

Linear Interpolation and Data Representation

1. Trilinear Interpolation

Suppose you have the following sampled data.

$f(0,0,0) = 3$	$f(0,0,1) = 2$
$f(1,0,0) = 19$	$f(1,0,1) = 10$
$f(0,1,0) = 4$	$f(0,1,1) = 24$
$f(1,1,0) = 8$	$f(1,1,1) = 0$

Using trilinear interpolation, what is the value of $f(1/4, 1/2, 4/5)$?

2. Barycentric Coordinates

Assuming the following points are given in barycentric coordinates using the three vertices of a triangle Δabc , which point lies on an edge of the triangle but not at a corner?

- a. $(0,0,1)$
- b. $(-1/2, 3/2, 0)$
- c. $(1/3, 2/3, 0)$
- d. $(1/2, 1/4, 1/4)$

3. Structured Grid

You have sampled scalar data at the grid vertices of a structured grid in 3-dimensional Euclidean space (\mathbb{R}^3). The grid has n cells along each axis for a total of n^3 cells. How many bytes of storage will the data structure require to specify the grid and data? Assume that all numbers, integer or floating point, require 4 bytes.