



计算机视觉表征与识别

Chapter 7: Interest Points: Detector

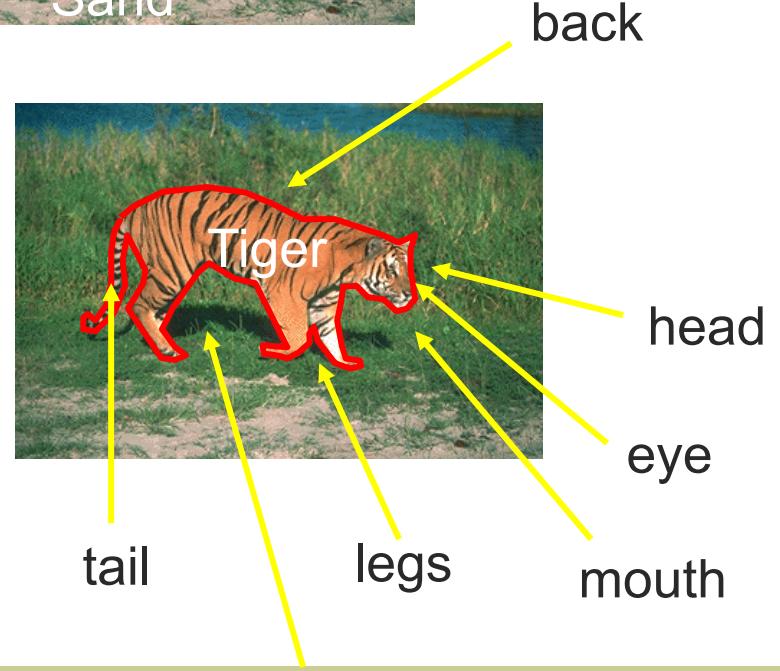
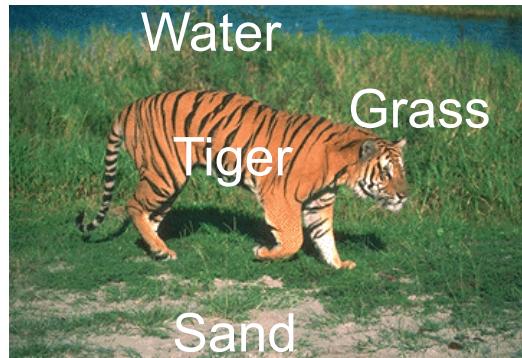
王利民

媒体计算课题组

<http://mcg.nju.edu.cn/>



From Pixels to Perception



**Mid-level operations of
Segmentation and Grouping**



Last Class

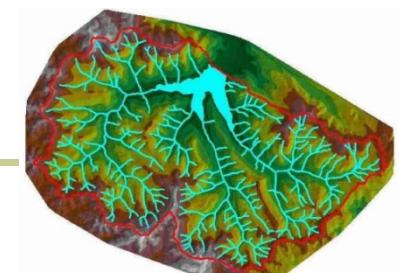
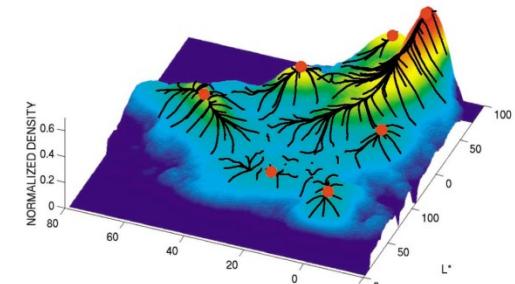
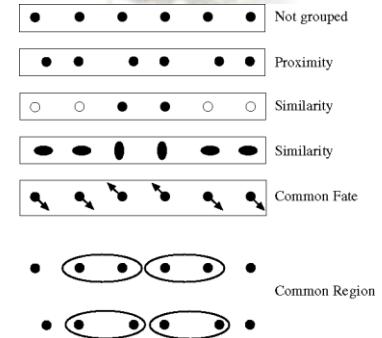


- What are grouping problems in vision?
- Inspiration from human perception
 - Gestalt properties
- Bottom-up segmentation via clustering
 - Mode finding and mean shift: k-means, GMM, mean-shift
- Graph-based segmentation: Normalized Cut
- Oversegmentation
 - Watershed algorithm, Felzenszwalb and Huttenlocher graph-based
- Multiple segmentation



Things to remember

- Gestalt cues and principles of organization
- Uses of segmentation
 - Efficiency
 - Better features
 - Propose object regions
 - Want the segmented object
- Mean-shift segmentation
 - Good general-purpose segmentation method
 - Generally useful clustering, tracking technique
- Normalized cuts
 - Produces regular regions
 - Slow but good for oversegmentation
- Watershed segmentation
 - Good for hierarchical segmentation
 - Use in combination with boundary prediction





Today's Class



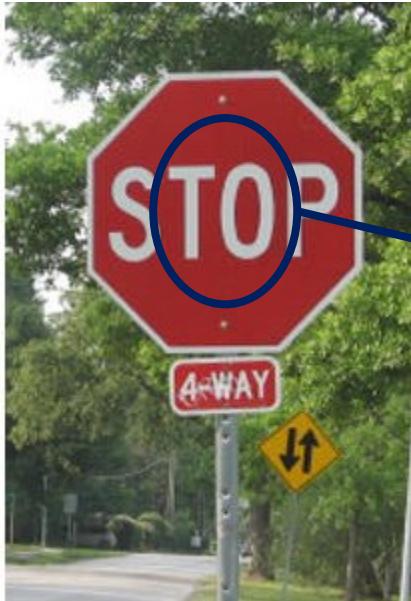
- **Introduction to correspondence and alignment**
- **Overview of interest points**
 - Matching pipeline
 - Repeatable & Distinctive
- **Keypoint Localization**
 - Harris detector
 - Hessian detector
- **Scale invariant region selection**
 - Automatic scale selection
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 - Combinations: Harris-Laplacian & Hessian-Laplacian



Correspondence and alignment



Correspondence: matching points, patches, edges, or regions across images



$$TO \approx \bar{TO}$$





Correspondence and alignment

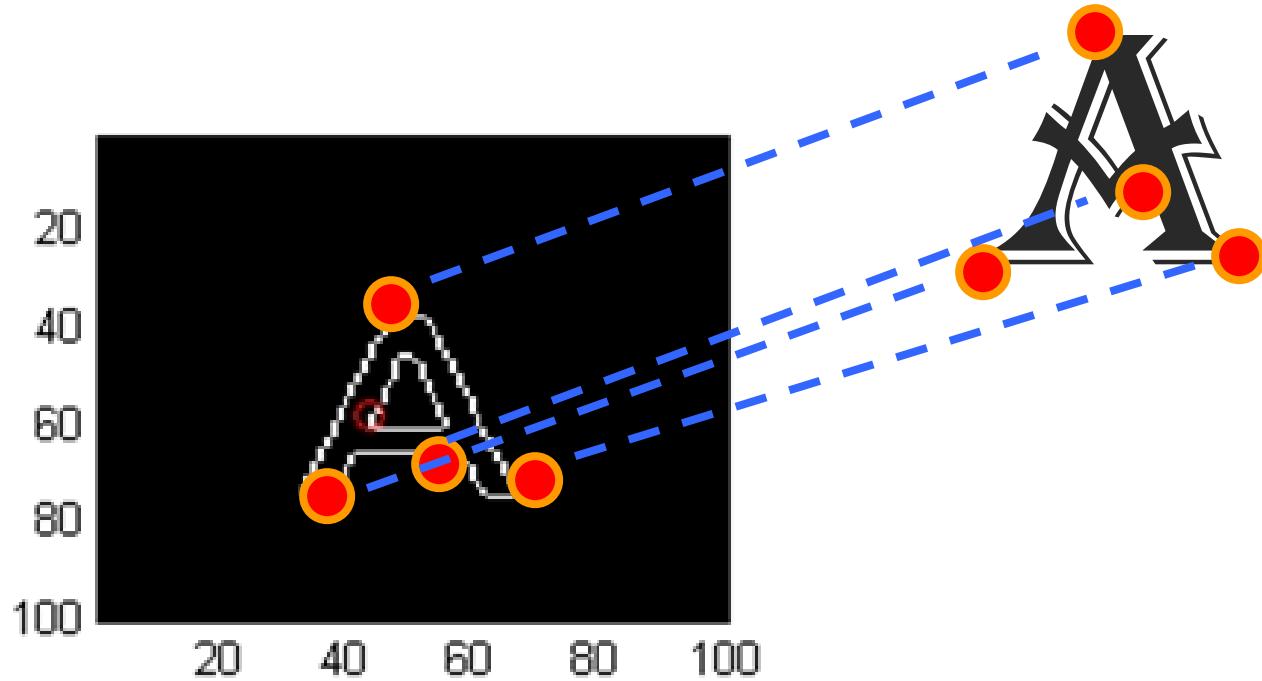


Alignment: solving the transformation that makes two things match better





Example: fitting an 2D shape template

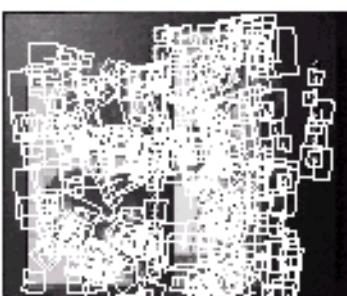
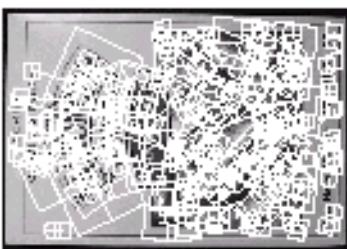
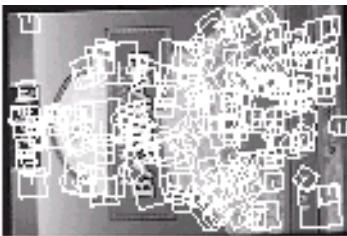
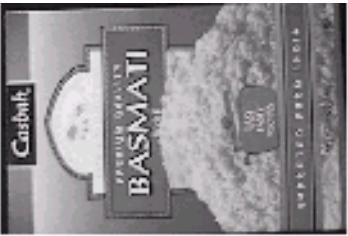




Planar object instance recognition



Database of planar objects



Instance recognition





3D object recognition



Database of 3D objects

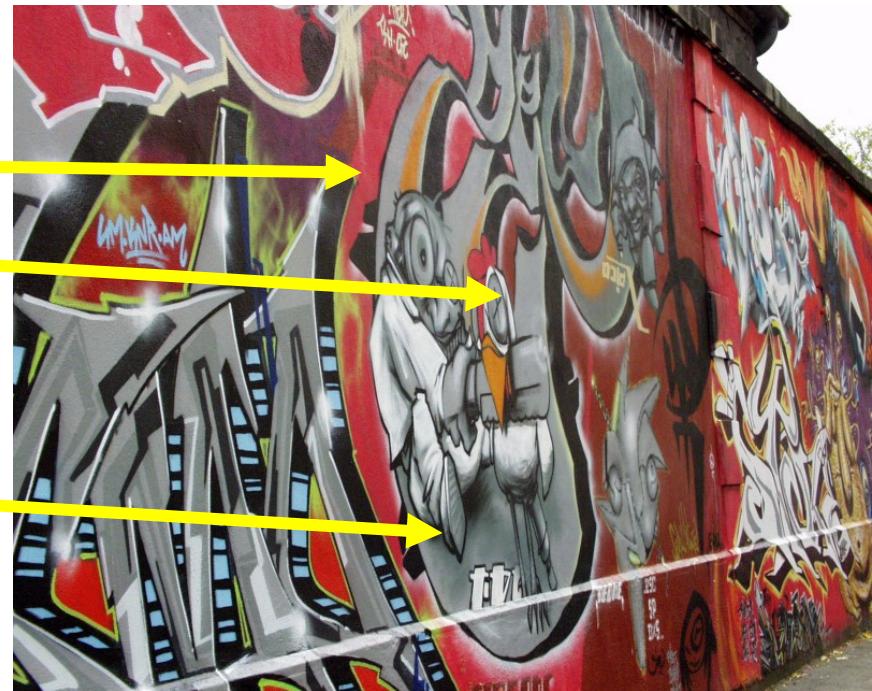
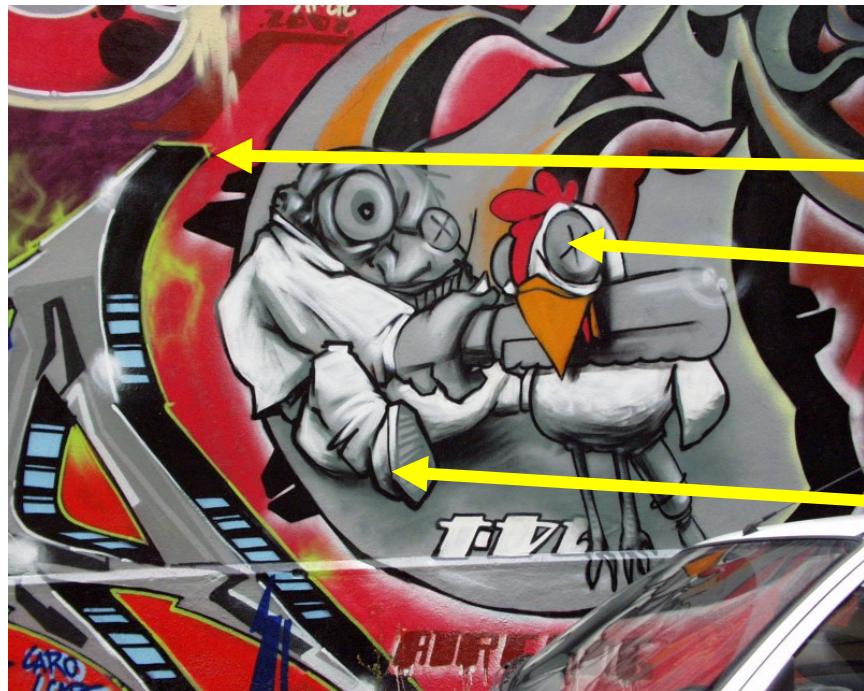


3D objects recognition



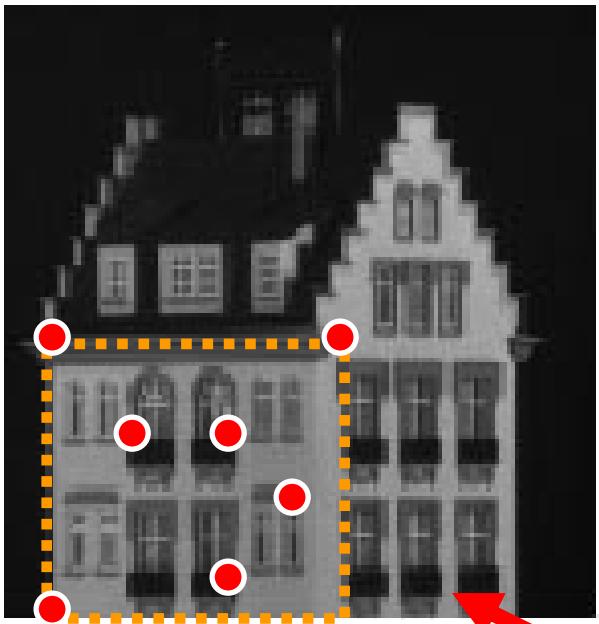
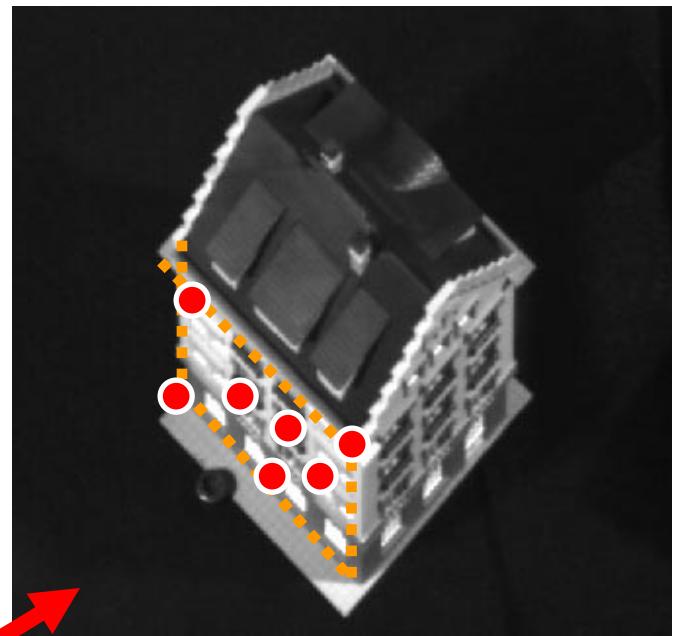


Example: Image matching





Example: Estimating an homographic transformation

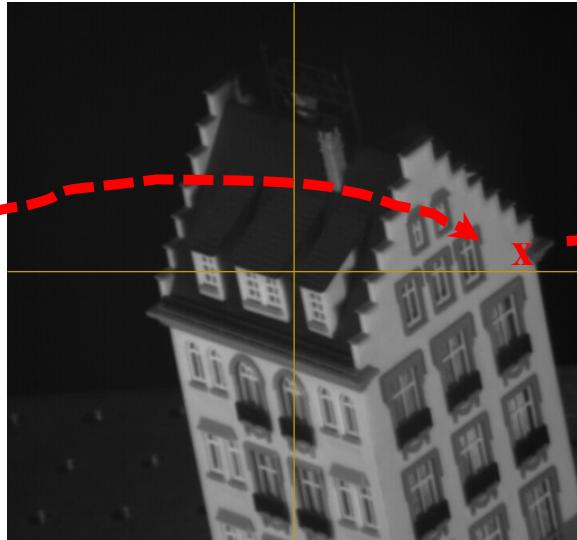
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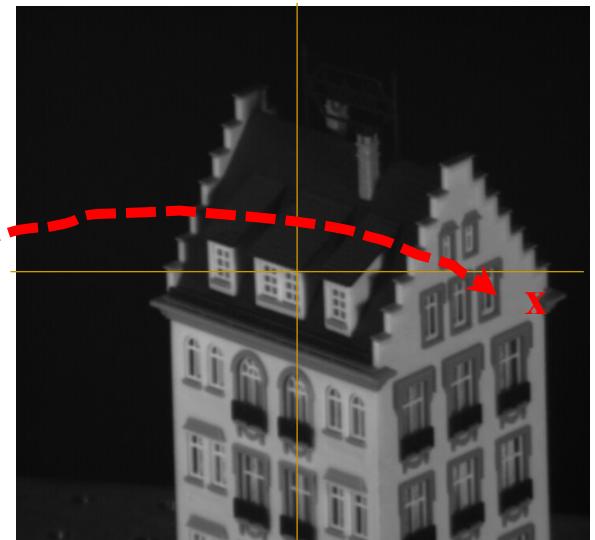
Example: tracking points



frame 0



frame 22



frame 49



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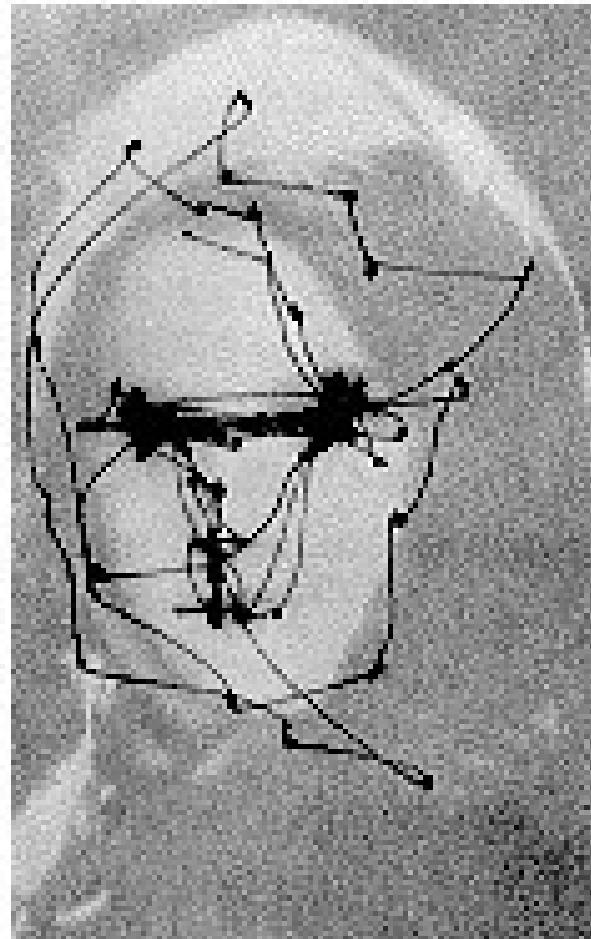
This class: interest points



- Note: “interest points” = “keypoints”, also sometimes called “local features”
- Many applications
 - tracking: which points are good to track?
 - recognition: find patches likely to tell us something about object category
 - 3D reconstruction: find correspondences across different views



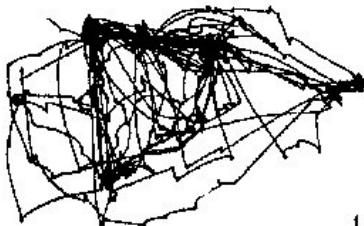
Human eye movements



Yarbus eye tracking



Human eye movements



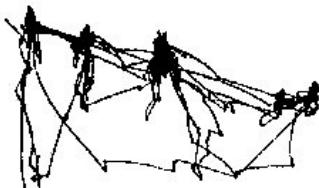
1

Free examination.



2

Estimate material circumstances
of the family



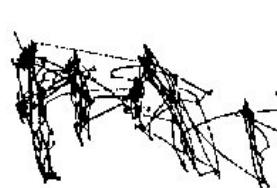
3

Give the ages of the people.



4

Surmise what the family had
been doing before the arrival
of the unexpected visitor.



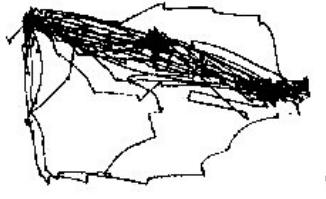
5

Remember the clothes
worn by the people.



6

Remember positions of people
and objects in the room.



7

Estimate how long the visitor had
been away from the family.

3 min. recordings
of the same
subject

Change blindness:
[http://www.simonslab.com/
videos.html](http://www.simonslab.com/videos.html)

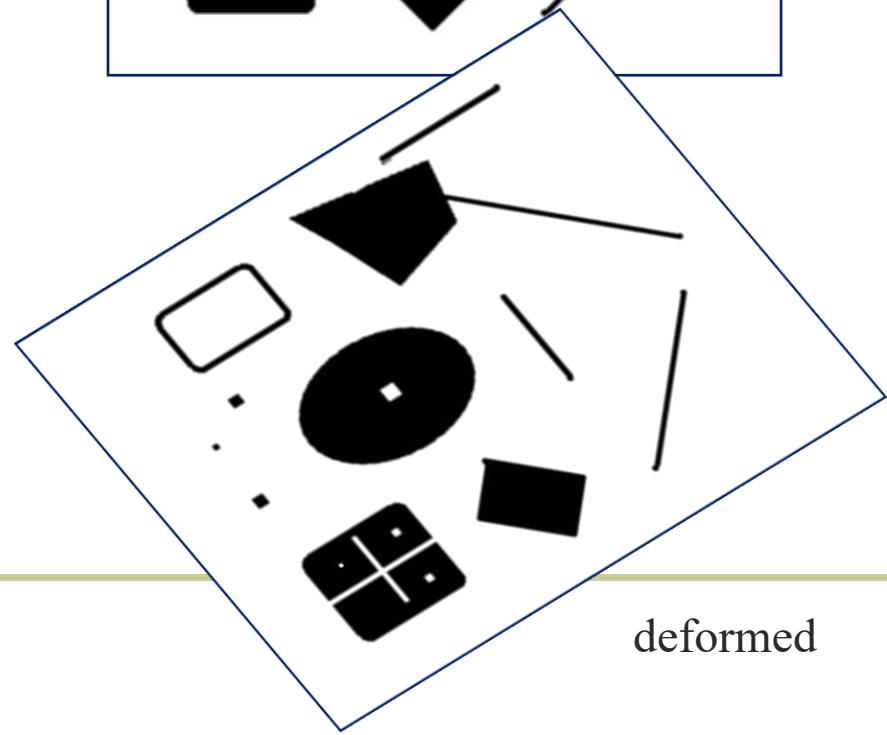
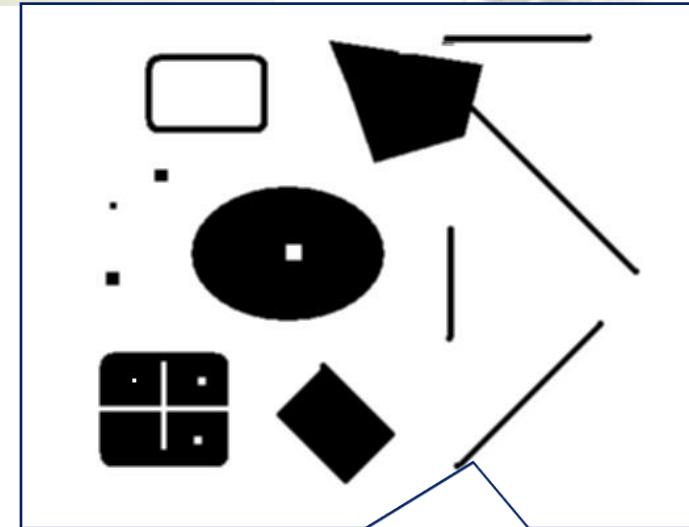
Study by Yarbus



This class: interest points



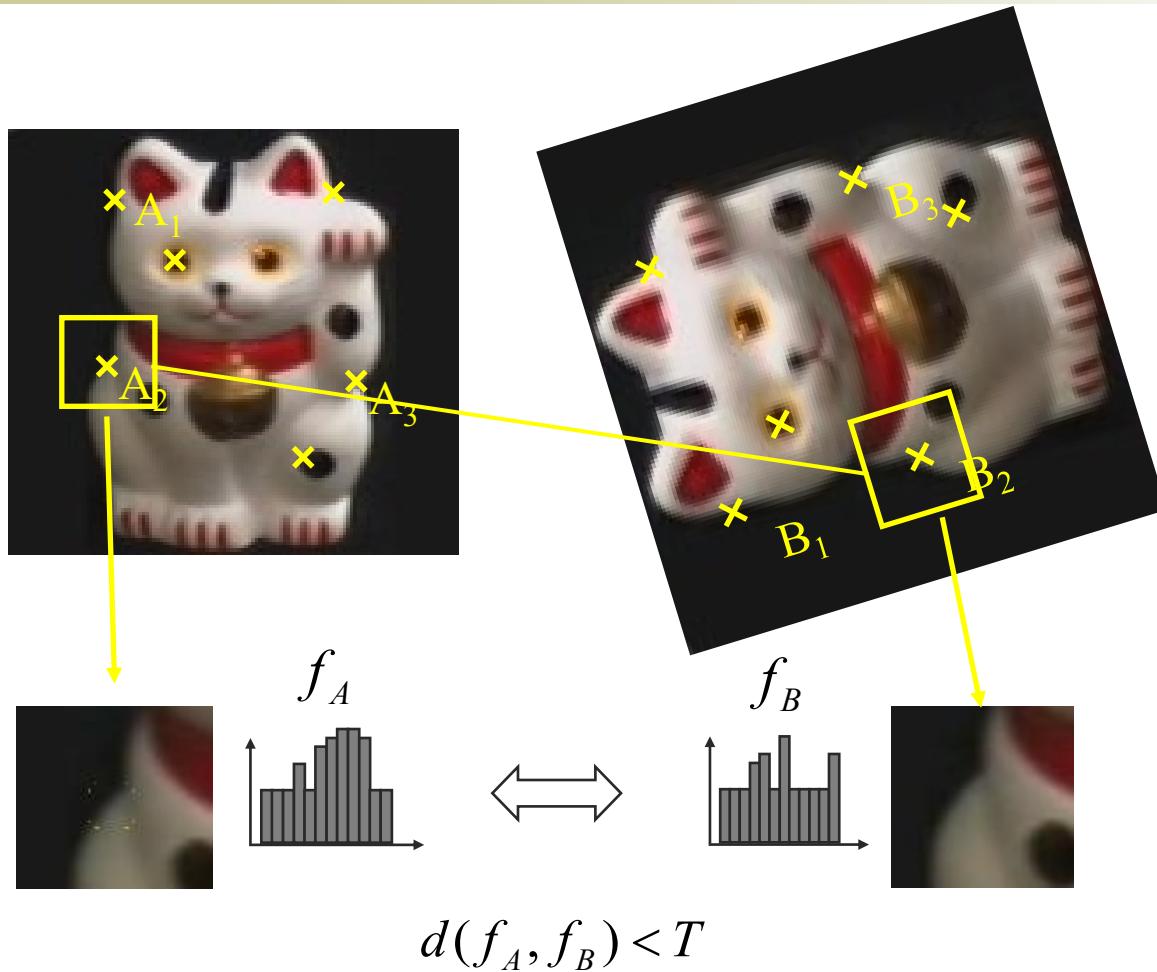
- Suppose you have to click on some point, go away and come back after I deform the image, and click on the same points again.
 - Which points would you choose?



deformed



Overview of Keypoint Matching



1. Find a set of distinctive keypoints
2. Define a region around each keypoint
3. Extract and normalize the region content
4. Compute a local descriptor from the normalized region
5. Match local descriptors



Goals for Keypoints



Detect points that are *repeatable* and *distinctive*



Goal: interest operator repeatability

- We want to detect (at least some of) the same points in both images.



No chance to find true matches!

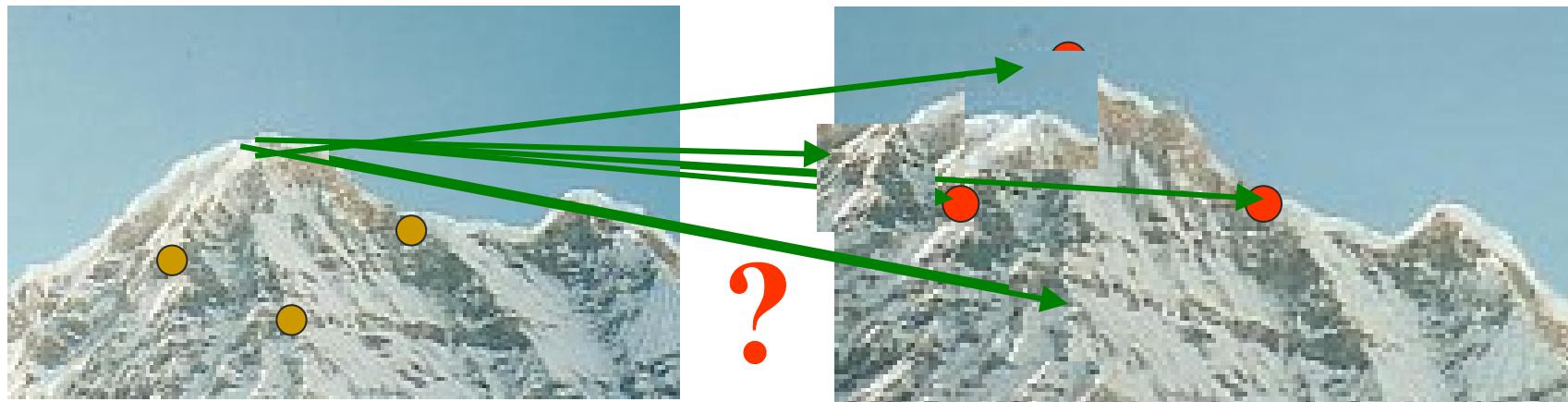
- Yet we have to be able to run the detection procedure *independently* per image.



Goal: descriptor distinctiveness



- We want to be able to reliably determine which point goes with which.



- Must provide some invariance to geometric and photometric differences between the two views.



Local features: desired properties

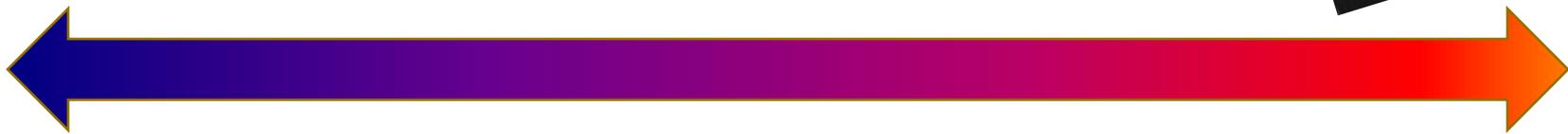


- Repeatability
 - The same feature can be found in several images despite geometric and photometric transformations
- Distinctiveness
 - Each feature has a distinctive description
- Compactness and efficiency
 - Many fewer features than image pixels
- Locality
 - A feature occupies a relatively small area of the image; robust to clutter and occlusion



Key trade-offs

Detection



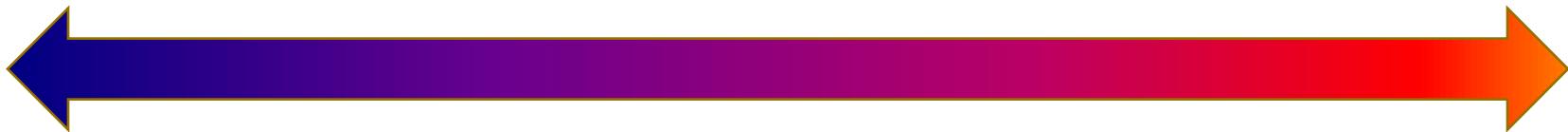
More Repeatable

Robust detection
Precise localization

More Points

Robust to occlusion
Works with less texture

Description



More Distinctive

Minimize wrong matches

More Flexible

Robust to expected variations
Maximize correct matches



Choosing interest points



Where would you tell
your friend to meet
you?



Corner detection



Choosing interest points



Where would you tell
your friend to meet
you?



Blob (valley/peak) detection



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Keypoint Localization



- Goals:
 - Repeatable detection
 - Precise localization
 - Interesting content
- ⇒ *Look for two-dimensional signal changes*

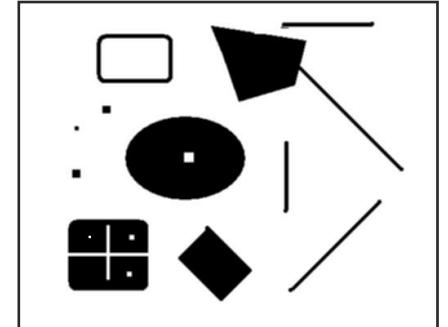


Harris Detector [Harris88]



■ Second moment matrix

$$\mu(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$



Intuition: Search for local neighborhoods where the image content has two main directions (eigenvectors).

C.Harris and M.Stephens. "A Combined Corner and Edge Detector."
Proceedings of the 4th Alvey Vision Conference, 1988.



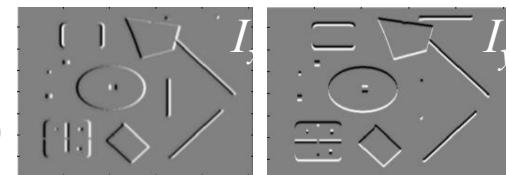
Harris Detector [Harris88]



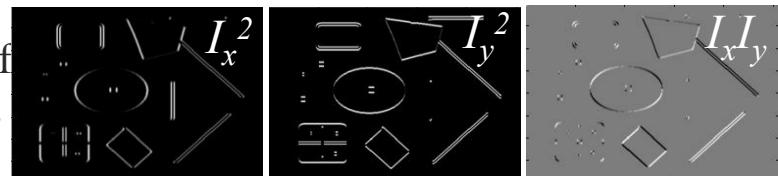
■ Second moment matrix

$$\mu(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$

1. Image derivatives
(optionally, blur first)



2. Square of derivatives



3. Gaussian filter $g(\sigma_D)$



$$\det M = \lambda_1 \lambda_2$$

$$\text{trace } M = \lambda_1 + \lambda_2$$

4. Cornerness function – both eigenvalues are strong

$$\begin{aligned} har &= \det[\mu(\sigma_I, \sigma_D)] - \alpha[\text{trace}(\mu(\sigma_I, \sigma_D))^2] = \\ &= g(I_x^2)g(I_y^2) - [g(I_x I_y)]^2 - \alpha[g(I_x^2) + g(I_y^2)]^2 \end{aligned}$$

5. Non-maxima suppression

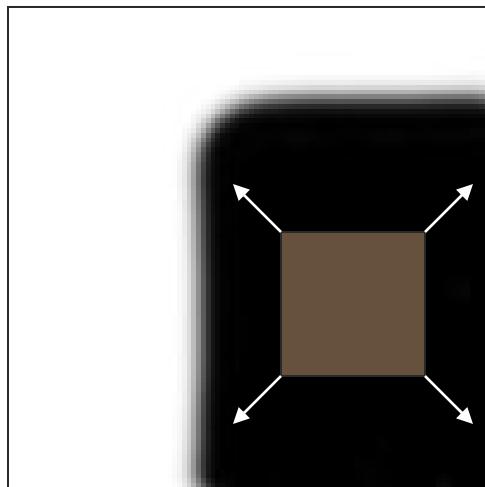




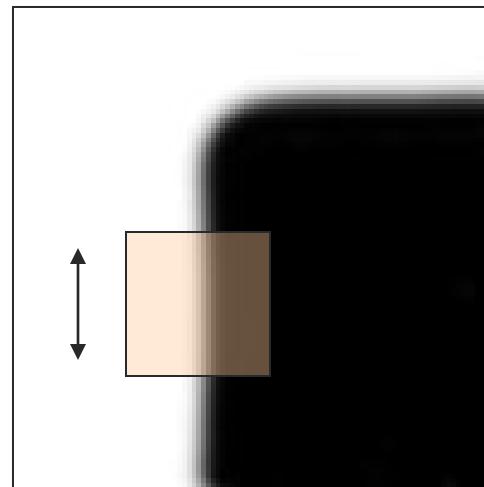
Corners as distinctive interest points



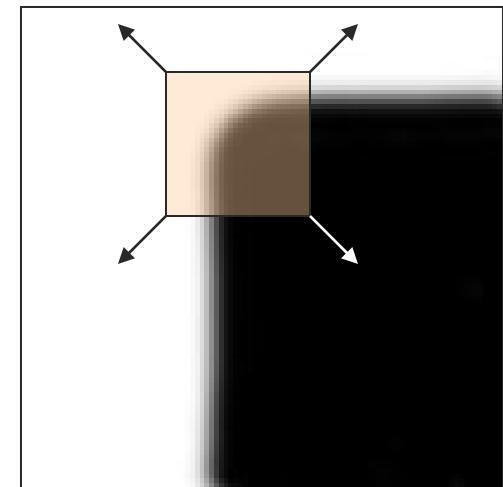
- We should easily recognize the point by looking through a small window
- Shifting a window in *any direction* should give a *large change* in intensity



“flat” region:
no change in
all directions



“edge”:
no change
along the edge
direction



“corner”:
significant
change in all
directions



Error function



Change of intensity for the shift $[u, v]$:

$$E(u, v) = \sum_{x, y} w(x, y)[I(x + u, y + v) - I(x, y)]$$

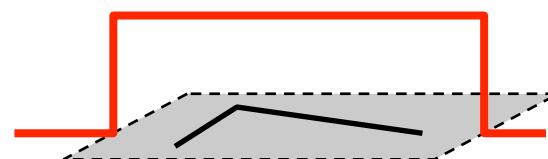
Error
function

Window
function

Shifted
intensity

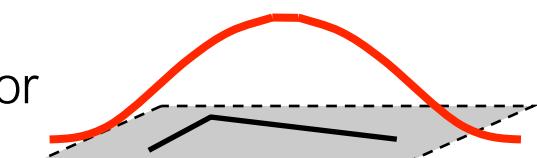
Intensity

Window function $w(x, y) =$



1 in window, 0 outside

or



Gaussian



Error function approximation



Change of intensity for the shift $[u, v]$:

$$E(u, v) = \sum_{x,y} w(x, y) [I(x + u, y + v) - I(x, y)]$$

First-order Taylor expansion of $I(x, y)$ about $(0, 0)$
(bilinear approximation for small shifts)



Bilinear approximation



For small shifts $[u, v]$ we have a ‘bilinear approximation’:

Change in
appearance for a
shift $[u, v]$

$$E(u, v) \cong [u, v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

where M is a 2×2 matrix computed from image derivatives:

‘second moment’ matrix
‘structure tensor’

$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$



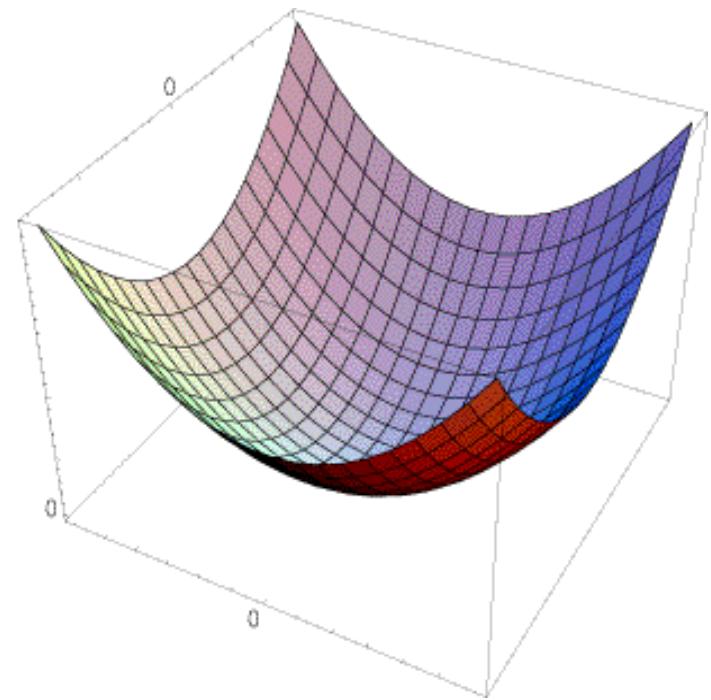
Visualization of a quadratic



The surface $E(u,v)$ is locally approximated by a quadratic form

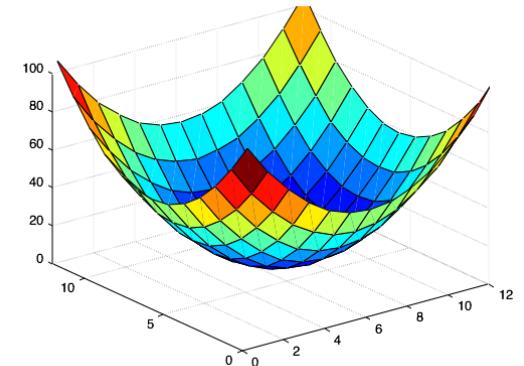
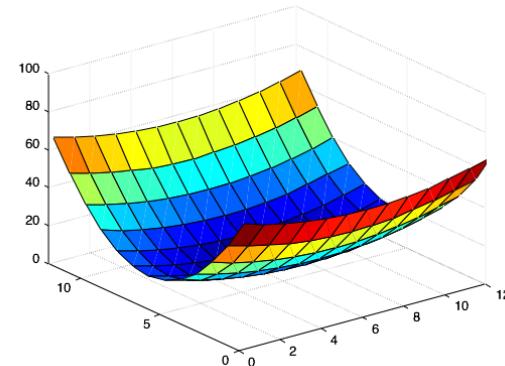
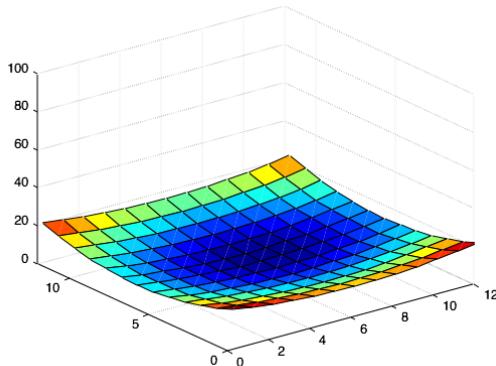
$$E(u,v) \approx [u \ v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

$$M = \sum \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$





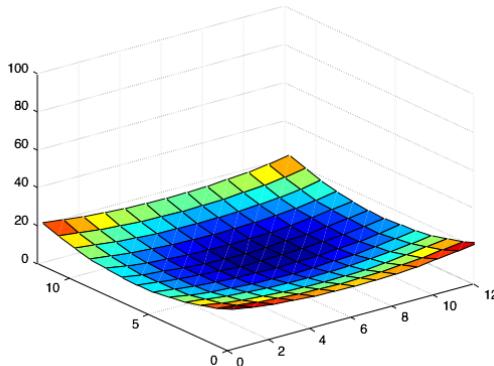
Which error surface indicates a good image feature?



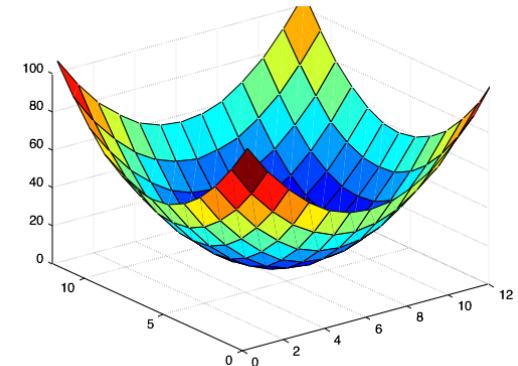
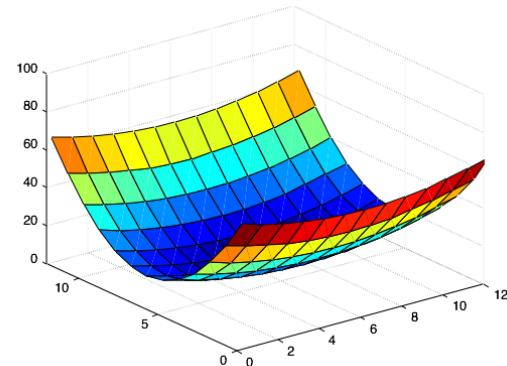
What kind of image patch do these surfaces represent?



Which error surface indicates a good image feature?

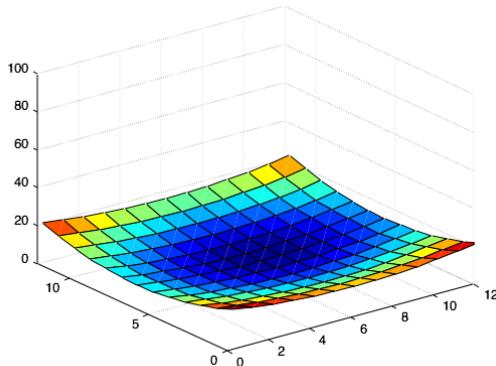


flat

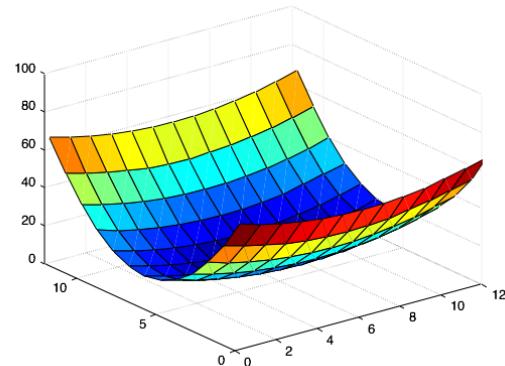




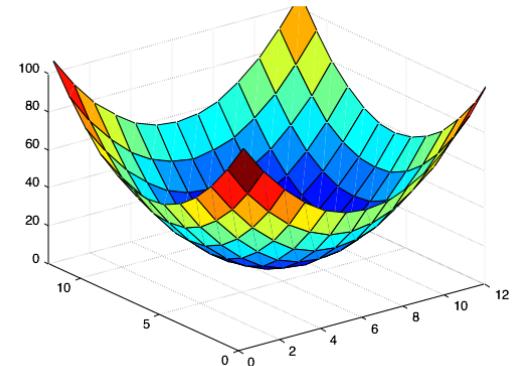
Which error surface indicates a good image feature?



flat

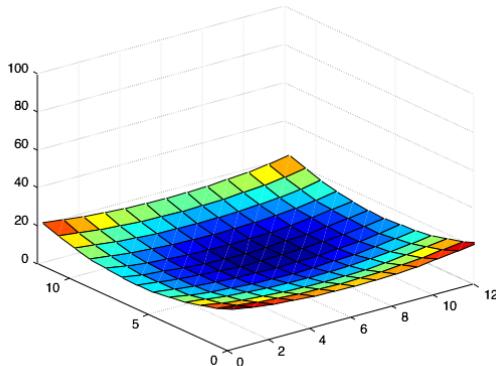


edge
'line'

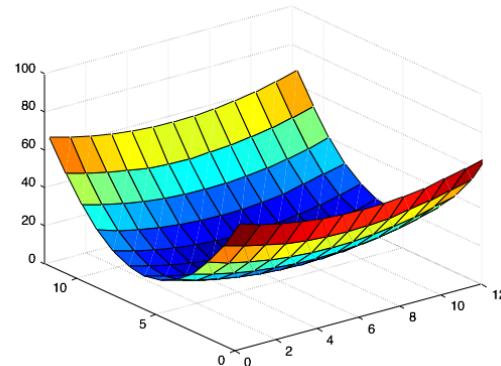




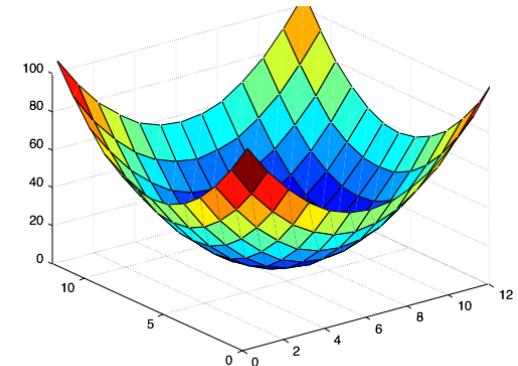
Which error surface indicates a good image feature?



flat



edge
'line'



corner
'dot'



Visualization as an ellipse



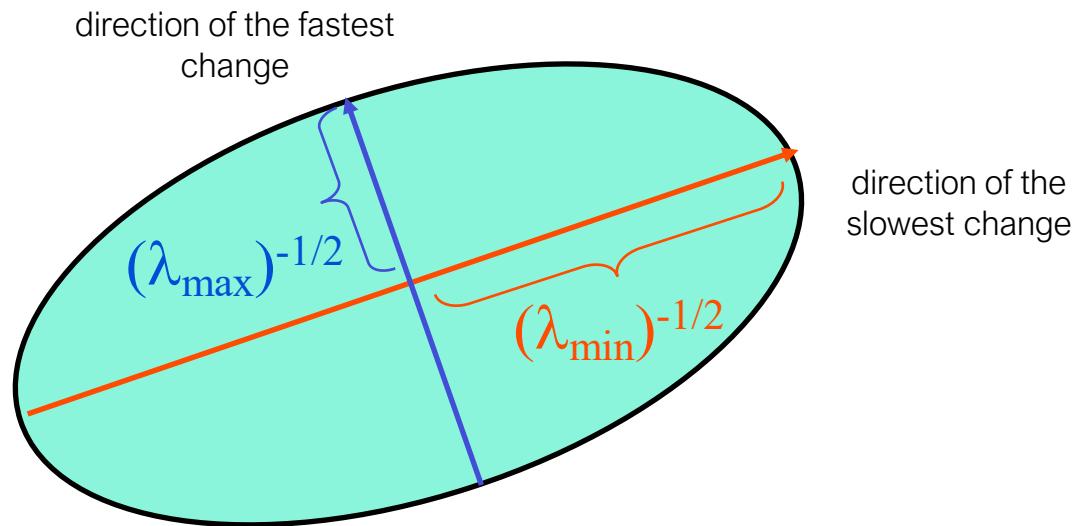
Since M is symmetric, we have

$$M = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

We can visualize M as an ellipse with axis lengths determined by the eigenvalues and orientation determined by R

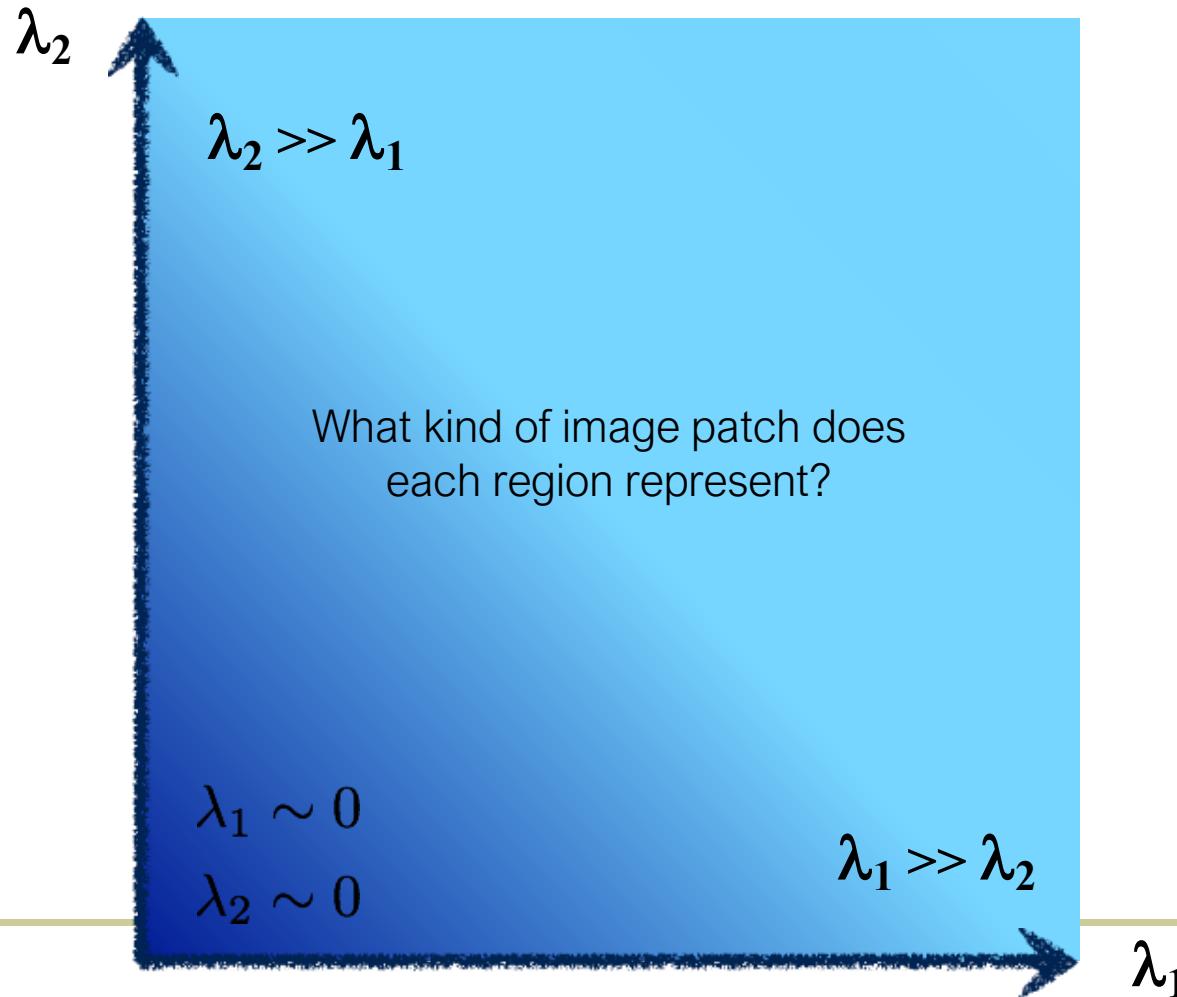
Ellipse equation:

$$[u \ v] M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$$



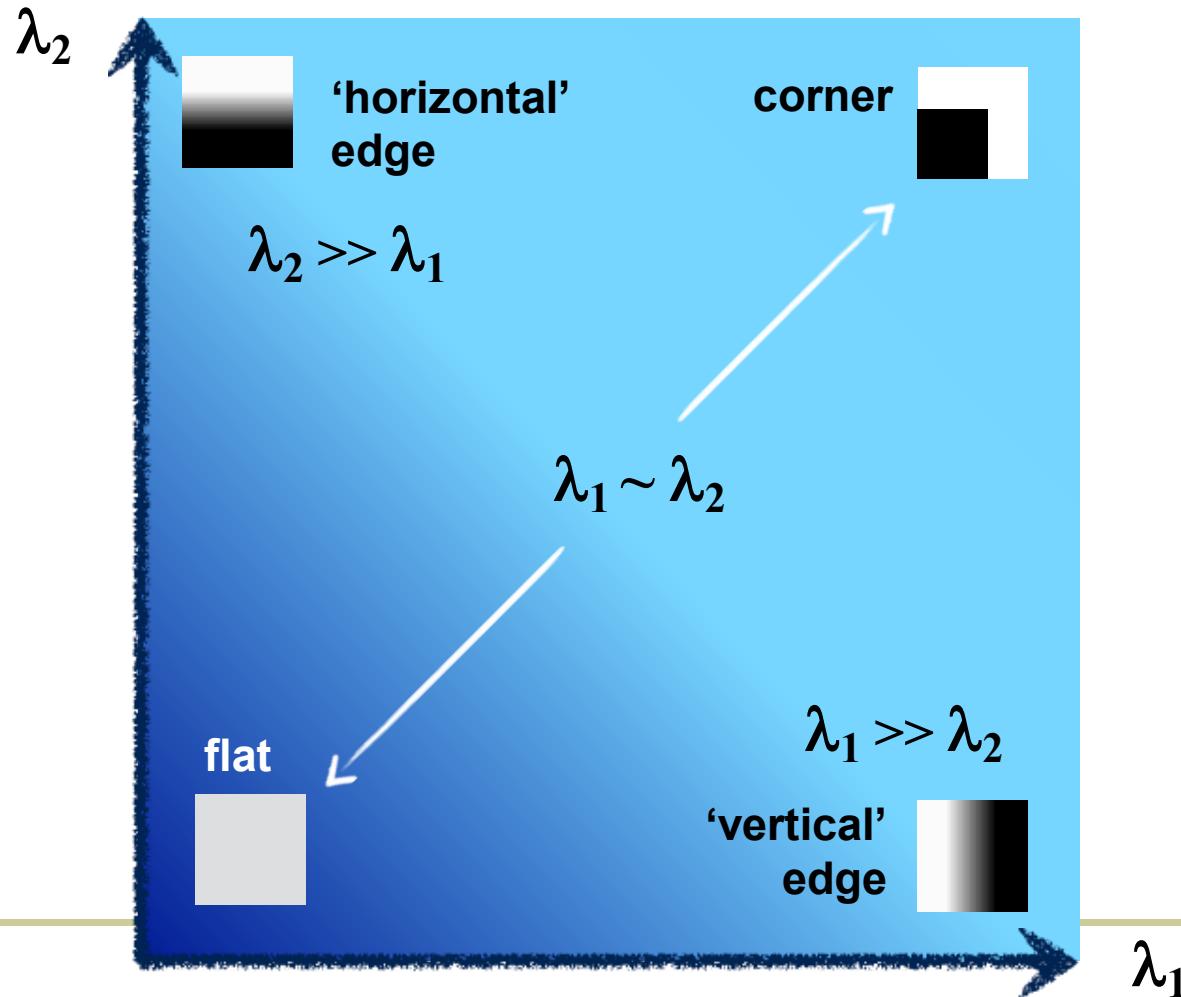


interpreting eigenvalues



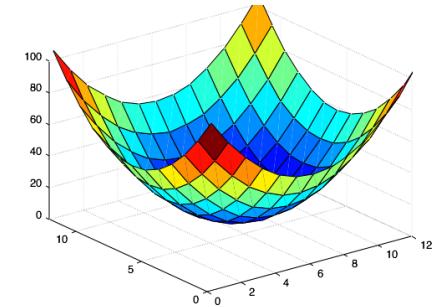
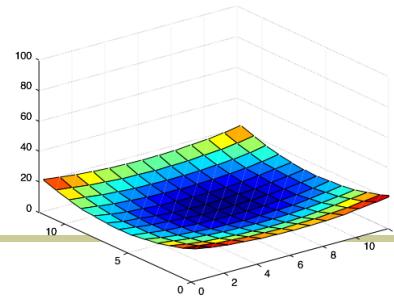
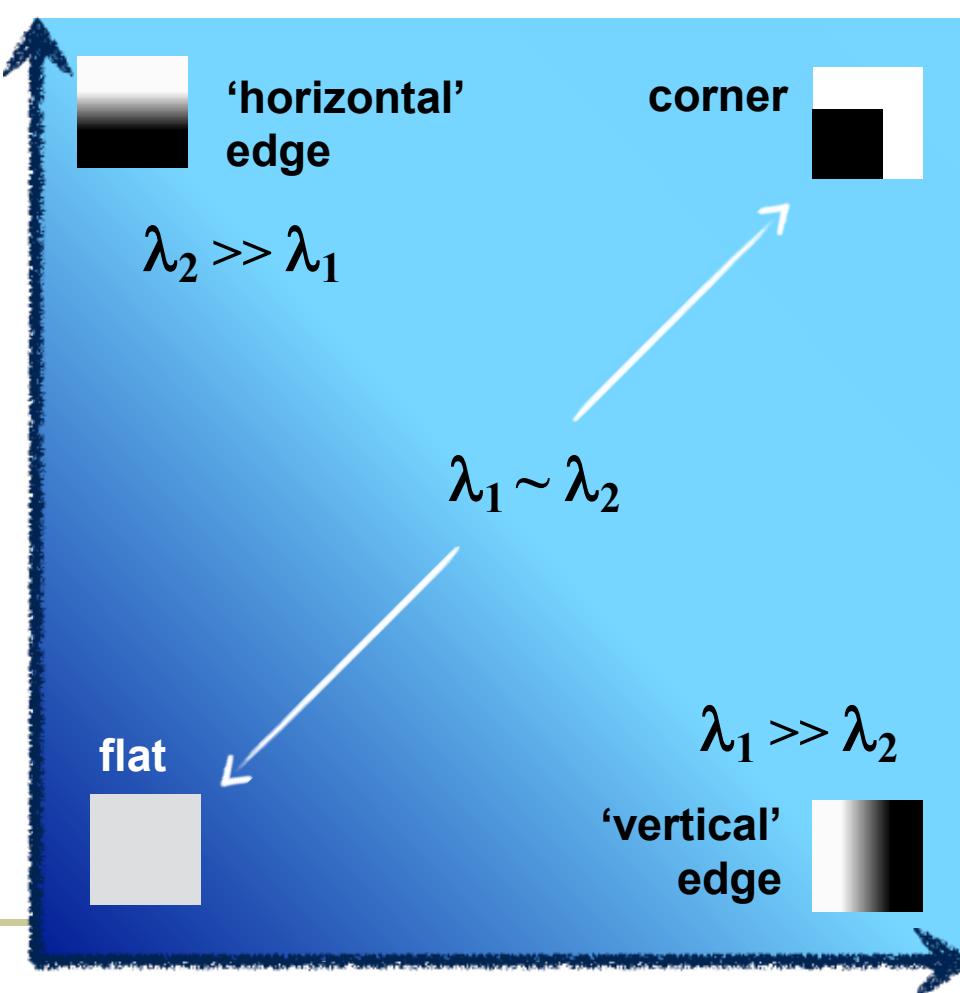
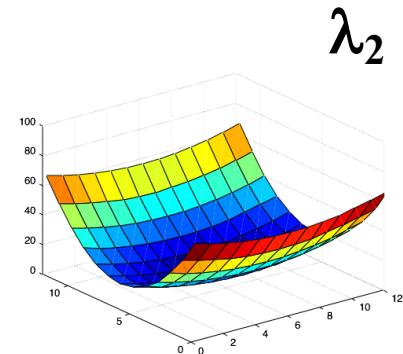


interpreting eigenvalues



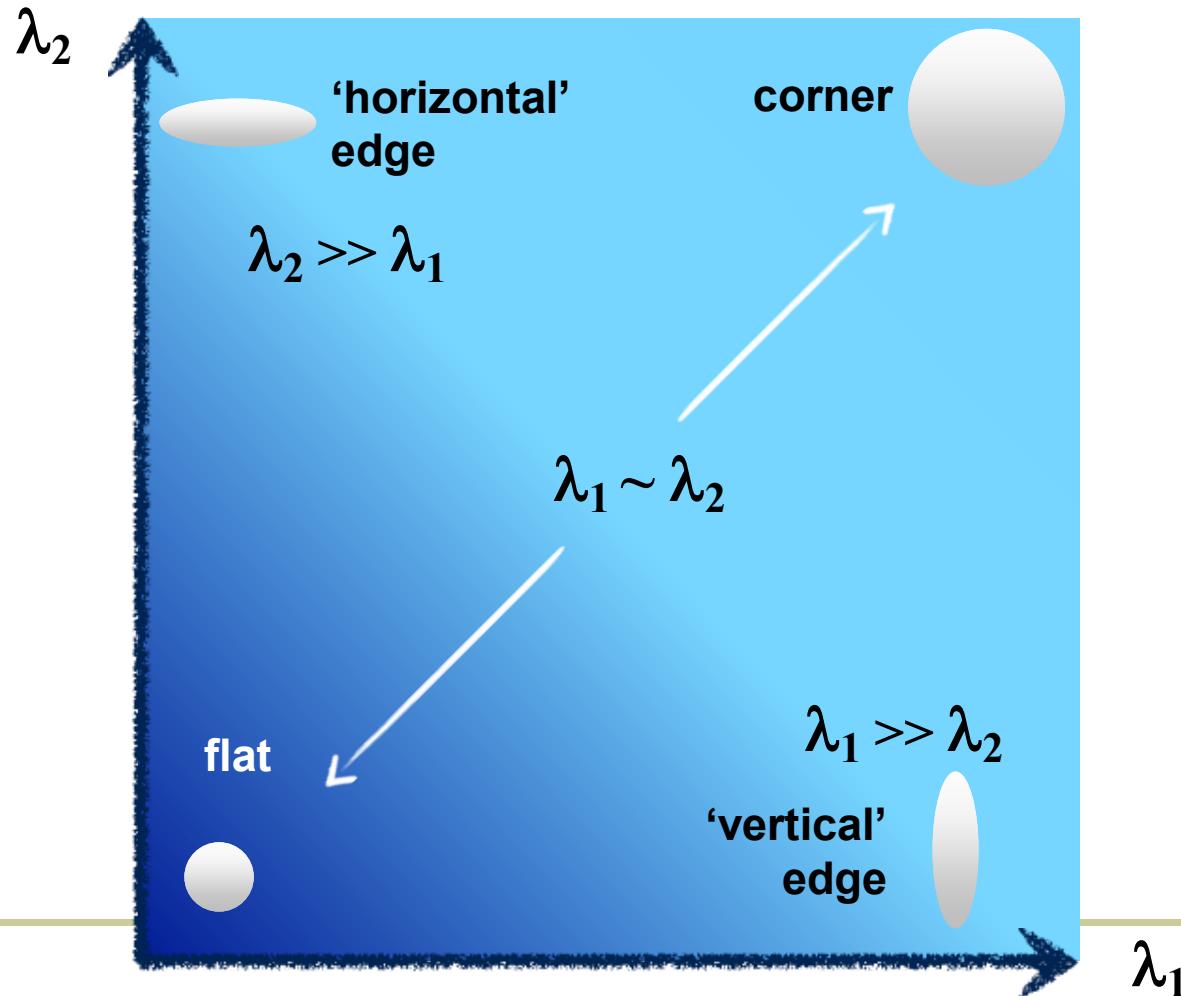


interpreting eigenvalues





interpreting eigenvalues



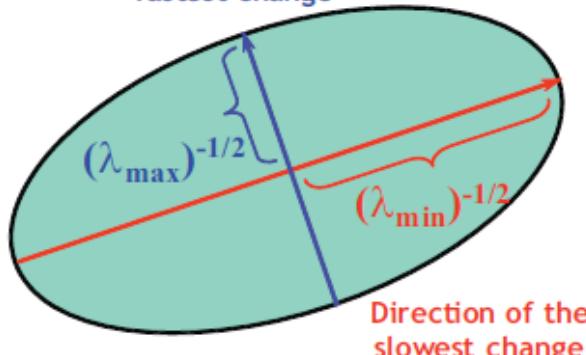


Explanation of Harris Criterion

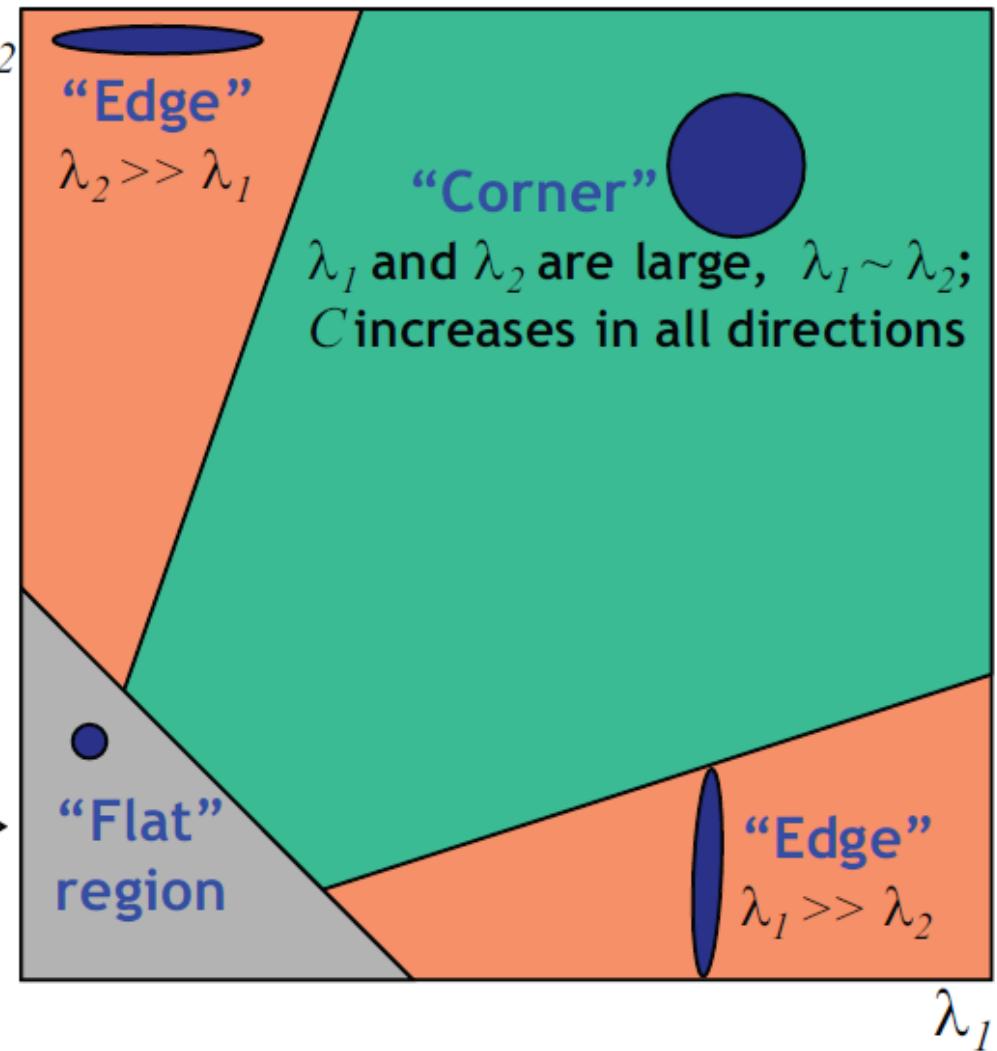


$$C = \begin{bmatrix} \sum I_x^2 & \sum I_x I_y \\ \sum I_x I_y & \sum I_y^2 \end{bmatrix} = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

Direction of the
fastest change



λ_1 and λ_2 are small;
 C is almost constant
in all directions





Harris Detector: Criteria



$$M = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$

1. Want large eigenvalues, and small ratio $\frac{\lambda_1}{\lambda_2} < t$

2. We know

$$\det M = \lambda_1 \lambda_2$$

$$\text{trace } M = \lambda_1 + \lambda_2$$

3. Leads to

$$\det M - k \cdot \text{trace}^2(M) > t$$

(k :empirical constant, $k = 0.04\text{-}0.06$)

Nice brief derivation on wikipedia



Harris Detector: Criteria



Harris & Stephens (1988)

$$R = \det(M) - \kappa \text{trace}^2(M)$$

Kanade & Tomasi (1994)

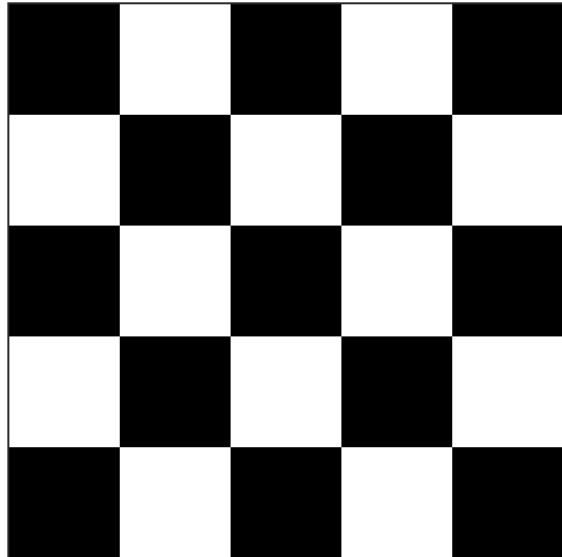
$$R = \min(\lambda_1, \lambda_2)$$

Nobel (1998)

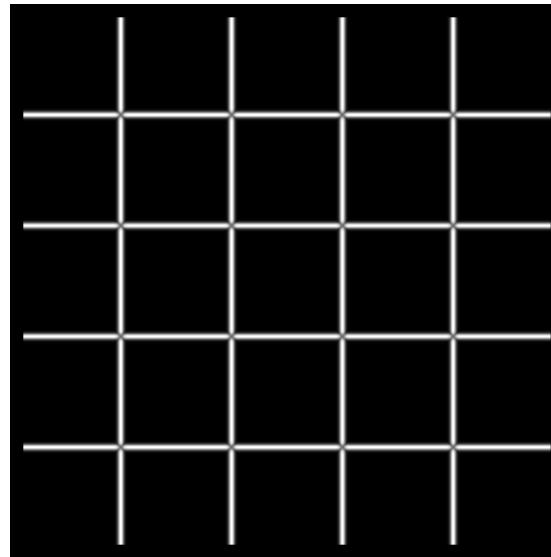
$$R = \frac{\det(M)}{\text{trace}(M) + \epsilon}$$



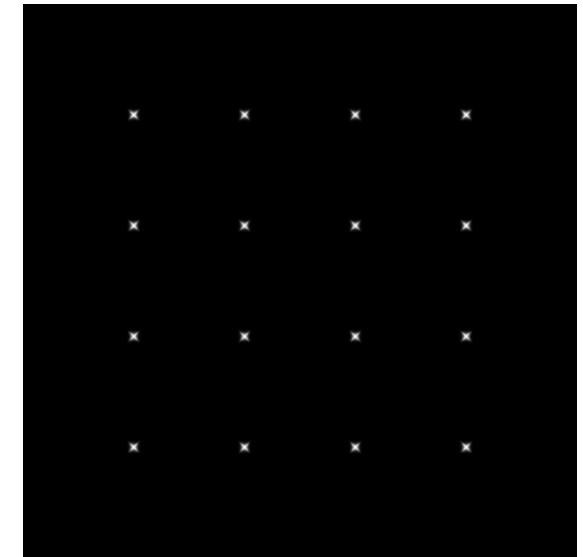
Harris Detector: Criteria



I



λ_{\max}



λ_{\min}

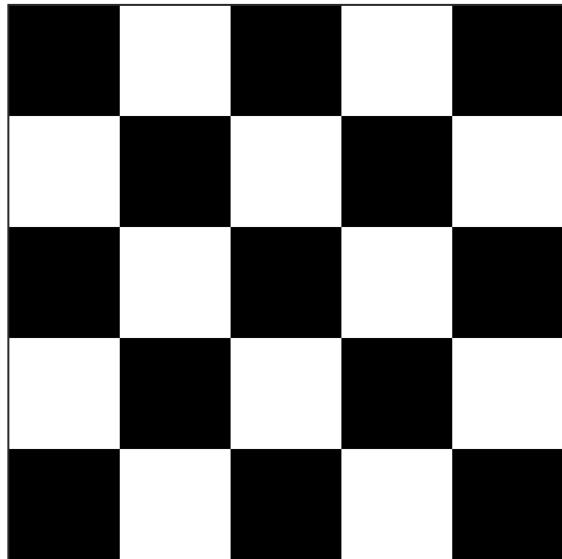
Yet another option:

$$f = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$$

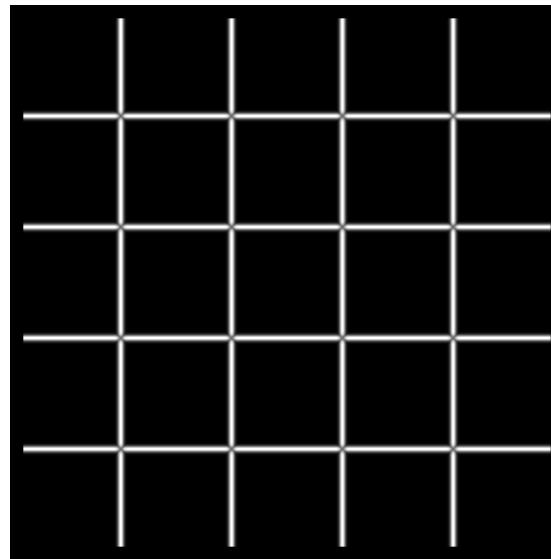
How do you write this equivalently
using determinant and trace?



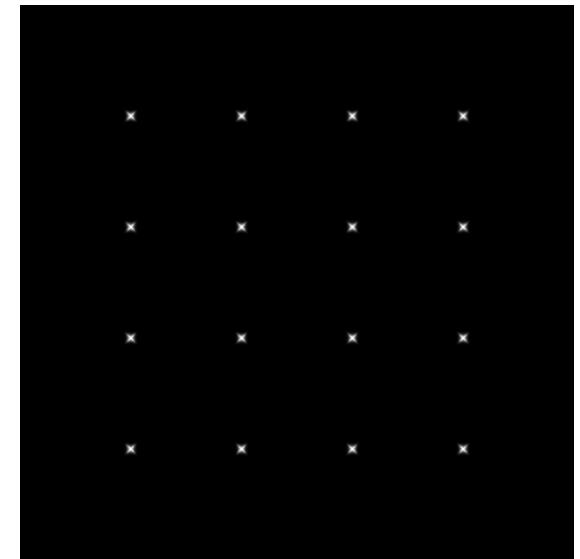
Harris Detector: Criteria



I



λ_{\max}



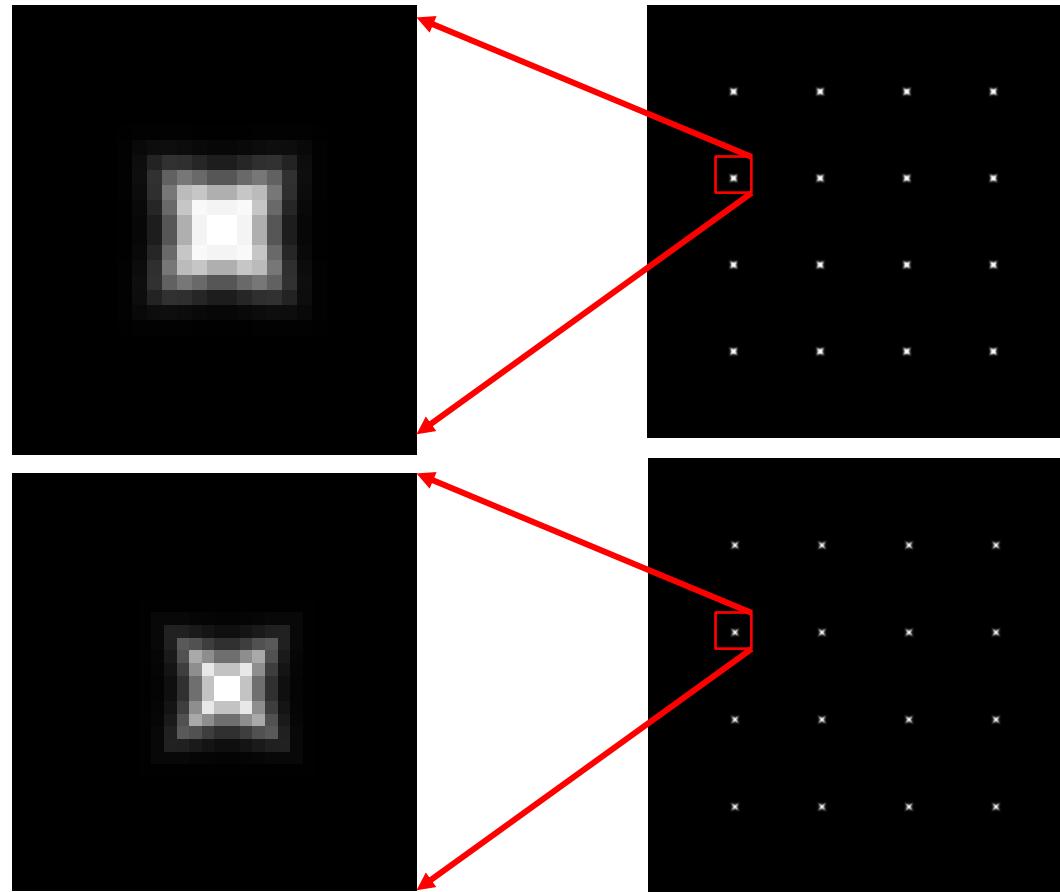
λ_{\min}

Yet another option:

$$f = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2} = \frac{\text{determinant}(H)}{\text{trace}(H)}$$



Different criteria

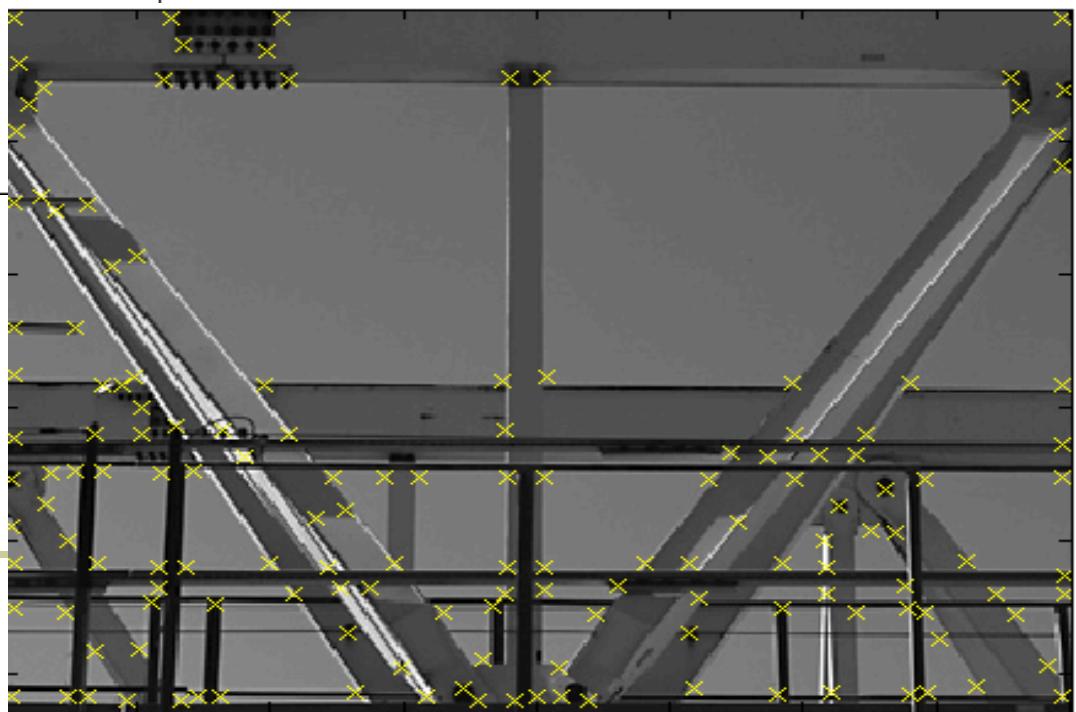
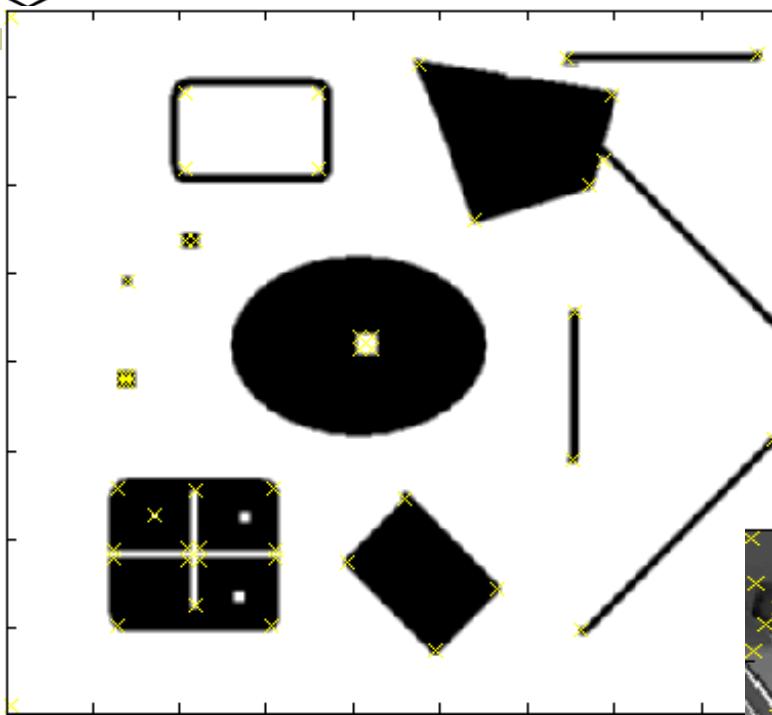


Harris criterion

λ_{\min}



Harris Detector – Responses [Harris88]



Effect: A very precise corner detector.



Harris Detector - Responses [Harris88]



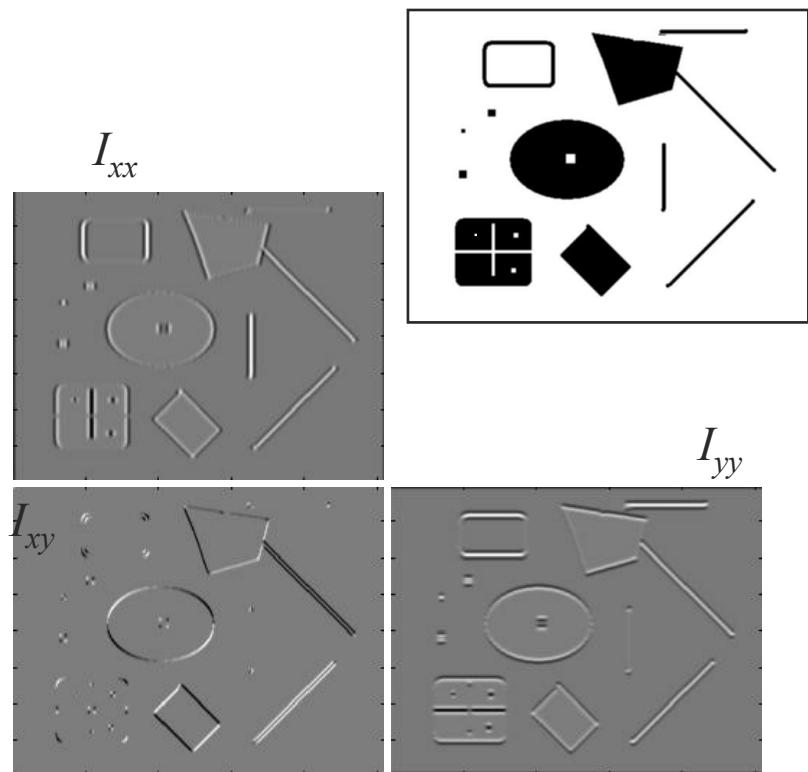


Hessian Detector [Beaudet78]



■ Hessian determinant

$$Hessian(I) = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix}$$



Intuition: Search for strong curvature in two orthogonal directions



Hessian Detector [Beaudet78]



■ Hessian determinant

$$Hessian(x, \sigma) = \begin{bmatrix} I_{xx}(x, \sigma) & I_{xy}(x, \sigma) \\ I_{xy}(x, \sigma) & I_{yy}(x, \sigma) \end{bmatrix}$$

$$\det M = \lambda_1 \lambda_2$$

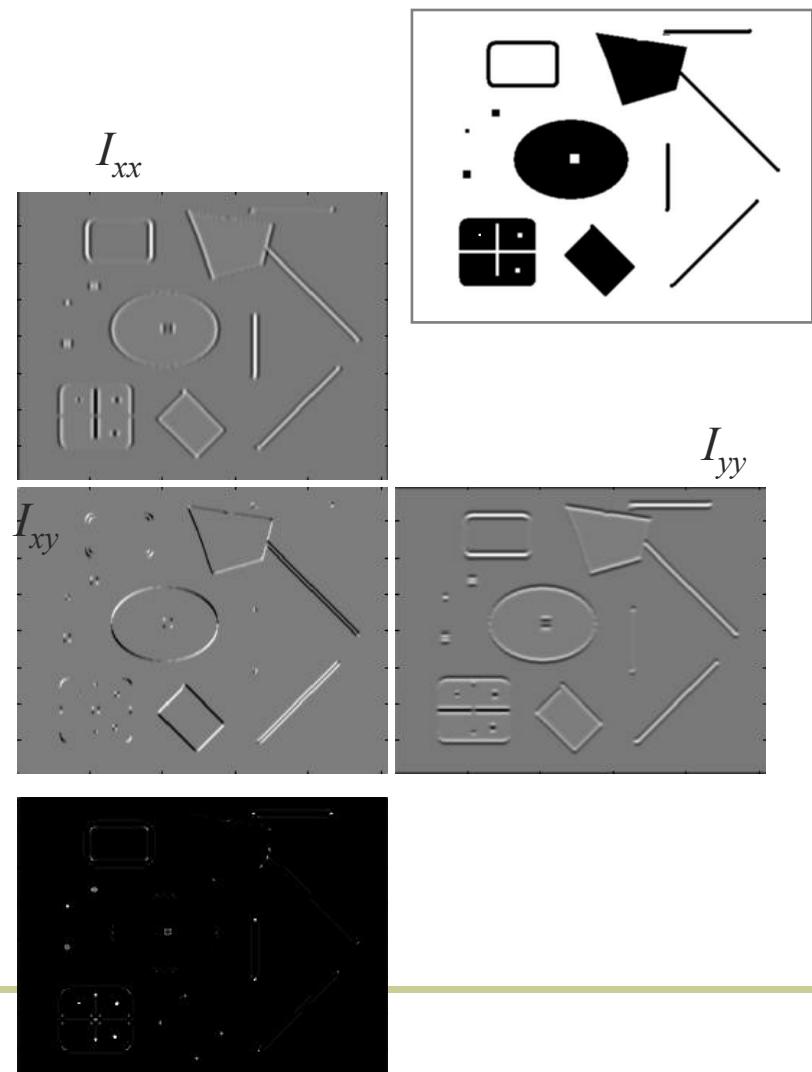
$$\text{trace } M = \lambda_1 + \lambda_2$$

Find maxima of determinant

$$\det(Hessian(x)) = I_{xx}(x)I_{yy}(x) - I_{xy}^2(x)$$

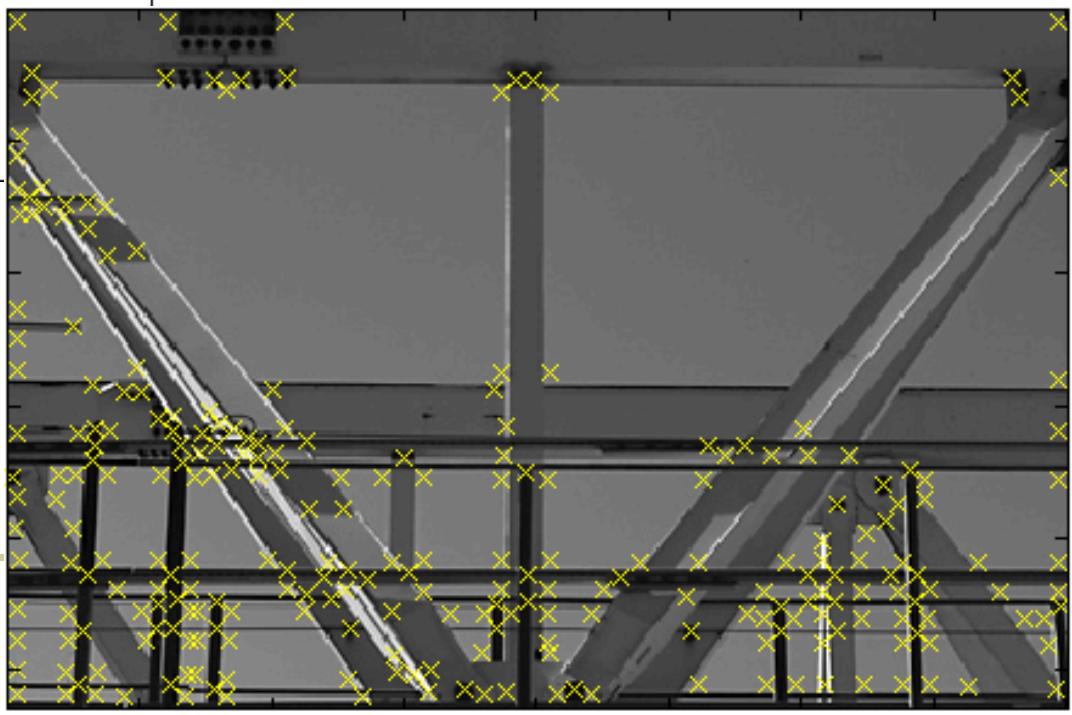
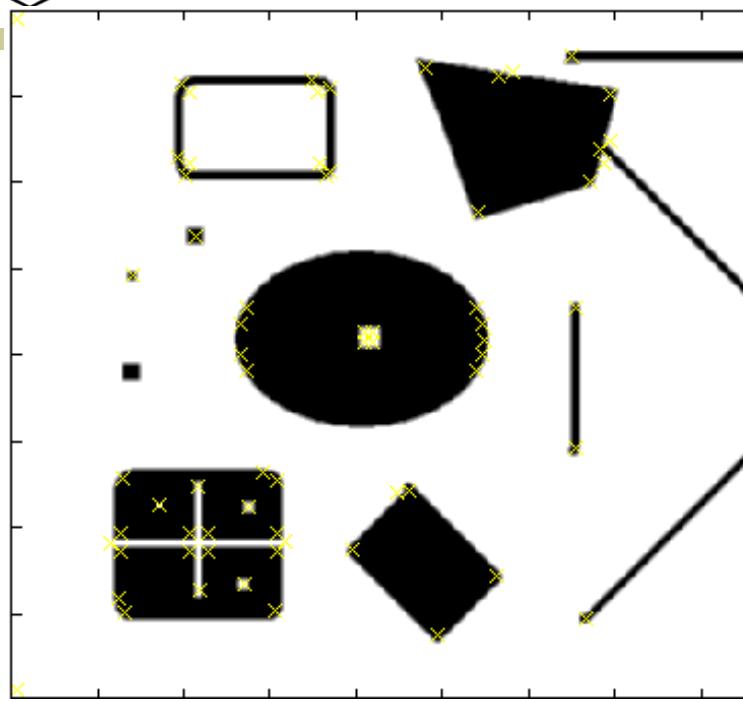
In Matlab:

$$I_{xx}.*I_{yy} - (I_{xy})^2$$





Hessian Detector – Responses [Beaudet78]



Effect: Responses mainly on corners and strongly textured areas.

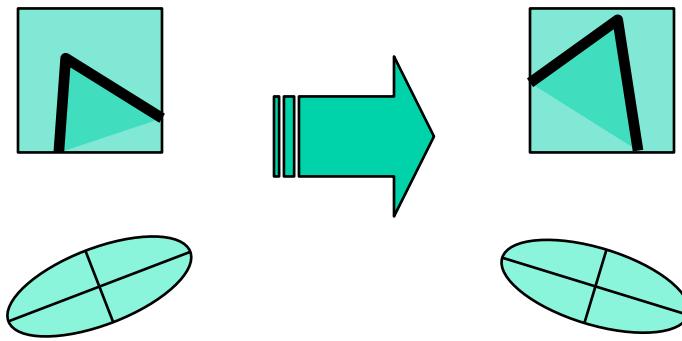


Hessian Detector – Responses [Beaudet78]





Harris corner response is invariant to rotation



Ellipse rotates but its shape
(eigenvalues) remains the same

Corner response R is invariant to image rotation



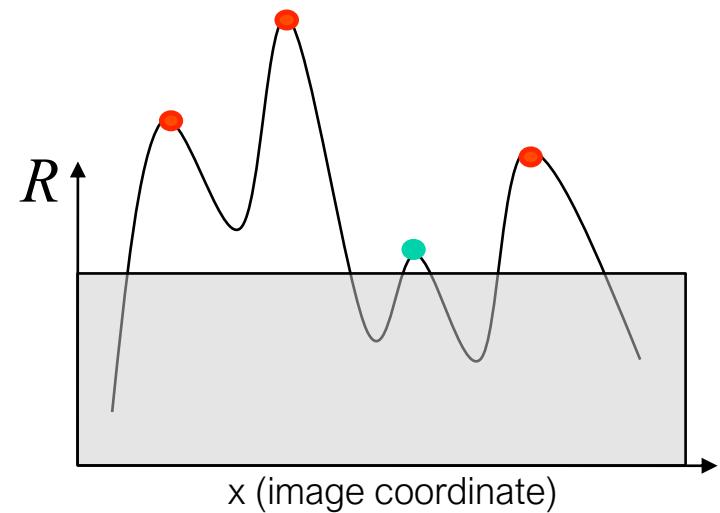
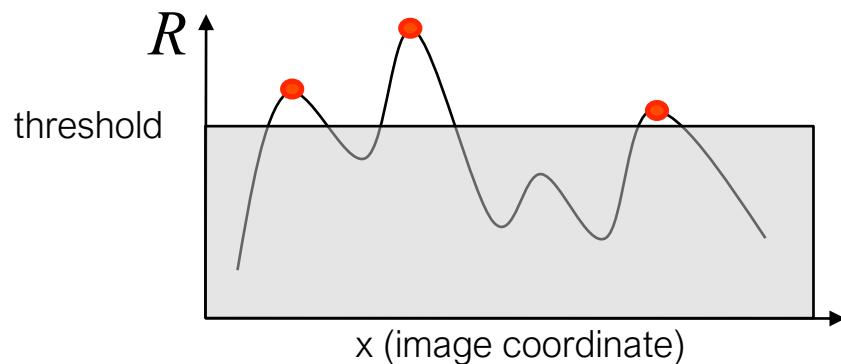
Harris corner response is invariant to intensity changes



Partial invariance to *affine intensity* change

Only derivatives are used => invariance to intensity shift $I \rightarrow I + b$

Intensity scale: $I \rightarrow a I$

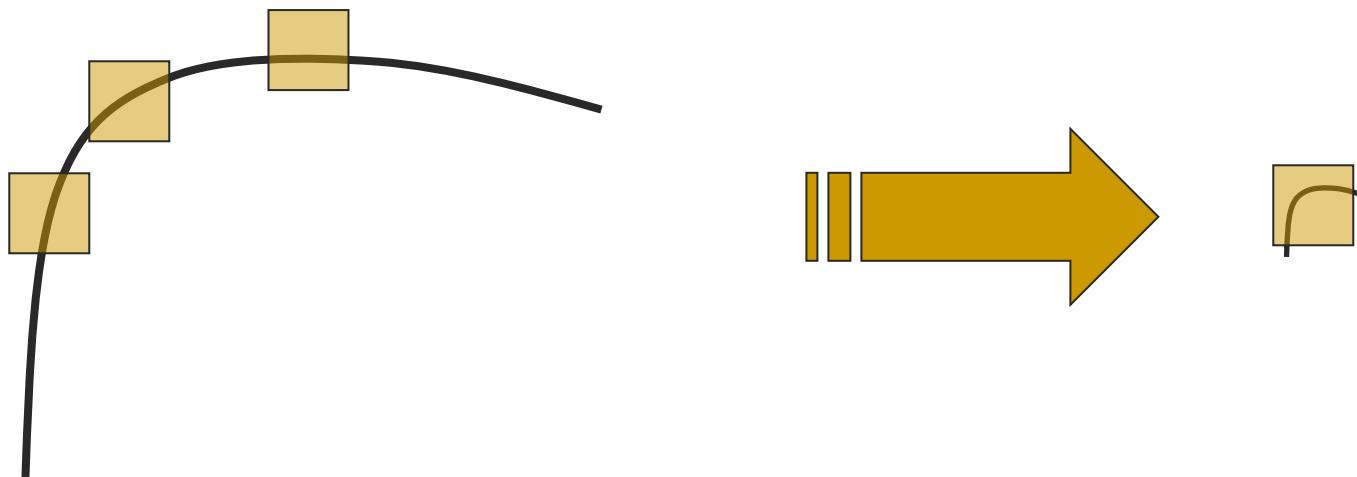




Scale invariance?



- Scale invariant? No



All points will be
classified as **edges**

Corner !



Today's Class



- Introduction to correspondence and alignment
- Overview of interest points
 - Matching pipeline
 - Repeatable & Distinctive
- Keypoint Localization
 - Harris detector
 - Hessian detector
- Scale invariant region selection
 - Automatic scale selection
 - Laplacian of Gaussian (LoG) & Difference of Gaussian (DoG)
 - Combinations: Harris-Laplacian & Hessian-Laplacian



From points to regions



- The Harris and Hessian operators define interest points.

- Precise localization
 - High repeatability



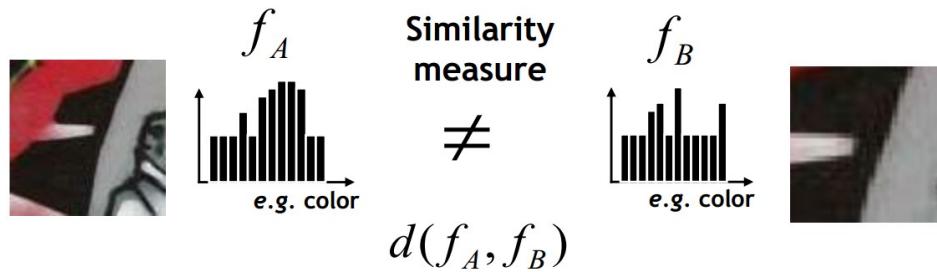
- In order to compare those points, we need to compute a descriptor over a region.
 - How can we define such a region in a scale invariant manner?
- *I.e. how can we detect scale invariant interest regions?*



Naïve approach: exhaustive search



- Multi-scale procedure
 - Compare descriptors while varying the patch size

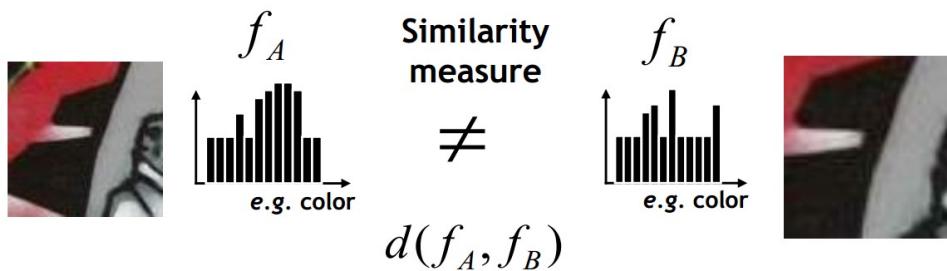
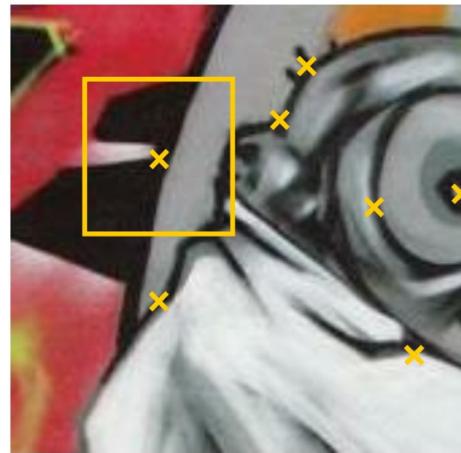




Naïve approach: exhaustive search



- Multi-scale procedure
 - Compare descriptors while varying the patch size

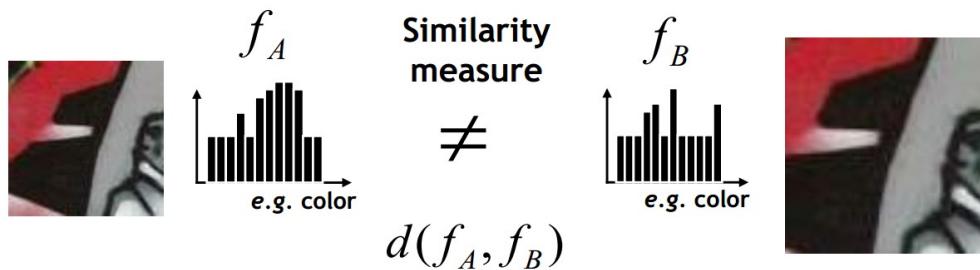




Naïve approach: exhaustive search



- Multi-scale procedure
 - Compare descriptors while varying the patch size

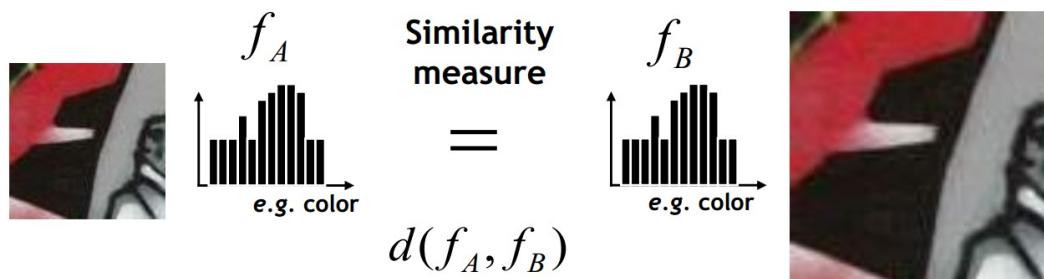




Naïve approach: exhaustive search



- Multi-scale procedure
 - Compare descriptors while varying the patch size

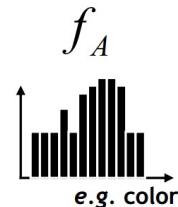




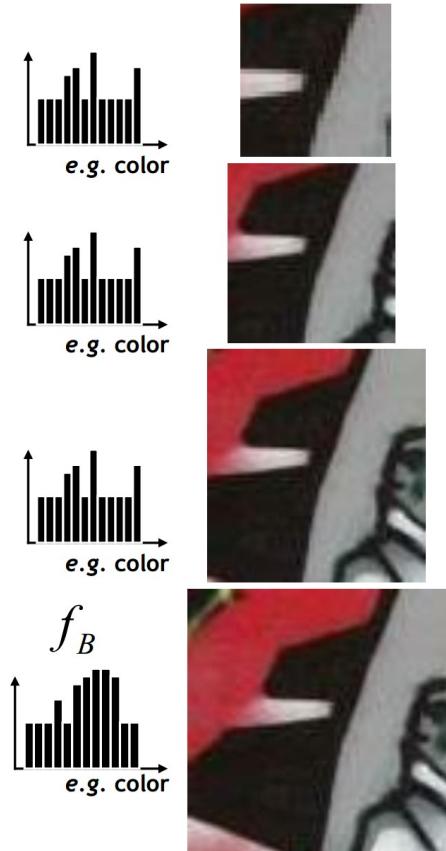
Naïve approach: exhaustive search



- Comparing descriptors while varying the patch size
 - Computationally inefficient
 - Inefficient but possible for matching
 - Prohibitive for retrieval in large databases
 - Prohibitive for recognition



Similarity measure
=
 $d(f_A, f_B)$

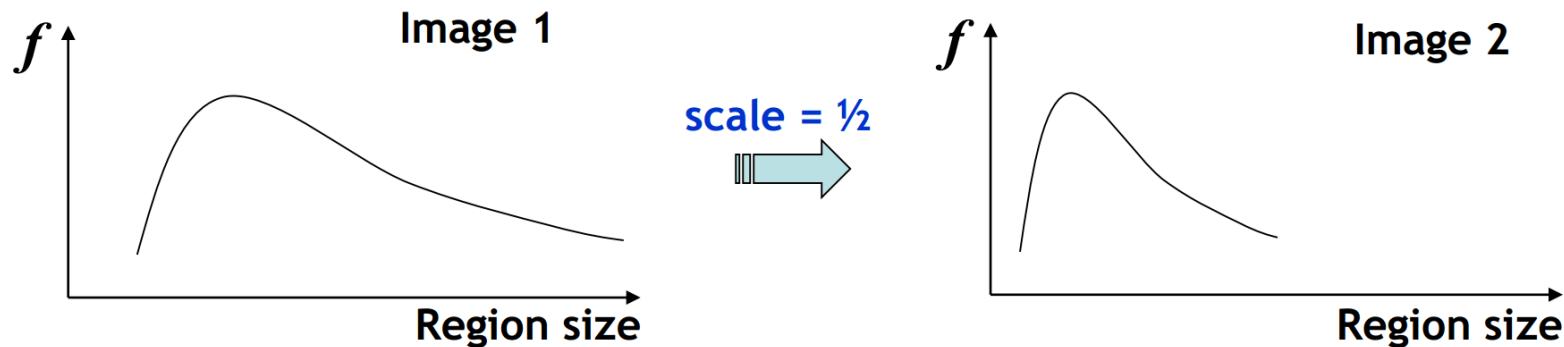




Automatic scale selection



- Solution:
 - Design a function on the region, which is “scale invariant” (*the same for corresponding regions, even if they are at different scales*)
Example: average intensity. For corresponding regions (even of different sizes) it will be the same.
 - For a point in one image, we can consider it as a function of region size (patch width)



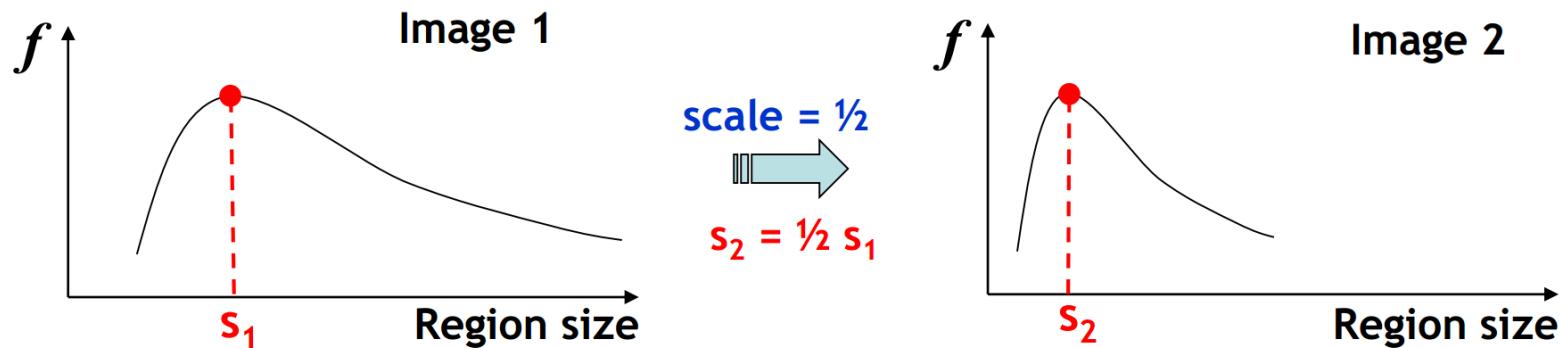


Automatic scale selection



- Common approach:
 - Take a local maximum of this function.
 - Observation: region size for which the maximum is achieved should be *invariant* to image scale.

Important: this scale invariant region size is found in each image independently!

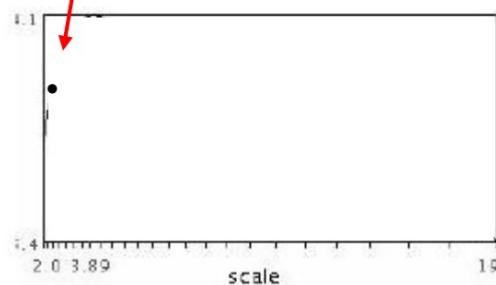




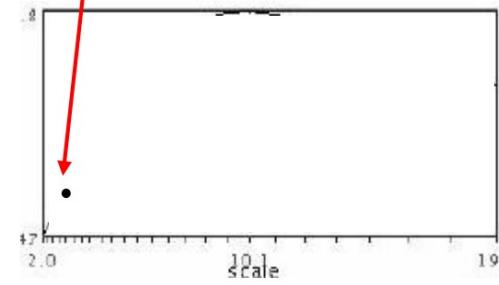
Automatic scale selection



- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$



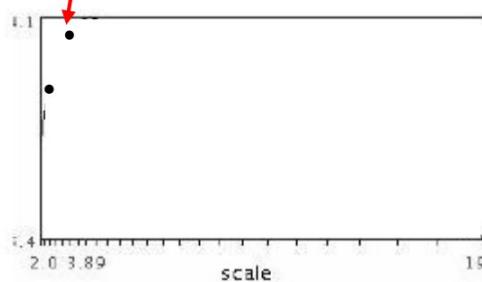
$$f(I_{i_1 \dots i_m}(x', \sigma))$$



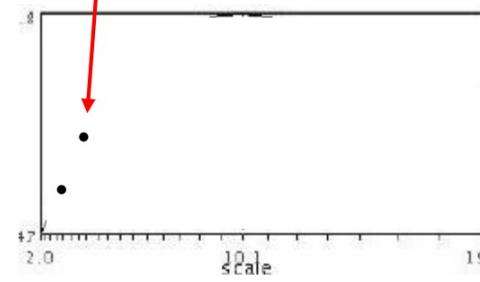
Automatic scale selection



- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$



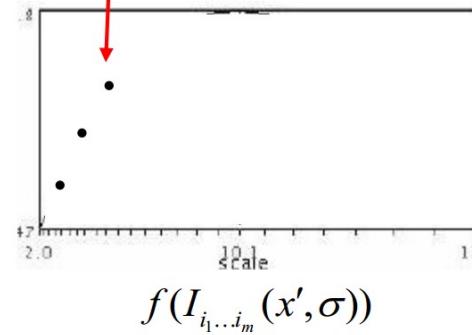
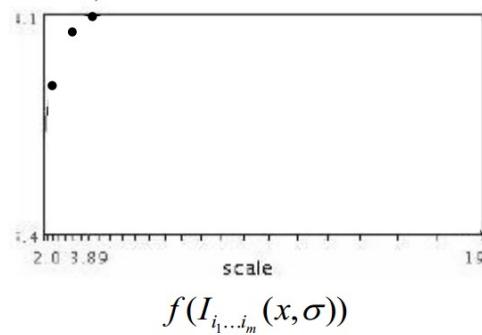
$$f(I_{i_1 \dots i_m}(x', \sigma))$$



Automatic scale selection



- Function responses for increasing scale (scale signature)

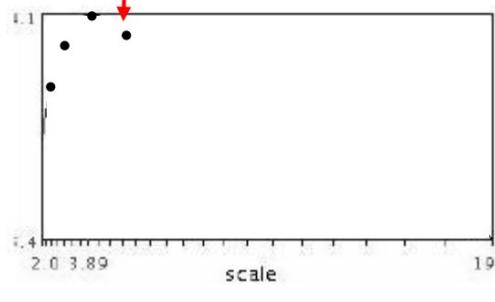




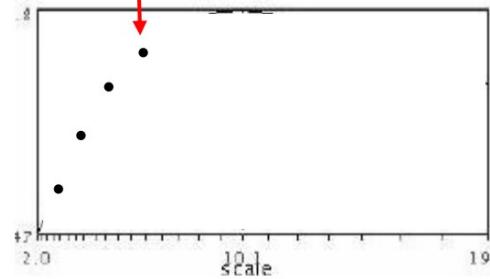
Automatic scale selection



- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$



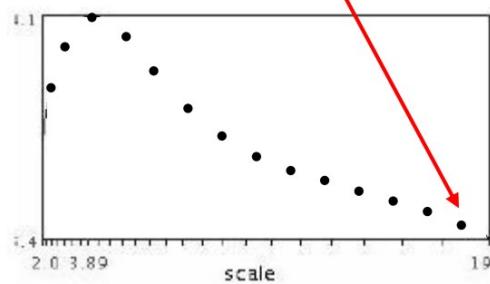
$$f(I_{i_1 \dots i_m}(x', \sigma))$$



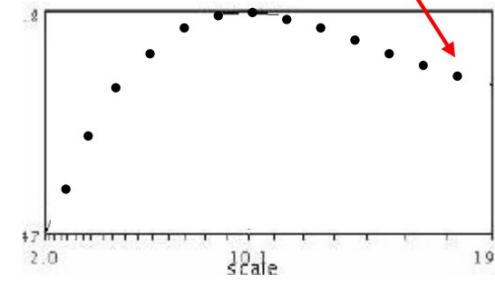
Automatic scale selection



- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$



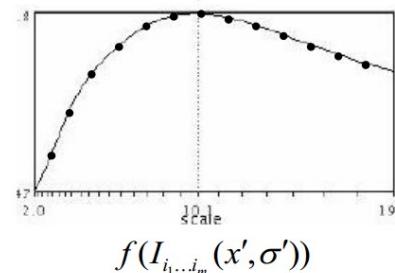
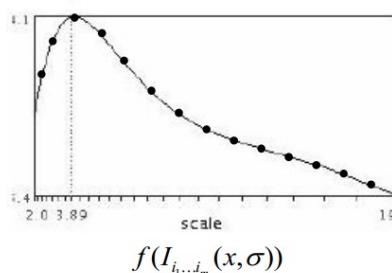
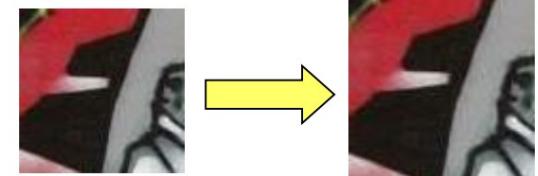
$$f(I_{i_1 \dots i_m}(x', \sigma))$$



Automatic scale selection

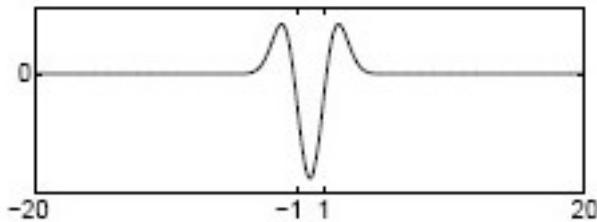


- Normalize: Rescale to fixed size

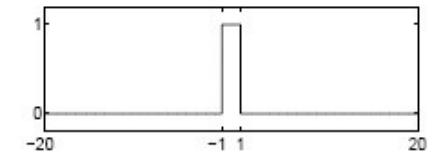
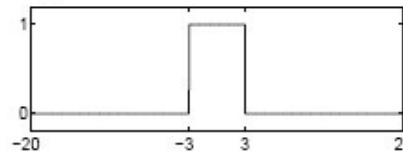
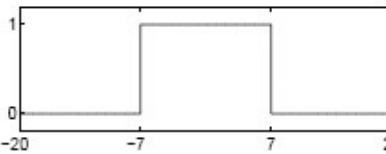
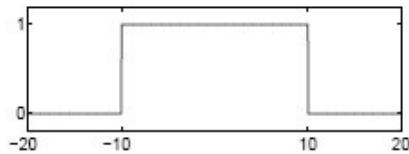




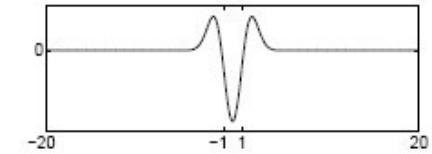
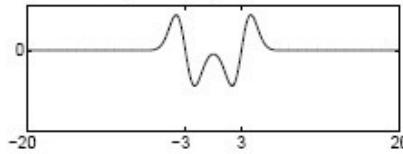
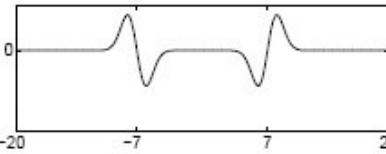
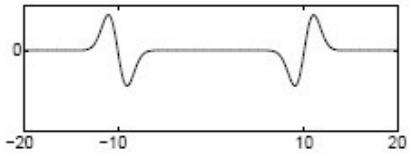
What can be the “signature” function?



Original signal



Convolved with Laplacian ($\sigma = 1$)



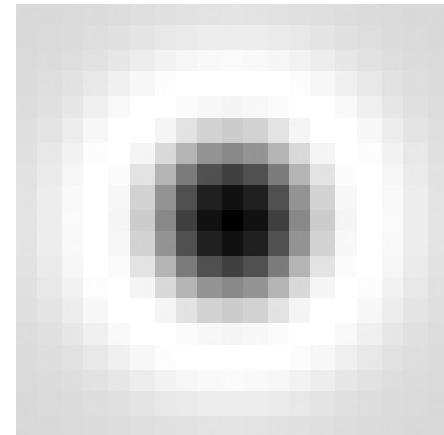
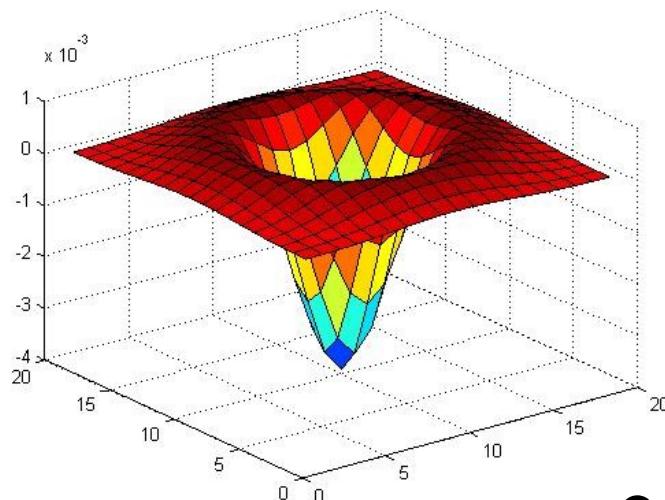
Highest response when the signal has the same **characteristic scale** as the filter



Blob detection in 2D



- Laplacian of Gaussian: Circularly symmetric operator for blob detection in 2D



$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$

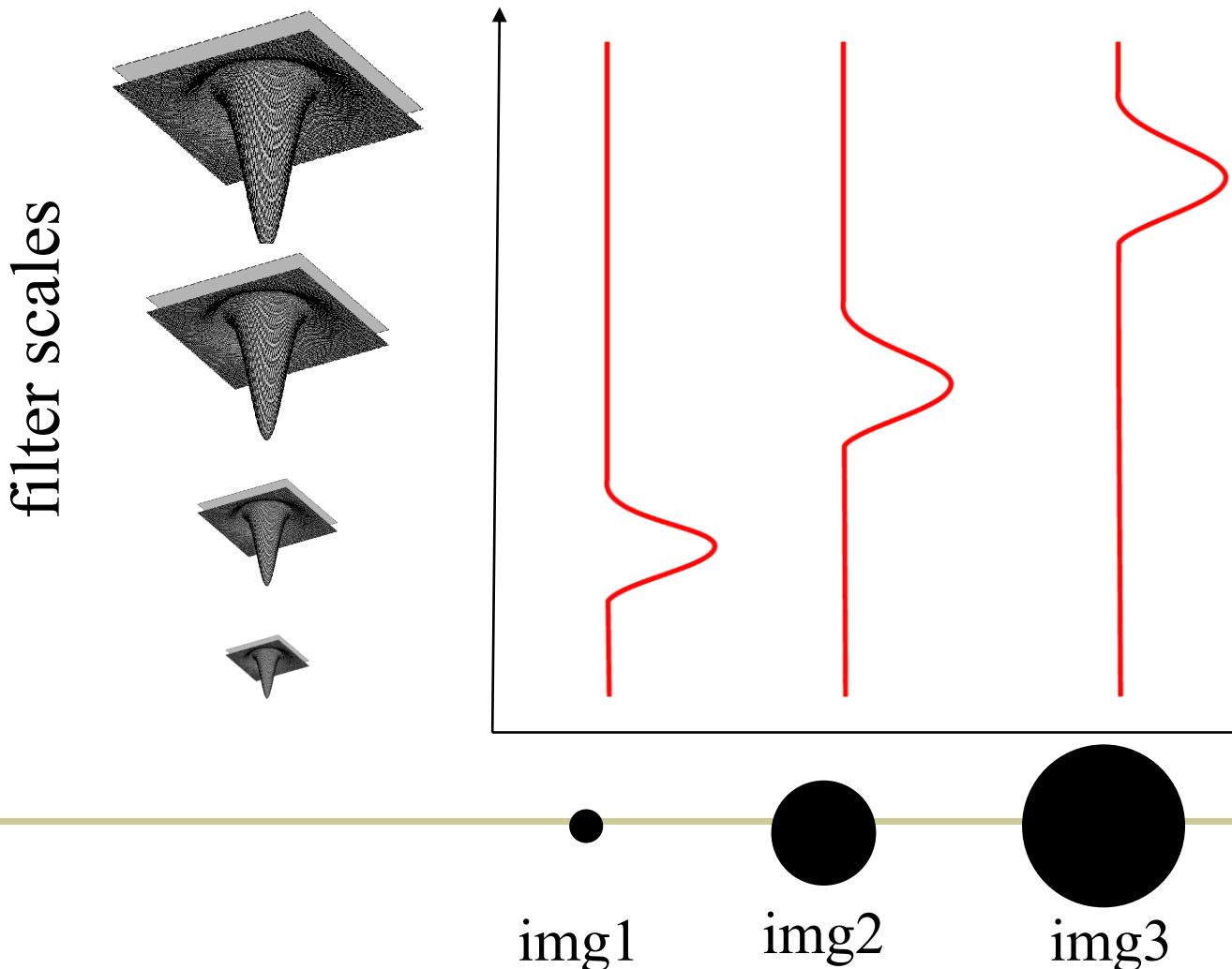


Blob detection in 2D



- Laplacian-of-Gaussian = “blob” detector

$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$

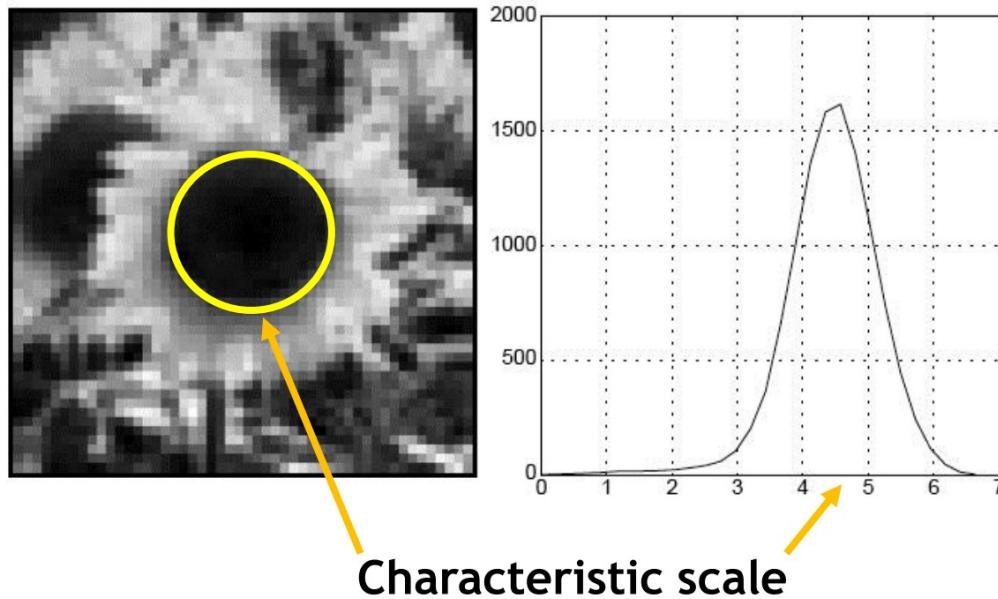




Characteristic scale



- We define the *characteristic scale* as the scale that produces peak of Laplacian response



T. Lindeberg (1998). ["Feature detection with automatic scale selection."](#)
International Journal of Computer Vision 30 (2): pp 77--116.



Example

Original image at
 $\frac{3}{4}$ the size



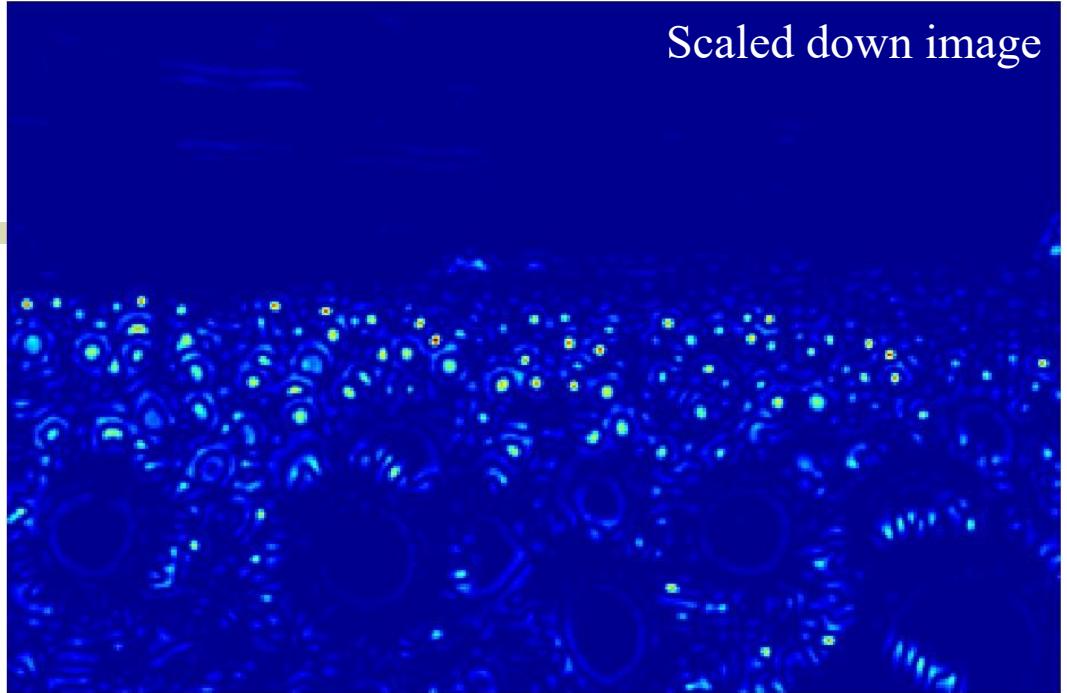
What happened
when you applied
different Laplacian
filters?



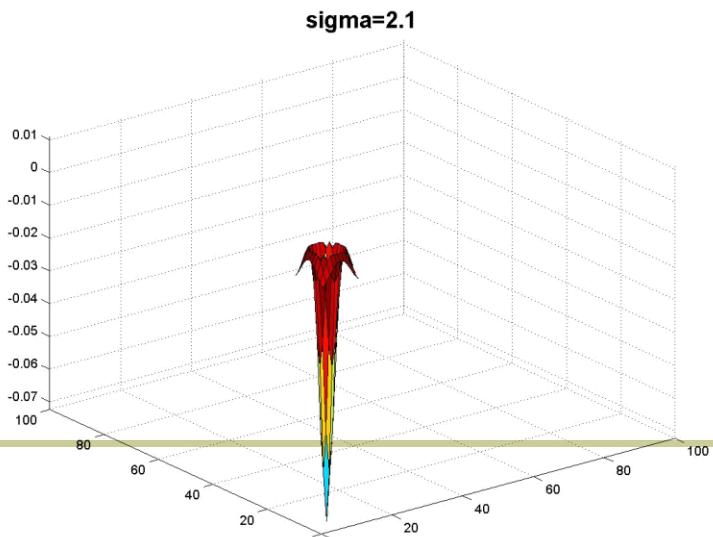


Original image at
3/4 the size

Scaled down image



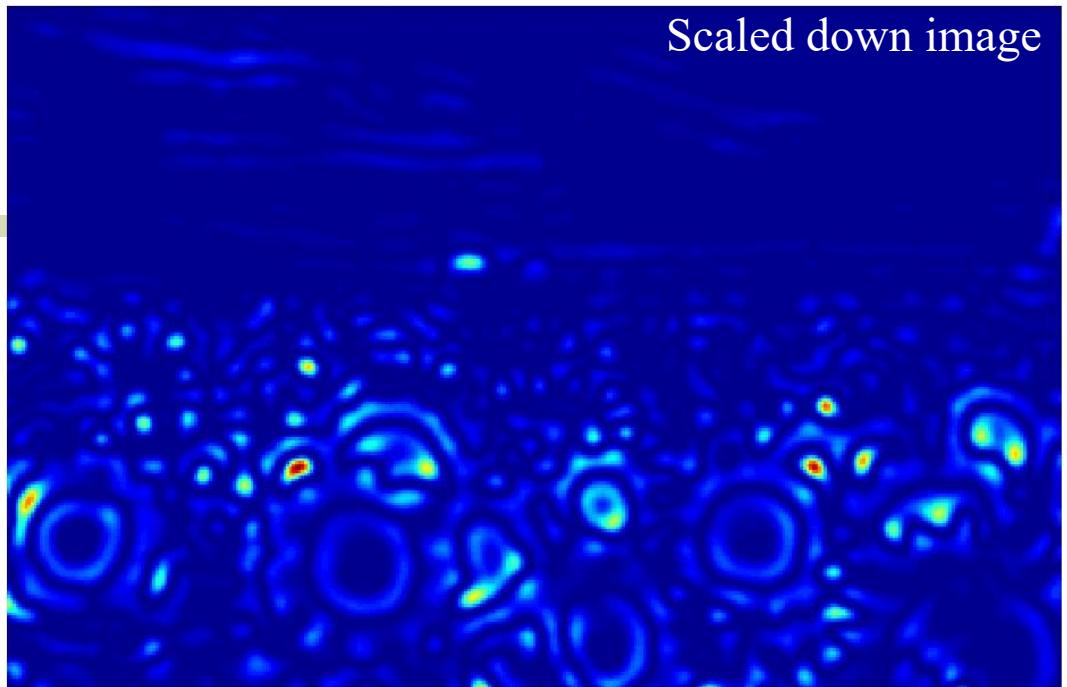
Original ima



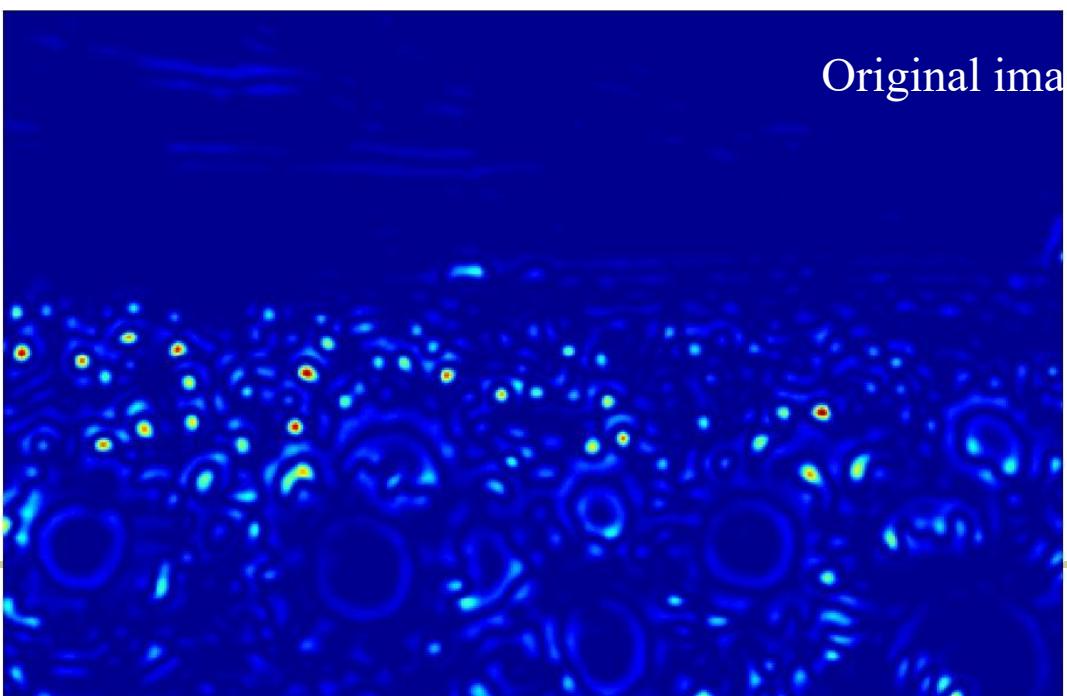
Slide credit: Kristen Grauman



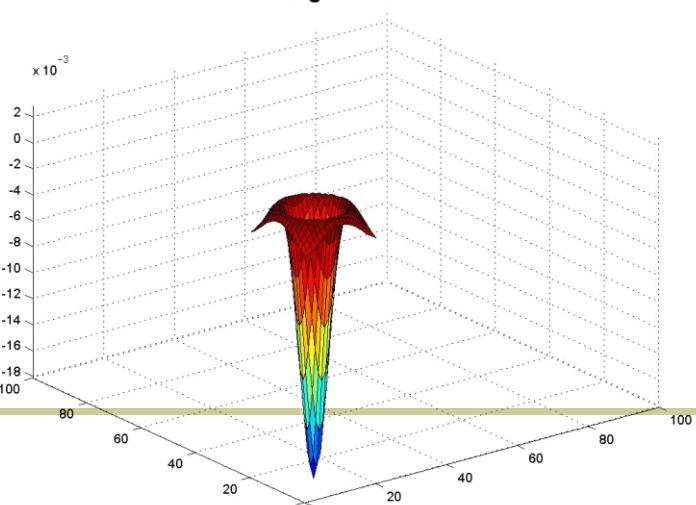
Scaled down image



Original ima



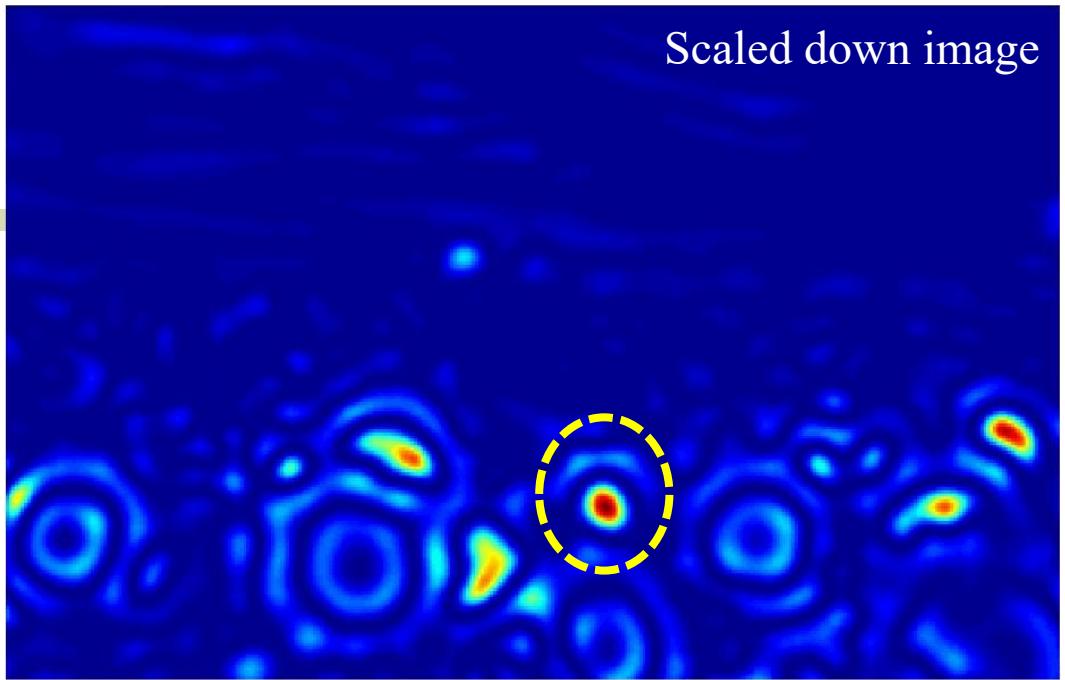
sigma=4.2



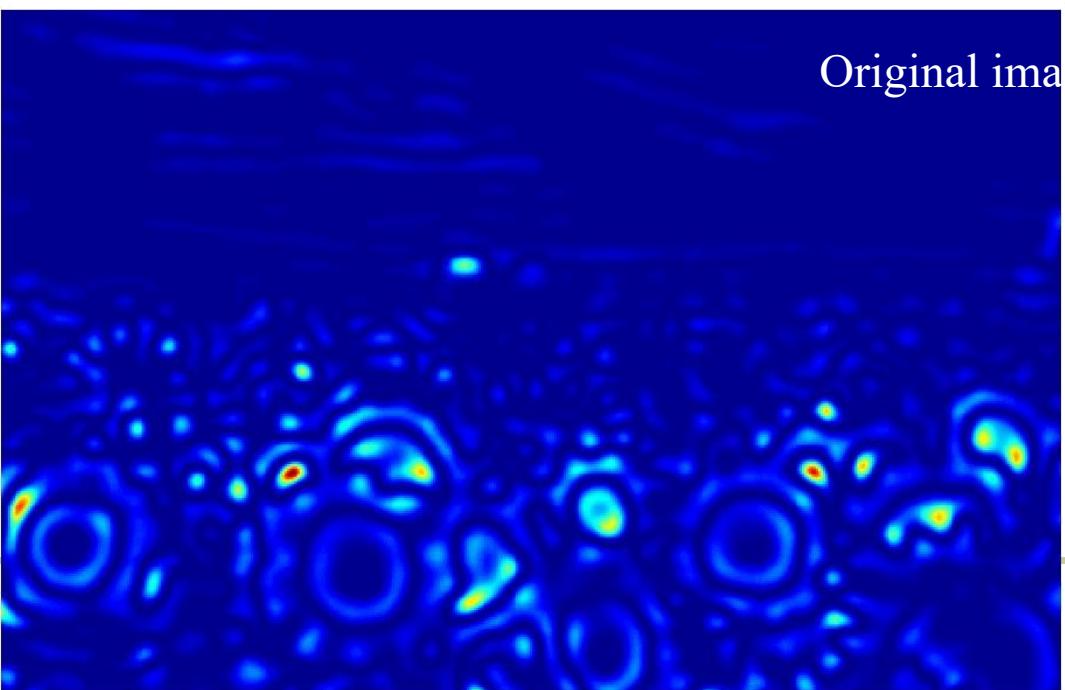
Slide credit: Kristen Grauman



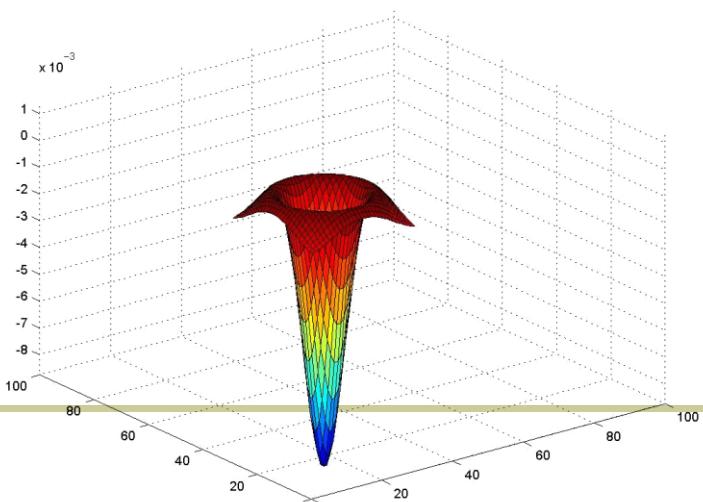
Scaled down image



Original ima



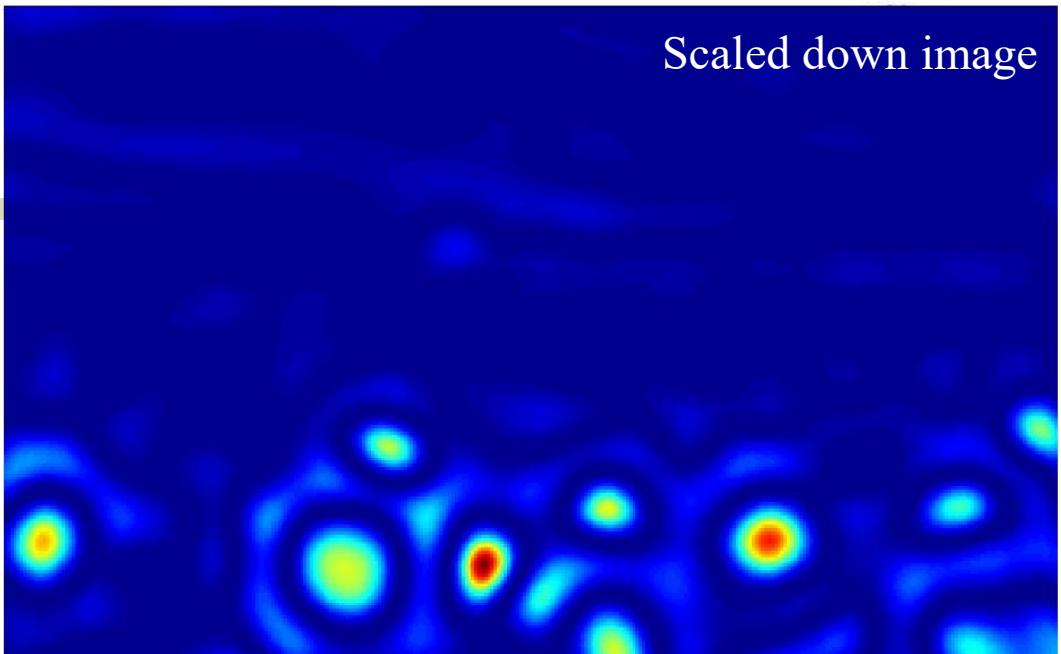
$\sigma=6$



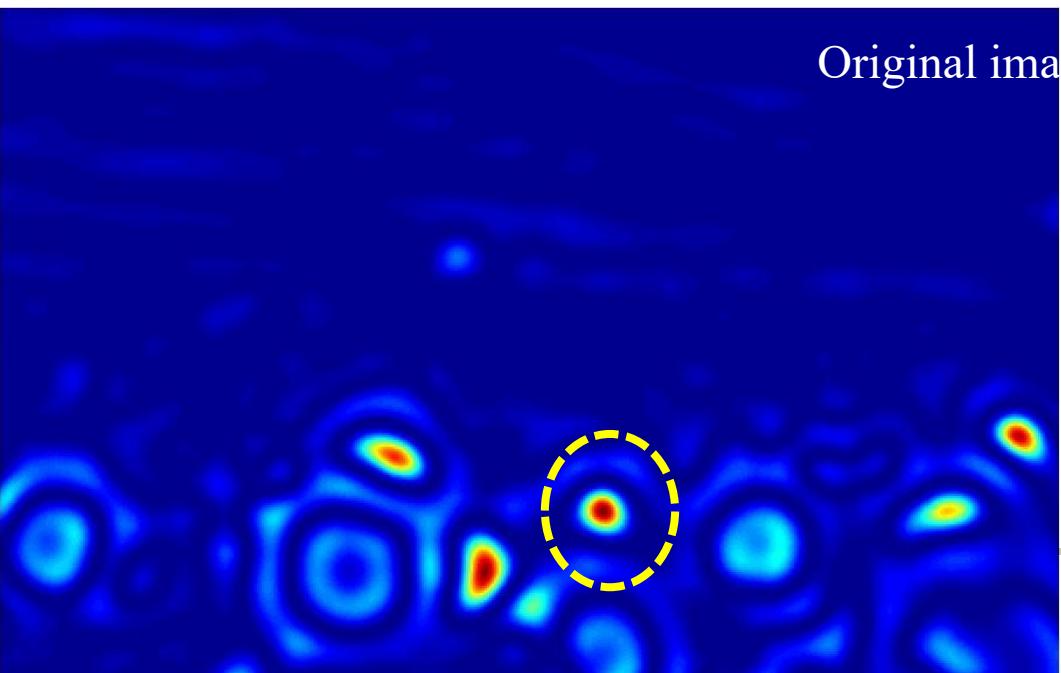
Slide credit: Kristen Grauman



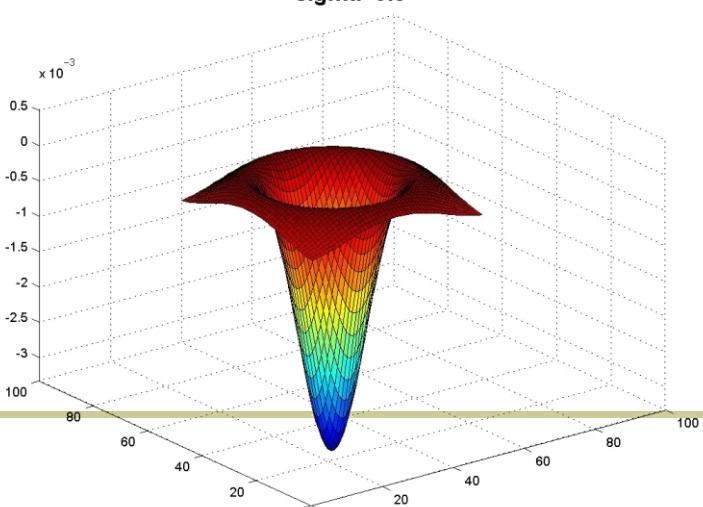
Scaled down image



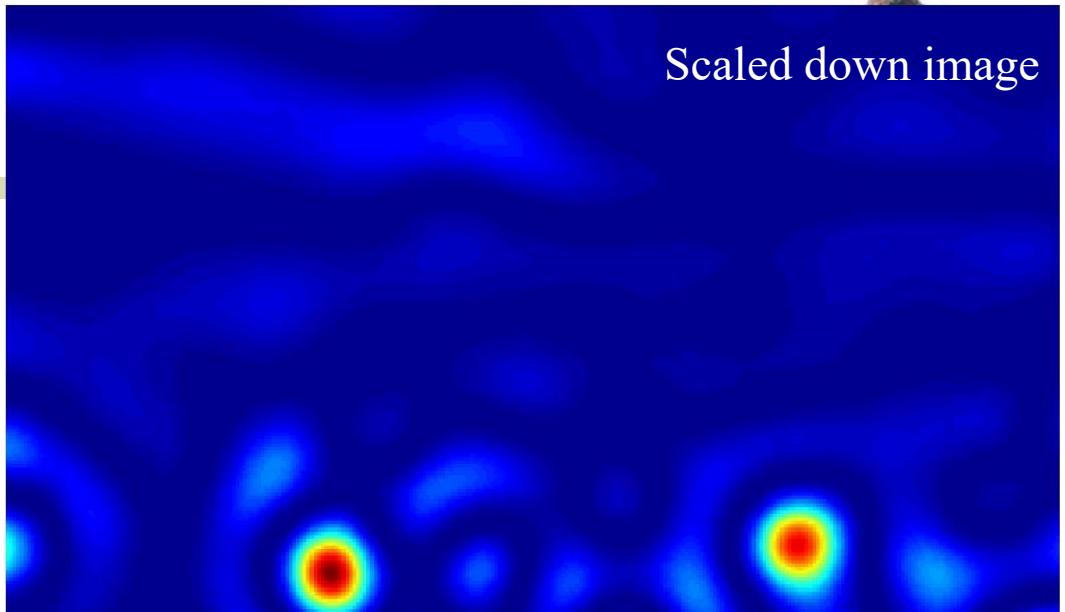
Original ima



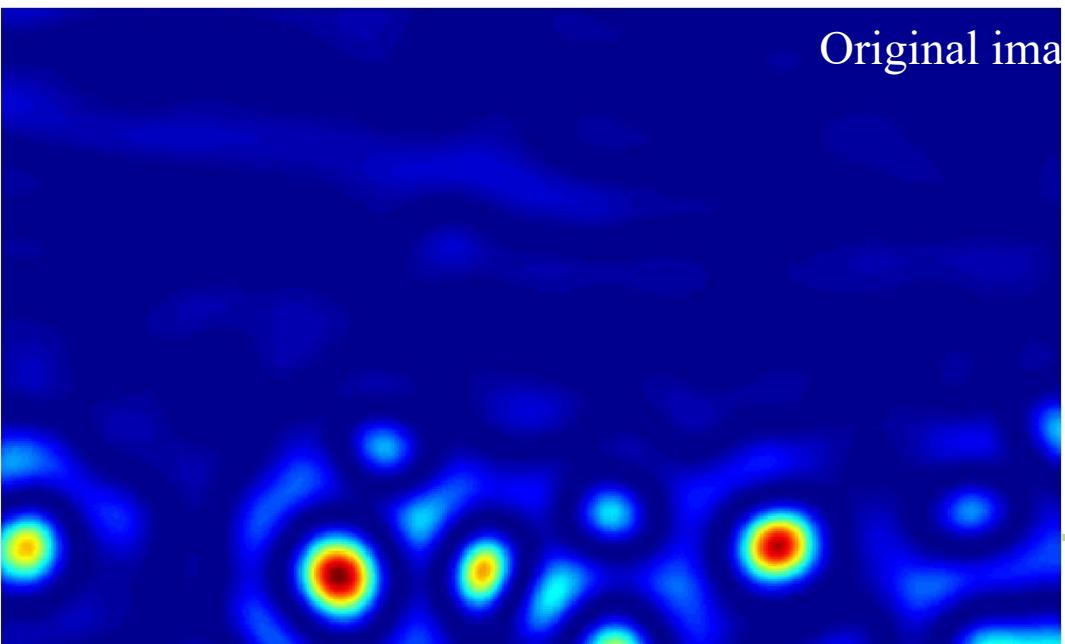
$\sigma = 9.8$



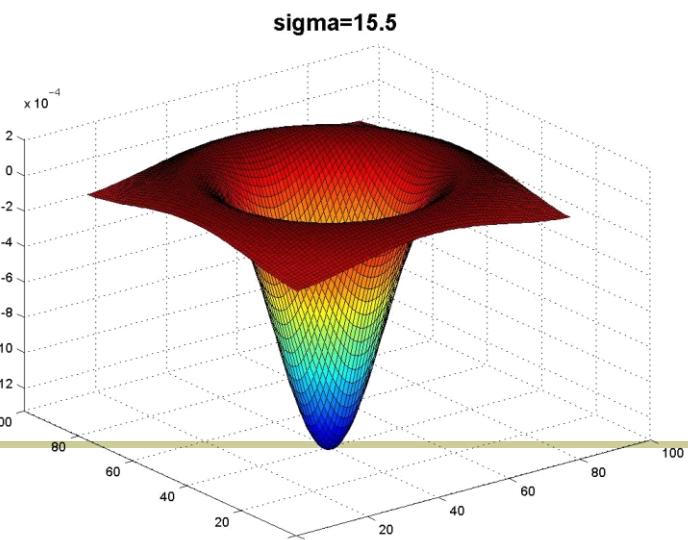
Slide credit: Kristen Grauman



Scaled down image



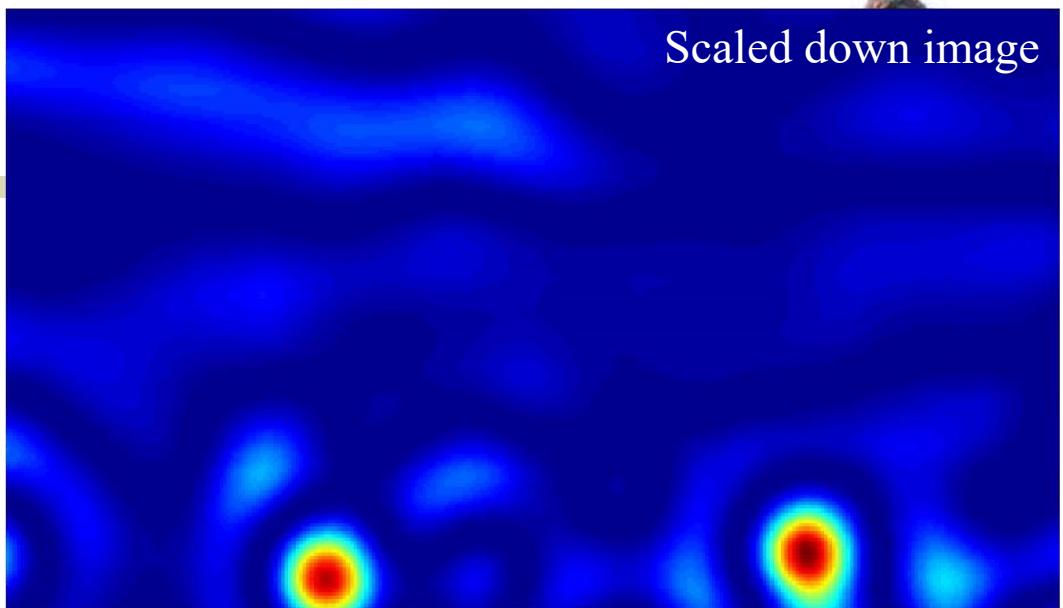
Original ima



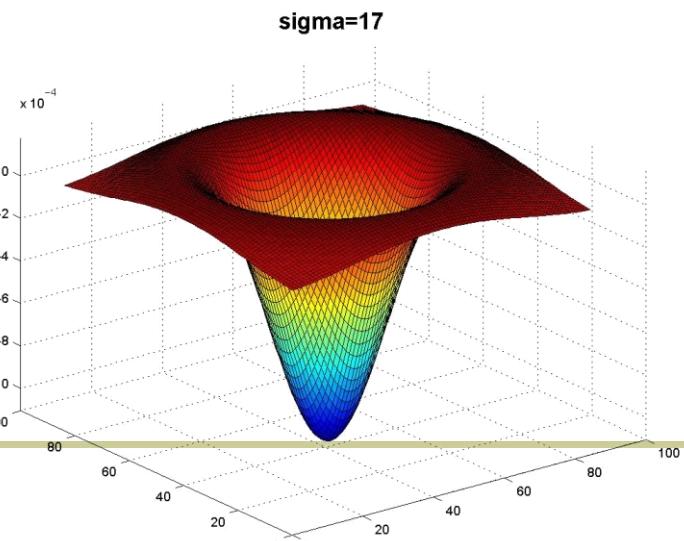
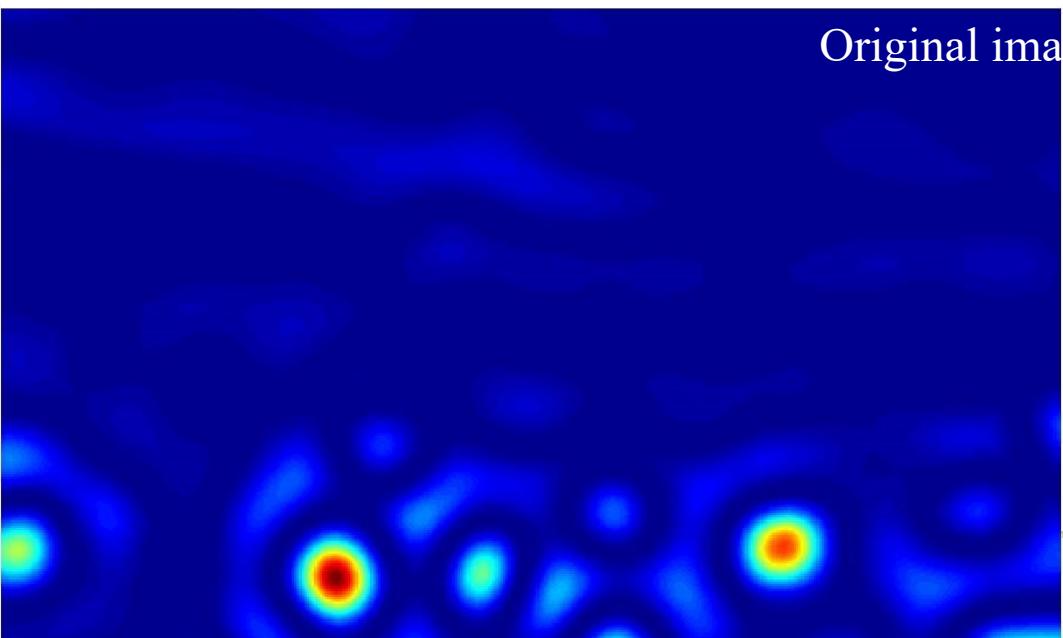
Slide credit: Kristen Grauman



Scaled down image



Original ima



Slide credit: Kristen Grauman



Optimal scale



2.1

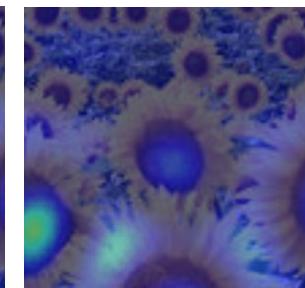
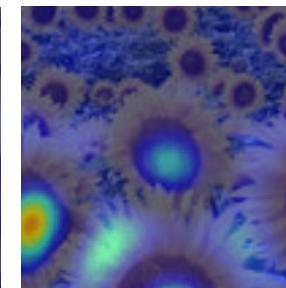
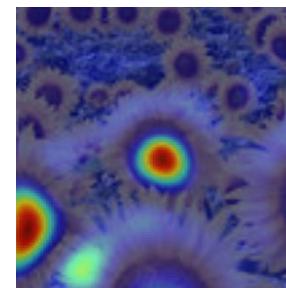
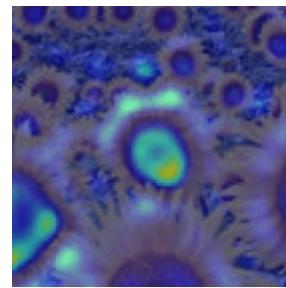
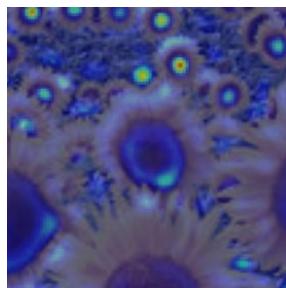
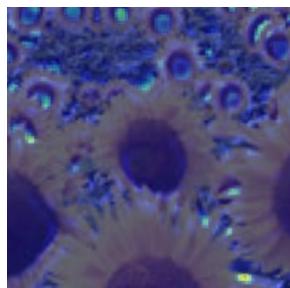
4.2

6.0

9.8

15.5

17.0



Full size image

2.1

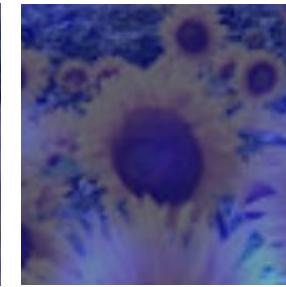
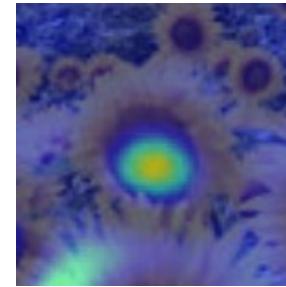
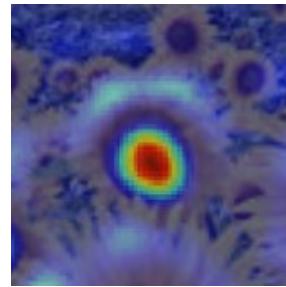
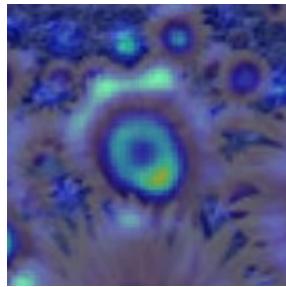
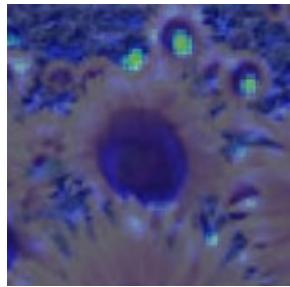
4.2

6.0

9.8

15.5

17.0



3/4 size image



Optimal scale



2.1

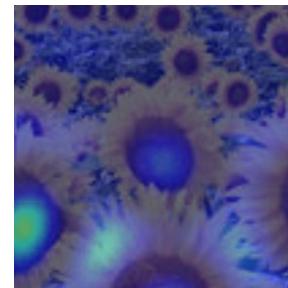
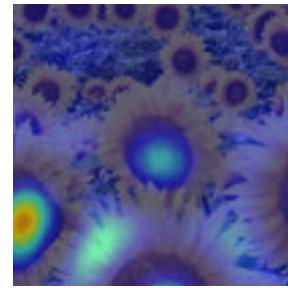
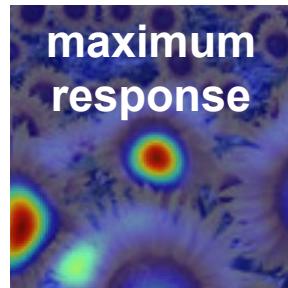
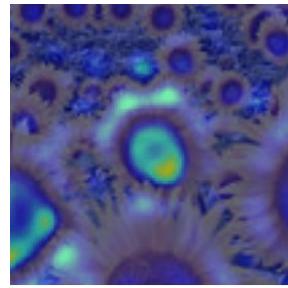
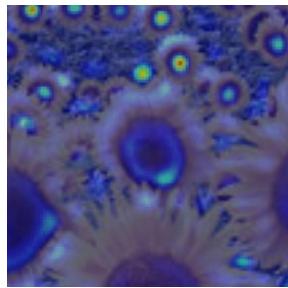
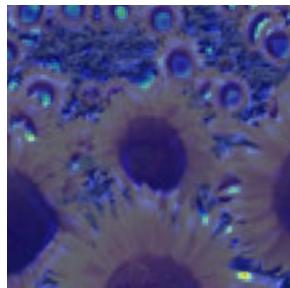
4.2

6.0

9.8

15.5

17.0



Full size image

2.1

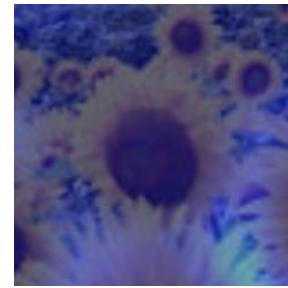
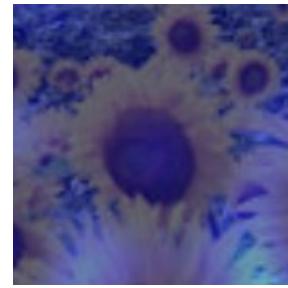
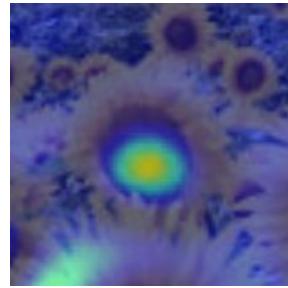
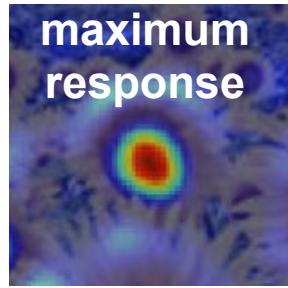
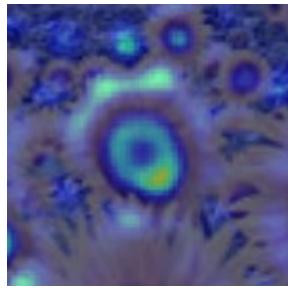
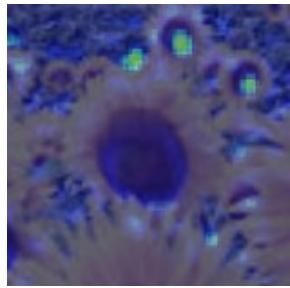
4.2

6.0

9.8

15.5

17.0



3/4 size image

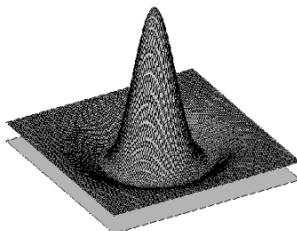


Laplacian-of-Gaussian (LoG)



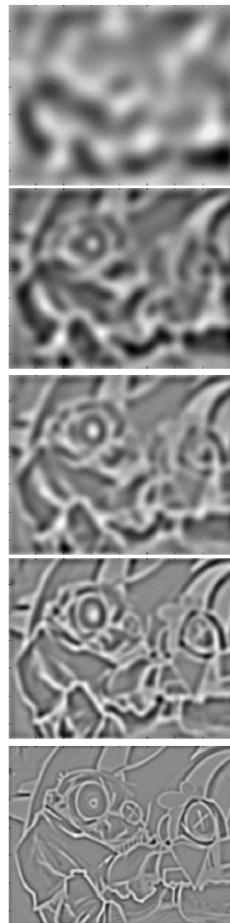
- **Interest points:**

- Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$$

Diagram illustrating the computation of the Laplacian of Gaussian (LoG) operator. It shows a flow from the original image to a series of blurred versions, labeled σ^2 , σ^3 , σ^4 , and σ^5 . The equation $L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$ indicates that the sum of the second-order spatial derivatives in the x and y directions is proportional to the third power of the scale parameter σ .



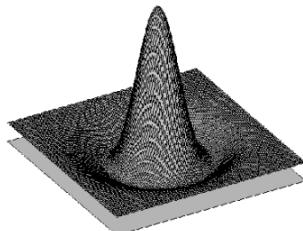


Laplacian-of-Gaussian (LoG)



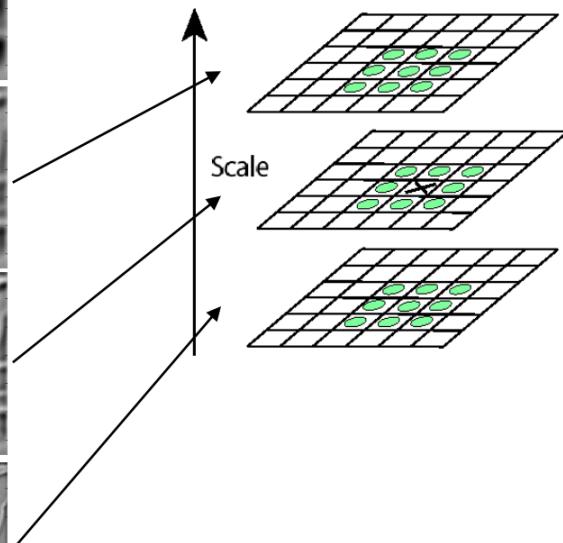
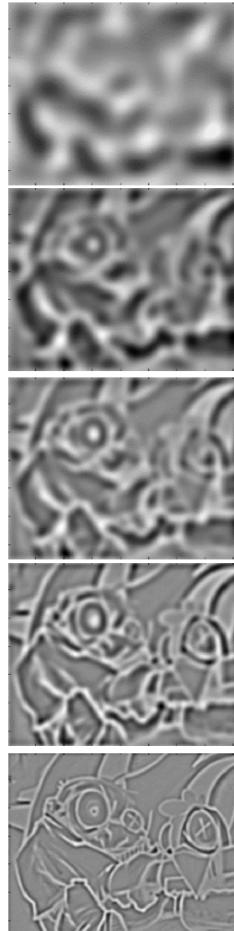
- Interest points:

- Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$$
$$\sigma^2$$
$$\sigma$$
$$\sigma^4$$
$$\sigma^5$$

A diagram illustrating the computation of the Laplacian of a Gaussian (LoG). It shows a flow from the original image (σ) through successive approximations (σ², σ³, σ⁴, σ⁵) to the final result ($L_{xx}(\sigma) + L_{yy}(\sigma)$).



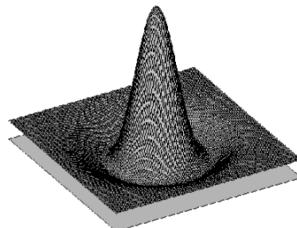


Laplacian-of-Gaussian (LoG)



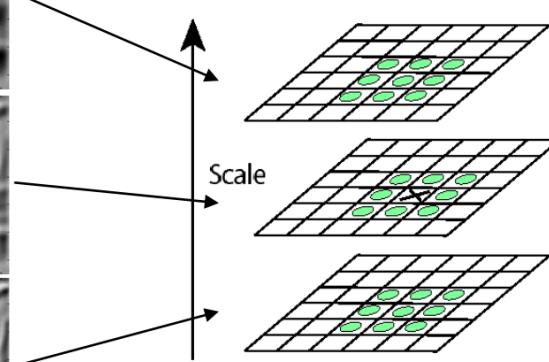
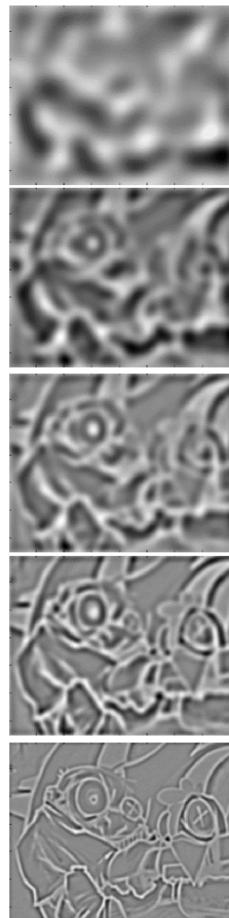
- **Interest points:**

- Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$$
$$\sigma^2$$
$$\sigma$$
$$\sigma^4$$
$$\sigma^5$$

A diagram illustrating the computation of the Laplacian of a Gaussian (LoG). It shows a sequence of five grayscale images representing the LoG at different scales (σ). Arrows point from the equation $L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$ to the second image, and from σ^2 and σ to the third and fourth images respectively. The fifth image shows the result of the LoG operation.



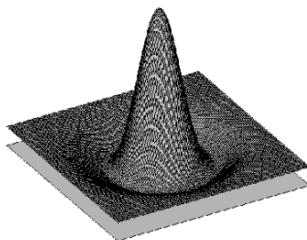


Laplacian-of-Gaussian (LoG)



- Interest points:

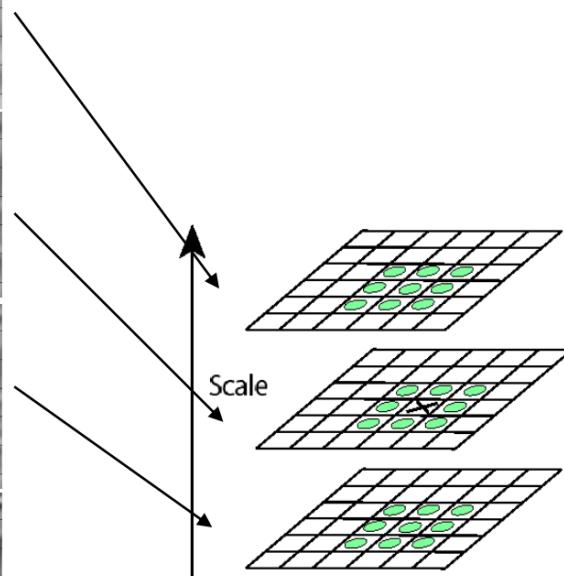
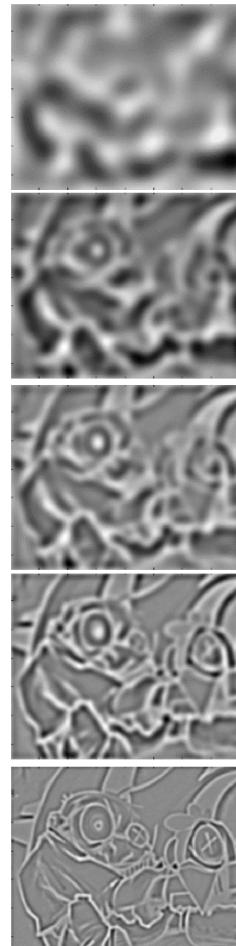
- Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma^3$$

σ^5
 σ^4
 σ^3
 σ^2
 σ

A diagram showing the relationship between the second derivatives of the image (L_{xx} and L_{yy}) and the resulting scale space. Arrows point from the sum of the second derivatives to successive powers of the standard deviation ($\sigma^3, \sigma^4, \sigma^5$).



⇒ List of (x, y, σ)



LoG detector: workflow





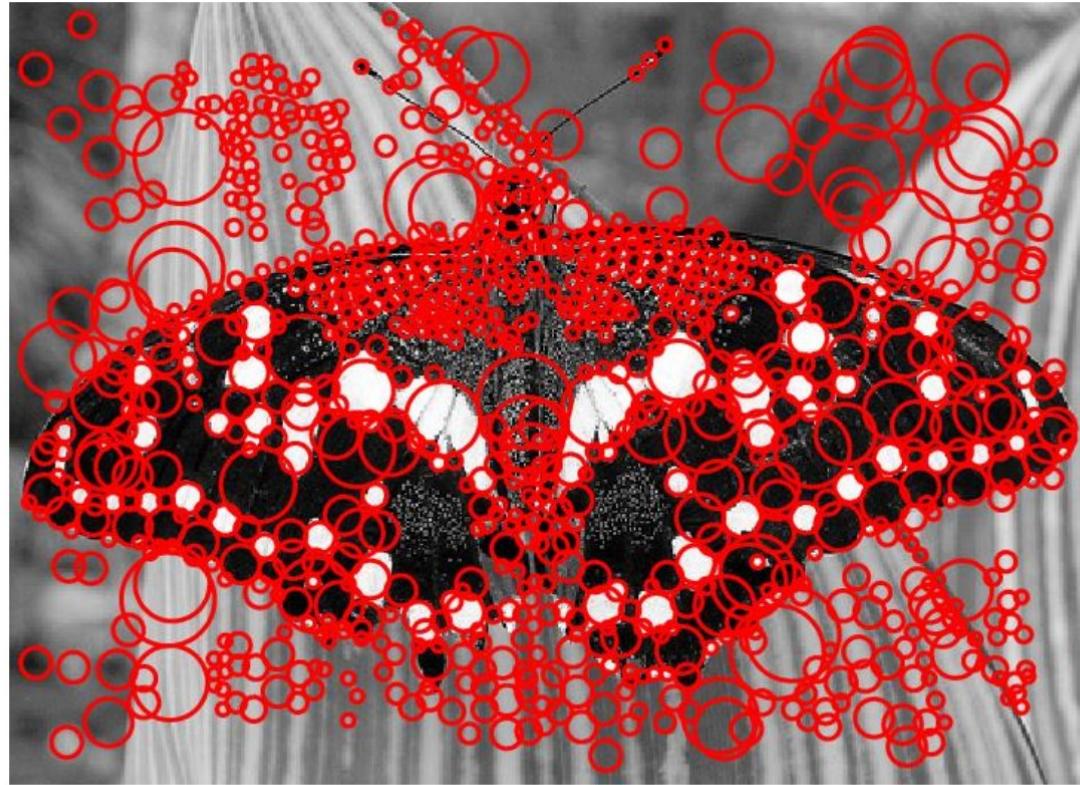
LoG detector: workflow



$\sigma = 11.9912$



LoG detector: workflow





Technical detail



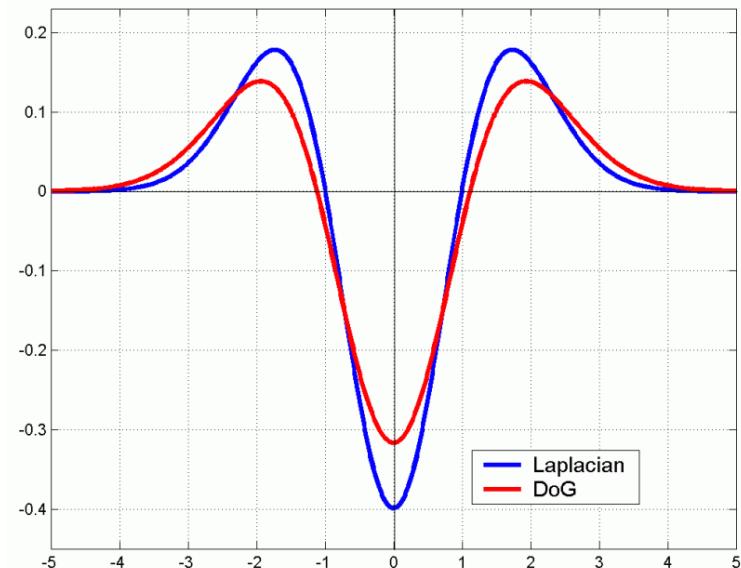
- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 (G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)

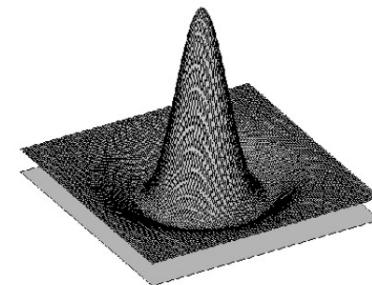




Difference-of-Gaussian(DoG)



- Difference of Gaussians as approximation of the LoG
 - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
 - No need to compute 2nd derivatives
 - Gaussians are computed anyway, e.g. in a Gaussian pyramid.

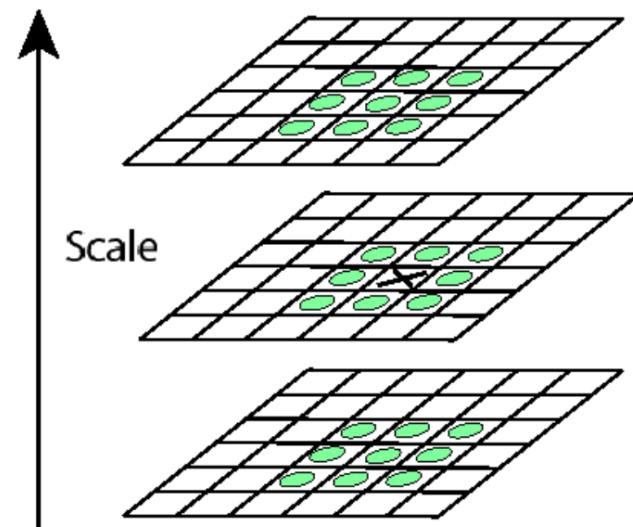




Keypoint localization with DoG



- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses



Candidate keypoints:
list of (x, y, σ)



DoG: Efficient implementation



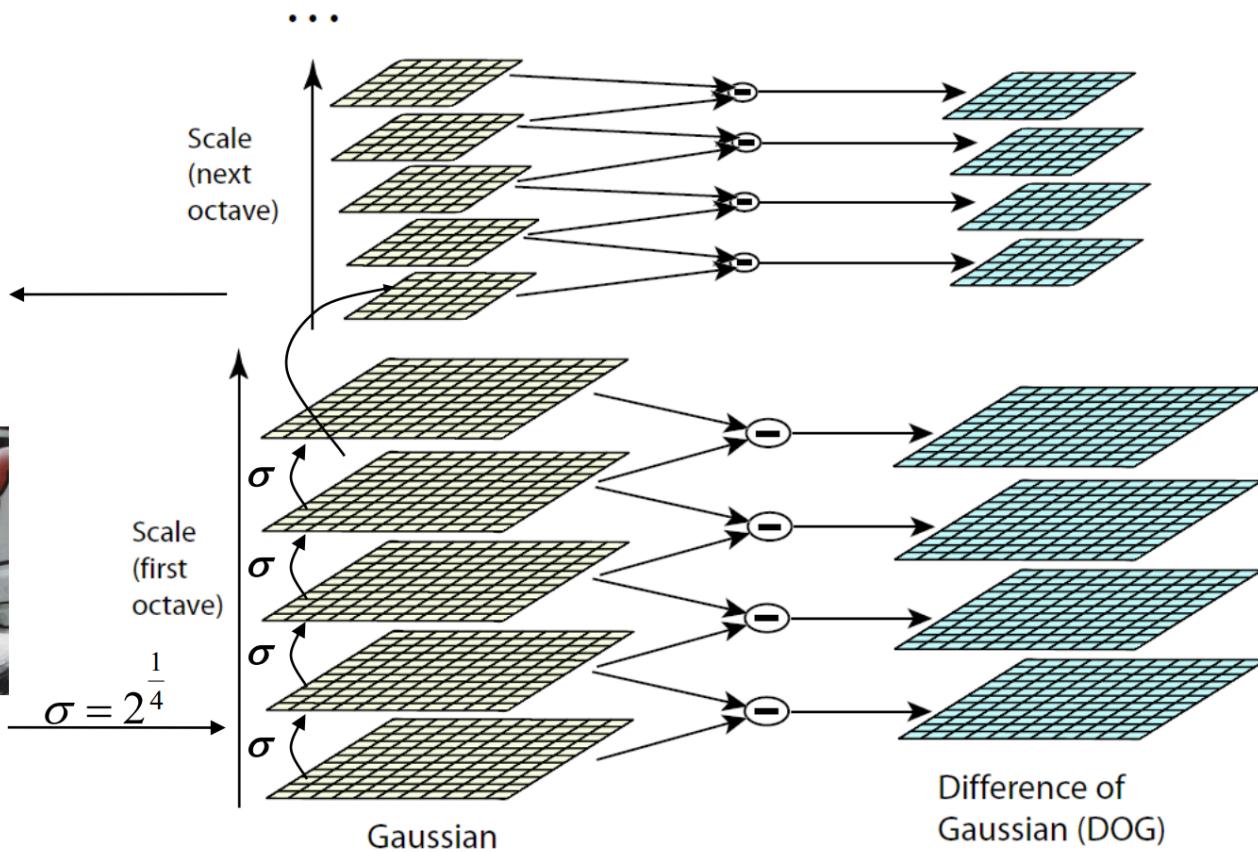
- Computation in Gaussian scale pyramid



*Sampling with
step $\sigma^4 = 2$*



Original image





Results: Lowe's DoG





Example of Keypoint Detection



(a) 233x189 image

(b) 832 DoG extrema

(c) 729 left after peak value threshold

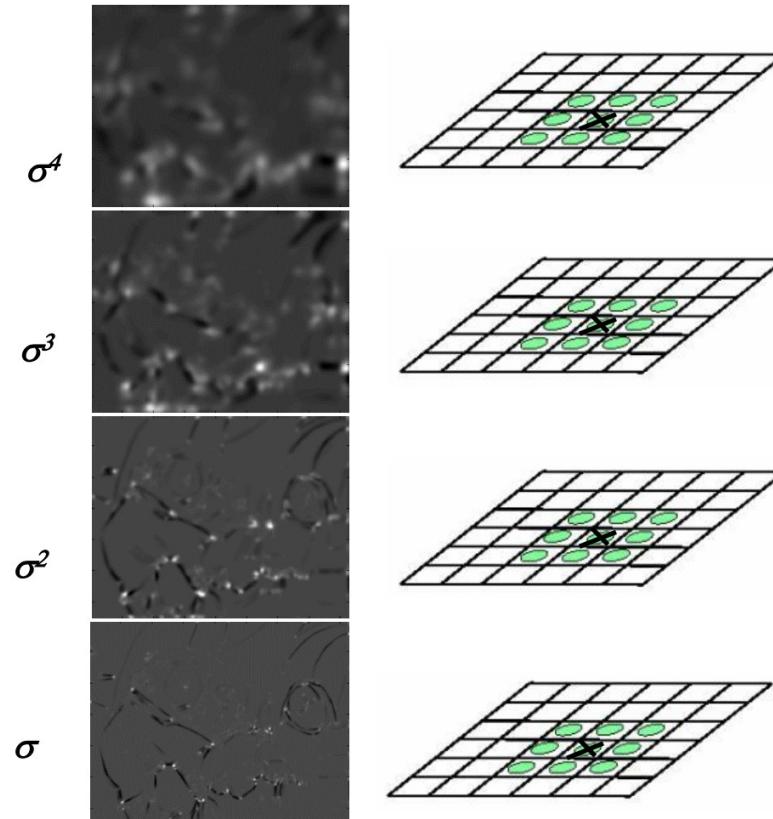
(d) 536 left after testing ratio of principle curvatures (removing edge responses)



Harris-Laplace [Mikolajczyk '01]



1. Initialization: Multiscale Harris corner detection



Computing Harris function

Detecting local maxima

Slide adapted from Krystian Mikolajczyk

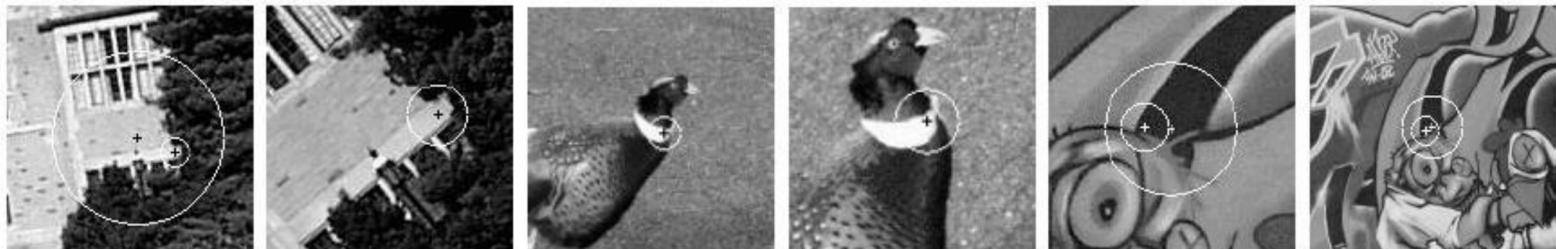
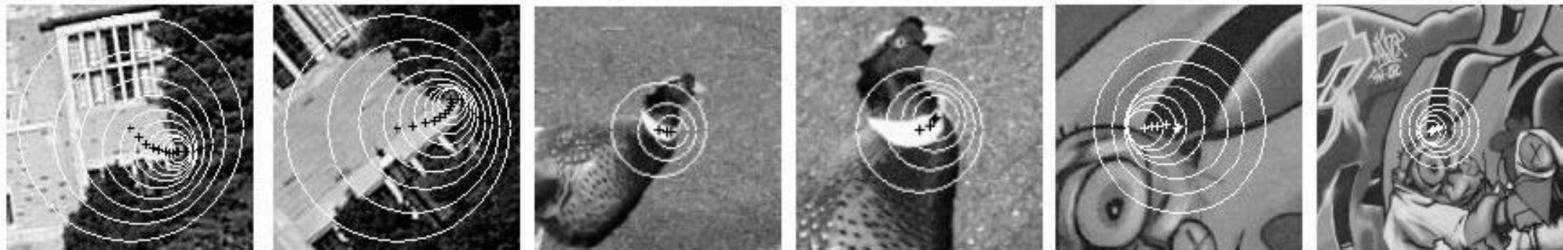


Harris-Laplace [Mikolajczyk '01]



1. Initialization: Multiscale Harris corner detection
2. Scale selection based on Laplacian
(same procedure with Hessian \Rightarrow Hessian-Laplace)

Harris points



Harris-Laplace points



Summary: Scale Invariant Detection

- **Given:** Two images of the same scene with a large *scale difference* between them.
- **Goal:** Find *the same* interest points *independently* in each image.
- **Solution:** Search for *maxima* of suitable functions in *scale* and in *space* (over the image).
- Two strategies
 - Laplacian-of-Gaussian (LoG)
 - Difference-of-Gaussian (DoG) as a fast approximation
 - *These can be used either on their own, or in combinations with single-scale keypoint detectors (Harris, Hessian).*



Summary



- Introduction to correspondence and alignment
- Overview of interest points
 - Matching pipeline
 - Repeatable & Distinctive
- Keypoint Localization
 - Harris detector
 - Hessian detector
- Scale invariant region selection
 - Automatic scale selection
 - Laplacian of Gaussian (LoG) & Difference of Gaussian (DoG)
 - Combinations: Harris-Laplacian & Hessian-Laplacian



You Can Try It at Home



- For most local feature detectors, executables are available online:
- <http://robots.ox.ac.uk/~vgg/research/affine>
- <http://www.cs.ubc.ca/~lowe/keypoints/>
- <http://www.vision.ee.ethz.ch/~surf>
- <http://homes.esat.kuleuven.be/~ncorneli/gpusurf/>

Affine Covariant Features



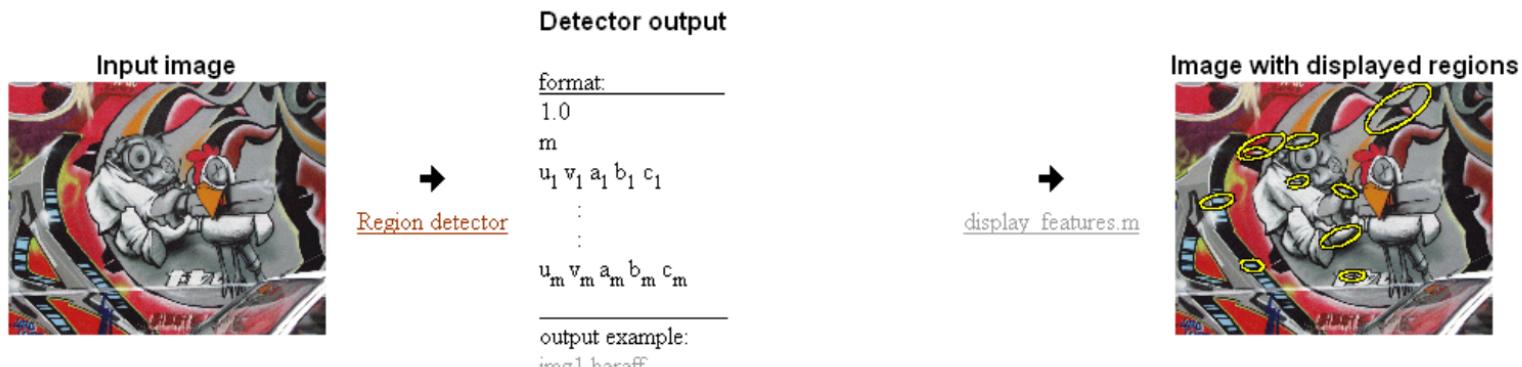
KATHOLIEKE UNIVERSITEIT
LEUVEN

INRIA
RHÔNE ALPES



Collaborative work between the Visual Geometry Group, Katholieke Universiteit Leuven, Inria Rhône-Alpes and the Center for Machine Perception.

Affine Covariant Region Detectors



Parameters defining an affine region

u, v, a, b, c in $a(x-u) + 2b(x-u)(y-v) + c(y-v)^2 = 1$
with $(0,0)$ at image top left corner

Code

- provided by the authors, see [publications](#) for details and links to authors web sites.

Linux binaries

[Harris-Affine & Hessian-Affine](#)

Example of use

prompt>./h_affine.ln -haraff -i [img1.ppm](#) -o img1.haraff -thres 1000 matlab>> [d](#)

prompt>./h_affine.ln -hesaff -i [img1.ppm](#) -o img1.hesaff -thres 500 matlab>> [d](#)

[MSER](#) - Maximally stable extremal regions (also Windows) prompt>./mser.ln -t 2 -es 2 -i [img1.ppm](#) -o img1.mser matlab>> [d](#)

[IBR](#) - Intensity extrema based detector prompt>./ibr.ln [img1.ppm](#) img1.ibr -scalefactor 1.0 matlab>> [d](#)

[EBR](#) - Edge based detector prompt> ./ebr.ln [img1.ppm](#) img1.ebr matlab>> [d](#)

[Salient](#) region detector prompt>./salient.ln [img1.ppm](#) img1.sal matlab>> [d](#)



References

- Read David Lowe's SIFT paper
 - D. Lowe,
Distinctive image features from scale-invariant keypoints,
IJCV 60(2), pp. 91-110, 2004
- Good survey paper on Int. Pt. detectors and descriptors
 - T. Tuytelaars, K. Mikolajczyk, Local Invariant Feature Detectors: A Survey, Foundations and Trends in Computer Graphics and Vision, Vol. 3, No. 3, pp 177-280, 2008.
- Try the example code, binaries, and Matlab wrappers
 - Good starting point: Oxford interest point page
<http://www.robots.ox.ac.uk/~vgg/research/affine/detectors.html#binaries>