Supplementary Material for 'A dynamic multi-objective evolutionary algorithm with variable stepsize and dual prediction strategies'

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This paper provides supplementary descriptions of the experimental data in the paper 'A dynamic multiobjective evolutionary algorithm with variable stepsize and dual prediction strategies'. Figure S-I illustrates the convergence curves of the IGD values for various test instances of the FDA, dMOP, and F test suites when $n_t = 10$ and $\tau_t = 10$. Figure S-II illustrates the convergence curves of the IGD values for various test instances of the DF test suite when $n_t = 10$ and $\tau_t = 10$. Table S-I and Table S-II describe the statistics of the MIGD values and MHV values obtained by VSDPS and its three variants on FDA, dMOP, F and DF test suites. Table S-III and Table S-IV describe the statistics of the MIGD values and MHV values obtained by VSDPS and its five ratios of dual prediction strategies related variants on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$. Table S-V and Table S-VI present the statistics of the MIGD values and MHV values acquired by VSDPS and its four stepsize related variants on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$. Table S-VII and Table S-VIII present the statistics of the MIGD values and MHV values acquired by VSDPS and different values of control number in static optimization on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

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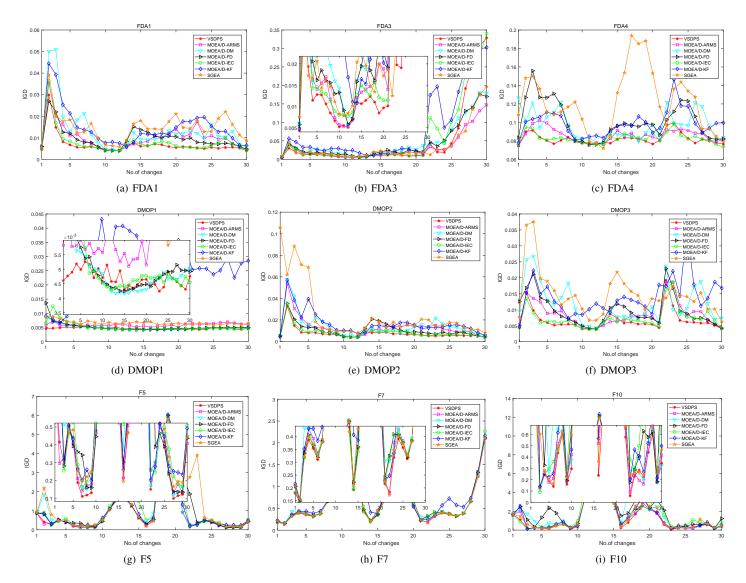


Figure S - I. The convergence curves of the IGD values for several test instances of the FDA, dMOP, and F test suites when $n_t = 10$ and $\tau_t = 10$.

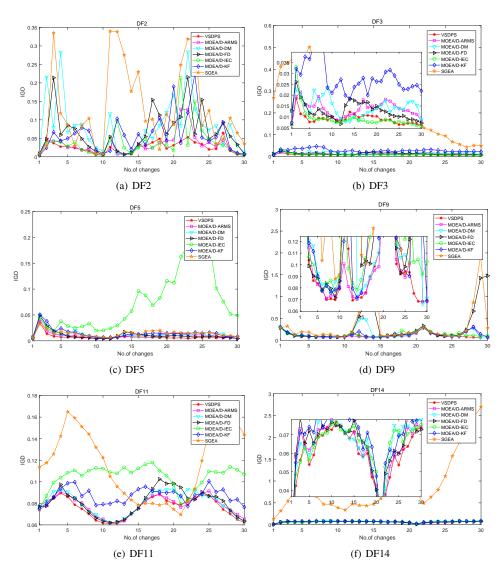


Figure S - II. The convergence curves of the IGD values for several test instances of the DF test suite when $n_t = 10$ and $\tau_t = 10$.

Table S - I. The statistics of the MIGD values obtained by VSDPS and its three variants were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-S	VSDPS-P	VSDPS-O	VSDPS
FDA1	(10,10)	9.8069e-3 (6.07e-4)-	7.3270e-3 (2.29e-4)-	7.4060e-3 (4.13e-4) -	6.7466e-3 (6.36e-4)
FDA2	(10,10)	7.8205e-3 (2.63e-4)-	5.3950e-3 (4.99e-5) +	5.9032e-3 (7.62e-5)-	5.8454e-3 (8.04e-4)
FDA3	(10,10)	5.2826e-2 (2.10e-3) -	4.4736e-2 (3.01e-3) +	5.5682e-2 (1.81e-3)-	4.8868e-2 (3.00e-3)
FDA4	(10,10)	9.8152e-2 (1.61e-3) -	8.3695e-2 (9.21e-4) =	8.4246e-2 (1.19e-3) =	8.3937e-2 (1.89e-3)
FDA5	(10,10)	2.9791e-1 (4.03e-2) - 1.7818e-1 (5.00e-3) + 2.7176e-1 (2.49e-2)-		2.2040e-1 (1.61e-2)	
DMOP1	(10,10)	1.1542e-2 (8.75e-4) -	4.8853e-3 (9.42e-5) -	5.5040e-3 (1.26e-4) -	4.7554e-3 (1.24e-4)
DMOP2	(10,10)	1.2369e-2 (9.41e-4) -	8.7618e-3 (4.09e-4) -	8.8833e-3 (5.72e-4) -	7.9824e-3 (4.23e-4)
DMOP3	(10,10)	1.0374e-2 (9.77e-4) -	7.5255e-3 (4.00e-4) =	7.1657e-3 (2.55e-4) =	7.3219e-3 (4.66e-4)
F5	(10,10)	9.1383e-1 (2.29e-2) +	1.2916e+0 (2.92e-1) -	9.4482e-1 (2.07e-2) -	9.1794e-1 (1.29e-2)
F6	(10,10)	6.1708e-1 (4.23e-3) =	6.9168e-1 (3.72e-2) -	6.2656e-1 (6.27e-3) -	6.1917e-1 (6.93e-3)
F7	(10,10)	7.2865e-1 (4.07e-3) -	7.3666e-1 (5.31e-3) -	7.3213e-1 (6.35e-3) -	7.2383e-1 (7.29e-3)
F8	(10,10)	1.1856e-1 (4.39e-3) -	8.8957e-2 (1.09e-3) +	9.1866e-2 (1.61e-3) =	9.2819e-2 (2.30e-3)
F9	(10,10)	4.8395e-1 (1.28e-1) =	1.4355e+0 (3.48e-1) -	5.5750e-1 (1.61e-1) =	5.4958e-1 (1.55e-1)
F10	(10,10)	1.8998e+0 (5.54e-2) -	2.0314e+0 (7.94e-2) -	1.8879e+0 (4.07e-2) -	1.8220e+0 (2.75e-2)
DF1	(10,10)	1.2120e-2 (1.34e-3) -	9.0115e-3 (4.12e-4) -	8.5278e-3 (5.47e-4) =	8.6641e-3 (4.25e-4)
DF2	(10,10)	3.4937e-2 (4.42e-3) -	4.4156e-2 (4.50e-3) -	4.5032e-2 (5.38e-3) -	2.9877e-2 (5.71e-3)
DF3	(10,10)	1.8176e-2 (8.85e-4) -	1.1288e-2 (4.17e-4) -	9.5954e-3 (3.38e-4) -	9.0387e-3 (3.37e-4)
DF4	(10,10)	8.1510e-2 (1.89e-3) =	8.1795e-2 (8.22e-4) =	8.3306e-2 (8.80e-4) -	8.2237e-2 (5.71e-4)
DF5	(10,10)	1.1117e-2 (4.83e-4) -	7.5300e-3 (2.69e-4) =	8.4010e-3 (3.65e-4) -	7.4775e-3 (3.14e-4)
DF6	(10,10)	2.2599e+0 (1.72e+0) +	4.5427e+0 (9.60e-1) =	1.9749e+0 (1.37e+0) +	4.2883e+0 (6.12e-1)
DF7	(10,10)	3.7361e-2 (3.26e-2) =	7.4027e-2 (4.60e-2) -	3.7477e-2 (3.09e-2) =	3.6343e-2 (2.98e-2)
DF8	(10,10)	1.5695e-1 (6.54e-3) -	1.3124e-1 (1.36e-3) +	1.3048e-1 (2.04e-3) +	1.3623e-1 (9.32e-3)
DF9	(10,10)	2.1002e+0 (8.97e-3) =	2.1164e+0 (1.88e-2) -	2.0919e+0 (4.88e-3) +	2.0982e+0 (8.87e-3)
DF10	(10,10)	2.1742e-1 (1.05e-2) -	1.8564e-1 (1.97e-2) =	1.9140e-1 (1.41e-2) -	1.8876e-1 (2.88e-2)
DF11	(10,10)	8.3012e-2 (8.93e-4) -	7.5338e-2 (5.24e-4) +	7.6617e-2 (3.78e-4) +	7.7054e-2 (1.79e-3)
DF12	(10,10)	2.8315e-1 (2.48e-3) -	2.7981e-1 (1.21e-3) +	2.7847e-1 (1.22e-3) +	2.8193e-1 (4.00e-3)
DF13	(10,10)	3.0499e-1 (6.18e-3) +	3.2511e-1 (2.75e-3) -	3.1946e-1 (3.63e-3) -	3.1168e-1 (3.14e-3)
DF14	(10,10)	6.4171e-2 (9.81e-4) -	5.8366e-2 (4.23e-4) +	5.9129e-2 (5.37e-4) =	5.8892e-2 (8.52e-4)
+/-/	/=	3/20/5	8/14/6	5/16/7	

Table S - II. The statistics of the MHV values obtained by VSDPS and its three variants were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-S	VSDPS-P	VSDPS-O	VSDPS
FDA1	(10,10)	7.0981e-1 (8.30e-4) -	7.1400e-1 (3.58e-4) -	7.1366e-1 (6.11e-4) -	7.1491e-1 (3.78e-4)
FDA2	(10,10)	5.2552e-1 (4.33e-4) -	5.2873e-1 (1.17e-4) +	5.2790e-1 (1.34e-4) -	5.2828e-1 (1.40e-4)
FDA3	(10,10)	5.4333e-1 (2.12e-3)-	5.5130e-1 (3.71e-3) +	5.4159e-1 (1.59e-3) -	5.4717e-1 (1.65e-3)
FDA4	(10,10)	4.7189e-1 (7.17e-3) -	5.1400e-1 (1.59e-3) =	5.0755e-1 (2.61e-3) -	5.1237e-1 (2.52e-3)
FDA5	(10,10)	4.6653e-1 (1.26e-2) -	5.1806e-1 (1.66e-3) +	4.9038e-1 (5.55e-3) -	5.0642e-1 (3.73e-3)
DMOP1	(10,10)	5.1284e-1 (1.85e-3) -	5.2499e-1 (2.30e-4) -	5.2376e-1 (2.60e-4) -	5.2518e-1 (2.13e-4)
DMOP2	(10,10)	5.1219e-1 (1.84e-3) -	5.1847e-1 (6.38e-4) -	5.1803e-1 (9.08e-4) -	5.1963e-1 (4.96e-4)
DMOP3	(10,10)	7.0969e-1 (1.31e-3) -	7.1371e-1 (4.61e-4) =	7.1404e-1 (3.95e-4) =	7.1397e-1 (7.41e-4)
F5	(10,10)	3.0034e-1 (1.13e-2) =	1.7963e-1 (2.53e-2) -	2.6812e-1 (1.13e-2) -	3.0041e-1 (9.60e-3)
F6	(10,10)	2.5522e-1 (2.86e-3) =	1.9777e-1 (1.10e-2) -	2.4661e-1 (5.71e-3) -	2.5434e-1 (3.65e-3)
F7	(10,10)	2.2515e-1 (2.17e-3) -	2.0653e-1 (5.15e-3) -	2.1963e-1 (1.64e-3) -	2.2710e-1 (1.65e-3)
F8	(10,10)	4.3203e-1 (6.21e-3) -	4.9423e-1 (2.22e-3) +	4.8635e-1 (3.30e-3) -	4.8724e-1 (2.46e-3)
F9	(10,10)	3.3572e-1 (2.32e-2) =	1.6402e-1 (3.17e-2) -	3.1910e-1 (1.64e-2) -	3.3623e-1 (1.82e-2)
F10	(10,10)	2.4203e-1 (9.57e-3) =	1.7950e-1 (1.48e-2) -	2.1326e-1 (1.63e-2) -	2.4701e-1 (1.15e-2)
DF1	(10,10)	5.1225e-1 (1.83e-3) -	5.1835e-1 (6.81e-4) -	5.1864e-1 (8.84e-4) =	5.1904e-1 (7.97e-4)
DF2	(10,10)	6.7642e-1 (5.62e-3) -	6.7148e-1 (6.54e-3) -	6.6739e-1 (3.86e-3) -	6.8351e-1 (3.51e-3)
DF3	(10,10)	4.7101e-1 (1.42e-3) -	4.7981e-1 (2.49e-3) -	4.8389e-1 (5.88e-4) -	4.8465e-1 (4.36e-4)
DF4	(10,10)	2.8345e-1 (1.15e-4) -	2.8434e-1 (4.95e-5) -	2.8393e-1 (7.99e-5) -	2.8442e-1 (6.12e-5)
DF5	(10,10)	1.2632e-1 (4.41e-4) -	1.2725e-1 (2.28e-4) =	1.2697e-1 (3.24e-4) -	1.2720e-1 (2.65e-4)
DF6	(10,10)	4.3347e-1 (1.60e-1) +	1.0120e-1 (5.28e-2) -	4.0810e-1 (1.57e-1) +	2.2196e-1 (7.12e-2)
DF7	(10,10)	1.4914e-1 (4.32e-3) =	1.4592e-1 (4.55e-3) -	1.5017e-1 (3.41e-3) =	1.5005e-1 (3.70e-3)
DF8	(10,10)	7.9356e-2 (3.74e-4) -	8.0848e-2 (1.07e-4) +	8.0874e-2 (8.95e-5) +	8.0692e-2 (1.38e-4)
DF9	(10,10)	3.9743e-2 (2.50e-2) =	4.1644e-2 (2.26e-2) =	3.1960e-2 (1.51e-3) =	4.0221e-2 (2.18e-2)
DF10	(10,10)	4.6679e-1 (1.09e-2) -	5.9859e-1 (2.48e-2) +	5.3418e-1 (1.55e-2) -	5.6423e-1 (3.33e-2)
DF11	(10,10)	2.8091e-1 (1.03e-3) -	2.8894e-1 (4.09e-4) =	2.8768e-1 (5.24e-4) -	2.8880e-1 (5.41e-4)
DF12	(10,10)	8.9467e-1 (1.81e-3) -	9.0481e-1 (9.87e-4) +	9.0391e-1 (4.60e-4) =	9.0370e-1 (1.05e-3)
DF13	(10,10)	4.5307e-1 (1.80e-2) -	5.6563e-1 (6.12e-3) +	5.2753e-1 (7.95e-3) -	5.5899e-1 (4.60e-3)
DF14	(10,10)	5.6538e-1 (2.10e-3) -	5.8168e-1 (7.91e-4) -	5.7808e-1 (1.06e-3) -	5.8230e-1 (1.15e-3)
+/-/	/=	1/21/6	8/15/5	2/21/5	

Table S - III. The statistics of the MIGD values obtained by VSDPS and its five ratios of dual prediction strategies related variants were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-P1	VSDPS-P2	VSDPS-P3	VSDPS-P4	VSDPS-P5	VSDPS
FDA1	(10,10)	7.5599e-3 (1.25e-3) -	6.9612e-3 (4.27e-4) -	6.8171e-3 (4.07e-4) =	6.7917e-3 (4.64e-4) =	6.7173e-3 (2.76e-4) =	6.7257e-3 (3.34e-4)
FDA2	(10,10)	5.9296e-3 (9.43e-4) -	5.7089e-3 (5.81e-4) =	5.5445e-3 (3.21e-4) +	5.3869e-3 (9.09e-5) +	5.3737e-3 (6.88e-5) +	5.6014e-3 (1.40e-4)
FDA3	(10,10)	5.3480e-2 (2.88e-3) -	5.3475e-2 (2.36e-3) -	5.3727e-2 (2.41e-3) -	5.3888e-2 (2.49e-3) -	5.3572e-2 (3.58e-3) -	5.1836e-2 (2.27e-3)
FDA4	(10,10)	8.5351e-2 (2.97e-3) =	8.4186e-2 (1.31e-3) =	8.4278e-2 (1.24e-3) =	8.3836e-2 (1.10e-3) =	8.4169e-2 (1.52e-3) =	8.3918e-2 (1.16e-3)
FDA5	(10,10)	2.3134e-1 (2.28e-2) =	2.3203e-1 (2.55e-2) =	2.2079e-1 (1.49e-2) =	2.2228e-1 (1.52e-2) =	2.1878e-1 (1.44e-2) =	2.2695e-1 (2.12e-2)
DMOP1	(10,10)	5.0144e-3 (1.06e-3) =	4.6410e-3 (4.72e-4) =	4.5236e-3 (2.80e-4) =	4.3646e-3 (7.83e-5) +	4.3468e-3 (4.47e-5) +	4.6079e-3 (1.69e-4)
DMOP2	(10,10)	9.0302e-3 (1.61e-3) -	8.2605e-3 (6.31e-4) -	8.0609e-3 (4.79e-4) =	7.8924e-3 (4.59e-4) =	8.1608e-3 (5.63e-4) =	7.8973e-3 (4.27e-4)
DMOP3	(10,10)	8.3378e-3 (9.86e-4) -	7.8019e-3 (5.92e-4) -	7.4452e-3 (4.17e-4) =	7.6905e-3 (5.75e-4) =	7.6809e-3 (6.02e-4) =	7.4214e-3 (4.85e-4)
F5	(10,10)	1.1203e+0 (2.34e-1) -	1.0701e+0 (1.49e-1) -	1.0658e+0 (1.59e-1) -	1.0811e+0 (1.77e-1) -	1.1430e+0 (1.73e-1) -	9.6233e-1 (1.03e-1)
F6	(10,10)	6.3446e-1 (1.98e-2) -	6.4064e-1 (3.60e-2) -	6.3510e-1 (1.71e-2) -	6.3393e-1 (2.13e-2) -	6.4870e-1 (1.82e-2) -	6.2297e-1 (1.80e-2)
F7	(10,10)	7.2640e-1 (7.20e-3) -	7.2548e-1 (6.27e-3) -	7.2540e-1 (8.02e-3) =	7.2619e-1 (5.78e-3) -	7.2811e-1 (5.21e-3) -	7.2271e-1 (8.73e-3)
F8	(10,10)	9.1818e-2 (8.56e-3) =	9.0822e-2 (6.79e-3) =	9.0314e-2 (6.84e-3) =	8.6626e-2 (1.83e-3) +	8.6090e-2 (1.20e-3) +	9.0036e-2 (2.64e-3)
F9	(10,10)	8.4155e-1 (3.33e-1) -	7.9601e-1 (2.16e-1) -	8.1103e-1 (2.61e-1) -	8.9625e-1 (2.74e-1) -	8.4651e-1 (2.25e-1) -	6.6372e-1 (2.42e-1)
F10	(10,10)	1.9704e+0 (1.20e-1) -	2.0045e+0 (1.41e-1) -	2.0051e+0 (1.54e-1) -	1.9762e+0 (1.13e-1) -	2.0524e+0 (6.73e-2) -	1.8849e+0 (1.20e-1)
DF1	(10,10)	8.8066e-3 (4.28e-4) =	9.1366e-3 (4.97e-4) -	8.6219e-3 (5.61e-4) =	8.5390e-3 (5.00e-4) =	1.1096e-2 (6.38e-4) -	8.6283e-3 (5.17e-4)
DF2	(10,10)	2.9131e-2 (4.53e-3) =	2.8883e-2 (4.23e-3) =	2.8438e-2 (4.73e-3) =	2.7187e-2 (2.85e-3) =	2.9845e-2 (4.96e-3) =	2.8284e-2 (4.80e-3)
DF3	(10,10)	8.4546e-3 (3.03e-4) -	1.0725e-2 (3.08e-4) -	9.8366e-3 (3.79e-4) -	8.5578e-3 (2.63e-4) -	1.3421e-2 (5.41e-4) -	8.1299e-3 (2.08e-4)
DF4	(10,10)	8.1826e-2 (6.76e-4) =	8.2521e-2 (7.54e-4) =	8.2221e-2 (5.58e-4) =	8.2099e-2 (7.36e-4) =	8.2885e-2 (6.42e-4) -	8.2087e-2 (6.82e-4)
DF5	(10,10)	7.4129e-3 (3.45e-4) =	8.3170e-3 (3.79e-4) -	7.8334e-3 (3.27e-4) -	7.1666e-3 (4.05e-4) +	1.1452e-2 (6.18e-4) -	7.3923e-3 (4.16e-4)
DF6	(10,10)	4.6688e+0 (8.28e-1) -	3.6995e+0 (1.31e+0) =	3.6242e+0 (1.51e+0) =	3.8882e+0 (1.32e+0) =	3.4582e+0 (8.82e-1) =	3.7917e+0 (1.36e+0)
DF7	(10,10)	3.3358e-2 (2.87e-2) =	3.0096e-2 (2.61e-2) =	3.7304e-2 (3.09e-2) =	3.1988e-2 (2.85e-2) =	5.7105e-2 (3.71e-2) -	3.7529e-2 (2.91e-2)
DF7	(10,10)	1.4110e-1 (9.85e-4) -	1.4019e-1 (2.25e-3) -	1.3847e-1 (2.47e-3) -	1.3738e-1 (2.28e-3) -	1.4205e-1 (3.02e-3) -	1.3531e-1 (2.49e-3)
DF9	(10,10)	2.1018e+0 (1.45e-2) =	2.0978e+0 (8.30e-3) =	2.0979e+0 (8.89e-3) =	2.1010e+0 (1.40e-2) =	2.1061e+0 (1.91e-2) =	2.1001e+0 (1.45e-2)
DF10	(10,10)	1.9896e-1 (2.99e-2) =	1.8223e-1 (1.77e-2) =	1.8612e-1 (1.94e-2) =	1.8232e-1 (1.60e-2) =	1.9041e-1 (1.65e-2) =	1.8859e-1 (1.94e-2)
DF11	(10,10)	7.5377e-2 (4.72e-4) +	7.7997e-2 (4.59e-4) -	7.7393e-2 (5.33e-4) -	7.6450e-2 (3.72e-4) +	7.9072e-2 (4.35e-4) -	7.6954e-2 (4.07e-4)
DF12	(10,10)	2.8794e-1 (8.94e-4) -	2.8331e-1 (1.64e-3) -	2.8410e-1 (1.90e-3) -	2.8396e-1 (1.10e-3) -	2.8269e-1 (1.70e-3) -	2.8184e-1 (1.24e-3)
DF13	(10,10)	3.1153e-1 (3.63e-3) =	3.0784e-1 (3.36e-3) +	3.1234e-1 (3.26e-3) =	3.1138e-1 (2.79e-3) =	3.0448e-1 (4.39e-3) +	3.1186e-1 (3.34e-3)
DF14	(10,10)	5.8922e-2 (4.52e-4) -	6.0202e-2 (4.76e-4) -	5.9387e-2 (5.62e-4) -	5.9283e-2 (4.82e-4) -	6.1629e-2 (6.86e-4) -	5.8623e-2 (3.85e-4)
+/-	/=	1/15/12	1/16/11	1/11/16	5/10/13	4/15/9	

Table S - IV. The statistics of the MHV values obtained by VSDPS and its ratio of dual prediction strategies five variants were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-P1	VSDPS-P2	VSDPS-P3	VSDPS-P4	VSDPS-P5	VSDPS
FDA1	(10,10)	7.1350e-1 (1.95e-3) -	7.1449e-1 (5.85e-4) -	7.1471e-1 (5.85e-4) =	7.1475e-1 (7.08e-4) =	7.1482e-1 (4.19e-4) =	7.1489e-1 (4.81e-4)
FDA2	(10,10)	5.2800e-1 (1.29e-3) -	5.2831e-1 (8.20e-4) -	5.2851e-1 (5.06e-4) +	5.2877e-1 (1.49e-4) +	5.2877e-1 (1.17e-4) +	5.2841e-1 (2.23e-4)
FDA3	(10,10)	5.4373e-1 (2.96e-3) -	5.4418e-1 (2.53e-3) -	5.4394e-1 (2.77e-3) -	5.4364e-1 (2.81e-3) -	5.4382e-1 (3.60e-3) -	5.4624e-1 (2.41e-3)
FDA4	(10,10)	5.0880e-1 (6.71e-3) -	5.1095e-1 (2.22e-3) -	5.1200e-1 (2.46e-3) -	5.1200e-1 (2.67e-3) -	5.1084e-1 (3.13e-3) -	5.1386e-1 (2.93e-3)
FDA5	(10,10)	5.0246e-1 (8.64e-3) -	5.0419e-1 (8.33e-3) =	5.0790e-1 (3.78e-3) =	5.0708e-1 (4.15e-3) =	5.0859e-1 (3.90e-3) =	5.0703e-1 (5.17e-3)
DMOP1	(10,10)	5.2483e-1 (1.94e-3) =	5.2552e-1 (8.79e-4) =	5.2570e-1 (5.30e-4) =	5.2604e-1 (1.70e-4) +	5.2605e-1 (1.25e-4) +	5.2559e-1 (3.31e-4)
DMOP2	(10,10)	5.1783e-1 (2.68e-3) -	5.1911e-1 (9.40e-4) -	5.1944e-1 (7.39e-4) =	5.1970e-1 (7.21e-4) =	5.1925e-1 (8.86e-4) -	5.1976e-1 (7.18e-4)
DMOP3	(10,10)	7.1232e-1 (1.58e-3) -	7.1325e-1 (8.82e-4) -	7.1375e-1 (6.19e-4) =	7.1341e-1 (8.67e-4) =	7.1337e-1 (8.47e-4) -	7.1383e-1 (7.34e-4)
F5	(10,10)	2.4644e-1 (4.44e-2) -	2.4718e-1 (4.14e-2) -	2.5476e-1 (3.79e-2) -	2.5014e-1 (4.02e-2) -	2.2813e-1 (2.70e-2) -	2.8401e-1 (3.05e-2)
F6	(10,10)	2.3907e-1 (1.53e-2) -	2.3602e-1 (1.75e-2) -	2.3738e-1 (1.50e-2) -	2.3830e-1 (1.49e-2) -	2.2736e-1 (1.14e-2) -	2.4881e-1 (1.28e-2)
F7	(10,10)	2.2042e-1 (7.39e-3) =	2.2038e-1 (7.00e-3) =	2.2027e-1 (7.64e-3) =	2.1884e-1 (5.92e-3) -	2.1709e-1 (2.52e-3) -	2.2421e-1 (7.34e-3)
F8	(10,10)	4.8702e-1 (1.70e-2) =	4.9029e-1 (1.13e-2) =	4.9105e-1 (1.20e-2) =	4.9803e-1 (3.07e-3) +	4.9790e-1 (2.87e-3) +	4.9364e-1 (4.02e-3)
F9	(10,10)	2.7054e-1 (5.18e-2) -	2.7620e-1 (4.23e-2) -	2.7191e-1 (4.43e-2) -	2.6571e-1 (4.73e-2) -	2.4797e-1 (3.26e-2) -	3.1157e-1 (4.43e-2)
F10	(10,10)	2.1410e-1 (3.26e-2) -	2.1122e-1 (3.22e-2) -	2.1589e-1 (2.92e-2) -	2.1173e-1 (3.17e-2) -	1.9252e-1 (2.11e-2) -	2.3621e-1 (2.60e-2)
DF1	(10,10)	5.1825e-1 (6.61e-4) -	5.1780e-1 (7.91e-4) -	5.1865e-1 (8.71e-4) =	5.1875e-1 (7.78e-4) =	5.1443e-1 (1.05e-3) -	5.1861e-1 (8.20e-4)
DF2	(10,10)	6.8463e-1 (3.48e-3) =	6.8424e-1 (4.27e-3) =	6.8494e-1 (4.31e-3) =	6.8638e-1 (4.00e-3) =	6.8333e-1 (5.20e-3) =	6.8549e-1 (4.45e-3)
DF3	(10,10)	4.8410e-1 (5.26e-4) -	4.8252e-1 (5.33e-4) -	4.8365e-1 (6.63e-4) -	4.8455e-1 (4.96e-4) -	4.7791e-1 (8.78e-4) -	4.8669e-1 (4.20e-4)
DF4	(10,10)	2.8448e-1 (5.57e-5) =	2.8436e-1 (7.32e-5) -	2.8444e-1 (5.46e-5) =	2.8446e-1 (5.28e-5) =	2.8427e-1 (6.91e-5) -	2.8446e-1 (5.50e-5)
DF5	(10,10)	1.2722e-1 (3.06e-4) =	1.2712e-1 (3.06e-4) =	1.2719e-1 (2.70e-4) =	1.2731e-1 (3.18e-4) =	1.2670e-1 (3.22e-4) -	1.2727e-1 (3.51e-4)
DF6	(10,10)	9.4925e-2 (4.43e-2) -	2.7387e-1 (1.15e-1) =	2.6983e-1 (1.24e-1) =	2.3520e-1 (1.07e-1) =	2.5113e-1 (8.57e-2) =	2.4350e-1 (1.21e-1)
DF7	(10,10)	1.5060e-1 (3.33e-3) =	1.5100e-1 (3.03e-3) =	1.5023e-1 (3.48e-3) =	1.5084e-1 (3.22e-3) =	1.4800e-1 (4.15e-3) -	1.5016e-1 (3.30e-3)
DF8	(10,10)	8.0496e-2 (1.40e-4) -	8.0349e-2 (1.03e-4) -	8.0398e-2 (1.57e-4) -	8.0454e-2 (1.38e-4) -	8.0277e-2 (2.31e-4) -	8.0623e-2 (1.51e-4)
DF9	(10,10)	3.1161e-2 (3.69e-3) =	3.1359e-2 (2.22e-3) =	3.0816e-2 (3.47e-3) =	3.1780e-2 (2.01e-3) =	3.1502e-2 (1.74e-3) =	3.1234e-2 (3.73e-3)
DF10	(10,10)	5.5665e-1 (3.11e-2) =	5.5657e-1 (3.41e-2) =	5.5681e-1 (3.73e-2) =	5.7108e-1 (2.86e-2) =	5.3811e-1 (3.52e-2) -	5.5702e-1 (3.22e-2)
DF11	(10,10)	2.8921e-1 (5.48e-4) +	2.8807e-1 (5.04e-4) -	2.8838e-1 (7.85e-4) -	2.8912e-1 (3.52e-4) =	2.8650e-1 (5.19e-4) -	2.8894e-1 (5.17e-4)
DF12	(10,10)	9.0329e-1 (4.08e-4) -	9.0193e-1 (6.48e-4) -	9.0144e-1 (6.77e-4) -	9.0210e-1 (4.12e-4) -	9.0052e-1 (6.26e-4) -	9.0503e-1 (3.95e-4)
DF13	(10,10)	5.5985e-1 (5.48e-3) =	5.5449e-1 (5.64e-3) -	5.5661e-1 (5.13e-3) -	5.5890e-1 (4.51e-3) =	5.2856e-1 (6.79e-3) -	5.6096e-1 (6.00e-3)
DF14	(10,10)	5.8247e-1 (8.37e-4) =	5.8072e-1 (1.34e-3) -	5.8183e-1 (1.12e-3) =	5.8234e-1 (7.88e-4) =	5.7575e-1 (1.26e-3) -	5.8238e-1 (8.96e-4)
+/	/=	1/16/11	0/18/10	1/11/16	3/10/15	3/20/5	

Table S - V. The statistics of the MIGD values obtained by VSDPS and its four stepsize related variants were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-S1	VSDPS-S2	VSDPS-S3	VSDPS-S4	VSDPS
FDA1	(10,10)	6.6957e-3 (1.37e-3) =	6.7199e-3 (4.47e-4) =	6.8433e-3 (4.42e-4) =	6.8900e-3 (3.04e-4) =	6.6058e-3 (2.61e-4)
FDA2	(10,10)	5.7391e-3 (5.52e-4) =	5.8991e-3 (1.37e-4) -	5.5615e-3 (1.99e-4) +	6.2062e-3 (9.31e-5) -	5.7197e-3 (8.28e-5)
FDA3	(10,10)	4.9037e-2 (6.10e-3) =	5.3855e-2 (2.57e-3) -	5.0182e-2 (2.86e-3) =	5.1411e-2 (2.28e-3) =	5.1048e-2 (1.73e-3)
FDA4	(10,10)	9.0203e-2 (5.12e-3) -	8.5984e-2 (1.59e-3) -	8.4119e-2 (1.60e-3) =	8.5572e-2 (1.37e-3) -	8.4406e-2 (1.10e-3)
FDA5	(10,10)	2.0121e-1 (1.50e-2) +	3.1079e-1 (4.02e-2) -	2.1445e-1 (1.39e-2) =	2.1110e-1 (6.98e-3) +	2.1907e-1 (8.37e-3)
DMOP1	(10,10)	4.3795e-3 (2.78e-4) +	4.6935e-3 (6.26e-5) +	4.7351e-3 (1.97e-4) =	5.5968e-3 (1.29e-4) -	4.7985e-3 (6.84e-5)
DMOP2	(10,10)	8.2655e-3 (1.83e-3) =	8.1160e-3 (6.22e-4) =	8.0948e-3 (7.72e-4) =	8.9581e-3 (4.60e-4) -	7.8956e-3 (4.13e-4)
DMOP3	(10,10)	1.6787e-2 (5.39e-3) -	7.4676e-3 (4.97e-4) =	7.3956e-3 (5.37e-4) =	7.6295e-3 (3.75e-4) -	7.1466e-3 (4.85e-4)
F5	(10,10)	9.1840e+0 (6.82e-2) =	9.1445e-1 (2.22e-2) =	9.5541e-1 (3.99e-2) -	9.1964e-1 (1.23e-2) =	9.1687e-1 (1.61e-2)
F6	(10,10)	6.1917e-1 (9.35e-3) =	6.1522e-1 (4.89e-3) =	6.2374e-1 (4.13e-3) -	6.1676e-1 (5.69e-3) =	6.1708e-1 (4.76e-3)
F7	(10,10)	7.2309e-1 (3.67e-2) =	7.2324e-1 (4.65e-3) =	7.2327e-1 (5.50e-3) =	7.3052e-1 (4.63e-3) -	7.2183e-1 (5.16e-3)
F8	(10,10)	1.0382e-1 (7.97e-3) -	9.4765e-2 (1.56e-3) =	9.2196e-2 (1.93e-3) +	9.9069e-2 (1.06e-3) -	9.3893e-2 (1.60e-3)
F9	(10,10)	1.3066e+0 (3.53e-1) -	4.9039e-1 (1.47e-1) =	7.9241e-1 (3.06e-1) -	4.8499e-1 (1.07e-1) =	4.8475e-1 (1.54e-1)
F10	(10,10)	2.1070e+0 (1.73e-1) -	1.8539e+0 (4.55e-2) -	1.8831e+0 (7.28e-2) -	1.8154e+0 (2.25e-2) =	1.8240e+0 (2.69e-2)
DF1	(10,10)	8.7743e-3 (6.08e-3) =	8.9170e-3 (7.01e-4) =	8.8799e-3 (7.20e-4) =	8.8944e-3 (4.14e-4) =	8.6271e-3 (5.66e-4)
DF2	(10,10)	9.1786e-2 (2.96e-2) -	3.5506e-2 (5.82e-3) -	4.4210e-2 (7.01e-3) -	2.4954e-2 (2.95e-3) +	2.9793e-2 (4.79e-3)
DF3	(10,10)	1.1409e-2 (2.20e-3) -	8.5231e-3 (3.45e-4) +	8.9701e-3 (6.00e-4) +	1.2014e-2 (3.63e-4) -	9.2705e-3 (3.35e-4)
DF4	(10,10)	8.0989e-2 (6.31e-4) +	8.2850e-2 (7.01e-4) -	8.2051e-2 (6.14e-4) =	8.3470e-2 (6.87e-4) -	8.2230e-2 (7.25e-4)
DF5	(10,10)	8.5721e-3 (1.72e-3) =	7.5615e-3 (4.22e-4) =	7.3793e-3 (7.27e-4) =	8.5245e-3 (4.01e-4) -	7.4444e-3 (4.33e-4)
DF6	(10,10)	3.7048e+0 (1.19e+0) =	2.5506e+0 (2.17e+0) =	3.5740e+0 (1.59e+0) =	4.2930e+0 (1.13e+0) =	3.9780e+0 (8.26e-1)
DF7	(10,10)	9.1911e-2 (4.40e-2) -	1.8189e-2 (8.70e-3) +	6.2268e-2 (3.32e-2) -	3.9278e-2 (2.86e-2) -	2.4659e-2 (1.59e-2)
DF8	(10,10)	1.4928e-1 (2.29e-3) -	1.3409e-1 (2.69e-3) +	1.3606e-1 (2.48e-3) =	1.3794e-1 (2.74e-3) -	1.3554e-1 (2.02e-3)
DF9	(10,10)	2.3162e+0 (1.17e-1) -	2.0964e+0 (7.45e-3) =	2.1057e+0 (9.31e-3) -	2.0952e+0 (6.42e-3) =	2.1009e+0 (1.81e-2)
DF10	(10,10)	1.9512e-1 (5.43e-2) =	2.0176e-1 (2.66e-2) -	1.7938e-1 (1.24e-2) =	1.8953e-1 (1.37e-2) =	1.8746e-1 (2.50e-2)
DF11	(10,10)	8.0760e-2 (2.63e-3) -	7.7717e-2 (8.29e-4) -	7.6875e-2 (6.52e-4) =	7.7975e-2 (3.79e-4) -	7.7088e-2 (4.50e-4)
DF12	(10,10)	3.2210e-1 (1.45e-2) -	2.8119e-1 (1.69e-3) +	2.8209e-1 (1.16e-3) =	2.8407e-1 (1.37e-3) -	2.8239e-1 (1.67e-3)
DF13	(10,10)	3.2419e-1 (8.62e-3) -	3.2090e-1 (3.42e-3) -	3.1750e-1 (5.65e-3) -	3.1929e-1 (4.14e-3) -	3.1314e-1 (3.31e-3)
DF14	(10,10)	6.1017e-2 (2.17e-3) -	5.9141e-2 (6.77e-4) =	5.8827e-2 (8.03e-4) =	5.9695e-2 (4.51e-4) -	5.8742e-2 (3.29e-4)
+/-/	/=	3/14/11	5/10/13	3/8/17	2/16/10	

Table S - VI. The statistics of the MHV values obtained by VSDPS and its four stepsize related variants were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-S1	VSDPS-S2	VSDPS-S3	VSDPS-S4	VSDPS
FDA1	(10,10)	7.1436e-1 (2.06e-3) =	7.1488e-1 (6.64e-4) =	7.1467e-1 (7.10e-4) =	7.1371e-1 (4.69e-4) -	7.1506e-1 (3.88e-4)
FDA2	(10,10)	5.2824e-1 (8.96e-4) =	5.2800e-1 (1.72e-4) -	5.2849e-1 (3.21e-4) +	5.2746e-1 (1.47e-4) -	5.2821e-1 (1.32e-4)
FDA3	(10,10)	5.4791e-1 (6.48e-3) =	5.4417e-1 (2.62e-3) -	5.4712e-1 (2.58e-3) =	5.4609e-1 (2.19e-3) =	5.4669e-1 (1.69e-3)
FDA4	(10,10)	5.0446e-1 (1.01e-2) -	5.0414e-1 (3.08e-3) -	5.1240e-1 (3.80e-3) =	5.1159e-1 (2.16e-3) =	5.1260e-1 (2.35e-3)
FDA5	(10,10)	5.0348e-1 (8.80e-3) =	4.7792e-1 (1.14e-2) -	5.0761e-1 (5.97e-3) =	5.0994e-1 (2.26e-3) +	5.0800e-1 (3.13e-3)
DMOP1	(10,10)	5.2636e-1 (5.43e-4) +	5.2536e-1 (1.54e-4) +	5.2536e-1 (3.70e-4) =	5.2370e-1 (2.51e-4) -	5.2522e-1 (1.40e-4)
DMOP2	(10,10)	5.1912e-1 (2.89e-3) =	5.1939e-1 (9.79e-4) =	5.1940e-1 (1.31e-3) =	5.1799e-1 (7.40e-4) -	5.1977e-1 (6.56e-4)
DMOP3	(10,10)	7.0057e-1 (7.54e-3) -	7.1369e-1 (7.23e-4) -	7.1385e-1 (7.96e-4) =	7.1354e-1 (5.03e-4) -	7.1426e-1 (7.30e-4)
F5	(10,10)	2.9520e-1 (3.01e-2) =	3.0336e-1 (9.43e-3) +	2.7222e-1 (2.07e-2) -	2.9180e-1 (1.20e-2) =	2.9738e-1 (8.33e-3)
F6	(10,10)	2.5467e-1 (9.07e-3) =	2.5718e-1 (1.82e-3) +	2.5117e-1 (2.86e-3) -	2.5197e-1 (2.29e-3) -	2.5569e-1 (1.92e-3)
F7	(10,10)	2.1455e-1 (1.34e-2) -	2.2729e-1 (2.36e-3) =	2.2607e-1 (3.05e-3) =	2.1962e-1 (1.25e-3) -	2.2738e-1 (1.79e-3)
F8	(10,10)	4.7792e-1 (1.23e-2) -	4.8092e-1 (3.93e-3) -	4.8946e-1 (3.86e-3) +	4.7766e-1 (1.92e-3) -	4.8559e-1 (3.56e-3)
F9	(10,10)	2.3477e-1 (2.88e-2) -	3.4657e-1 (1.84e-2) =	3.0477e-1 (2.63e-2) -	3.3711e-1 (1.14e-2) =	3.4384e-1 (1.81e-2)
F10	(10,10)	1.8260e-1 (3.61e-2) -	2.4313e-1 (1.99e-2) =	2.1983e-1 (2.07e-2) -	2.4461e-1 (1.29e-2) =	2.4850e-1 (1.01e-2)
DF1	(10,10)	5.1545e-1 (8.65e-3) =	5.1806e-1 (1.10e-3) =	5.1813e-1 (1.14e-3) =	5.1720e-1 (5.99e-4) -	5.1862e-1 (9.33e-4)
DF2	(10,10)	6.2362e-1 (2.95e-2) -	6.7518e-1 (5.46e-3) -	6.6975e-1 (8.50e-3) -	6.8859e-1 (2.40e-3) +	6.8444e-1 (4.47e-3)
DF3	(10,10)	4.8087e-1 (3.72e-3) -	4.8561e-1 (6.28e-4) +	4.8491e-1 (9.63e-4) +	4.8011e-1 (6.11e-4) -	4.8444e-1 (5.77e-4)
DF4	(10,10)	2.8476e-1 (1.51e-4) +	2.8434e-1 (6.71e-5) -	2.8448e-1 (1.13e-4) =	2.8401e-1 (5.22e-5) -	2.8444e-1 (5.53e-5)
DF5	(10,10)	1.2642e-1 (8.58e-4) -	1.2701e-1 (3.35e-4) -	1.2730e-1 (4.25e-4) =	1.2690e-1 (3.19e-4) -	1.2728e-1 (3.21e-4)
DF6	(10,10)	2.8214e-1 (8.09e-2) =	3.9328e-1 (2.20e-1) +	2.8186e-1 (1.52e-1) =	2.0281e-1 (9.14e-2) =	2.3099e-1 (8.83e-2)
DF7	(10,10)	1.4508e-1 (3.60e-3) -	1.5228e-1 (1.23e-3) +	1.4743e-1 (3.69e-3) -	1.4962e-1 (3.53e-3) -	1.5155e-1 (1.93e-3)
DF8	(10,10)	7.9997e-2 (1.24e-4) -	8.0654e-2 (1.58e-4) =	8.0677e-2 (1.58e-4) =	8.0599e-2 (1.34e-4) =	8.0585e-2 (1.61e-4)
DF9	(10,10)	2.8355e-2 (4.71e-3) -	3.0046e-2 (2.59e-3) -	3.1532e-2 (2.00e-3) =	3.1843e-2 (1.12e-3) =	3.1593e-2 (1.95e-3)
DF10	(10,10)	6.0449e-1 (2.85e-2) +	5.1350e-1 (1.79e-2) -	5.7985e-1 (3.17e-2) =	5.7622e-1 (2.39e-2) =	5.6241e-1 (3.42e-2)
DF11	(10,10)	2.8655e-1 (2.11e-3) -	2.8696e-1 (1.18e-3) -	2.8862e-1 (6.74e-4) =	2.8828e-1 (3.24e-4) -	2.8880e-1 (4.69e-4)
DF12	(10,10)	8.9854e-1 (2.23e-3) -	9.0282e-1 (7.52e-4) -	9.0420e-1 (5.78e-4) +	9.0307e-1 (4.91e-4) -	9.0367e-1 (3.64e-4)
	(10,10)	5.6690e-1 (6.83e-3) +	5.3105e-1 (9.50e-3) -	5.5496e-1 (5.53e-3) -	5.5512e-1 (4.54e-3) -	5.5824e-1 (3.78e-3)
DF14	(10,10)	5.8389e-1 (1.21e-3) +	5.7929e-1 (1.32e-3) -	5.8165e-1 (1.64e-3) =	5.8108e-1 (1.05e-3) -	5.8225e-1 (7.88e-4)
+/-,	/=	5/14/9	6/15/7	4/7/17	2/17/9	

Table S - VII. The statistics of the MIGD values obtained by VSDPS and different values of control number in static optimization were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-O1	VSDPS-O2	VSDPS-O3	VSDPS-O4	VSDPS-O5	VSDPS
FDA1	(10,10)	7.4060e-3 (4.13e-4) -	6.7243e-3 (2.55e-4) =	6.5386e-3 (2.63e-4) =	6.4322e-3 (3.26e-4) =	6.5973e-3 (3.92e-4) =	6.5922e-3 (3.63e-4)
FDA2	(10,10)	5.9032e-3 (7.62e-5) -	5.7452e-3 (1.10e-4) =	5.8717e-3(9.27e-5) -	5.7028e-3 (9.38e-5) =	5.7460e-3 (1.24e-4) =	5.6651e-3 (1.29e-4)
FDA3	(10,10)	5.5682e-2 (1.81e-3) -	5.0812e-2 (3.15e-3) =	4.8914e-2 (2.48e-3) +	4.8114e-2 (2.37e-3) +	4.7013e-2 (3.34e-3) +	5.0620e-2 (2.16e-3)
FDA4	(10,10)	8.4246e-2 (1.19e-3) =	8.3745e-2 (1.04e-3) =	8.3761e-2 (1.16e-3) =	8.4585e-2 (1.43e-3) =	8.4815e-2 (1.16e-3) -	8.3709e-2 (9.80e-4)
FDA5	(10,10)	2.7176e-1 (2.49e-2) -	2.2925e-1 (1.95e-2) =	2.1279e-1 (9.75e-3) +	2.1466e-1 (1.05e-2) +	2.1858e-1 (3.46e-2) +	2.2425e-1 (1.11e-2)
DMOP1	(10,10)	5.5040e-3 (1.26e-4) -	4.9582e-3 (2.14e-4) -	4.6357e-3 (1.08e-4) +	4.4739e-3 (6.89e-5) +	4.4370e-3 (1.99e-4) +	4.8205e-3 (6.76e-5)
DMOP2	(10,10)	8.8833e-3 (5.72e-4) -	8.1140e-3 (5.77e-4) =	7.6295e-3 (3.44e-4) +	7.7911e-3 (6.03e-4) =	8.0755e-3 (9.49e-4) =	7.9433e-3 (3.76e-4)
DMOP3	(10,10)	7.1657e-3 (2.55e-4) +	7.2444e-3 (3.06e-4) =	8.0186e-3 (4.49e-4) -	8.3517e-3 (6.55e-4) -	9.3956e-3 (1.74e-3) -	7.3717e-3 (4.65e-4)
F5	(10,10)	9.4482e-1 (2.07e-2) -	9.1849e-1 (1.34e-2) =	9.1179e-1 (9.81e-3) =	9.1268e-1 (1.68e-2) =	9.2068e-1 (1.91e-2) =	9.2556e-1 (2.54e-2)
F6	(10,10)	6.2656e-1 (6.27e-3) -	6.1951e-1 (4.80e-3) =	6.2749e-1 (5.53e-3) -	6.1545e-1 (4.11e-3) =	6.1799e-1 (4.24e-3) =	6.1780e-1 (4.27e-3)
F7	(10,10)	7.3213e-1 (6.35e-3) -	7.2476e-1 (5.10e-3) -	7.1889e-1 (3.52e-3) =	7.1813e-1 (4.94e-3) =	7.2022e-1 (3.97e-3) =	7.1942e-1 (3.68e-3)
F8	(10,10)	9.1866e-2 (1.61e-3) =	9.2736e-2 (1.63e-3) =	9.3603e-2 (2.05e-3) =	9.6068e-2 (2.75e-3) -	9.8949e-2 (4.03e-3) -	9.3173e-2 (1.18e-3)
F9	(10,10)	5.5750e-1 (1.61e-1) =	5.8437e-1 (2.40e-1) =	5.3344e-1 (1.66e-1) =	5.9435e-1 (1.63e-1) =	6.0110e-1 (2.25e-1) =	5.8956e-1 (2.42e-1)
F10	(10,10)	1.8879e+0 (4.07e-2) -	1.8370e+0 (4.15e-2) =	1.8155e+0 (3.35e-2) =	1.8205e+0 (3.33e-2) =	1.8418e+0 (6.38e-2) =	1.8381e+0 (3.46e-2)
DF1	(10,10)	8.5278e-3 (5.47e-4) =	8.6648e-3 (4.21e-4) =	8.9984e-3 (7.83e-4) =	9.9277e-3 (1.13e-3) -	1.1058e-2 (2.01e-3) -	8.5648e-3 (5.87e-4)
DF2	(10,10)	4.5032e-2 (5.38e-3) -	3.2806e-2 (6.64e-3) -	2.7238e-2 (4.23e-3) =	2.3516e-2 (3.17e-3) +	2.3774e-2 (4.36e-3) +	2.8000e-2 (4.24e-3)
DF3	(10,10)	9.5954e-3 (3.38e-4) -	9.2048e-3 (2.98e-4) =	9.4282e-3 (2.72e-4) -	9.8269e-3 (3.55e-4) -	1.0803e-2 (8.13e-4) -	9.1315e-3 (2.26e-4)
DF4	(10,10)	8.3306e-2 (8.80e-4) -	8.2677e-2 (7.17e-4) =	8.1711e-2 (4.75e-4) +	8.1121e-2 (5.20e-4) +	8.1238e-2 (5.43e-4) +	8.2233e-2 (6.42e-4)
DF5	(10,10)	8.4010e-3 (3.65e-4) -	7.5481e-3 (3.48e-4) =	7.3054e-3 (3.17e-4) =	7.4377e-3 (4.86e-4) =	7.5753e-3 (4.89e-4) =	7.3832e-3 (3.69e-4)
DF6	(10,10)	1.9749e+0 (1.37e+0) +	3.8439e+0 (1.23e+0) =	4.4457e+0 (9.91e-1) =	4.5675e+0 (9.37e-1) =	4.7318e+0 (1.15e+0) =	4.3751e+0 (1.29e+0)
DF7	(10,10)	3.7477e-2 (3.09e-2) =	3.6671e-2 (3.10e-2) =	4.6648e-2 (3.02e-2) =	4.0143e-2 (3.10e-2) =	3.7316e-2 (2.68e-2) -	3.2462e-2 (2.52e-2)
DF8	(10,10)	1.3048e-1 (2.04e-3) +	1.3466e-1 (3.38e-3) =	1.3961e-1 (2.64e-3) -	1.4136e-1 (2.07e-3) -	1.4434e-1 (4.18e-3) -	1.3489e-1 (1.96e-3)
DF9	(10,10)	2.0919e+0 (4.88e-3) +	2.0971e+0 (8.39e-3) =	2.1044e+0 (1.68e-2) -	2.1162e+0 (2.64e-2) -	2.1162e+0 (2.10e-2) -	2.1035e+0 (1.39e-2)
DF10	(10,10)	1.9140e-1 (1.41e-2) -	1.9114e-1 (1.21e-2) -	1.7966e-1 (2.60e-2) =	1.7211e-1 (2.17e-2) =	2.0778e-1 (5.11e-2) =	1.7818e-1 (1.31e-2)
DF11	(10,10)	7.6617e-2 (3.78e-4) =	7.6764e-2 (5.84e-4) =	7.7097e-2 (7.04e-4) =	7.7805e-2 (6.76e-4) -	7.8228e-2 (1.05e-3) -	7.6530e-2 (4.59e-4)
DF12	(10,10)	2.7847e-1 (1.22e-3) =	2.8098e-1 (1.85e-3) =	2.8404e-1 (1.87e-3) -	2.8985e-1 (3.23e-3) -	3.0397e-1 (1.49e-2) -	2.8165e-1 (1.06e-3)
DF13	(10,10)	3.1946e-1 (3.63e-3) -	3.1384e-1 (4.81e-3) =	3.1326e-1 (3.73e-3) =	3.1326e-1 (3.43e-3) =	3.1453e-1 (4.76e-3) -	3.1187e-1 (3.65e-3)
DF14	(10,10)	5.9129e-2 (5.37e-4) =	5.8974e-2 (8.20e-4) =	5.8861e-2 (4.51e-4) =	5.8780e-2 (4.35e-4) =	5.9249e-2 (8.18e-4) -	5.8681e-2 (4.19e-4)
+/-	/=	4/16/8	0/4/24	5/7/16	5/8/15	5/12/11	

Table S - VIII. The statistics of the MHV values obtained by VSDPS and different values of control number in static optimization were run 30 times independently on FDA, dMOP, F, and DF test suites when $n_t = 10$, $\tau_t = 10$.

Problem	(n_t, τ_t)	VSDPS-O1	VSDPS-O2	VSDPS-O3	VSDPS-O4	VSDPS-O5	VSDPS
FDA1	(10,10)	7.1366e-1 (6.11e-4) -	7.1481e-1 (3.71e-4) -	7.1422e-1 (3.83e-4) -	7.1446e-1 (4.57e-4) -	7.1425e-1 (6.07e-4) -	7.1507e-1 (5.57e-4)
FDA2	(10,10)	5.2790e-1 (1.34e-4) -	5.2820e-1 (1.44e-4) =	5.2831e-1 (1.62e-4) =	5.2829e-1 (1.50e-4) =	5.2720e-1 (2.15e-4) -	5.2831e-1 (2.07e-4)
FDA3	(10,10)	5.4159e-1 (1.59e-3) -	5.4669e-1 (3.16e-3) =	5.4268e-1 (2.50e-3) -	5.4313e-1 (2.26e-3) -	5.5112e-1 (3.32e-3) +	5.4713e-1 (2.10e-3)
FDA4	(10,10)	5.0755e-1 (2.61e-3) -	5.1139e-1 (3.39e-3) =	5.1417e-1 (2.80e-3) =	5.1494e-1 (2.96e-3) +	5.0486e-1 (3.12e-3) -	5.1290e-1 (2.60e-3)
FDA5	(10,10)	4.9038e-1 (5.55e-3) -	5.0265e-1 (5.20e-3) =	5.0903e-1 (2.56e-3) +	5.0969e-1 (2.95e-3) +	5.0680e-1 (1.05e-2) +	5.0534e-1 (2.98e-3)
DMOP1	(10,10)	5.2376e-1 (2.60e-4) -	5.2486e-1 (4.65e-4) -	5.2455e-1 (2.31e-4) -	5.2593e-1 (1.72e-4) +	5.2607e-1 (4.86e-4) +	5.2515e-1 (1.68e-4)
DMOP2	(10,10)	5.1803e-1 (9.08e-4) -	5.1940e-1 (9.65e-4) =	5.2021e-1 (5.46e-4) +	5.1002e-1 (9.53e-4) -	5.1967e-1 (1.38e-3) =	5.1965e-1 (6.09e-4)
DMOP3	(10,10)	7.1404e-1 (3.95e-4) +	7.1406e-1 (4.29e-4) =	7.1358e-1 (6.58e-4) =	7.1255e-1 (9.74e-4) -	7.1098e-1 (2.56e-3) -	7.1392e-1 (6.75e-4)
F5	(10,10)	2.6812e-1 (1.13e-2) -	2.9226e-1 (1.16e-2) =	2.9165e-1 (6.36e-3) -	3.0520e-1 (8.33e-3) +	3.0326e-1 (7.80e-3) +	2.9671e-1 (7.66e-3)
F6	(10,10)	2.4661e-1 (5.71e-3) -	2.5277e-1 (3.93e-3) -	2.5697e-1 (2.16e-3) +	2.5657e-1 (2.64e-3) =	2.5669e-1 (2.93e-3) +	2.5565e-1 (2.17e-3)
F7	(10,10)	2.1963e-1 (1.64e-3) -	4.5659e-1 (1.17e-1) -	4.5826e-1 (1.18e-1) =	4.5950e-1 (1.18e-1) =	4.5699e-1 (1.17e-1) -	5.1605e-1 (1.38e-3)
F8	(10,10)	4.8635e-1 (3.30e-3) -	4.8647e-1 (2.62e-3) =	4.8682e-1 (3.41e-3) =	4.8453e-1 (4.56e-3) =	4.7980e-1 (5.44e-3) -	4.8681e-1 (2.17e-3)
F9	(10,10)	3.1910e-1 (1.64e-2) -	3.3038e-1 (2.83e-2) =	3.4024e-1 (1.51e-2) =	3.3603e-1 (1.80e-2) =	3.4079e-1 (2.15e-2) =	3.3153e-1 (2.50e-2)
F10	(10,10)	2.1326e-1 (1.63e-2) -	2.4035e-1 (1.37e-2) -	2.5608e-1 (1.22e-2) +	2.5496e-1 (6.73e-3) =	2.4407e-1 (1.15e-2) -	2.4870e-1 (1.03e-2)
DF1	(10,10)	5.1864e-1 (8.84e-4) =	5.1848e-1 (6.70e-4) =	5.1804e-1 (1.19e-3) =	5.1677e-1 (1.65e-3) -	5.1512e-1 (2.95e-3) -	5.1868e-1 (9.74e-4)
DF2	(10,10)	6.6739e-1 (3.86e-3) -	6.7984e-1 (7.24e-3) -	6.8691e-1 (4.07e-3) =	6.9118e-1 (3.25e-3) +	6.9090e-1 (4.48e-3) +	6.8578e-1 (4.36e-3)
DF3	(10,10)	4.8389e-1 (5.88e-4) -	4.8458e-1 (5.93e-4) =	4.8339e-1 (5.01e-4) -	4.8355e-1 (6.65e-4) -	4.8198e-1 (1.36e-3) -	4.8466e-1 (4.34e-4)
DF4	(10,10)	2.8393e-1 (7.99e-5) -	2.8430e-1 (1.38e-4) -	2.8455e-1 (6.61e-5) +	2.8470e-1 (5.29e-5) +	2.8471e-1 (1.38e-4) +	2.8441e-1 (6.55e-5)
DF5	(10,10)	1.2697e-1 (3.24e-4) -	1.2728e-1 (2.64e-4) =	1.2719e-1 (2.95e-4) =	1.2696e-1 (4.36e-4) -	1.2679e-1 (4.54e-4) -	1.2728e-1 (3.16e-4)
DF6	(10,10)	4.0810e-1 (1.57e-1) +	2.3565e-1 (1.19e-1) =	1.7811e-1 (6.48e-2) -	2.4047e-1 (8.55e-2) =	2.2632e-1 (8.70e-2) =	2.1134e-1 (1.07e-1)
DF7	(10,10)	1.5017e-1 (3.41e-3) =	1.5028e-1 (3.47e-3) =	1.4907e-1 (3.47e-3) =	1.4973e-1 (3.63e-3) =	1.4994e-1 (3.14e-3) =	1.5069e-1 (2.90e-3)
DF8	(10,10)	8.0874e-2 (8.95e-5) +	8.0682e-2 (2.01e-4) =	8.0439e-2 (1.54e-4) -	8.0294e-2 (1.16e-4) -	8.0167e-2 (2.19e-4) -	8.0653e-2 (1.22e-4)
DF9	(10,10)	3.1960e-2 (1.51e-3) =	3.1355e-2 (2.13e-3) =	2.9453e-2 (5.20e-3) -	2.8134e-2 (5.78e-3) -	2.8849e-2 (5.47e-3) -	3.1362e-2 (4.08e-3)
DF10	(10,10)	5.3418e-1 (1.55e-2) -	5.4242e-1 (3.11e-2) -	5.9050e-1 (3.21e-2) +	6.0323e-1 (2.87e-2) +	5.9402e-1 (2.46e-2) =	5.7489e-1 (2.67e-2)
DF11	(10,10)	2.8768e-1 (5.24e-4) -	2.8842e-1 (5.81e-4) =	2.8885e-1 (7.26e-4) =	2.8884e-1 (6.93e-4) =	2.8870e-1 (8.25e-4) =	2.8874e-1 (4.52e-4)
DF12	(10,10)	9.0391e-1 (4.60e-4) -	9.0393e-1 (4.06e-4) =	9.0395e-1 (5.22e-4) =	9.0243e-1 (7.90e-4) -	8.9959e-1 (2.68e-3) -	9.0414e-1 (4.86e-4)
DF13	(10,10)	5.2753e-1 (7.95e-3) -	5.5070e-1 (9.35e-3) -	5.4397e-1 (5.24e-3) -	5.5172e-1 (5.96e-3) -	5.7452e-1 (8.10e-3) +	5.5998e-1 (3.94e-3)
DF14	(10,10)	5.7808e-1 (1.06e-3) -	5.8055e-1 (1.87e-3) -	5.8283e-1 (1.36e-3) =	5.8440e-1 (8.32e-4) +	5.8486e-1 (2.11e-3) +	5.8193e-1 (1.02e-3)
+/-	/=	3/22/3	0/10/18	6/9/13	8/11/9	9/13/6	