
  - Can only see the cost accumulated so far (i.e. the uniform cost), thus exploring next state in every “direction”
  - No information about goal location





Search Heuristics

- Recall the heuristic introduced in **Greedy Best First Search**
- Overcome the shortcomings of uniform cost search by inferring the least cost to goal (i.e. goal cost)
- Designed for particular search problem
- Examples: Manhattan distance VS. Euclidean distance



A*: Dijkstra with a Heuristic A*： 启发函数的Dijkstra

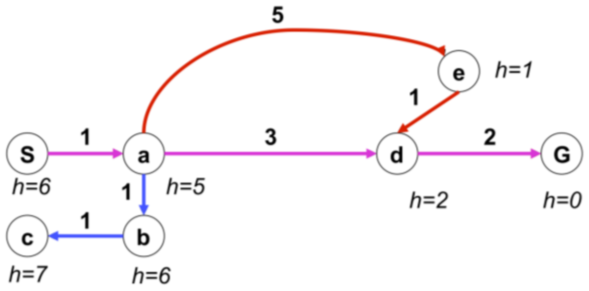
- Accumulated cost
  - g(n): The current best estimates of the accumulated cost from the start state to node “n”
- Heuristic
  - h(n): The **estimated least cost** from node n to goal state (i.e. goal cost)
- The least estimated cost from start state to goal state passing through node “n” is f(n) = g(n) + h(n)
- Strategy: expand the node with cheapest f(n) = g(n) + <u>h(n)</u>
  - Update the accumulated costs g(m) for all unexpanded neighbors “m” of node “n”
  - A node that has been expanded is guaranteed to have the smallest cost from the start state

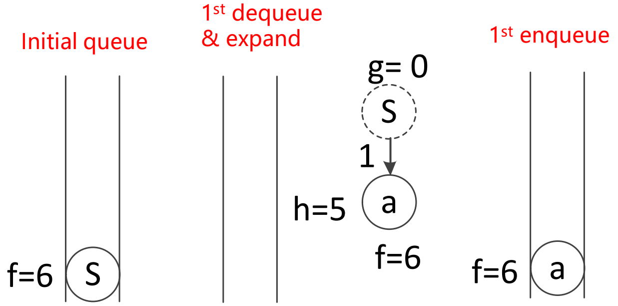
A* Algorithm

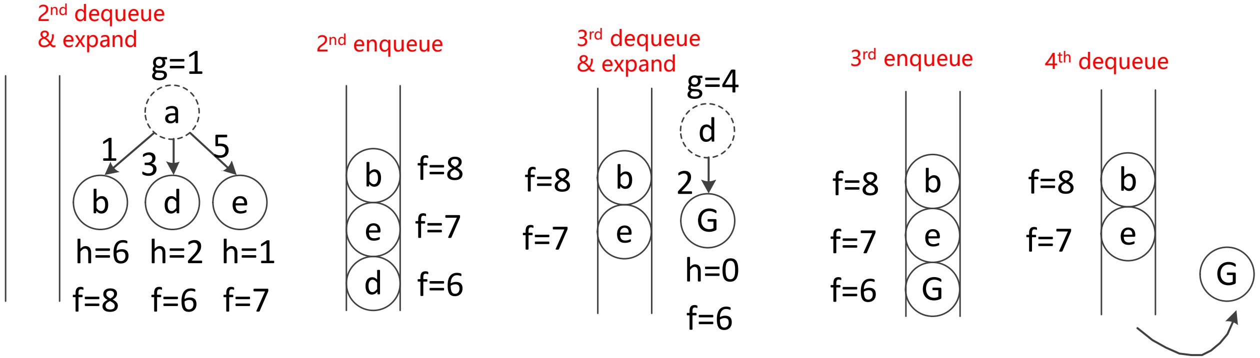
- Maintain a priority queue to store all the nodes to be expanded
- The heuristic function h(n) for all nodes are pre-defined
- The priority queue is initialized with the start state X_S
- Assign $g(X_S)=0$, and g(n)=infinite for all other nodes in the graph
- Loop
  - If the queue is empty, return FALSE; break;
  - Remove the node "n" with the lowest f(n)=g(n)+h(n) from the priority queue
  - Mark node "n" as expanded
  - If the node "n" is the goal state, return TRUE; break;
  - For all unexpanded neighbors "m" of node "n"
    - If g(m) = infinite
      - g(m)= g(n) + Cnm
      - Push node "m" into the queue
    - If g(m) > g(n) + C_{nm}
      - g(m)= g(n) + Cnm
  - end
- End Loop

Only difference comparing to Dijkstra' s algorithm

A* Example

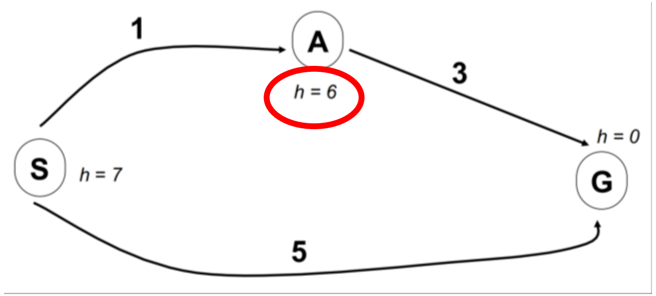

5
e
h=1
1
S
1
a
3
d
2
G
h=6
1
h=5
h=2
h=0
c
1
b
h=7
h=6


Initial queue
f=6
S
1st dequeue & expand
g= 0
S
1
h=5
a
f=6
1st enqueue
f=6
a


2nd dequeue & expand
g=1
a
1
3
5
b
d
e
h=6
h=2
h=1
f=8
f=6
f=7
2nd enqueue
b
f=8
e
f=7
d
f=6
3rd dequeue & expand
g=4
d
f=8
b
2
f=7
e
G
h=0
f=6
3rd enqueue
f=8
b
f=7
e
f=6
G
4th dequeue
f=8
b
f=7
e
G

A* Optimality

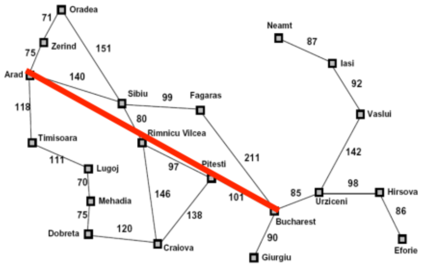
保证A*最优性：h <= h*(n)
真实cost

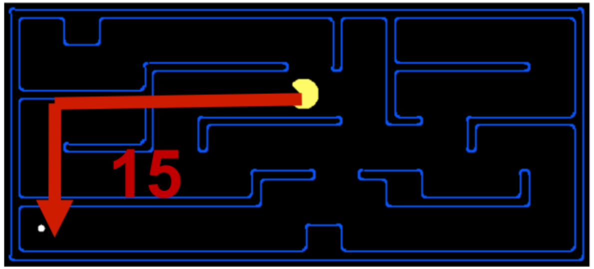


- What went wrong?
- For node A: actual least cost to goal (i.e. goal cost) < estimated least cost to goal (i.e. heuristic)
- We need the estimate to be less than actual least cost to goal (i.e. goal cost) for all nodes!

Admissible Heuristics

- A Heuristic h is admissible (optimistic) if:
  - h(n) <= h*(n) for all node "n", where h*(n) is the true least cost to goal from node "n"
- If the heuristic is admissible, the A* search is optimal
- Coming up with admissible heuristics is most of what's involved in using A* in practice.
- Example:

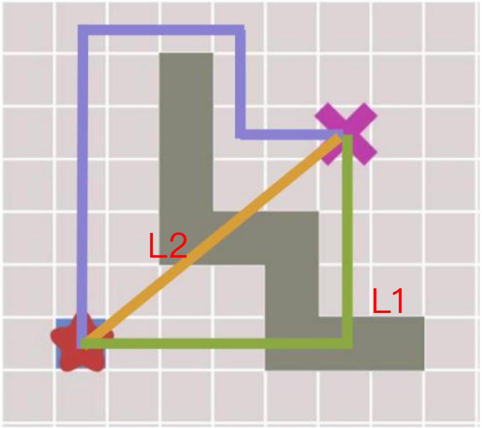




Heuristic Design

An admissible heuristic function has to be designed case by case.

- Euclidean Distance
- Manhattan Distance



Is Euclidean distance (L2 norm) admissible? Always

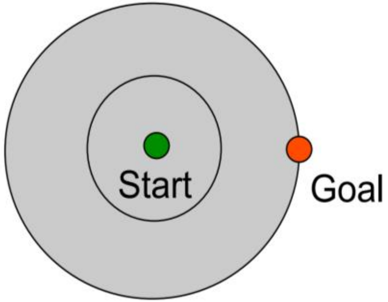
Is Manhattan distance (L1 norm) admissible? Depends

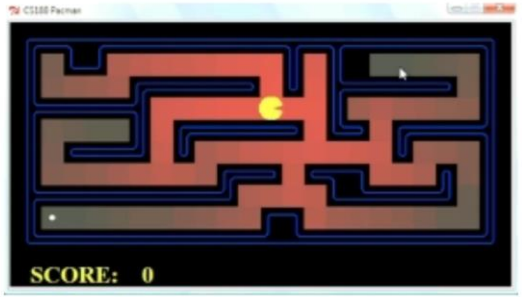
Is L∞ norm distance admissible? Always

Is 0 distance admissible? Dijkstra具有最优性 Always

Dijkstra’s VS A*

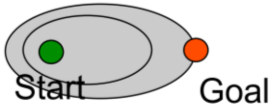
- Dijkstra’s algorithm expanded in all directions

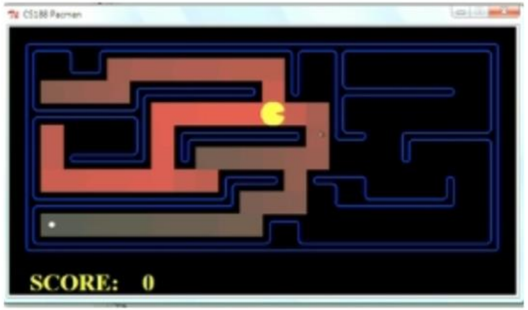




A*使Dijkstra具有向终点贪心的引导性

- A* expands mainly towards the goal, but does not hedge its bets to ensure optimality



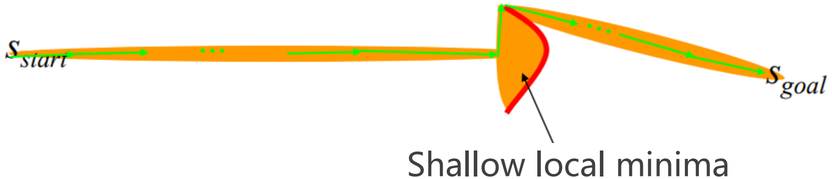


Sub-optimal Solution

What if we intend to use an over-estimate heuristic?

- Suboptimal path
- Faster

Weighted A*: Expands states based on $f = g + \varepsilon h, \varepsilon > 1$ =bias towards states that are closer to goal.



ε： >>1 weighted 可忽略g 贪心算法
等于0 Dijkstra
等于1 A* f = g+h

- Weighted A* Search:

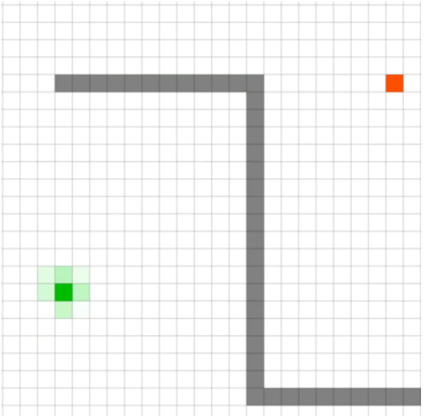
➢ Optimality vs. speed 用最优性换取速度
➢ ε-suboptimal:
cost(solution) <= εcost (optimal solution)
➢ It can be orders of magnitude faster than A*

Weighted A*-> Anytime A*-> ARA*->D*

Beyond the scope of this course

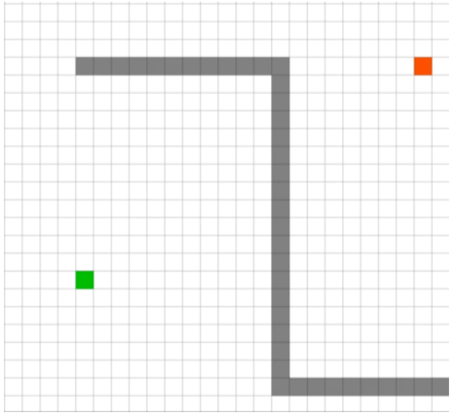
Greedy Best First Search vs. Weighted A* vs. A*

$$f = a \cdot g + b \cdot h$$



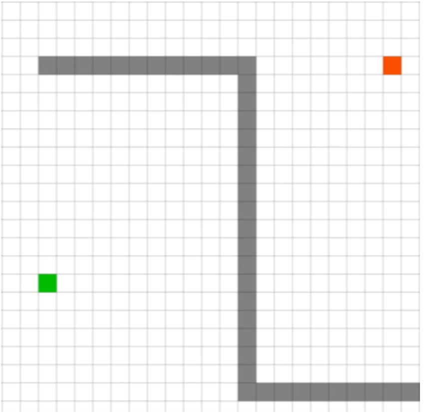
Most Greedy 贪心

$a = 0, b = 1$



Tunable Greediness

$a = 1, b = \varepsilon > 1$



Optimal A*

$a = 1, b = 1$

Animation from: http://qiao.github.io/PathFinding.js/visual/

Dijkstra: $a = 1, b = 0$

Engineering Considerations

Example: Grid-based Path Search

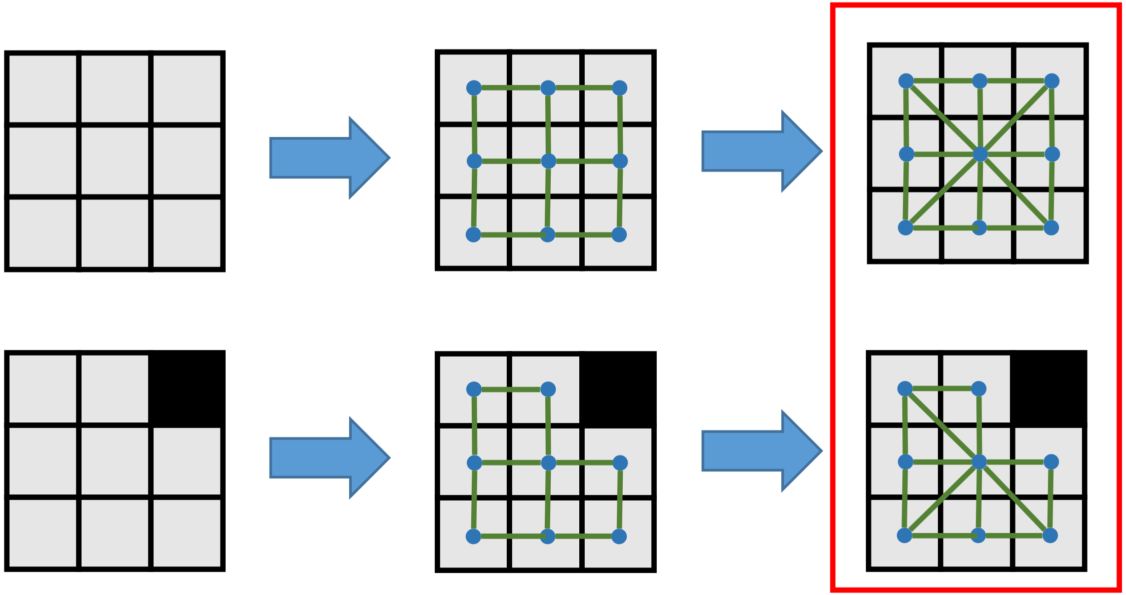
How to represent grids as graphs?

Each cell is a node. Edges connect adjacent cells.

2D： 8 connection

3D： 26 connection

9+8+9=26

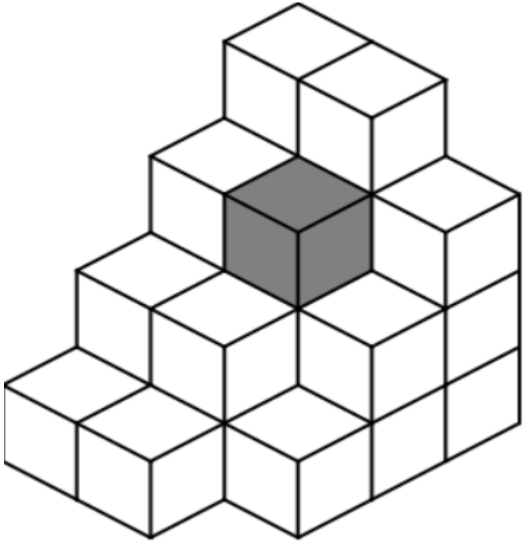


Common Choice!

4 connection

8 connection

Grid-based Path Search: Implementation



- Create a dense graph.
- Link the occupancy status stored in the grid map.
- Neighbors discovered by grid index.
- Perform A* search.

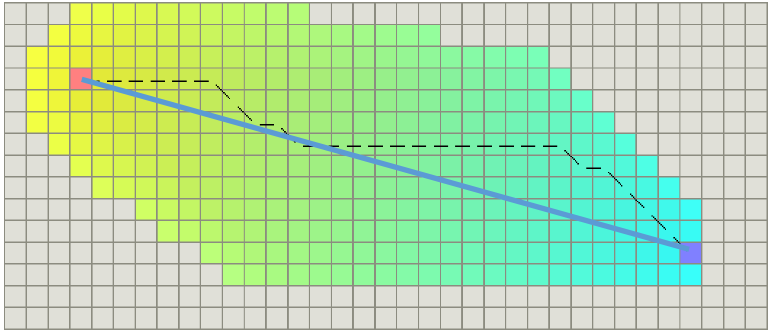
- Priority queue in C++
  - std::priority_queue
  - std::make_heap
  - std::multimap

std：标准库

The Best Heuristic 最优启发函数

- Recall:
  - Is Euclidean distance (L2 norm) admissible? ✓
  - Is Manhattan distance (L1 norm) admissible? ✗ 可以走对角线
  - Is L∞ norm distance admissible? ✓
  - Is 0 distance admissible? ✓

Euclidean Heuristic



They are useful, but none of them is the best choice, why?

Because none of them is tight.

Tight means who close they measure the true shortest distance.

h(n) <= h*(n)

但是h(n) 太小了，导致走很多无用的expand

Why so many nodes expanded?

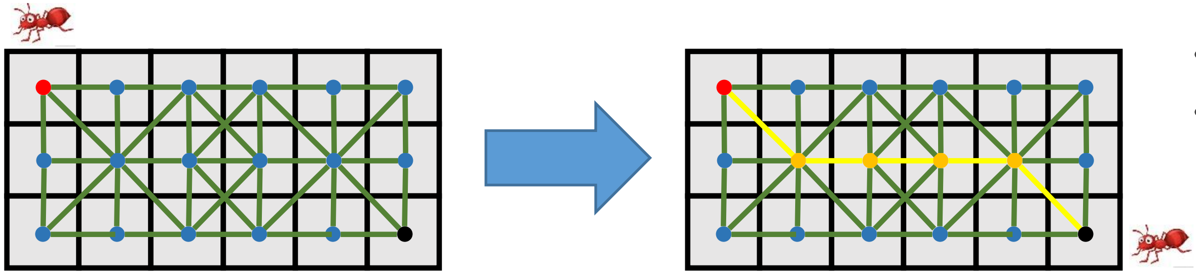
Because Euclidean distance is far from the truly theoretical optimal solution.

The Best Heuristic

How to get the truly theoretical optimal solution?

Fortunately, the grid map is highly structural.

当地图有结构，可以直接计算出最短距离，此时h(n)=h*(n),tightest



- You don’ t need to search the path.
- It has the closed-form solution!

dx=abs(node.x −goal.x)

dy=abs(node.y −goal.y)

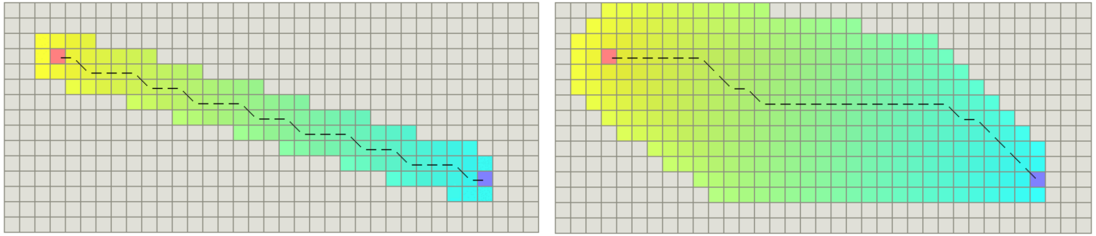
$h=(dx+dy)+(\sqrt{2}-2)*\min(dx,dy)$

For 3D case, we also have a similar version of this.

Compare

Diagonal Heuristic

对角heuristic



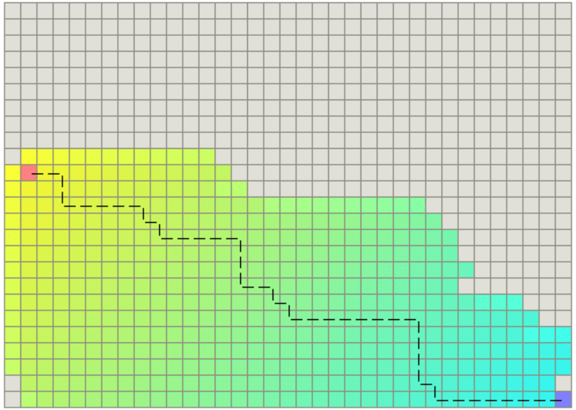
L2

欧式 heuristic

两条路线形状不同但是长度相同（对称性）

Tie Breaker

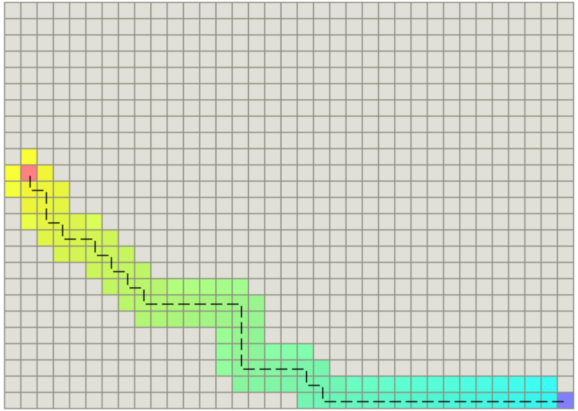
- Many paths have the same f value.
- No differences among them making them explored by A* equally.



- Manipulate the f value breaks the tie.
- Make same f values differ.
- Interfere h slightly.

$$\mathrm{h} = \mathrm{h} \times (1.0 + \mathrm{p})$$

$$p < \frac{minimum\ cost\ of\ one\ step}{expected\ maximum\ path\ cost}$$



Slightly breaks the admissibility of h, does it matter?

实际工程中影响非常小（有障碍）

Tie Breaker

Core idea of tie breaker:

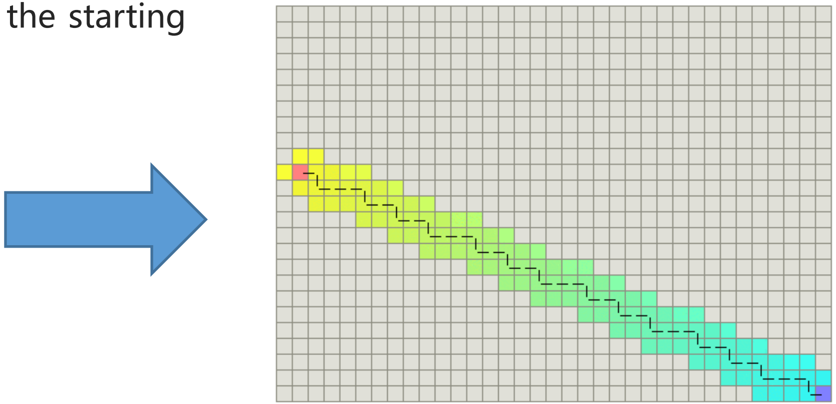
Find a preference among same cost paths

核心思想：打破路径的对称性

Better/other **tie breaker**?

- When nodes having same f, compare their h.
- Add deterministic random numbers to the heuristic or edge costs (A hash of the coordinates).
- Prefer paths that are along the straight line from the starting point to the goal.

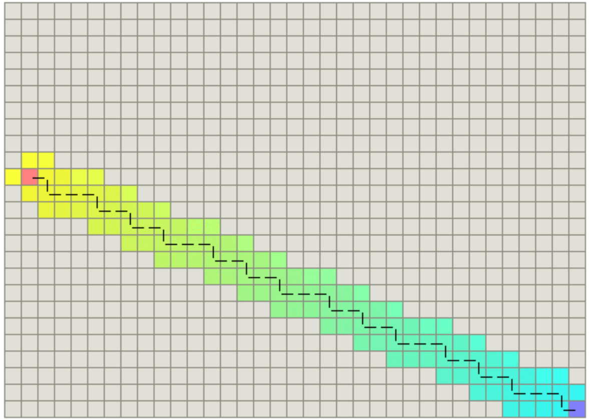
$$dx1 = abs(node.x - goal.x)$$
$$dy1 = abs(node.y - goal.y)$$
$$dx2 = abs(start.x - goal.x)$$
$$dy2 = abs(start.y - goal.y)$$
$$cross = abs(dx1 \times dy2 - dx2 \times dy1)$$
$$\mathrm{h} = h + cross \times 0.001$$



- … Many customized ways

Tie Breaker

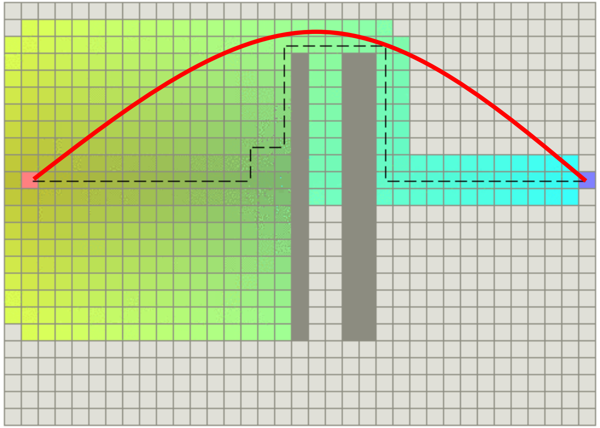
- Prefer paths that are along the straight line from the starting point to the goal.



Both optimal, but ...

Looks wired

Looks good



It' s the shortest path, but harm for trajectory generation (smoothing).

Or a systematic approach: Jump Point Search (JPS)

Jump Point Search

Algorithm Workflow

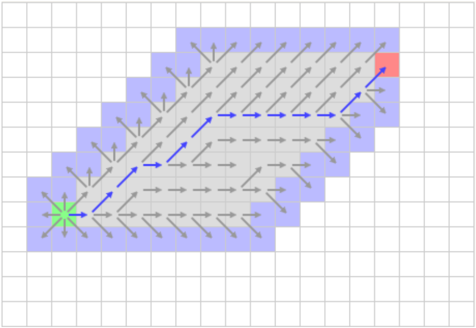
Jump Point Search

系统性消灭路径对称性的一种方法
对称性坏处：进行无谓的探索

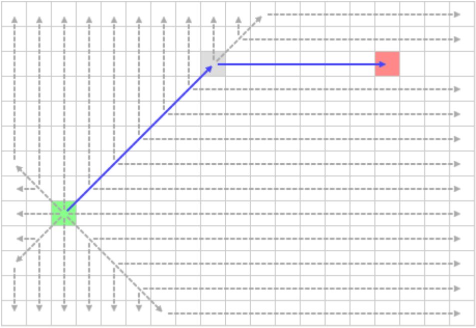
Core idea of JPS:

Find symmetry and break them.

A* explore all symmetric path.



JPS choose one path.



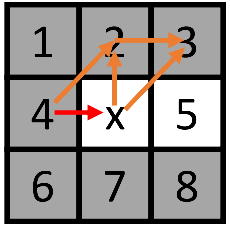
Grey node: Added in the Open List.

JPS explores intelligently, because it always looks ahead based on a rule.

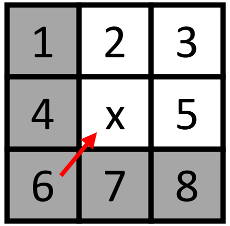
Look Ahead Rule

=pruning rule

straight

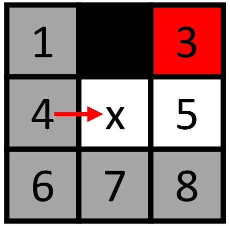


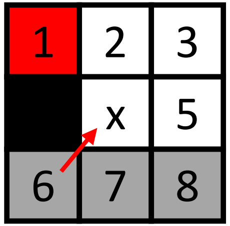
diagonal



Consider:

- current node x
- x's expanded direction





Neighbor Pruning

- Gray nodes: inferior neighbors, when going to them, the path without x is cheaper. Discard.
- White nodes: natural neighbors.
- We only need to consider natural neighbors when expand the search.

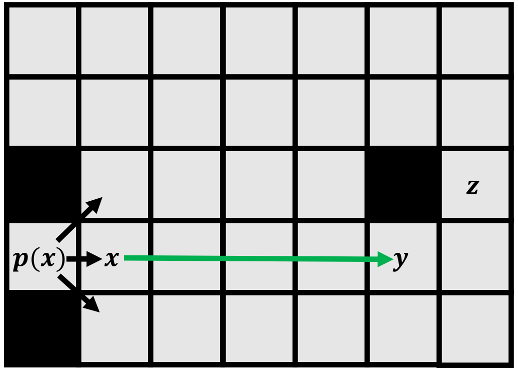
灰色：劣性节点（丢掉）
白色：自然节点（保留）

Forced Neighbors

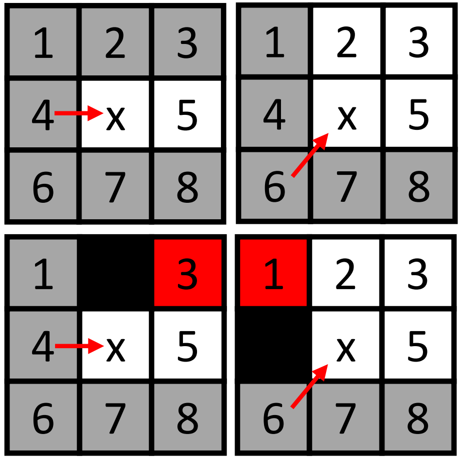
- There is obstacle adjacent to x
- Red nodes are forced neighbors.
- A cheaper path from x's parent to them is blocked by obstacle.

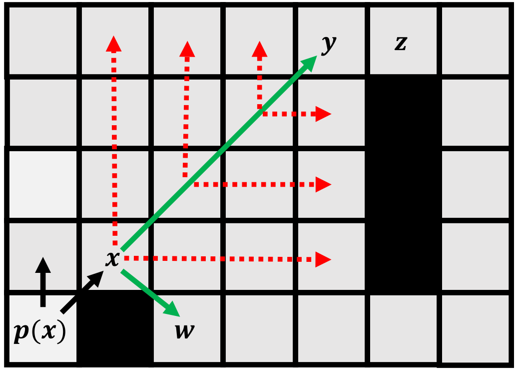
Jumping Rules

Look Ahead Rule



Jumping Straight

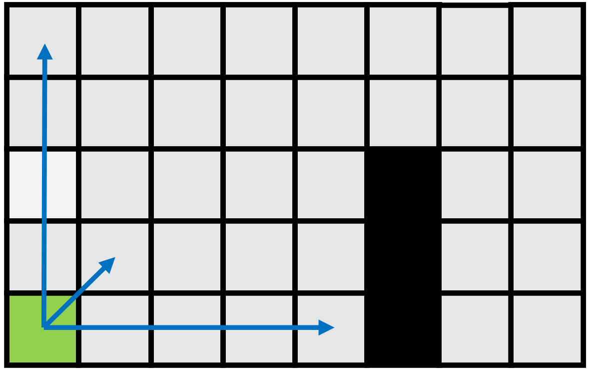




Jumping Diagonally

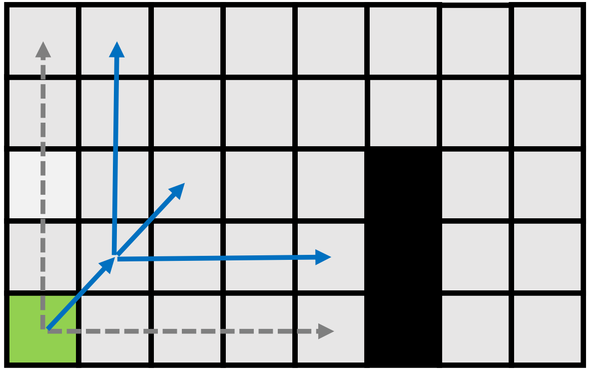
- Recursively apply straight pruning rule and identify y as a jump point successor of x. This node is interesting because it has a neighbor z that cannot be reached optimally except by a path that visits x then y.
- Recursively apply the diagonal pruning rule and identify y as a jump point successor of x.
- Before each diagonal step we first recurse straight. Only if both straight recursions fail to identify a jump point do we step diagonally again.
- Node w, a forced neighbor of x, is expanded as normal. (also push into the open list, the priority queue)

Jump Point Search



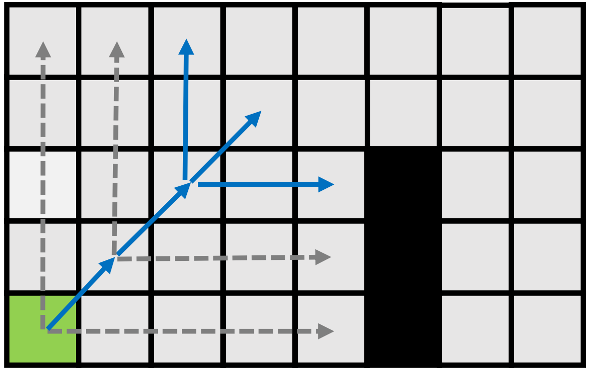
- Expand horizontally and vertically.
- Both jumps end in obstacles.
- Move diagonally.

Jump Point Search



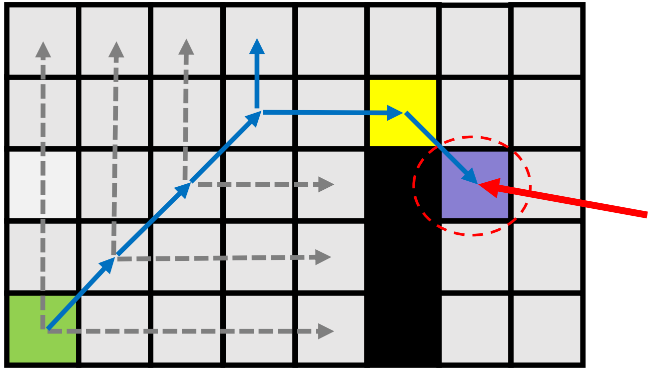
- Expand horizontally and vertically.
- Both jumps end in obstacles.
- Move diagonally.

Jump Point Search



- Expand horizontally and vertically.
- Both expansions end in obstacles.
- Move diagonally.

Jump Point Search

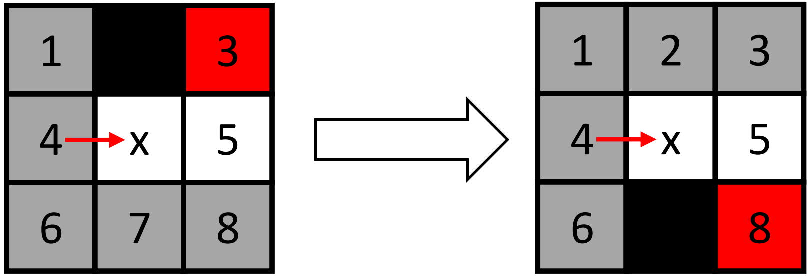


- Remember: you can only jump straight or diagonally; never piecewise jump

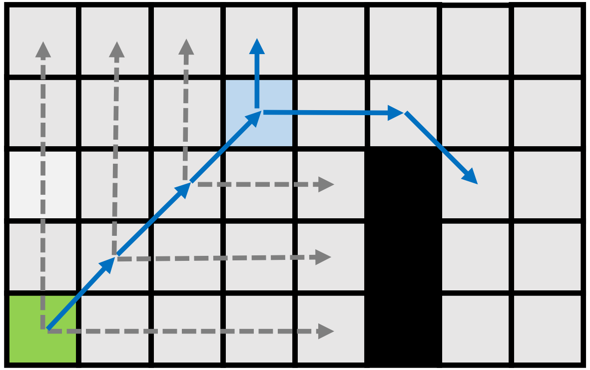
- Vertically expansion end in obstacle.
- Right-ward expansion finds a node with a forced neighbor.

Recall the rule

So we have



Jump Point Search



- Now this node is of interested.
- Put it to open list.

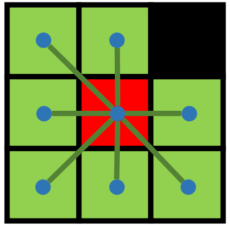
Jump Point Search

Recall A*'s pseudo-code, JPS's is all the same!

- Maintain a priority queue to store all the nodes to be expanded
- The heuristic function h(n) for all nodes are pre-defined
- The priority queue is initialized with the start state X_S
- Assign $g(X_S)=0$, and g(n)=infinite for all other nodes in the graph
- Loop
    - If the queue is empty, return FALSE; break;
    - Remove the node "n" with the lowest f(n)=g(n)+h(n) from the priority queue
    - Mark node "n" as expanded
    - If the node "n" is the goal state, return TRUE; break;
    - For all unexpanded neighbors "m" of node "n"
        - If g(m) = infinite
            - $g(m)= g(n) + C_{nm}$
            - Push node "m" into the queue
        - If $g(m) > g(n) + C_{nm}$
            - $g(m)= g(n) + C_{nm}$
    - end
- End Loop

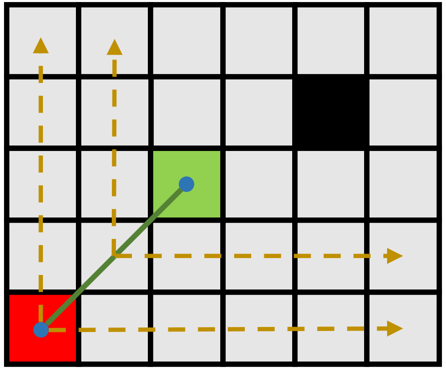
A*：几何邻居

A*: "Geometric" neighbors



JPS：空旷区域大范围跳跃

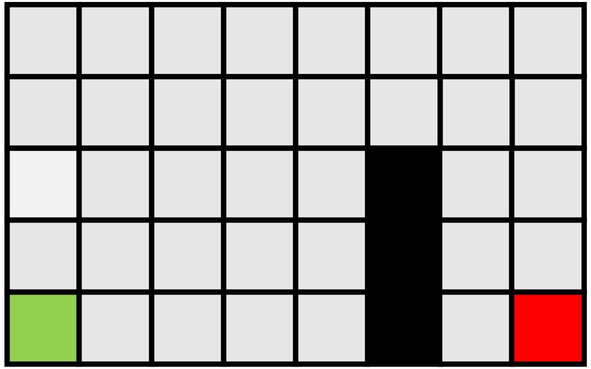
JPS: "Jumping" neighbors



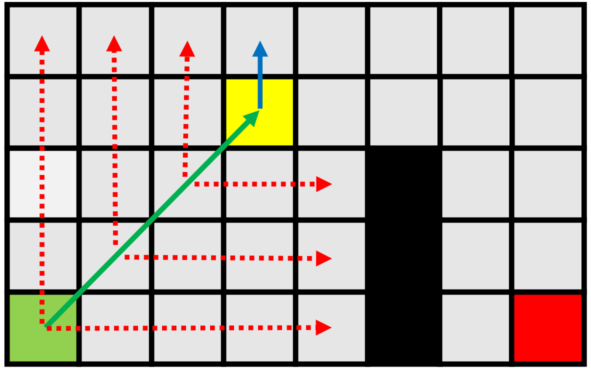
Example

Jumping Example

Planning Case

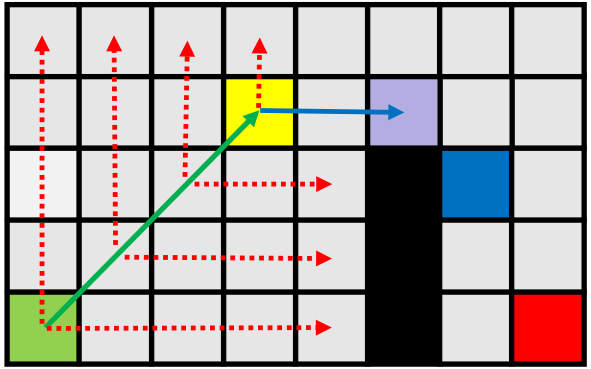


Jumping Example



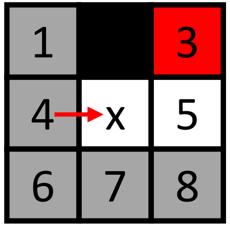
- Expand—>move diagonally
- Find a critical node finally, add it into open list.
- Pop it (the only one) from the open list.
- Expand vertically, end at obstacles.

Jumping Example

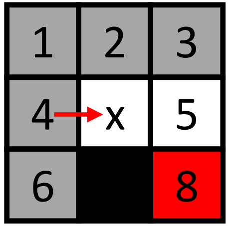


- Expand horizontally, meets a node with a forced neighbor.
- Add it to open list

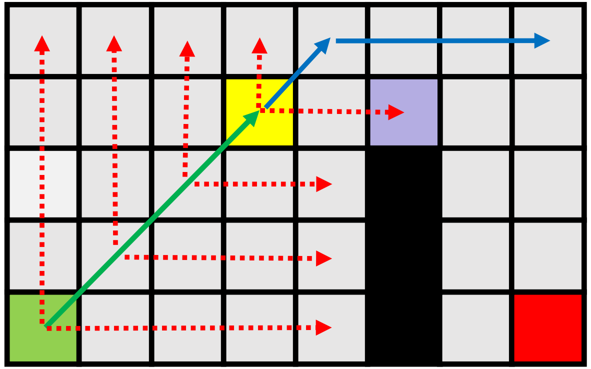
Recall the rule



So we have

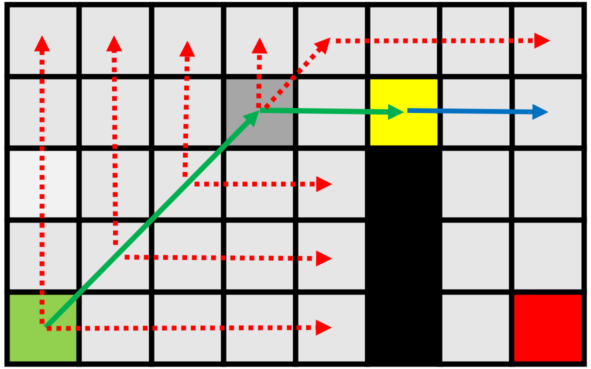


Jumping Example



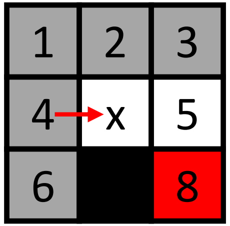
- Expand diagonally, expand, find nothing.
- Finish the expansion of the current node.

Jumping Example

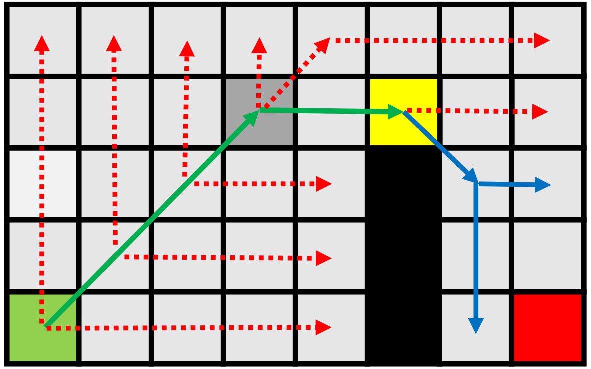


- Examine the “new best” node in the open list.
- Expand horizontally.
- Finds nothing.

Remember the rule

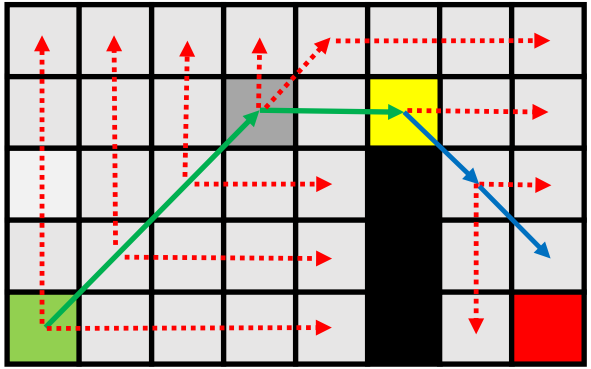


Jumping Example



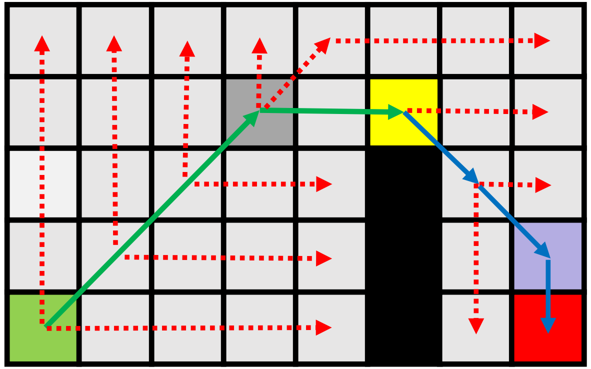
- Move diagonally.
- Expand along vertical and horizontal first.

Jumping Example



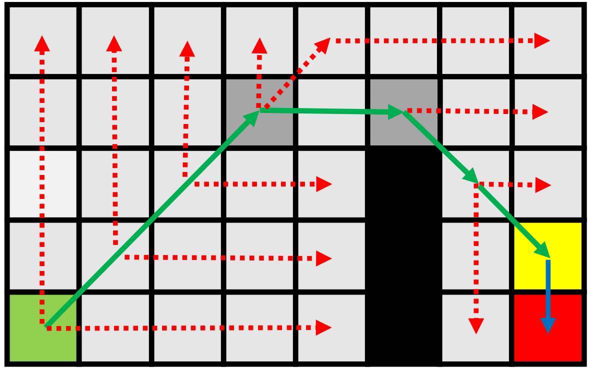
- Finds nothing.
- Move diagonally.

Jumping Example



- Expand horizontally and vertically.
- Finds the goal. Equally interested as finding a node with a forced neighbor.
- Add this node to open list.
- Finish the expand of the current node (No naturally neighbors left).
- Pop it out of the open list.

Jumping Example

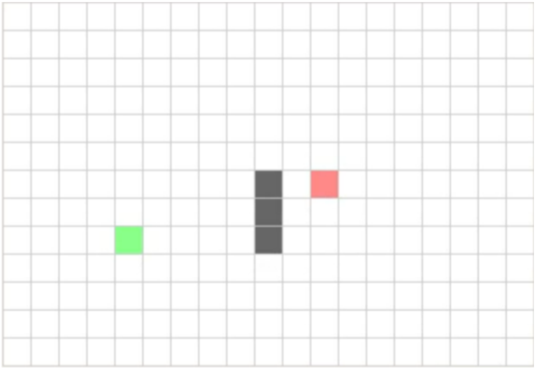


- Examine the "new best" node in the open list.
- Expand horizontally (nowhere), and vertically (finds the goal).
- The end.

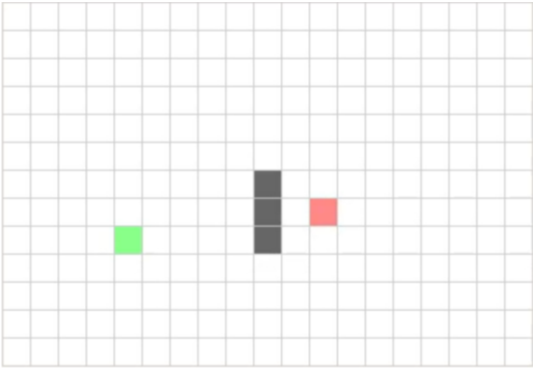
Jumping Example

Final Path

Example



(1)



(2)

Thanks:

https://zerowidth.com/2013/a-visual-explanation-of-jump-point-search.html

Extension

3D JPS

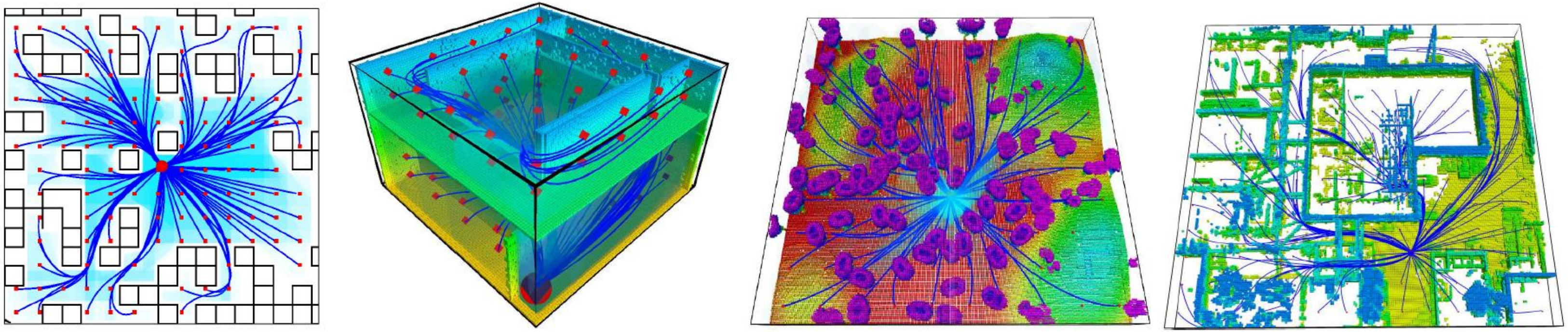


Table 1. Trajectory Generation Run Time (sec)

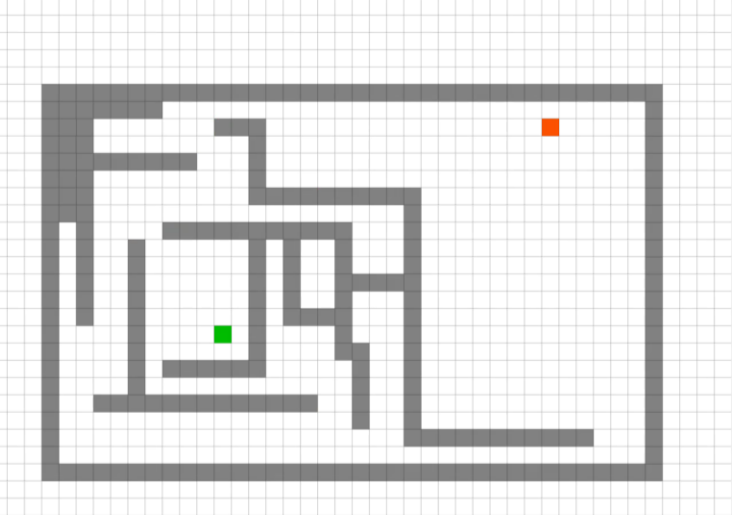
Map	Size	# of Cells	# of Trajs	Time (s)	Path Planning A*	Path Planning JPS	Convex Decomp	Traj Opt	Replan (JPS)
Random Blocks	$40 \times 40 \times 1$	1.4×10^6	130	Avg	0.57	0.034	0.0021	0.028	0.065
				Std	1.26	0.034	0.0028	0.022	0.051
				Max	9.98	0.19	0.020	0.099	0.27
Multiple Floors	$10 \times 10 \times 6$	5.9×10^5	147	Avg	6.12	0.039	0.0064	0.082	0.13
				Std	15.77	0.046	0.0038	0.041	0.081
				Max	84.56	0.22	0.021	0.23	0.45
The Forest	$50 \times 50 \times 6$	1.8×10^6	89	Avg	0.65	0.033	0.0039	0.055	0.094
				Std	1.57	0.044	0.0024	0.031	0.068
				Max	7.78	0.20	0.010	0.12	0.30
Outdoor Buildings	$100 \times 110 \times 7$	6.2×10^5	127	Avg	0.54	0.028	0.0066	0.099	0.14
				Std	1.46	0.045	0.0053	0.064	0.10
				Max	10.96	0.27	0.027	0.24	0.47

Planning Dynamically Feasible Trajectories for Quadrotors using Safe Flight Corridors in 3-D Complex Environments, Sikang Liu, RAL 2017

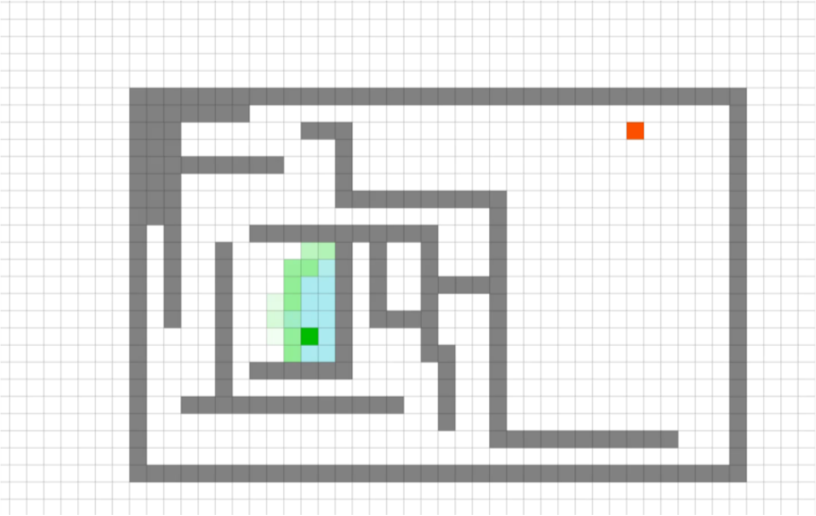
https://github.com/KumarRobotics/jps3d

Is JPS always better? NO！！

Maze-like environments



JPS

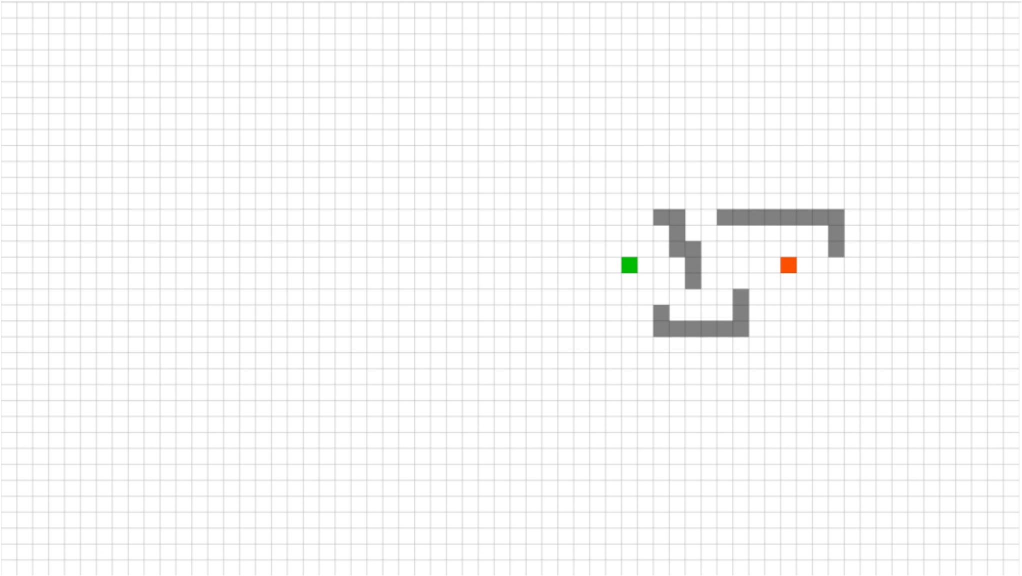


A*

Do more tests by yourself!

Thanks: http://qiao.github.io/PathFinding.js/visual/

Is JPS always better?



- This is a simple example saying "No."
- This case may commonly occur in robot navigation.
- Robot with limited FOV, but a global map/large local map.

机器人视野有限，地图很大，且很多空旷的地方需要collision query

Conclusion:

复杂环境：JPS优于A*

- Most time, especially in complex environments, JPS is better, but far away from "always". Why?
- JPS reduces the number of nodes in Open List, but increases the number of status query. =collision query
- You can try JPS in Homework 2. 按照几何特征
- JPS's limitation: only applicable to uniform grid map.

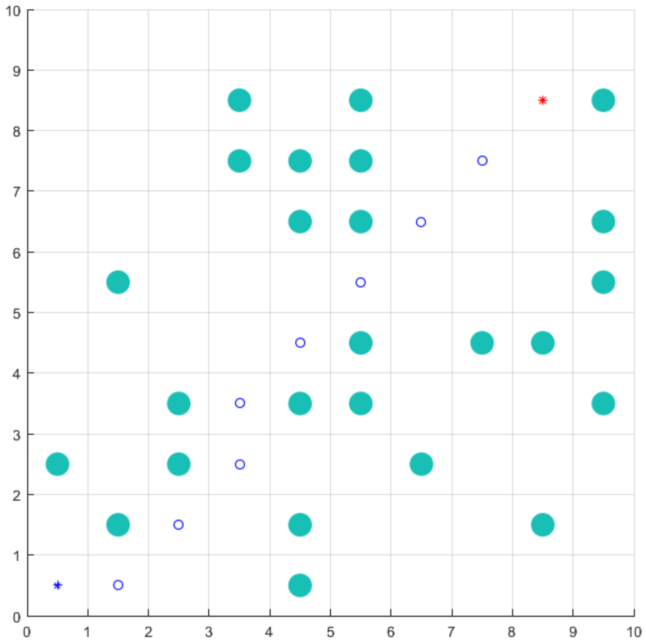
减少open list中node数量，但增加碰撞查询

不适用那种有不同weight的广义graph search

Homework

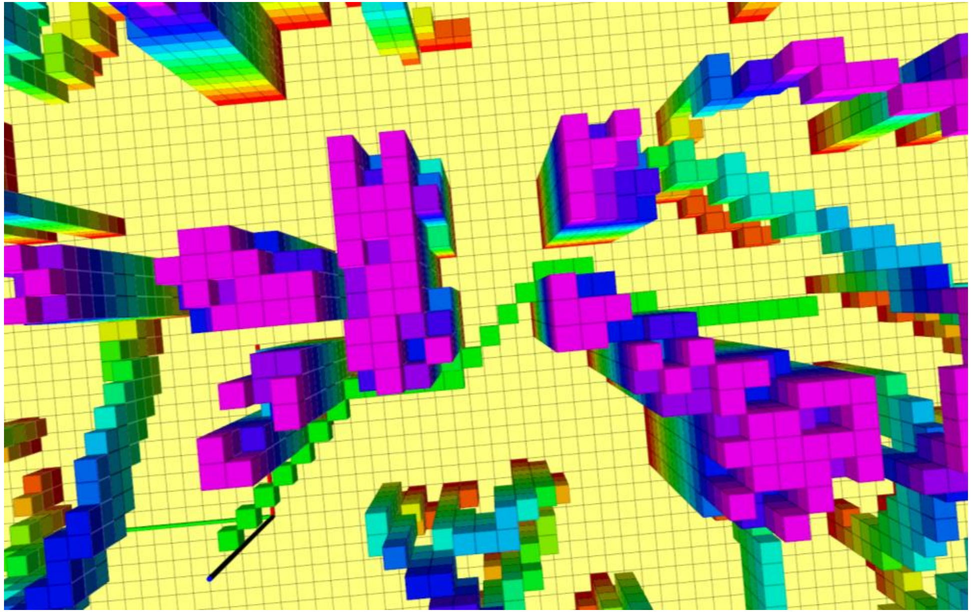
Testing Environment

Matlab



Basic

C++



Advance

Assignment：Basic

- This project work will focus on path Þnding and obstacle avoidance in a 2D grid map.
- A 2D grid map is generated randomly every time the Project is run, which contains the obstacles, start point and target point locations will be provided. You can also change the probability of obstacles in the map in obstacle_map.m
- You need to implement a 2D A* path search method to plan an optimal path with safety guarantee.

Assignment: Advance

- I highly suggest you implement Dijkstra/A* with C++/ROS.
- Complex 3d map can be generated randomly. The sparsity of obstacles in this map is tunable.
- An implementation of JPS is also provided. Comparisons can be made between A* and JPS in different map set-up.

Thanks for Listening!