## **Problem Set 3**

## **Tsunami**

The open ocean propagation of tsunami waves is approximated by the long-wavelength, shallow-water equation:

$$\partial_t^2 P = \nabla \cdot (v^2 \nabla P) \tag{1}$$

$$= \partial_x v^2 \partial_x P + \partial_y v^2 \partial_y P + v^2 (\partial_x^2 P + \partial_y^2 P)$$
 (2)

where P=P(x,y,t) is the height of tsunami waves above sea level,  $v=\sqrt{gH(x,y)}$  the wave speed, g the gravity acceleration, H the ocean depth.

When the term  $v^2$  is not changing rapidly, an approximation form of the governing equation that will accurately predict the speed, dispersion and focusing of the waves is:

$$\partial_t^2 P = v^2 \, \nabla^2 P \tag{3}$$

Equation (3) is called 'homogeneous', since it assumes that  $v^2$  is constant, i.e., a homogeneous medium. Extra terms in equation (2) are called 'inhomogeneous'.

## **Problem:**

An example code is provided to you, which can solve the homogeneous equation to 2nd-order in space and time.

- (a) modify the code to (keep 2nd-order scheme in time) make it 4th-order in space
- (b) derive formula for the inhomogeneous terms, both in 2nd-order and 4th-order

## Additional information:

1. The C-code can be compiled with:

```
cc -o class_tsunami class_tsunami.c -lm (use 'gcc' instead of 'cc' on linux)
```

2. Then the code is executed by simply typing:

```
./class_tsunami
```

3. The output is in the file 'slice.out', which can be viewed in Matlab with the script 'class\_movie.m'