

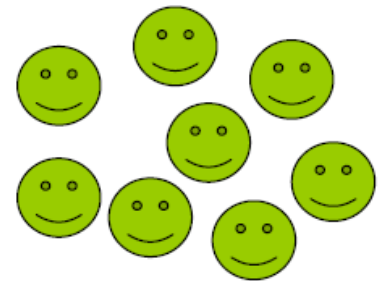
Molecular evolution: traditional tests of neutrality

Mutation+Selection=Evolution

Relative importance of each for maintaining
variation in population?

Early Criticism of Darwin

Blending inheritance, 'gemmules'



Fleeming Jenkin (1867):

$$\text{Var}[X(t+1)] = \frac{1}{2} \text{Var}[X(t)]$$

Mendelian Inheritance

published 1865-66, rediscovered 1900

Law of Segregation:

- allelic variation
- offspring receive 1 allele from each parent
- dominance/recessivity
- parental alleles 'segregate' to form gametes

Law of Independent Assortment

Simple case: no selection

The Hardy-Weinberg Law (1908)

Requires:

- infinite population size
- random mating
- non-overlapping generations
- no selection, mutation, or migration

The Hardy-Weinberg Law

Genotype:	AA	Aa	aa
Frequency at time 0:	u_0	v_0	w_0

$$u_0 + v_0 + w_0 = 1$$

$$\text{frequency of } A (p_0) = u_0 + v_0/2$$

$$\text{frequency of } a (q_0) = w_0 + v_0/2$$

$$p_0 + q_0 = 1$$

The Hardy-Weinberg Law

Genotype: AA Aa aa

Frequency at time 0: u_0 v_0 w_0

Mating Pair	Frequency	Offspring		
		AA	Aa	aa
$AA \times AA$	u_0^2	1	0	0
$AA \times Aa$	$u_0 v_0$	$\frac{1}{2}$	$\frac{1}{2}$	0
$Aa \times AA$	$u_0 v_0$	$\frac{1}{2}$	$\frac{1}{2}$	0
$Aa \times Aa$	v_0^2	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{1}{4}$

Frequency of AA in next generation: $u_1 = u_0^2 + u_0 v_0 + \frac{1}{4} v_0^2$
 $= (u_0 + v_0 / 2)^2$
 $= p_0^2$

The Hardy-Weinberg Law

If assumptions met:

- allele frequencies don't change
- after a single generation of random mating, genotype frequencies are:

$$u = p^2 \quad v = 2pq \quad w = q^2$$

- entire system characterized by one parameter (p)

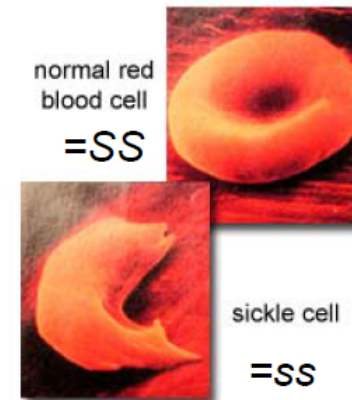
Deviation from expectations indicates failure of 1 or more assumptions—selection?

HW application: Sickle cell anemia

	Observed Counts	Expected Counts
SS	834	
Ss	161	$2pq * 1000 = 129$
ss	5	

$$p = \sqrt{0.834} = 0.91$$

$$q = \sqrt{0.005} = 0.071$$



Approach: Detect selection through comparison to neutral expectation

Kimura: neutral theory

Ewens: sampling formula

Coalescence

Neutral Theory History

- Motoo Kimura (1924-1994)
- 1968: a large proportion of genetic change is not driven by selection
- Adapted diffusion approximations to genetics
- Dealt with finite pops



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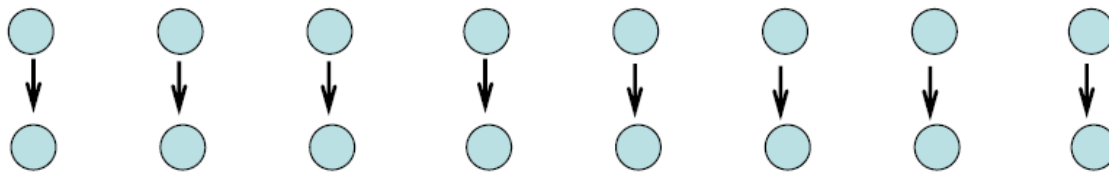
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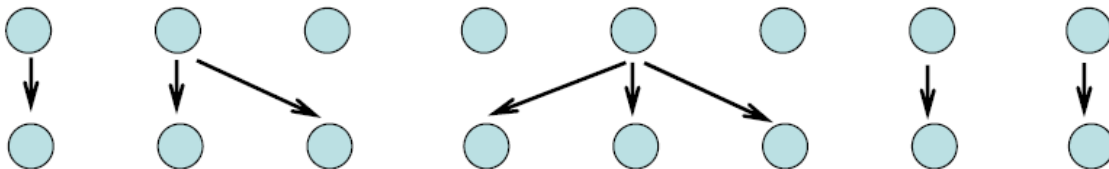
Kimura worked on a wide spectrum of theoretical population genetics problems, many of them in collaboration with **Takeo Maruyama**. He introduced the "**infinite alleles**" and "**infinite sites**" models for the study of **genetic drift**, both of which would be used widely as the field of **molecular evolution** grew alongside the number of available **peptide** and **genetic sequences**. He also created the "ladder model" that could be applied to **electrophoresis** studies where



Genetic Drift

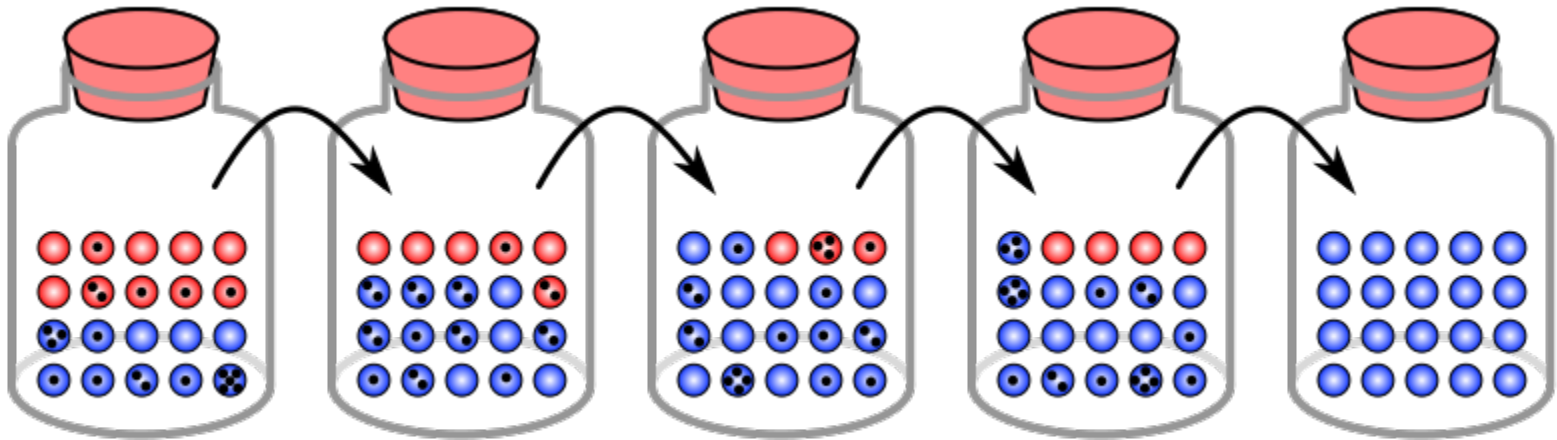


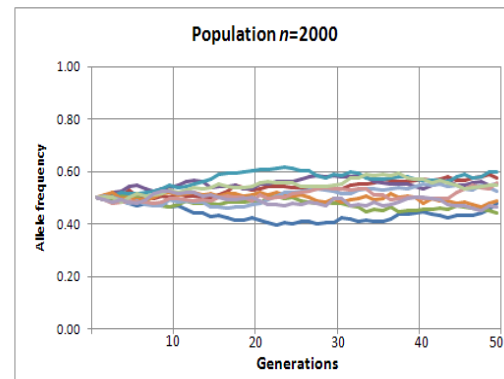
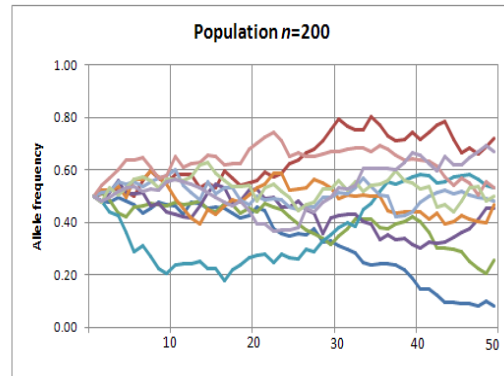
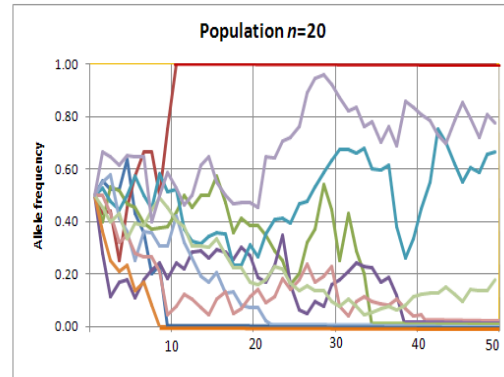
no drift
infinite pop



drift
finite pop

Genetic drift





Test of the evolution model

Rate-based selection metric:

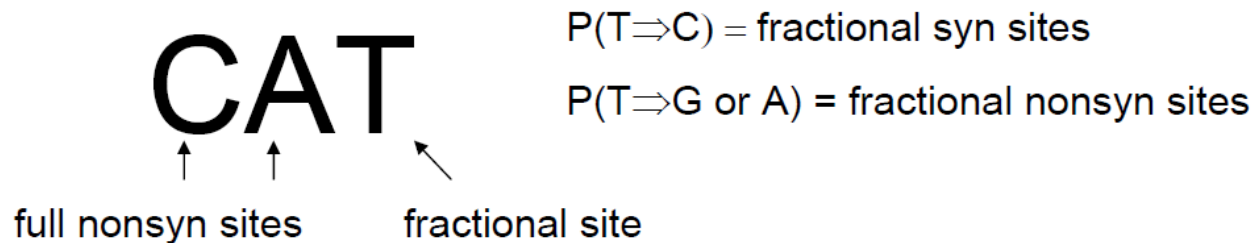
$$d_N/d_S$$

d_N = no. nonsynonymous changes/ no. nonsynonymous sites

d_S = no. synonymous changes/ no. synonymous sites

Counting codon 'sites' example: CAT

Histidine is encoded by only one other codon: CAC



Rate-based selection metric:

$$d_N/d_S$$

$d_N/d_S < 1$ purifying selection

$d_N/d_S = 1$ neutral expectation

$d_N/d_S > 1$ positive selection

Rate-based selection metric:

$$d_N/d_S$$

- Can be calculated using various methods
- Goldman & Yang implementation (PAML):

nucleotide changes modelled as continuous-time
Markov chain with state space = 61 codons

$$q_{ij} = \begin{cases} 0: & \text{if the two codons differ at } > 1 \text{ position} \\ \pi_j: & \text{synonymous transversion} \\ \kappa\pi_j: & \text{synonymous transition} \\ \omega\pi_j: & \text{nonsynonymous transversion} \\ \omega\kappa\pi_j: & \text{nonsynonymous transition} \end{cases}$$

