## Supplementary File for "A Place-timed Petri Net-based Method to Avoid Deadlock and Conflict in Railway Networks"

The PN model of the network, i.e.,  $(N_2, M_{20})$  is given in Fig. 7.  $F_{2006}[12]$  for  $(N_2, M_{20})$  contains nine constraints:

- 1)  $M(p_1) + M(p_{13}) + M(p_{15}) + M(p_{23}) \le 2$ ;
- 2)  $M(p_2) + M(p_{12}) + M(p_{16}) + M(p_{22}) \le 2$ ;
- 3)  $M(p_5) + M(p_9) \le 1$ ;
- 4)  $M(p_6) + M(p_8) \le 1$ ;
- 5)  $M(p_{17}) + M(p_{21}) \le 2$ ;
- 6)  $M(p_{18}) + M(p_{20}) \le 1$ ;
- 7)  $M(p_2) + M(p_{12}) + M(p_{16}) + M(p_{17}) + M(p_{21}) + M(p_{22}) \le 3$ ;
- 8)  $M(p_5) + M(p_6) + M(p_7) + M(p_8) + M(p_9) + M(p_{10}) \le 1$ ;
- 9)  $M(p_3) + M(p_{12}) + M(p_{17}) + M(p_{18}) + M(p_{19}) + M(p_{20}) + M(p_{21}) + M(p_{22}) \le 2$ .

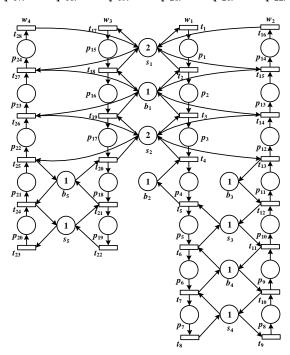


Fig. 7. PN of the railway network in [12].

The PN model of the network, i.e.,  $(N_3, M_{30})$  is given in Fig. 8, where  $s_1$  corresponds to  $p_2$ ,  $b_1$  corresponds to  $p_5$ ,  $s_2$  corresponds to  $p_8$ ,  $b_2$  corresponds to  $p_{11}$ ,  $b_3$  corresponds to  $p_{12}$ ,  $s_3$  corresponds to  $p_{15}$ ,  $b_4$  corresponds to  $p_{18}$ , and  $s_4$  corresponds to  $p_{21}$  in the PN model in [14].  $G_{2008}[14]$  for  $(N_3, M_{30})$  contains nine constraints:

- 1)  $M(p_4) + M(p_9) \le 2$ ;
- 2)  $M(p_{17}) + M(p_{22}) \le 2$ ;
- 3)  $M(p_{14}) + M(p_{19}) \le 2$ ;
- 4)  $M(p_{14}) + M(p_{22}) \le 3$ ;
- 5)  $M(p_1) + M(p_6) \le 3$ ;
- 6)  $M(p_1) + M(p_9) \le 4$ ;
- 7)  $M(p_7) + M(p_{10}) + M(p_{12}) + M(p_{16}) \le 5$ ;
- 8)  $M(p_4) + M(p_7) + M(p_9) + M(p_{10}) + M(p_{12}) + M(p_{16}) \le 6$ ;

9) 
$$M(p_7) + M(p_{10}) + M(p_{12}) + M(p_{14}) + M(p_{16}) + M(p_{19}) \le 6.$$

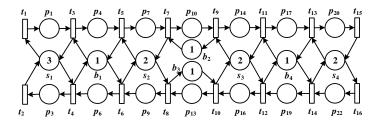


Fig. 8. PN of the railway network in [14].