Unit 8: Advanced Production Techniques

In this unit we will describe two additional mechanisms which can be used in the procedural system of ACT-R. They are called procedural partial matching and dynamic pattern matching. These capabilities allow for a lot more flexibility in the procedural system, and they can make it easier to create models which are able to work in situations where all of the details of the task are not know in advance and thus cannot be explicitly encoded within the model.

8.1 Procedural partial matching

Procedural partial matching is very similar to the partial matching of declarative memory as was described in unit 5 of the tutorial. When procedural partial matching is enabled by setting the **:ppm** parameter to a number, a production may be selected to fire even when its conditions do not perfectly match the current buffer contents. This mechanism applies to all productions being tested and it modifies the conflict resolution process used when multiple productions match under the looser definition of matching. Other than that however it does not change any of the other operations of the procedural system and all other procedural functionality is as described in the previous units.

8.1.1 Condition testing with procedural partial matching

When procedural partial matching is enabled the slot tests for the buffer chunk's values are slightly relaxed, but most of the conditions in a production are still tested explicitly. These conditions must still be true for the production to match: if the production tests a buffer then that buffer must contain a chunk and the chunk must be of the appropriate type, all queries must be true as specified, all inequality tests on slots (negations, less-than, and greater-than comparisons) must be true, and all special conditions specified with eval or bind operators must be true. The only tests which do not have to be true are equality tests on the buffer slot contents i.e. tests that specify a specific value for a slot or tests with variables which are comparing two or more slots. If all of the equality tests are true, then the production matches just as it would without procedural partial matching enabled. If some of them are not true the production may still be considered a match under procedural partial matching.

If a value specified for a buffer's slot in the production does not match the buffer's slot's current value, then in order for it to be considered a match under procedural partial matching the mismatching values must be similar. Similarity is defined in the same way that it is for declarative memory. Thus they must be chunks for which a similarity value has been specified either through the set-similarities command or a modeler provided similarity hook function which provides a similarity between the items. [Note, if the items are not both chunks then they could still be similar if there is a similarity hook function set as was done for numbers in the 1-hit blackjack model.] The only difference between the procedural partial matching and declarative partial matching is that for procedural partial matching items are only considered to be similar if they have a

similarity value which is greater than the current minimum similarity (as set with the :md parameter). That additional constraint on the similarities is done for practical reasons because by default, all chunks have a similarity of the :md value to all other chunks. Without that constraint, any chunk could potentially be a partial match to any other in the production matching, and that would lead to a lot of difficulty in specifying the control flow through the model's productions since explicit state markers could not be used to guarantee ordering. By disallowing procedural partial matching from using the default minimum similarity value it allows the modeler to control which items are allowed to be partial matched in productions.

8.1.2 Conflict resolution with procedural partial matching

If only one production matches then it is selected and fired. When there is more than one production which matches (including partially matched productions) the production with the highest utility is the one selected and fired. The only difference when procedural partial matching is enabled is that productions which are not a perfect match receive a reduction to their utility. The equation for the utility of production i when procedural partial matching is enabled is:

Utility_i(t)=U_i(t)+
$$\varepsilon$$
+ $\sum_{j} ppm*similarity(d_{j},v_{j})$

Ui(t): Production i's current true utility value.

E: The noise which may be added to the utility.

i: The set of slots for which production *i* had a partially matched value.

ppm: The value of the :ppm parameter.

 d_i : The desired value for slot j in production i.

 v_i : The actual value in slot j of the chunk in the buffer.

Thus, the production's utility is decreased by the similarity of each mismatched value multiplied by the :ppm setting.

That adjusted utility value is only used for the purposes of conflict resolution. It does not affect the $U_i(t)$ value used in the utility learning equation or the utility values used during production compilation learning.

8.1.3 Simple procedural partial matching model

The simple-ppm-test model included with the tutorial unit shows a very simple example of procedural partial matching. If you open that model you will see that it has only three productions and there is no Lisp code for an experiment. Everything there except the :ppm and :cst parameters has been described in previous units, so it should be easy to understand. If you load the model you will see that the goal buffer holds a chunk which looks like this:

```
TEST0-0
ISA TEST
VALUE SMALL
```

and there are three productions which simply test the value slot of the goal chunk and then output the value from that slot:

If you load the model and run it as it is, with procedural partial matching disabled, you will see a trace like this:

```
> (run 1.0)
     0.000 PROCEDURAL CONFLICT-RESOLUTION
(P SMALL
   =GOAL>
        ISA TEST
        VALUE SMALL
        VALUE SMALL
 ==>
   !OUTPUT! SMALL
   -GOAL>
)
Parameters for production SMALL:
 :UTILITY 0.000
 :U 0.000
     0.000 PROCEDURAL PRODUCTION-SELECTED SMALL
0.000 PROCEDURAL BUFFER-READ-ACTION GOAL
0.050 PROCEDURAL PRODUCTION-FIRED SMALL
SMALL
     0.050 PROCEDURAL CLEAR-BUFFER GOAL
0.050 PROCEDURAL CONFLICT-RESOLUTIO
0.050 ----- Stopped because no
                                            CONFLICT-RESOLUTION
      0.050 -----
                                            Stopped because no events left to process
```

As expected the production small is selected and fired. Before describing the results with procedural partial matching enabled the additional output in the trace will be described.

8.1.3.1 The conflict set trace parameter

The :cst parameter which is set to \mathbf{t} in the model is the conflict set trace parameter. It is a model debugging aid similar to the activation trace parameter used with the declarative memory module. If it is set to \mathbf{t} then during every conflict resolution occurrence it will display the instantiation of each production which matches along with its current utility parameters. That set of matching productions is referred to as the conflict set. In this case that is only the production small, and because there is no utility learning on or any noise in the system that production has a utility and U(t) of 0:

8.1.3.2 Turning on ppm

If you change the model to enable procedural partial matching by setting the :ppm parameter to 1, save and reload it, then run it you will see a trace like this:

```
> (run 1.0)
    0.000 PROCEDURAL
                                   CONFLICT-RESOLUTION
(P SMALL
  =GOAL>
      ISA TEST
      VALUE SMALL
      VALUE SMALL
==>
  !OUTPUT! SMALL
  -GOAL>
)
Parameters for production SMALL:
:UTILITY 0.000
:U 0.000
(P MEDIUM
  =GOAT<sub>1</sub>>
      ISA TEST
      VALUE [MEDIUM, SMALL, -0.5]
      VALUE SMALL
  !OUTPUT! SMALL
  -GOAL>
Parameters for production MEDIUM:
:UTILITY -0.500
 :U 0.000
    0.000 PROCEDURAL
                                  PRODUCTION-SELECTED SMALL
    0.000 PROCEDURAL
                                   BUFFER-READ-ACTION GOAL
```

```
0.050 PROCEDURAL PRODUCTION-FIRED SMALL

0.050 PROCEDURAL CLEAR-BUFFER GOAL
0.050 PROCEDURAL CONFLICT-RESOLUTION
0.050 ----- Stopped because no events left to process
```

Again we see the production small being selected and fired, but now we see that the production medium was also a member of the conflict set. For a partially matched production the instantiation of the production will show additional information about the partial match. Here is the instantiation for the production medium from the trace:

In the comparison for the value slot, instead of just seeing medium as was specified in the production, we see a set of items in brackets (the red text above). That indicates that the test was not a perfect one. The first item in the brackets was the value specified in the production. The second item is the buffer chunk's value for that slot, and the third item is the similarity between those items.

Another important thing to notice is that the binding for the variable =val in that production is small (the blue text above). That is because that is the actual content of that slot in the chunk in the buffer -- the variable bindings come from the slots of the buffer's chunk and not values specified in the production.

After the instantiation of medium we see its current utility values:

```
Parameters for production MEDIUM:
:UTILITY -0.500
:U 0.000
```

The U(t) value for medium is 0 just as it is for small. The utility used for deciding which production to fire however is not 0 because it was not a perfect match. The similarity between small and medium is set to -0.5 in the model and the :ppm value was set to 1. So, the utility of medium is: 0 + 1 * (-0.5) = -0.5.

8.1.3.3 The large production

Why isn't the production large also considered in the conflict set as a partial match? The reason is because there is no similarity set between the chunks small and large in the model. Thus, those chunks have the minimum similarity value and a test for the chunk large will not be considered a partial match to the chunk small in a production.

8.1.3.4 Adding noise

If the :egs parameter is set to a value greater than 0 then occasionally the medium production will be selected over the small production because of the noise added to the utilities. Here is a run where :egs was set to 1 showing medium being selected:

```
> (run 1.0)
     0.000 PROCEDURAL
                                          CONFLICT-RESOLUTION
(P SMALL
   =GOAL>
        ISA TEST
       VALUE SMALL
       VALUE SMALL
 ==>
   !OUTPUT! SMALL
   -GOAT.>
)
Parameters for production SMALL:
 :UTILITY -0.713
 :U 0.000
(P MEDIUM
   =GOAL>
       ISA TEST
       VALUE [MEDIUM, SMALL, -0.5]
       VALUE SMALL
   !OUTPUT! SMALL
   -GOAL>
)
Parameters for production MEDIUM:
 :UTILITY 0.453
 :U 0.000
     0.000 PROCEDURAL PRODUCTION-SELECTED MEDIUM
0.000 PROCEDURAL BUFFER-READ-ACTION GOAL
0.050 PROCEDURAL PRODUCTION-FIRED MEDIUM
SMATIT
     0.050 PROCEDURAL CLEAR-BUFFER GOAL
0.050 PROCEDURAL CONFLICT-RESOLUTION
0.050 Stopped begans no
      0.050 -----
                                         Stopped because no events left to process
```

8.1.4 Building Sticks Task alternate model

To see procedural partial matching used in an actual task this unit contains a different model of the learning version of the Building Sticks Task from unit 6 of the tutorial. The main difference between this model and the one presented in unit 6 is that instead of having separate productions to force and decide for the over and under strategies this model only has a decide production for each strategy.

There are several minor differences between this models and the previous one with respect to how the encoding is performed to enable the simpler test, but we will only be looking in detail at the two major differences between them. Those differences are in how the strategy is initially chosen and how the model computes the difference between the current stick's length and the goal stick's length.

8.1.4.1 Strategy choice

In this model these are the productions which decide between the overshoot and undershoot strategies:

```
(p decide-over
   =goal>
     isa try-strategy state choose-strategy
   - strategy over
   =imaginal>
     isa encoding
     goal-length =d
     b-len =d
   =imaginal>
   =goal>
     state prepare-mouse
     strategy over
   +visual-location>
     isa visual-location kind oval
     screen-y 60)
(p decide-under
   =goal>
     isa
              try-strategy
     state choose-strategy
   - strategy under
   =imaginal>
     isa encoding
     goal-length =d
     c-len =d
==>
   =imaginal>
   =goal>
             prepare-mouse
     state
     strategy under
   +visual-location>
     isa visual-location kind oval
     screen-v 85)
```

They are essentially a combination of the force and decide productions from the previous model for each strategy. Because they test the current strategy value they still operate as a forcing production when the model fails and has to choose the other strategy, but when there is no current strategy either one can be potentially chosen and the utilities will determine which one is chosen.

Procedural partial matching is enabled for this task and a similarity between numbers is set up for this model with these parameter settings in the model:

```
(sgp :ppm 40 :sim-hook number-sims)
```

The :ppm value of 40 was estimated to produce a good fit to the data.

The similarities between numbers (the line lengths in pixels) are computed by the number-sims function specified and are set using a simple linear function to scale the possible differences into the default similarity range of 0 to -1:

Similarity
$$(a,b) = -\frac{abs(a-b)}{300}$$

Unlike the previous model of this task, this one does not need to compute the difference between the goal stick's length and the b and c sticks' lengths explicitly to determine whether overshoot or undershoot should be used. Now that happens as a result of the partial matching in the **imaginal** buffer test of those productions. Whichever stick is closer to the goal stick's length will bias the utility toward that choice.

The initial utilities of the decide-over and decide-under productions are set at 10 in the model. Given that, we can look at how utility is determined when those productions are competing on the first problem which has stick lengths of a=15, b=250, c=55, and a goal of 125. The chunk in the **imaginal** buffer at that time will look like this:

```
ENCODING0-0
ISA ENCODING
A-LOC VISUAL-LOCATION8-0-0
B-LOC VISUAL-LOCATION9-0-0
C-LOC VISUAL-LOCATION10-0-0
GOAL-LOC VISUAL-LOCATION11-0-0
LENGTH NIL
GOAL-LENGTH 125
B-LEN 250
C-LEN 55
DIFFERENCE NIL
```

The length of the goal, b, and c sticks are the important tests for the decide productions in the imaginal buffer tests:

Each production is checking to see if the desired stick and the goal stick are the same length, and the procedural partial matching will adjust the utilities of those productions based on the similarity between the compared sticks. Here are the instantiations of those productions showing the similarities as computed from the number-sims function:

```
(P DECIDE-OVER
   =GOAL>
      ISA TRY-STRATEGY
      STATE CHOOSE-STRATEGY
   - STRATEGY OVER
  =IMAGINAL>
      ISA ENCODING
       GOAL-LENGTH [250, 125, -0.41666666]
      B-LEN 250
   =IMAGINAL>
   =GOAL>
      STATE PREPARE-MOUSE
      STRATEGY OVER
   +VISUAL-LOCATION>
      ISA VISUAL-LOCATION
      KIND OVAL
      SCREEN-Y 60
)
(P DECIDE-UNDER
  =GOAL>
      ISA TRY-STRATEGY
      STATE CHOOSE-STRATEGY
      STRATEGY UNDER
   =IMAGINAL>
      ISA ENCODING
      GOAL-LENGTH [55, 125, -0.23333333]
      C-LEN 55
==>
  =IMAGINAL>
   =GOAL>
      STATE PREPARE-MOUSE
      STRATEGY UNDER
   +VISUAL-LOCATION>
      ISA VISUAL-LOCATION
      KIND OVAL
       SCREEN-Y 85
)
```

The effective utility of decide-over is -6.666666 (10 + 40 * -0.41666666) and the effective utility of decide-under is 0.666667 (10 + 40 * -0.23333333). Knowing that the noise for utilities is set at 3 in the model we can compute the probabilities of choosing over vs under on the initial trial using the equation presented in unit 6:

Probability (i) =
$$\frac{e^{U_i/\sqrt{2}s}}{\sum_{j} e^{U_j/\sqrt{2}s}}$$

$$Probability (over) = \frac{e^{-6.666/4.24}}{e^{-6.666/4.24} + e^{.666/4.24}}$$

$$\approx .15$$

$$Probability (under) = \frac{e^{0.666/4.24}}{e^{-6.666/4.24} + e^{.666/4.24}}$$

$$\approx .85$$

Thus, the model will pick undershoot about 85% of the time for the first problem.

As in the unit 6 model of the task, this model is also learning utilities based on the rewards it gets. So, the base utility values of the strategies will be adjusted as it progresses. Here are the results from running the unit 6 model of the task showing the average learned utility values for the four productions it needs to make the decision:

```
> (bst-experiment 100)
CORRELATION: 0.803
MEAN DEVIATION: 17.129

Trial 1  2  3  4  5  6  7  8  9  10  11  12  13  14  15
        23.0 60.0 59.0 70.0 91.0 42.0 80.0 86.0 59.0 34.0 33.0 22.0 54.0 72.0 56.0

DECIDE-OVER: 13.1506
DECIDE-UNDER: 11.1510
FORCE-OVER : 12.1525
FORCE-UNDER: 6.5943
```

Here are the results of running this new model of the task:

We see a similar shift in the utilities with over gaining utility and under losing utility and overall this model produces a slightly better fit to the data.

8.1.4.2 Attributing actions to the imaginal module

Before moving on to the other new procedural mechanism there is one other new capability to look at in the new Building Sticks model. In the previous model of the task the productions computed the difference between the current stick length and the goal

stick length to decide whether to select stick a or stick c for each of the actions after the strategy choice had been made using a !bind! action in the production to do the math and then place that value into a slot of the **imaginal** buffer:

In many models abstractions like that are easy to justify and do not cause any issues for data comparison. However, if one is interested in more low-level details, often when comparing model data to human data collected from fMRI or EEG studies, then accounting for the timing of such actions and attributing them to an appropriate module are important. In the case of the imaginal module, there is a built in mechanism that allows the modeler to assign user defined functionality to the imaginal module and this version of the Building Sticks task does so instead of using a !bind! action for computing the difference. The details of how that is done are in the additional text for this unit if you are interested in how to do that.

8.2 Dynamic Pattern Matching

Dynamic pattern matching is a powerful mechanism which allows the model to test and extend its representations based on the current context without that specific information having to be explicitly encoded into the model. It is particularly important for tasks where instruction or example following are involved, but can also be useful in other situations where flexibility or context dependence is necessary.

8.2.1 Basic Operation

The distinguishing feature between dynamic pattern matching and the standard pattern matching which has been used so far in the tutorial is that with dynamic pattern matching one can use variables to specify the slots in the conditions and actions of the productions. Other than that, a dynamically matched production operates just like the standard productions that have been used throughout the tutorial. Thus, whether standard or

dynamic the following things still apply: only one production can be selected and fired at a time, the production which is selected will be the one that has the highest utility among those that match the current state, it takes 50ms to fire the production, utility learning applies to all productions which have fired when a new reward is received, and if production compilation is enabled every pair of successive productions which fire may be combined into a single new production.

Because there is a different syntax for dynamically matched productions a separate command must be used when one is defining a dynamically matched production (this is done primarily as a safety measure to prevent unintended modeling errors). Instead of using the p command, one uses the p* command to create a dynamically matched production. The syntax for creating a production with p* is a superset of the standard production syntax – every production which can be defined with p could also be defined using p*.

There are three things which dynamic pattern matching allows that cannot be done with standard pattern matching and they will be described in the following sections. For those descriptions we will be using a very simple model found in the simple-dynamic-model file. It has three productions which demonstrate those capabilities, and it is a very simplified version of something that is often done in a model that is following a set of declarative instructions. All the model does is update the chunk in the **imaginal** buffer based on information it retrieves from declarative memory. Because all the components of this model are known in advance it is not actually necessary to use dynamic pattern matching, but that should make it easier to understand since it can be compared to the static productions which would perform the same operations in this case.

8.2.2 Arbitrary slots in conditions

The first thing that dynamic pattern matching allows is the ability to test arbitrary slots in the conditions of a production. The conditions of the productions start and retrieve-first-step from the example model show this:

```
(p* start
    =goal>
      isa fact
      context =context
      =context =x
     ?imaginal>
      state free
      buffer empty
     ==>
     ...)
 (p* retrieve-first-step
    =qoal>
      isa fact
      context =slot
      data = x
    =imaginal>
      isa result
```

```
=retrieval>
  isa step
  =slot =target
  step first
==>
...)
```

The slot tests in red above are instances of dynamic pattern matching. By using a variable to name a slot in a condition that test now depends on the contents of a buffer at the time of the test instead of specifying the slot name in advance. That means that the same production could test different slots based on the current context.

First we will look at the production start.

```
(p* start
   =goal>
     isa fact
     context =context
     =context =x
   ?imaginal>
     state free
     buffer empty
   =goal>
     context destination
   +imaginal>
     isa result
     data1 =x
   +retrieval>
     isa step
    step first
 )
```

The only things different in that production, relative to those seen previously, are that it is defined using p* instead of p and this test in the **goal** buffer's condition:

```
=context = x
```

That means that the slot being tested will be the one which corresponds to the binding of the variable =context. The variable =x will be bound to the value of that slot. The =context variable is bound to the value of the context slot of the chunk in the **goal** buffer just as it is done for static productions.

Before running the model we will look at the contents of the **goal** buffer and see how this will apply for pattern matching. [If you want, you could run the model using the environment's stepper in tutor mode as was used in unit 1 and try to instantiate the production yourself before continuing.]

Here is the initial chunk placed in the **goal** buffer in the model:

```
FACT0-0
ISA FACT
CONTEXT DATA
DATA 10
```

and here is the **goal** buffer test from the start production:

```
=goal>
  isa fact
  context =context
=context =x
```

The chunk-type matches the isa specification. The =context variable is bound to the value in the context slot, which is data. Then the slot which corresponds to the binding of =context, which is data, is used to bind the variable =x. Thus, =x gets bound to 10. If the binding of =context did not correspond to a slot of the chunk in the buffer then the production would not match. The rest of the start production operates just like all the other productions that have been seen previously in the tutorial and thus should not need further explanation.

When we run the model with the :cst parameter on to show the instantiation of matching productions this is what the start production looks like:

```
(P* START
   =GOAL>
      ISA FACT
      CONTEXT DATA
      DATA 10
   ?IMAGINAL>
      STATE FREE
      BUFFER EMPTY
==>
  =GOAL>
      CONTEXT DESTINATION
   +IMAGINAL>
      ISA RESULT
      DATA1 10
  +RETRIEVAL>
      ISA STEP
      STEP FIRST
)
```

That instantiation looks just like one from a statically matched production, but the important thing to remember is that the instantiation of a dynamic production may have instantiated variables in both the slot value and slot name positions.

The retrieve-first-step production also has a dynamic test in its conditions:

```
==>
```

In this case, that test involves multiple buffers. The value for the =slot variable is bound from one buffer and used to test a slot in a different buffer. Again, you may want to step through that in tutor mode with the environment and instantiate it yourself to get a better feel for how this works before looking at the instantiation below.

After the start production fires, the **goal** buffer's chunk looks like this:

```
FACT0-0
ISA FACT
CONTEXT DESTINATION
DATA 10
```

Thus, in the **goal** buffer condition of retrieve-first-step the =slot variable will be bound to destination and the =x variable will be bound to 10.

The chunk created by the start production in the **imaginal** buffer looks like this:

```
RESULT0-0
ISA RESULT
DATA1 10
DATA2 NIL
```

That matches the isa specification which is the only condition for the **imaginal** buffer.

The chunk which is in the **retrieval** buffer looks like this:

```
A-0
ISA STEP
STEP FIRST
DESTINATION DATA2
```

and this is the condition for that buffer from the retrieve-first-step production:

```
=retrieval>
  isa step
  =slot =target
  step first
```

The isa test and the step slot both match the chunk in the buffer. The =slot variable is bound to destination from the **goal** buffer, and thus the variable =target will be bound to the value of the destination slot from the chunk in the **retrieval** buffer, which is data2. If there was not a slot named destination in the chunk in the **retrieval** buffer then this condition would not have matched and the production would not be selected.

Here is the instantiation of that production from the trace:

```
(P* RETRIEVE-FIRST-STEP
   =GOAL>
      ISA FACT
      CONTEXT DESTINATION
      DATA 10
   =IMAGINAL>
      ISA RESULT
   =RETRIEVAL>
       ISA STEP
       DESTINATION DATA2
       STEP FIRST
 ==>
   =GOAL>
      DATA 11
   =IMAGINAL>
      DATA2 10
   +RETRIEVAL>
      ISA STEP
      STEP SECOND
)
```

Though not shown in these examples, the dynamic conditions may also be used with any of the modifiers for a slot test as well as multiple times within or across buffer conditions. Thus, this set of conditions would be valid in a dynamically specified production (assuming appropriate chunk-type definitions):

```
=goal>
  isa state
  context =context
=imaginal>
  isa representation
> =min-s 0
  =min-s =min
> =max-s =min
= context current
=retrieval>
  isa fact
- =context complete
  max-slot =max-s
  min-slot =min-s
```

However, there are some constraints imposed on the use of dynamic conditions and those will be described in a later section.

8.2.3 Arbitrary slots in actions

The actions of the retrieve-first-step production show how dynamic pattern matching can be used to specify an action based on the current context. In the modification of the **imaginal** buffer we see this action:

```
=imaginal>
     =target =x
```

As with the conditions, that means that the slot of the chunk in the **imaginal** buffer that will be modified will be the one bound to the variable =target. From the previous section we saw that that was the value data2, and that the =x variable was bound to 10. Thus this action will modify the chunk in the **imaginal** buffer so that its data2 slot has the value 10.

Here is the chunk in the imaginal buffer after retrieve-first-step fires.

```
RESULT0-0
ISA RESULT
DATA1 10
DATA2 10
```

A variable may be used to specify a slot in any buffer modification or buffer request action of a dynamically matching production. However, because such values are only determined when the production actually matches, it is possible that the production may attempt to make a modification or request with a slot that is not valid for the chunk-type that corresponds to the action. In the event of buffer modification actions there is a special mechanism which handles that, as described in the next section. For buffer requests, if an invalid slot is specified that will usually lead to a warning and the failure to execute the request, but could also result in errors occurring during the run. Thus, if slots of requests are specified dynamically, care should be taken to ensure the productions perform other tests, either in that production, or elsewhere in the sequence of productions, to protect against invalid requests.

8.2.4 Extending chunks with new slots

The final production in the test model, retrieve-second-step, shows the final new capability which dynamic pattern matching allows. Here is the production:

Other than specifying that the step slot of the retrieved chunk is the value second the conditions of this production are exactly the same as they are for the retrieve-first-step production, and the action of this production is a modification to the chunk in the

imaginal buffer which looks exactly the same as the one from the retrieve-first-step production.

The significant difference between retrieve-first-step and retrieve-second-step is not in the specifications of the productions, but the contents of the buffers when they are selected. Retrieve-first-step was described in the previous section, and essentially the same matching process holds true for retrieve-second-step. However, the bindings for the variables are now different. Here are the chunks from the **goal** and **retrieval** buffers after retrieve-first-step fires which match the retrieve-second-step production:

```
GOAL: FACTO-0

FACTO-0

ISA FACT

CONTEXT DESTINATION

DATA 11

RETRIEVAL: B-0 [B]

B-0

ISA STEP

STEP SECOND

DESTINATION DATA3
```

The variable bindings from the conditions of the production are thus: =slot is bound to destination, =x is bound to 11, and =target is bound to data3. Given those bindings, the instantiation of the action of this production will look like this:

```
=imaginal> data3 11
```

Here is the chunk which is in the **imaginal** buffer at that time:

```
RESULT0-0
ISA RESULT
DATA1 10
DATA2 10
```

and here is the specification of the corresponding chunk-type:

```
(chunk-type result data1 data2)
```

The important thing to notice is that the chunk does not have a slot named data3, but that is what the modification action specifies to change. When a dynamically determined modification action specifies a slot which does not exist in the chunk being modified it will extend that chunk's type to add the specified slot. Looking at the trace resulting from this production firing we see an event which indicates that the result chunk-type is being extended to contain a slot named data3:

```
0.350 PROCEDURAL PRODUCTION-FIRED RETRIEVE-SECOND-STEP
0.350 PROCEDURAL MOD-BUFFER-CHUNK IMAGINAL
```

Here is the result for the chunk in the **imaginal** buffer after that occurs:

```
IMAGINAL: RESULT0-0
RESULT0-0
ISA RESULT
DATA1 10
DATA2 10
DATA3 11
```

This mechanism allows the model to build its chunk-type representations as needed instead of requiring all possible slots be specified up front.

8.2.5 Constraints on dynamic pattern matching

Dynamic pattern matching adds a lot of flexibility to the specification of productions, and this flexibility allows for a lot more powerful productions to be created. However, since ACT-R is intended to be a model of human cognition, there are two constraints imposed upon how dynamic pattern matching works to maintain the plausibility of the system.

8.2.5.1 No Search

The first constraint on dynamic pattern matching is that it does not require searching to find a match. All productions which use dynamic pattern matching must be specified so that all variables are bound directly based on the contents of slots. The procedural module will not allow the specification of a condition like this:

```
=goal>
  isa example
  =some-slot desired-value
```

which requires finding a slot which has a particular value. If search like that were allowed then the matching of a production could become an NP complete task.

8.2.5.2 One level of indirection

The other constraint on dynamic pattern matching is that it only allows one level of indirection. All of the variables which are used as slot indicators must be bound to slots which are specified as constants. Thus, one cannot use a dynamically matched slot's value as a slot indicator like this:

Allowing an unbounded level of indirection is not plausible, thus some constraint needed to be determined for the indirection. A single level was chosen as the constraint because

that was all that was necessary to provide the abstractions needed and such a mechanism appears to be realizable within the human brain.

8.2.6 New paired-learning model

In unit 7 the paired-learning model performed the paired associate task based on a set of declarative instructions and a set of somewhat general productions for interpreting instructions. By using dynamically matched productions, a new model of the task can be written using a more general declarative representation and with productions which are able to handle more situations than those of the previous model. The basic operation of the model is the same, and it uses the same set of instructions but with a different declarative representation. Thus, this unit will not describe the new model in detail and will only note the significant differences from the previous model.

8.2.6.1 Chunk-type hierarchy

Before looking at the productions of the new model, there is one other feature used which has not been presented previously in the tutorial. That feature is the ability to create a hierarchy of chunk-types for a model. When creating a new chunk-type one can optionally specify an existing chunk-type to be the parent type of that new type. The newly created type will have all the slots of the parent type by default, and it may add additional slots of its own. This is a modeling feature which can help when writing a model to make the productions easier to write and understand.

When looking at descriptions of a chunk-type, for instance by calling chunk-type without any parameters, if a chunk-type has a parent type that will be shown with an arrow pointing to the chunk-type name followed by the parent type. For example, all of the chunk-types for the visual objects which the model attends, like text and lines, are sub-types of the chunk-type visual-object as shown in the output from the chunk-type command here:

```
VISUAL-OBJECT
SCREEN-POS
VALUE
STATUS
COLOR
HEIGHT
WIDTH

TEXT <- VISUAL-OBJECT
SCREEN-POS
VALUE
STATUS
COLOR
HEIGHT
WIDTH
```

```
LINE <- VISUAL-OBJECT
SCREEN-POS
VALUE
STATUS
COLOR
HEIGHT
WIDTH
END1-X
END1-Y
END2-X
END2-Y
```

When testing the conditions for a chunk in a buffer the isa test will match to the specific type named as well as any type which has that type as a parent. Thus, this condition in a production:

```
=visual>
isa visual-object
value =val
```

would not discriminate based on the type of object being attended and could match to a line, text, or any other chunk-type which has visual-object as a parent. Whereas these conditions:

```
=visual>
  isa text
  value =val

=visual>
  isa line
  value =val
```

will only match if the item is of the specific chunk-type listed (or a type which has that type as a parent).

To create a chunk-type as a sub-type of another type one needs to specify that using an :include in the chunk-type definition like this as used in the paired-learning-dynamic model:

```
(chunk-type operator pre)
(chunk-type (action (:include operator)) action required label post)
(chunk-type (test (:include operator)) slot success failure)
```

It creates a chunk-type called operator with one slot named pre, and then it defines two other chunk-types called action and test which are both sub-types of the operator chunk-type. Each of those sub-types will have a slot called pre along with their own set of slots as specified above. Here is how they are shown in the list of chunk-types:

```
OPERATOR
PRE
```

```
ACTION <- OPERATOR
PRE
ACTION
REQUIRED
LABEL
POST

TEST <- OPERATOR
PRE
SLOT
SUCCESS
FAILURE
```

In this model, using a chunk-type hierarchy allows the use of a single production to retrieve the next operator like this:

Then (as will be seen in the next section) it has productions which are specific to the type of operator which is retrieved to perform the actions needed. Thus, with the chunk-type hierarchy the productions should be easier to understand because different operators are indicated appropriately in the isa tests of the productions and have slots with names that are meaningful to the task being performed. Of course it would also be possible to write the model using a single chunk-type which either had all of the slots needed or which reused slots for different purposes based on the action, as the arg1 and arg2 slots were in the previous paired-learning model, and it would still perform the same way. Thus, the chunk-type hierarchy is essentially just a modeling convenience in ACT-R.

8.2.6.2 Generality from the instructions

One difference between this model and the previous one is that the instructions themselves specify the contents of the items to be learned. In the previous model the chunk-type for holding the pairs that were learned was prespecified to have two slots, arg1 and arg2:

```
(chunk-type args arg1 arg2)
```

In this model however the chunk-type used by the model is specified like this:

```
(chunk-type result)
```

It does not have any slots initially, but when the model does the task it will create a chunk like this for a pair of items:

```
RESULT10-0
ISA RESULT
WORD "zinc"
NUMBER "9"
```

That happens during the interpretation of an instruction which has the action to read an item like these:

```
(op1 isa action pre start action read label word post stimulus-read)
(op5 isa action pre wait action read label number post new-trial)
```

The label slot of the action specifies the name of the slot into which the item should be stored in the **imaginal** buffer and is handled by these two productions:

```
(p read
   =goal>
    isa task
step retrieving-operator
   =retrieval>
     isa action
     action read
     label =destination
post =state
     post
   =visual-location>
     isa
              visual-location
   ?visual>
     state
               free
   ?imaginal>
     buffer
              full
   +visual>
             move-attention
     isa
     screen-pos =visual-location
   =goal>
     context =destination
     step process
state =state)
(p* encode
   =goal>
     isa task
step process
context =which-slot
   =visual>
                text
     isa
              =val
     value
   =imaginal>
              result
     isa
   =imaginal>
     =which-slot =val
   =goal>
     step
                ready)
```

The read production saves the value of the label slot in the **goal** buffer's context slot and requests a shift of visual attention to the item. When the item is attended the encode

production can fire and place the value of the text which was read into that slot of the chunk in the **imaginal** buffer. If the chunk in the buffer does not have a slot by that name then that modification in the dynamic production will extend the chunk to have such a slot.

That makes this set of instruction following productions much more general than the previous ones seen because the representation does not have to be encoded in the model's chunk-types and could have any number of slots in the representation based on the instructions. The model also does not need to have a separate production to set each possible slot that is used in the representation. Of course, since the instructions are specifically encoded in this particular model's definition that generality is not necessary since the representation is known in advance, but these same productions could be used for other tasks without changing them, or they could be used with an even more general version of the model which had other productions for reading the instructions themselves. Similarly, we see that by using dynamically matched productions this new version of the model can also perform the retrieval based on a slot specified in the instructions:

```
(p* retireve-associate
   =goal>
    isa
            task
     step retrieving-operator
   =imaginal>
    isa
            result
    =target =stimulus
   =retrieval>
    isa action
     action retrieve
    required =target
     label =other
    post
             =state
 ==>
   =imaginal>
   +retrieval>
    isa result
    =target =stimulus
   <fre>coal>
    step
            retrieving-result
     context =other
     state =state)
```

and also respond using an arbitrary slot specified in the instructions:

```
?manual>
    state free
==>
=imaginal>
+manual>
    isa press-key
    key =val
=goal>
    state =state
    step ready)
```

8.2.6.3 Dynamic matching and production compilation

As in the previous version of this task, this model uses production compilation to learn specific productions for doing the task as it is repeatedly following the instructions. There is no difference in how the production compilation mechanism works with dynamically matched productions. It still combines successive productions which are fired into a single production when possible using the rules described in unit 7. However, it is worth looking at a couple of examples to see how that applies when dynamically matched productions are involved. When one or both of the productions being composed together contain dynamically matched components, the resulting production may retain some of those dynamic components or they could be replaced with statically matched values. They will be replaced by static values in the same way that other variables are replaced – when a retrieval request and harvesting are removed between the productions.

We can see examples of this very early in the model's trace with the :pct parameter set to t. When the encode and retrieve-operator productions are combined the result still has the dynamically specified components from the encode production:

```
(P* PRODUCTION1
 "ENCODE & RETRIEVE-OPERATOR"
  =GOAT_{i}>
      ISA TASK
      CONTEXT =WHICH-SLOT
      STEP PROCESS
      STATE =STATE
  =TMAGTNAT,>
      ISA RESULT
  =VISUAL>
       ISA TEXT
      VALUE =VAL
==>
  =IMAGINAL>
      =WHICH-SLOT =VAL
  =GOAT_{i}>
      STEP RETRIEVING-OPERATOR
  +RETRIEVAL>
      ISA OPERATOR
      PRE =STATE)
```

However, when the retrieve-operator and retrieve-associate productions are combined the instantiation of the variables used from the retrieved chunk results in a statically matched production:

```
(P PRODUCTION2
 "RETRIEVE-OPERATOR & RETIREVE-ASSOCIATE - OP2"
      ISA TASK
      STATE STIMULUS-READ
      STEP READY
  =IMAGINAL>
      ISA RESULT
      WORD =STIMULUS
  =IMAGINAL>
  =GOAL>
      CONTEXT NUMBER
      STATE RECALLED
      STEP RETRIEVING-RESULT
  +RETRIEVAL>
      ISA RESULT
      WORD =STIMULUS)
```

8.2.6.4 Data fit

Despite the model being more general, it still performs the task the same way as the previous version of the model does, and with production compilation enabled provides the same fit to the data.

Here are the results from the unit 7 model:

```
> (paired-experiment 10)
Latency:
CORRELATION: 0.997
MEAN DEVIATION: 0.143
Trial 1 2
                  3
                              5
                        4
                                    6
      0.000 2.339 2.118 1.967 1.739 1.718 1.509 1.582
Accuracy:
CORRELATION: 0.996
MEAN DEVIATION: 0.045
Trial 1 2
                 3
                        4
                              5
                                    6
                                          7
                                                 8
      0.000 0.445 0.660 0.755 0.835 0.895 0.895 0.955
```

and here are the results from the model from this unit:

```
> (paired-experiment 10)
Latency:
CORRELATION: 0.998
MEAN DEVIATION: 0.110
                   3
                         4
                               5
                                            7
Trial 1
            2.
                                     6
      0.000 2.328 2.109 1.883 1.746 1.600 1.503 1.558
Accuracy:
CORRELATION: 0.996
MEAN DEVIATION: 0.043
Trial 1 2
                  3
                         4
                               5
                                     6
     0.000 0.430 0.620 0.770 0.875 0.910 0.915 0.935
```

8.3 Assignment

The assignment for this unit will be to use both of the new production techniques described above to create a model which can perform a simple categorization task. The experiment this model will be performing is a simplification of an experiment which was performed by Robert M. Nosofsky (which was based on an experiment performed by Stephen K. Reed) that required participants to classify schematic face drawings into one of two learned categories.

In the experiment the participants first trained on learning 10 faces each of which belonged to one of two categories. The faces themselves were varied along four features: eye height, eye separation, nose length, and mouth height. Then there was a testing phase in which they were presented with both old and new faces and asked to specify to which category the face belonged. The data collected was the probability of classifying the face as a member of each category in the testing phase. For this assignment we will not be modeling the whole task, nor will we be trying to fit all of the data from the experiment because a thorough model of this task would require a lot more work than is reasonable for an assignment.

Here is the general description of the task which the model for this assignment will have to perform. It will be presented with the attributes of a stimulus one at a time, indicating the name of a feature and its value. It must collect those attributes into a single chunk. Using that chunk, it can then retrieve a best matching example from declarative memory. Based on that retrieved chunk, it will make a category choice for the current stimulus. The model will not have to perceive the face images nor will it be required to perform the initial training phase, and it will not involve any learning mechanisms. Each trial will be completed separately with the model being reset before each one. Thus the model will be similar to the fan experiment model from unit 5, with the training information preencoded in declarative memory and the model only needing to perform one trial of the task. The details of how those steps are to be performed are described below.

The important part of the exercise is the first step – creating the stimulus representation from the individual attributes. The focus of the assignment will be on how to perform this task in a general way because that sort of encoding is something which can be applicable to many different tasks.

8.3.1 The Stimulus Attributes

The attributes of the stimulus to categorize will be presented to the model one at a time through the **goal** buffer. The experiment code will set the **goal** buffer to a chunk of type attribute, and the attribute chunk-type is defined like this:

```
(chunk-type attribute name value)
```

The name slot of the chunk will contain a symbol specifying the name of the attribute being presented. The value slot will hold a value for that attribute in the current stimulus and that will be a number. Thus, a goal chunk at the start of a trial may look like this:

```
ATTRIBUTEO
ISA ATTRIBUTE
NAME MH
VALUE 0.178
```

The first thing the model should do is convert that value into a discrete description. The reason for doing so is because instead of storing the raw values for the learned examples the model will have example chunks like this stored in declarative memory which it has to be able to retrieve:

```
EXAMPLE1
ISA EXAMPLE
CATEGORY 1
EH SMALL
ES LARGE
NL MEDIUM
MH SMALL
```

Those chunks provide a more general representation of the stimuli instead of just recording explicit measurements or distance values. By converting the attributes as they are encoded the model will be able to create a similarly structured chunk in the **imaginal** buffer. In a more complete model of the task a similar process would take place during the training phase of the experiment to strengthen and learn the examples.

For this task all of the attributes can be classified as either small, medium, or large, and to make things easier, the numeric values of the attributes used have all been scaled to the same range based on data also collected by Nosofsky for this task. To perform that conversion from numeric value to descriptive name, procedural partial matching should be used by the model. The starting model has a similarity function provided that assigns a similarity score between the attribute values and the labels small, medium, and large. Thus, one can have competing productions which test the value for each of those labels and the production which specifies the most similar label will be the one selected.

The specific range of values used should not be explicitly encoded into the model, and in fact this unit will not describe how the similarity values are computed between the labels and the numbers. Thus, your model should not explicitly test the values against any particular numbers, but should be able to work with any value given relying on the similarity function to provide the comparison to the appropriate labels. Thus, a production like this is *not* a good thing to use in this model:

```
(p bad-way-to-test-medium
=goal>
    isa attribute
```

```
> value -.5
< value .5
...
```

After determining what the appropriate label for the attribute is, the model must record that value in the chunk in the **imaginal** buffer. When the first attribute is presented, the **imaginal** buffer will be set to a chunk of type example, where the example chunk-type is defined like this:

```
(chunk-type example category)
```

The category slot of that initial imaginal chunk will be the value unknown, and thus the initial **imaginal** buffer chunk will look like this:

```
EXAMPLE1
ISA EXAMPLE
CATEGORY UNKNOWN
```

Note that it does not have any slots for holding the specific attributes of the task. This is where dynamic pattern matching will need to be used. The model will need to add a slot to the chunk based on the name of the attribute provided. Thus, the complete encoding of the attribute shown above should result in the imaginal buffer looking like this when done:

```
EXAMPLE1
ISA EXAMPLE
CATEGORY UNKNOWN
MH MEDIUM
```

Again, it is important that the model be general in how it performs that modification to the **imaginal** buffer's chunk. The model should be able to encode any attribute name which is provided, and should not have any specific attribute names mentioned in the productions. Thus this action in a production is *not* the way that it should be handled:

As with the values, the unit will not be specifying the names that the attributes will have. The experiment code will guarantee that the example chunks created in declarative memory have the same attributes as those that are presented to the model, and the model should be able to work with any attribute names it is given.

After updating the **imaginal** buffer, the model should stop and wait for the next attribute to be provided. An easy way to do that would be to make sure that all of the productions which are processing the attribute test the **goal** buffer chunk in their conditions (which is

likely to occur since it contains the information needed) and then clear the chunk from the **goal** buffer after the attribute has been processed. Thus, the model should be able to process any number of attributes for a stimulus. The result will be a chunk in the **imaginal** buffer which has a slot for each of the attributes that was provided and the value in each of those slots is a label (small, medium, or large) as determined through procedural partial matching based on the numeric value from the attribute.

8.3.2 Model Response

After all of the attributes have been provided to the model a different goal chunk will be set to indicate that it is time for the model to retrieve an example and classify the stimulus that is currently encoded in the **imaginal** buffer. The new goal is of the chunk-type categorize which is defined like this:

```
(chunk-type categorize state)
```

The state slot of the goal chunk will be nil, and that slot may be used as needed for coordinating the model's actions during the response task.

To make a response, the model needs to do two things. First, it must retrieve a chunk from declarative memory which is similar to the chunk in the **imaginal** buffer. The model will have 10 examples already encoded in declarative memory which have their features set based on the examples from the original experiment. Half of the examples are in category 1 and the other half are in category 2, and here are two examples:

```
EXAMPLE 4

ISA EXAMPLE
CATEGORY 1
EH SMALL
ES MEDIUM
NL LARGE
MH LARGE

EXAMPLE 5
ISA EXAMPLE
CATEGORY 2
EH LARGE
ES SMALL
NL SMALL
MH SMALL
```

Because the names of the slots to specify in the retrieval request are not known in advance the easiest way to perform the retrieval request is using a direct request, as was shown in the siegler model from unit 5 of the tutorial. That will look like this as an action in the production:

(p ...

```
==>
+retrieval> =imaginal
...)
```

and is equivalent to specifying all of the slots and values from the chunk that is in the **imaginal** buffer explicitly in the request.

Declarative partial matching is also enabled for this model, and that will allow for the retrieval of a chunk which has values close to the requested values in the event that there is not a perfectly matching example. The other declarative parameters for the model are set such that if the chunk in the **imaginal** buffer is created correctly there should always be a chunk retrieved in a reasonable amount of time.

After the model retrieves a chunk, the final step it needs to do is to set the category slot of the chunk in the **imaginal** buffer to be the same as the category value of the chunk that was retrieved. That can be done with a production that looks more or less like this, but you may also need a goal buffer test depending on how you testing state in other productions:

After that happens the model should again stop because it is then done with the trial.

8.3.3 Running the experiment

There are three commands provided for running the task. The first is present-one-attribute which takes two parameters, an attribute name and an attribute value. It can be used to test the model's encoding ability. The attribute name can be any symbol and the value should be a number between -1 and 1. It will generate an attribute goal chunk for the model with the name and value slots set using the values provided and run the model to perform the encoding. Thus, it could be called like this:

```
(present-one-attribute size -1)
```

Which would create this chunk in the **goal** buffer:

```
ATTRIBUTE0-0 ISA ATTRIBUTE
```

```
NAME SIZE VALUE -1
```

and should result in the model having a chunk like this in the **imaginal** buffer when it is done:

```
EXAMPLE10-0
ISA EXAMPLE
CATEGORY UNKNOWN
SIZE SMALL
```

because a value of -1 is most similar to the small label (though sometimes noise in the utility calculations could cause one of the other labels to also be applied). You should work with this command only until your model is able to do that part of the task reliably.

Once the model is able to properly encode attributes you can test its ability to retrieve examples based on a stimulus with multiple attributes using the present-one-stimulus command. It requires four parameters which should each be a number in the range of -1 to 1. It will reset the model, generate an attribute goal for the model (using a default set of names for the attributes) and run it with each of the values specified, and then generate a categorize goal and run the model to make the response. The return value will be the category which the model has set in the **imaginal** buffer's chunk or nil if it does not properly set a category. Here is an example of calling it and showing it responded with category 1:

```
(present-one-stimulus -1 .5 -.2 0)
```

Once you have a model which can handle individual trials with present-one-stimulus you should then test it on the experiment data using the categorize command. It requires one parameter which is the number of times to repeat the experiment. It will run the model over the 14 stimuli from the experiment which we are using for testing as many times as specified and print out the proportion of times that each item was classified as category 1 along with the experimental data, number of responses the model made, and the model's fit to the experimental data:

The numbers in parentheses should all be the same as the number of trials that were run indicating that the model always responds. We will discuss the data fit and other running options below.

8.3.4 Fitting the data

If your model works as described above, then it should produce a fit to the data similar to this using the default parameters in the model:

If the correlation and deviation are significantly worse than that, then you will want to go back and make sure your model is doing all of the steps described above correctly.

Because fitting the data is not the focus of this exercise it is not necessary to adjust the parameters to improve that fit, but if you would like to explore the parameters for improving the fit then the ones that are recommended to be changed would be these four from the model:

```
(sgp :mp 1 :ppm 1 :egs .25 :ans .25)
```

Those are the partial matching scale parameters for declarative and procedural partial matching and the noise values for those mechanisms. Through adjusting those parameters the reference model was able to achieve this fit which improves the deviation:

```
> (categorize 500)
MEAN DEVIATION: 0.145
CORRELATION: 0.950
```

8.3.5 Generality

If your model fits the data adequately then the final thing to test is to make sure that it is doing the task in a general way. The categorize command takes optional parameters which can be used to modify the attribute names and the range of values it uses. Providing a second number to categorize will shift the attribute values provide to the model by that amount and also shift the similarities to the labels accordingly. Thus, the model should be unaffected by that change and produce the same fit to the data regardless of such a shift:

```
> (categorize 100 4.5)
MEAN DEVIATION: 0.161
CORRELATION: 0.968
```

In addition to that, one can also specify the four names to use for the attributes. Those provided names will be used to generate the examples in declarative memory and to provide the attributes to the model. The names can be any Lisp symbols other than category, since the example chunks already have such a slot. To specify different names they must be passed to categorize after the offset value. Here is an example with no effective offset to the values (a shift of 0) and new names for the attributes:

```
> (categorize 100 0 slot-1 b other name)
MEAN DEVIATION: 0.161
CORRELATION: 0.975
```

Here is what an example from declarative memory looks like in that case:

```
EXAMPLE 0
ISA EXAMPLE
CATEGORY 1
SLOT-1 SMALL
B LARGE
OTHER MEDIUM
NAME SMALL
```

and that is also how the chunk in the imaginal buffer should look at the end of a trial (though the specific labels for the slots will likely be different).

Again, this change should not affect the model's ability to do the task if it has been written to perform the task generally. The best test of the model is to provide both a non-zero shift to the attribute values and new attribute names. A good model for the assignment will still provide the same fit to the data under those circumstances:

```
> (categorize 100 -3 a b c d)
MEAN DEVIATION: 0.162
CORRELATION: 0.936
```

References

Nosofsky, R. M. (1991). Tests of an exemplar model for relating perceptual classification and recognition memory. *Journal of Experimental Psychology: Human Perception and Performance*. 17, 3-27.

Reed, S. K. (1972). Pattern recognition and categorization. *Cognitive Psychology*. *3*, 382-407.