Supplementary File for "A Place-timed Petri Net-based Method to Avoid Deadlock and Conflict in Railway Networks"

The PN model of the network, i.e., (N_2, M_{20}) is given in Fig. 7. $F_{2006}[12]$ for (N_2, M_{20}) contains nine constraints:

- 1) $M(p_1) + M(p_{13}) + M(p_{15}) + M(p_{23}) \le 2$;
- 2) $M(p_2) + M(p_{12}) + M(p_{16}) + M(p_{22}) \le 2$;
- 3) $M(p_5) + M(p_9) \le 1$;
- 4) $M(p_6) + M(p_8) \le 1$;
- 5) $M(p_{17}) + M(p_{21}) \le 2$;
- 6) $M(p_{18}) + M(p_{20}) \le 1$;
- 7) $M(p_2) + M(p_{12}) + M(p_{16}) + M(p_{17}) + M(p_{21}) + M(p_{22}) \le 3$;
- 8) $M(p_5) + M(p_6) + M(p_7) + M(p_8) + M(p_9) + M(p_{10}) \le 1$;
- 9) $M(p_3) + M(p_{12}) + M(p_{17}) + M(p_{18}) + M(p_{19}) + M(p_{20}) + M(p_{21}) + M(p_{22}) \le 2$.

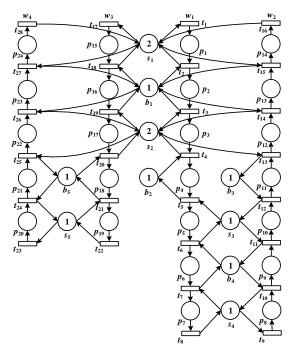


Fig. 7. PN of the railway network in [12].

The PN model of the network, i.e., (N_3, M_{30}) is given in Fig. 8, where s_1 corresponds to p_2 , b_1 corresponds to p_5 , s_2 corresponds to p_8 , b_2 corresponds to p_{11} , b_3 corresponds to p_{12} , s_3 corresponds to p_{15} , b_4 corresponds to p_{18} , and s_4 corresponds to p_{21} in the PN model in [14]. $G_{2008}[14]$ for (N_3, M_{30}) contains nine constraints:

- 1) $M(p_4) + M(p_9) \le 2$;
- 2) $M(p_{17}) + M(p_{22}) \le 2$;
- 3) $M(p_{14}) + M(p_{19}) \le 2$;
- 4) $M(p_{14}) + M(p_{22}) \le 3$;
- 5) $M(p_1) + M(p_6) \le 3$;
- 6) $M(p_1) + M(p_9) \le 4$;
- 7) $M(p_7) + M(p_{10}) + M(p_{12}) + M(p_{16}) \le 5$;
- 8) $M(p_4) + M(p_7) + M(p_9) + M(p_{10}) + M(p_{12}) + M(p_{16}) \le 6$;

9)
$$M(p_7) + M(p_{10}) + M(p_{12}) + M(p_{14}) + M(p_{16}) + M(p_{19}) \le 6;$$

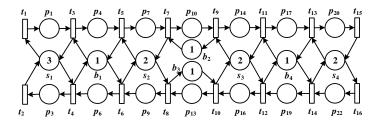


Fig. 8. PN of the railway network in [14].