Python Machine Learning: The 5th Book Circle Data Compression Algorithm: Principle Component Analysis and Linear Discriminant Analysis

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Disclaimer

All opinions and statements in this presentation are mine and do not in any way represent the company

Any comment or correction of error is welcome, please contact me chisyliu@hotmail.com

Acknowledgement

Acknowledgement

Here I would like to thank for Binru Huang and Caj Zell in my group. The discussion between us made me understanding of PCA/LDA deeper

The Fifth Book Circle of Python Machine Learning

In this presentation belongs to algorithm part of the book

- If you have time, please read the book first. This slide could be used as complementary resource for the book
- We will try to go through every algorithm in chapter 5 of book Python Machine Learning, also show the mathematics behind each algorithm. But we only use the mathematics conclusion to explain algorithm rather than showing mathematical derivation
- All of us need to debug the python code, in order to get practice of implementing machine learning algorithm

Overview

- Principle Component Analysis
 - PCA, Modeled as Minimize SSE(Least Square Error) Problem
 - PCA, From a LS Problem to Maximize Variance Problem
 - Eigen Decomposition to Solve Maximize Variance Problem
 - PCA, Another Explanation by Singular Value Decomposition
 - Relationship with MIMO
 - Relationship with OFDM
- 2 Linear Discriminant Analysis
- 3 Kernel for Principle Component Analysis
- 4 Conclusion

Algorithms in Chapter 5

From this slide we go through the data compression/dimension reduction algorithms PCA(unsupervised) and LDA(supervised) in chapter 5

Data set (y, X)

Suppose we have L samples, each sample has D features/dimensions(So the input \mathbf{X} is L by D matrix, label \mathbf{y} is L by 1 vector). If we only consider the I^{th} data sample pair, \mathbf{x}_I is 1 by D vector which represents D features/dimension for I^{th} training data sample, \mathbf{w} is D by 1 vector which represents weight and y_I represents the label of I^{th} data sample

Outline for Section 1

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The Main Idea Behind PCA

PCA, Modeled as Minimize SSE(Least Square Error) Problem

Model The Idea as a Least Square Error Problem

Principle Component Analysis

PCA, From a LS Problem to Maximize Variance Problem

Maximize Variance Problem to Replace of LS Problem

Principle Component Analysis

Eigen Decomposition to Solve Maximize Variance Problem

Eigen Decomposition: Solution to Maximize Variance Problem

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Principle Component Analysis

PCA, Another Explanation by Singular Value Decomposition

SVD

PCA, Another Explanation by Singular Value Decomposition

SVD: The Other View of PCA

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Principle Component Analysis
Relationship with MIMO

MIMO

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Principle Component Analysis
Relationship with OFDM

OFDM

Outline for Section 2

- Principle Component Analysis
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LDA

Outline for Section 3

- Principle Component Analysis
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Kernel PCA for Nonlinear Mapping

Outline for Section 4

- Principle Component Analysis
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- 4 Conclusion

Conclusion

Conclusion

References



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Question?