

# CS 418: Interactive Computer Graphics

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## Texture Filtering

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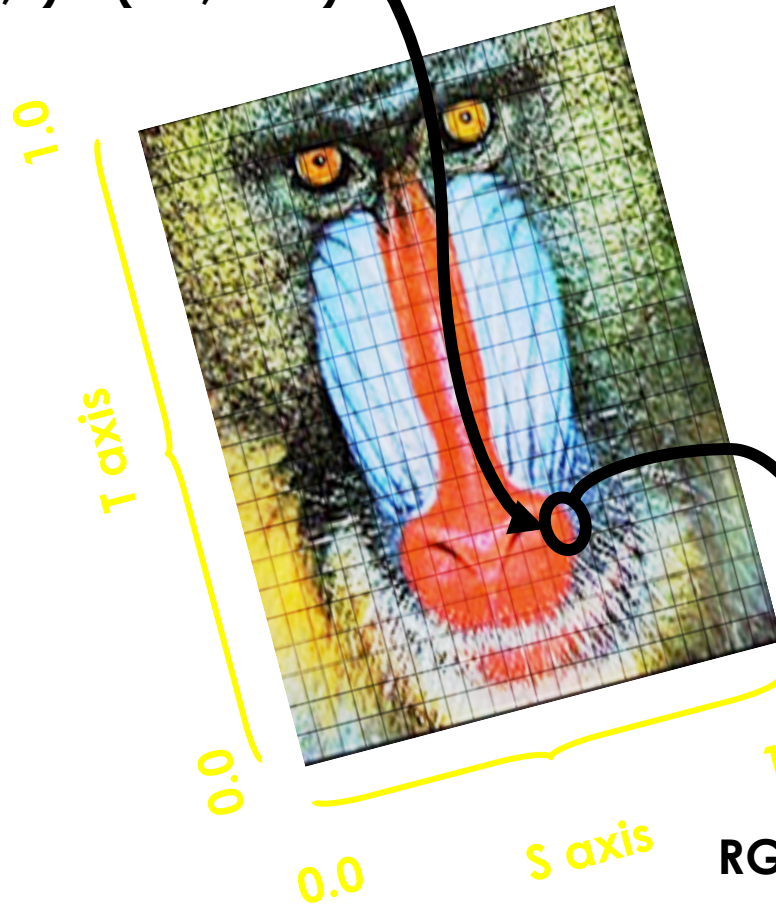
# A note about coordinates...

- ▣ We're using the following convention:
- ▣  $(u,v)$  are the texture coordinates assigned in the parametric space with  $u$  and  $v$  in  $[0,1]$
- ▣  $(s,t)$  are the texel coordinates in a texture
- ▣ ....some people use  $(s,t)$  to denote the parametric coordinates...

# A Texture Fetch Simplified

- Seems pretty simple...
- Given
  1. An image
  2. A position
- Return the color of image at position

Fetch at  
 $(u,v) = (0.6, 0.25)$



RGBA Result is  
0.95,0.4,0.24,1.0

# Filtering Textures

- ▣ Magnification occurs when we have more fragments than texels
- ▣ What are two filters we can use to map texels to fragments?
- ▣ If we are magnifying a texture, what is the maximum number of texels that must be fetched per fragment?

# Filtering Textures

- Magnification occurs when we have more fragments than texels
- What are two filters we can use to map texels to fragments?
  - Nearest Neighbor
  - Bilinear Filtering
- If we are magnifying a texture, what is the maximum number of texels that must be fetched per fragment?
  - Four for bilinear filtering.

# Filtering Textures

- ▣ Minification occurs when we have more texels than fragments
- ▣ Using NN or Bilinear Filtering can lead to aliasing
- ▣ Why?
- ▣ What would a better strategy be?
- ▣ What is the maximum number of texels fetched per fragment?

# Filtering Textures

- Minification occurs when we have more texels than fragments
- Using NN or Bilinear Filtering can lead to aliasing
- Why?
  - Sparse sampling will can cause us to miss featues
  - e.g. a checkerboard pattern could be turned into solid color
- What would a better strategy be?
  - Average all of the texels that map into a fragment
- What is the maximum number of texels fetched per fragment?
  - The entire texture

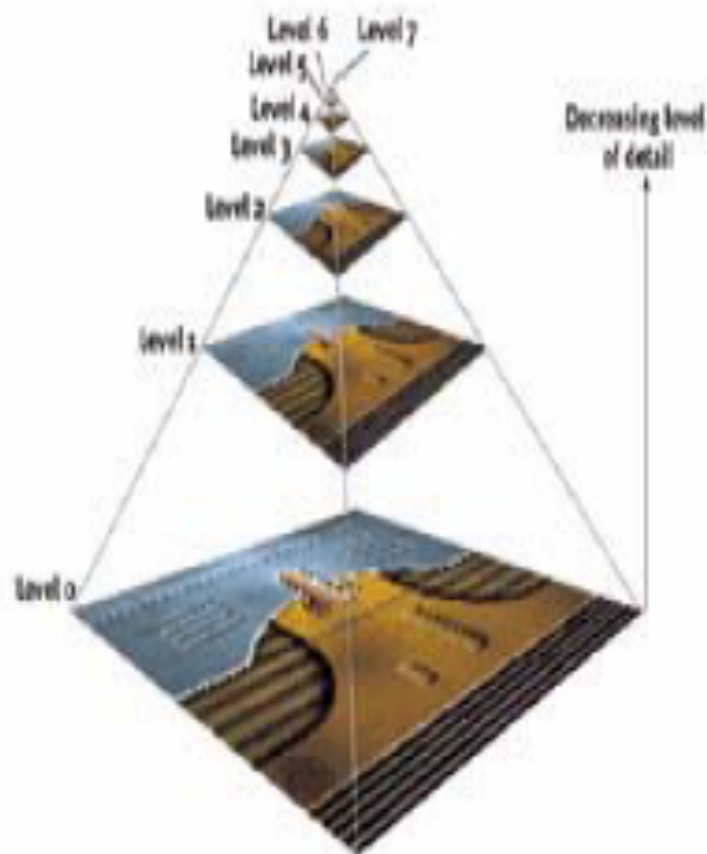


# Mipmapping

- Mipmapping is a method of pre-filtering a texture for minification
  - History: 1983 Lance Williams introduced the word “mipmap” in his paper “Pyramidal Parametrics”
  - mip = “multum in parvo”.... latin: many things in small place(?)
- We generate a pyramid of textures
  - Bottom-level is the original texture
  - Each subsequent level reduces the resolution by  $\frac{1}{4}$  (by  $\frac{1}{2}$  along s and t)



# Mipmapping



# Pre-filtered Image Versions

- Base texture image is say 256x256
  - Then down-sample 128x128, 64x64, 32x32, all the way down to 1x1



**Trick:** When sampling the texture, pixel the mipmap level with the closest mapping of pixel to texel size

**Why?** Hardware wants to sample just a small (1 to 8) number of samples for every fetch—and want constant time access

# Creating a Mipmap

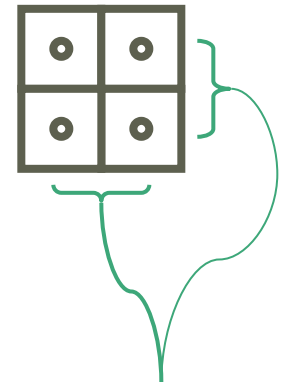
- In WebGL you can manually generate and upload a mipmap
- Or you can have WebGL generate it for you

```
gl.generateMipmap(GL_TEXTURE_2d)
```

- Usually, bilinear filtering is used to minify each level
- ...but that's up to the implementation of the library

# Mipmap Level-of-detail Selection

- Hardware uses 2x2 pixel entities
  - Typically called quad-pixels or just *quad*
  - Finite difference with neighbors to get change in  $u$  and  $v$  with respect to window space
    - Approximation to  $\partial u/\partial x, \partial u/\partial y, \partial v/\partial x, \partial v/\partial y$
    - Means 4 subtractions per quad (1 per pixel)
- Now compute approximation to gradient length
  - $p = \max(\text{sqrt}((\partial u/\partial x)^2 + (\partial u/\partial y)^2), \text{sqrt}((\partial v/\partial x)^2 + (\partial v/\partial y)^2))$



one-pixel separation

# Level-of-detail Bias and Clamping

- Convert p length to level-of-detail and apply LOD bias
  - $\lambda = \log_2(p) + \text{lodBias}$
- Now clamp  $\lambda$  to valid LOD range
  - $\lambda' = \max(\text{minLOD}, \min(\text{maxLOD}, \lambda))$

# Determine Mipmap Levels

- ▣ Determine lower and upper mipmap levels
  - ▣  $b = \text{floor}(\lambda')$  is bottom mipmap level
  - ▣  $t = \text{floor}(\lambda' + 1)$  is top mipmap level
- ▣ Determine filter weight between levels
  - ▣  $w = \text{frac}(\lambda')$  is filter weight

# WebGL Computing a Color from a Mipmap

WebGL offers 6 ways to generate a color from a mipmap

NEAREST = choose 1 pixel from the biggest mip

LINEAR = choose 4 pixels from the biggest mip and blend them

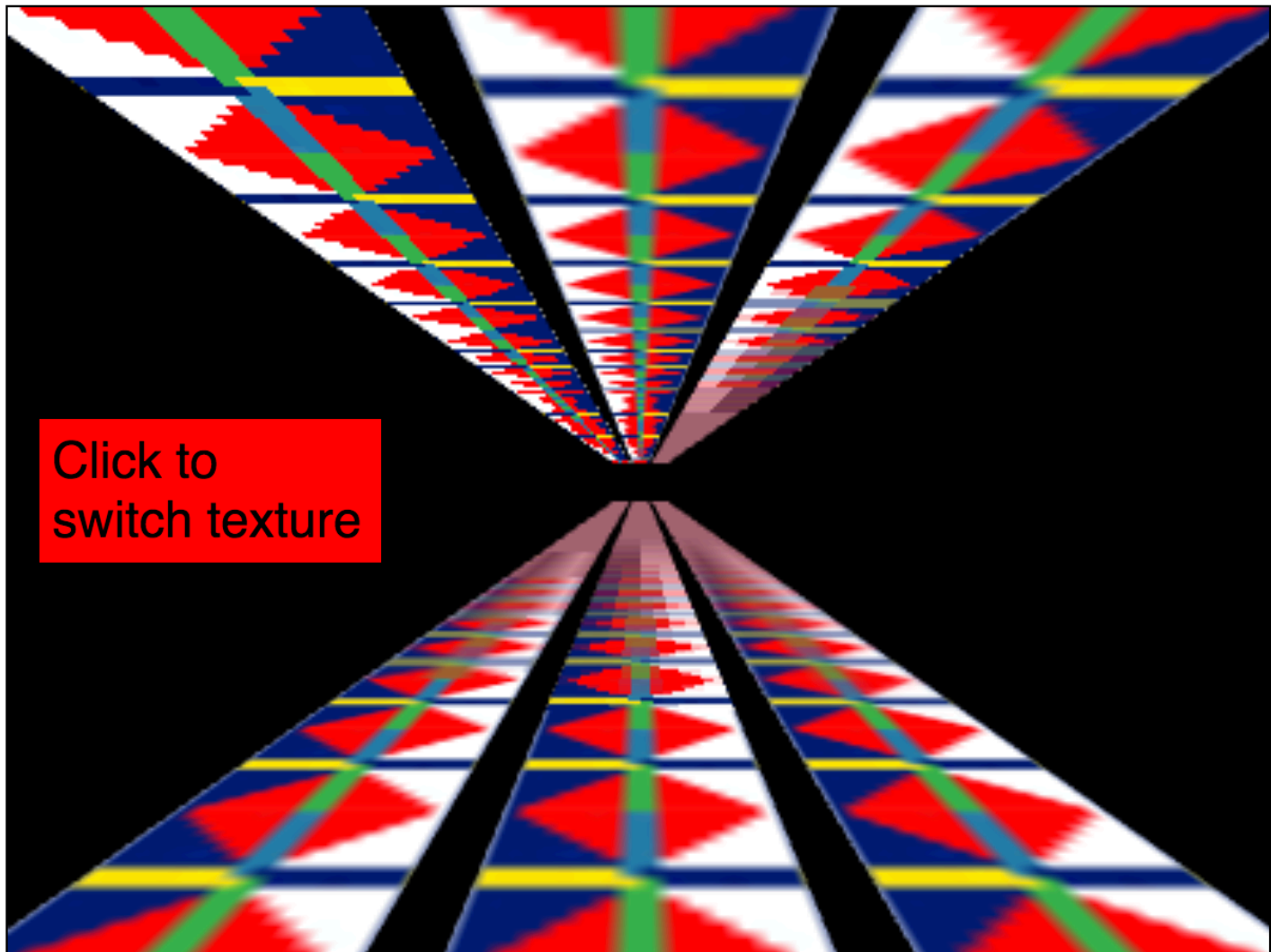
NEAREST\_MIPMAP\_NEAREST = choose the best mip,  
then pick one pixel from that mip

LINEAR\_MIPMAP\_NEAREST = choose the best mip,  
then blend 4 pixels from that mip

NEAREST\_MIPMAP\_LINEAR = choose the best 2 mips,  
choose 1 pixel from each, blend them

LINEAR\_MIPMAP\_LINEAR = choose the best 2 mips.  
choose 4 pixels from each, blend them

# Mipmap Texture Filtering



Click to  
switch texture



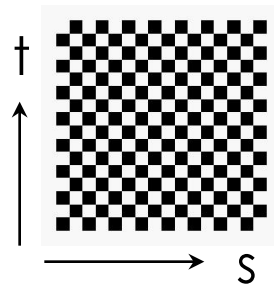
# WebGL: Highest Quality Filtering

```
gl.texParameteri(gl.TEXTURE_2D, gl.TEXTURE_MIN_FILTER, gl.LINEAR_MIPMAP_LINEAR);  
gl.texParameteri(gl.TEXTURE_2D, gl.TEXTURE_MAG_FILTER, gl.LINEAR);
```

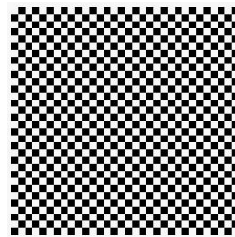
Although some WebGL implementations may now support anisotropic texture filtering...which is even better

# Wrap Modes

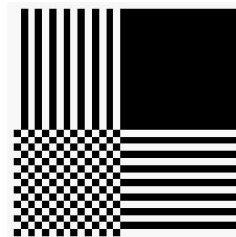
- Texture image is defined in  $[0..1] \times [0..1]$  region
  - What happens outside that region?
  - Texture wrap modes say



texture



GL\_REPEAT  
wrapping



GL\_CLAMP  
wrapping

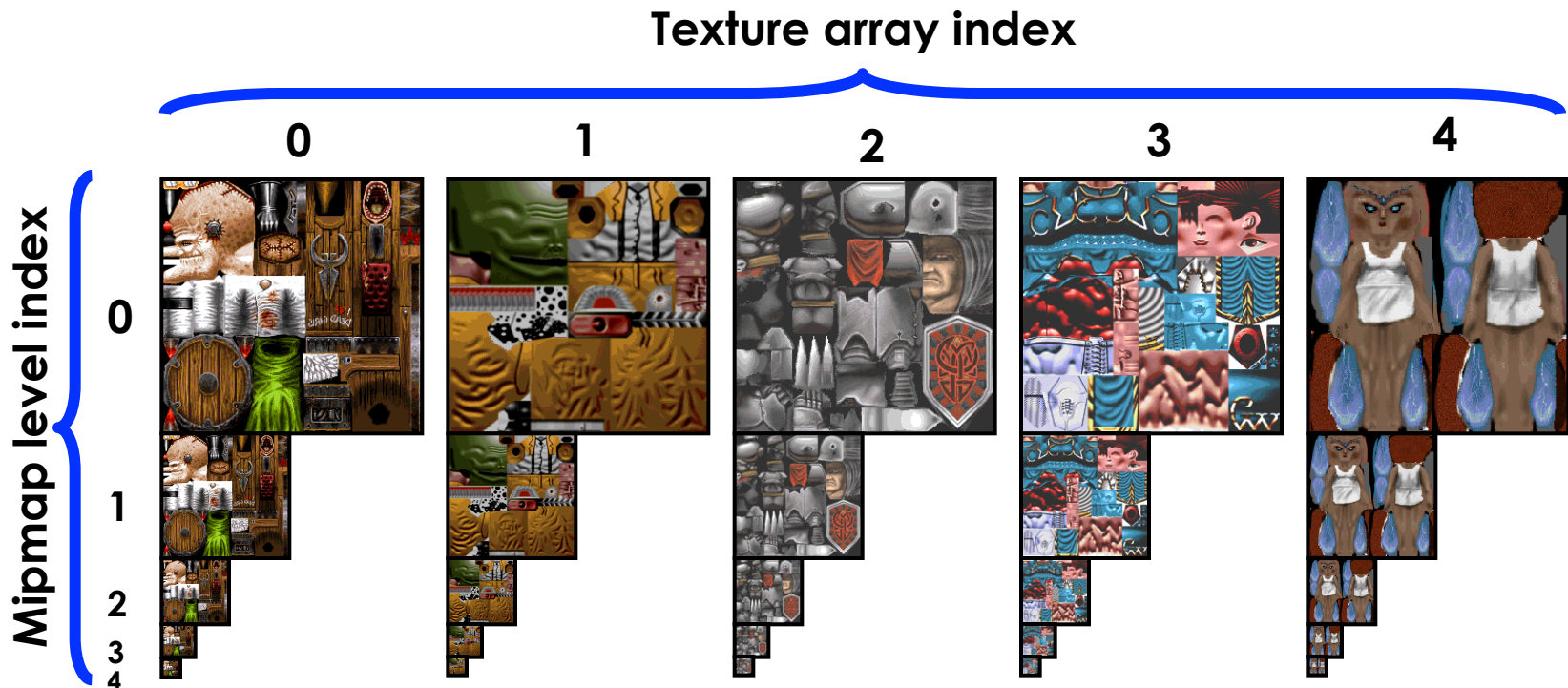
# WebGL: Non-power of 2 textures

- ▣ You should use textures that are  $2^k \times 2^k$
- ▣ You can use textures that are not powers of two
- ▣ but must
  - ▣ set the wrap mode to CLAMP\_TO\_EDGE
  - ▣ turn off mipmapping by setting filtering to LINEAR or NEAREST...

# Texture Arrays

## ▣ Multiple skins packed in texture array

- ▣ Motivation: binding to one multi-skin texture array avoids texture bind per object



# Anisotropic Texture Filtering

- ▣ Standard (isotropic) mipmap LOD selection
  - ▣ Uses magnitude of texture coordinate gradient (not direction)
  - ▣ Tends to spread blurring at shallow viewing angles
- ▣ Anisotropic texture filtering considers gradients direction
  - ▣ Minimizes blurring



Isotropic



Anisotropic

# Texturing in WebGL: Vertex Shader

Need to alter the vertex shader to pass-through texture coordinates

```
attribute vec4 a_position;  
attribute vec2 a_texcoord;  
uniform mat4 uMVmatrix;  
uniform mat4 uPMatrix;  
varying vec2 v_texcoord;  
  
void main() {  
    gl_Position = uPMatrix * uMVmatrix * a_position;  
    // Pass the texcoord to the fragment shader.  
    v_texcoord = a_texcoord;  
}
```

# Texturing in WebGL: Fragment Shader

Need to alter the fragment shader to fetch colors from textures

```
precision mediump float;

// Passed in from the vertex shader.
varying vec2 v_texcoord;

// The texture.
uniform sampler2D u_texture;

void main() {
    gl_FragColor = texture2D(u_texture, v_texcoord);
}
```