

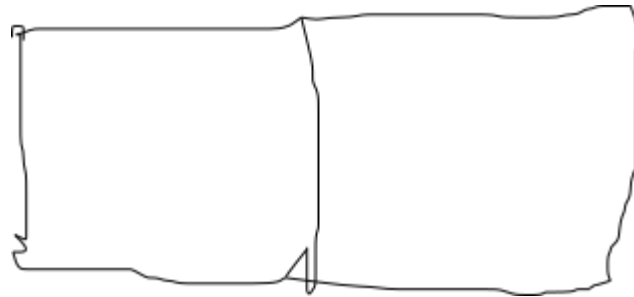
# COMP9020 - Assignment 2

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## Question 1

(a) For graph  $G = (E, V)$  as follows:



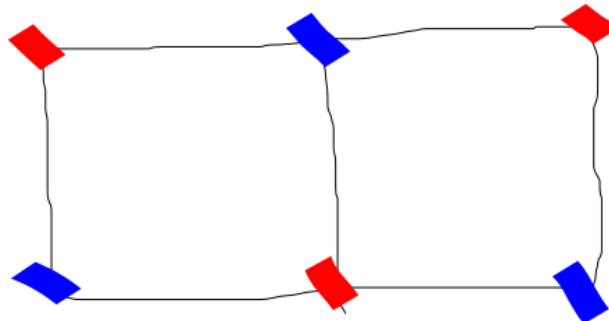
For every  $e = (v, w) \in E$

$$c(v) \neq c(w)$$

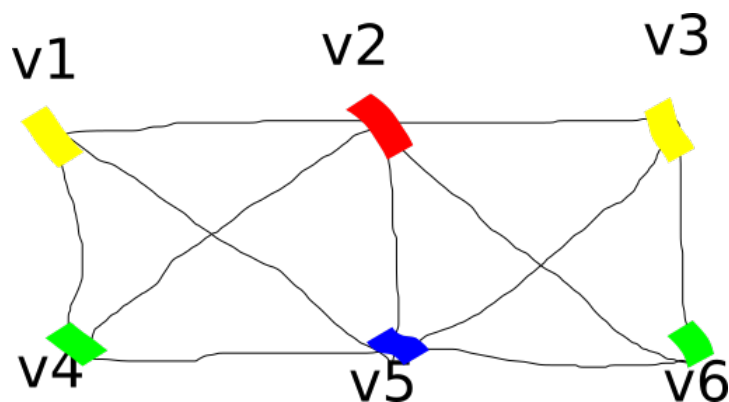
The minimum number of colors to sufficient effect such a mapping, denoted:

$$\chi(G)$$

(b) The minimum number of colors is 2, as follows:



(c) The connection of the graph changes, as follows:



Because  $v_2$  connect to  $v_3$ , so they must be different colours,  $c(v_2) \neq c(v_3)$   $v_2$  and  $v_3$  connect to all other vertex, so other vertex must use different colours other than  $c(v_2)$  and  $c(v_3)$

$$c(v_1) \neq c(v_2) \neq c(v_3)$$

also,  $v_1$  connect to  $v_4$ , so  $c(v_1) \neq c(v_4)$ , at lease we should use 4 different colors  
Because I can use 4 different colors as shows in graph, therefore:

$$\chi(G) = 4$$

## Question 2

- (a)
- (b)
- (c)