From Datalog to FLIX: A Declarative Language for Fixed Points on Lattices

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Motivation

Implementation of static analyses is difficult:

- analyses are often interrelated:
 - (e.g. conditional constant propagation)
 - (e.g. points-to analysis and call graph construction)
- requires a complicated arrangement of work lists.
- ⇒ Hard to ensure correctness.
- ⇒ Hard to ensure performance/scalability.
- ⇒ Renewed interest in declarative programming.

What is Declarative Programming? (aka logic programming)

The what, not the how.

Find x such that:

$$3 + x = 15$$

⇒ Easy to understand whether we are solving the right problem!

What is Declarative Programming?

Separates the choice of:

- evaluation strategy (e.g. work list order)
- data structures (e.g. bitsets/hashsets/BDDs)

from the specification of the problem.

⇒ We can leave these choices up to the solver or override them when needed.

What is **Datalog?**

A declarative language for constraints on relations:

- Prolog-style rules (horn clauses).
- Successfully used in large-scale points-to analyses [Bravenboer et al.], [Smaragdakis et al.]

Useful theoretical and practical properties:

- Every Datalog program eventually terminates.
- Every Datalog program has a unique solution.

⇒ Debugging is easier!

Examples

Computing your aunts and uncles:

```
AuntOrUncle(x, z) :- Parent(x, y), Brother(y, z).
AuntOrUncle(x, z) :- Parent(x, y), Sister(y, z).
```

Computing the transitive closure of a graph:

```
Path(x, z) :- Path(x, y), Edge(y, z).
```

What we can and can't do in Datalog:

Analyses based on *relations*:

- Points-To
- Definite Assignment
- Reaching Definitions
- ...

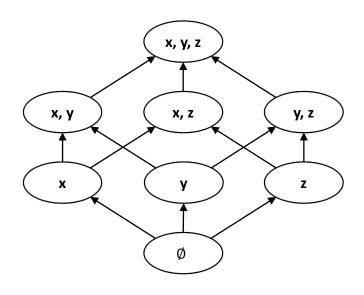
Analyses based on *lattices*:

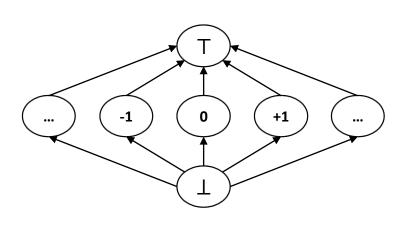
- Sign Analysis
- Constant Propagation
- Interval Analysis
- ...

Example: Constant Propagation

What Datalog has:

What we wanted:





infinite set

fixed finite set

- **⇒** We need lattices.
- ⇒ We need functions.

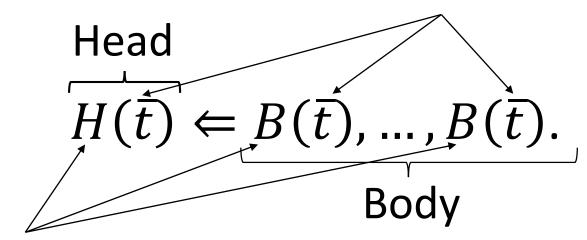
Introducing Flix

A blend of **Logic** and **Functional** programming.

- Inspired by Datalog.
- User-defined lattices.
- User-defined monotone filter and transfer functions.
- Interoperates with languages on the JVM.

The Anatomy of a **Datalog** Rule

Terms: Variables or Constants



Predicates

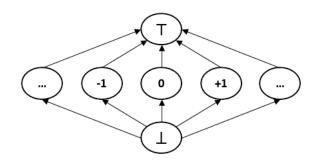
The Anatomy of a Flix Rule

Filter Function

$$H_{\ell}(\overline{t}, \underline{f(t)}) \Leftarrow \varphi(\overline{t}), B_{\ell}(\overline{t}), \dots, B_{\ell}(\overline{t}).$$

Transfer Function

Datalog vs. Flix



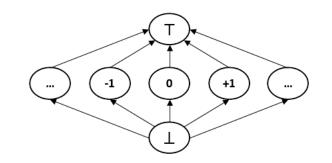
The **Datalog** program:

has the minimal model:

The **Flix** program:

has the minimal model:

Flix Semantics



The **Flix** program:

$$R(x) :- A(x)$$
.

$$R(x) :- B(x)$$
.

has the minimal model:

The **Flix** program:

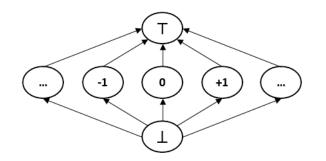
$$A(Cst(1))$$
. $B(Cst(2))$.

$$R(x) :- A(x), B(x).$$

has the minimal model:

$$\{A(Cst(1)),$$

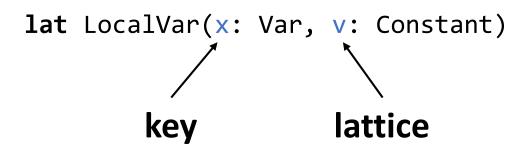
Constant Propagation



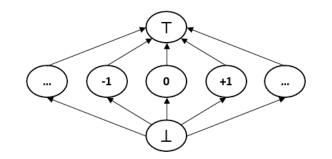
Input Relations:

```
rel AddExp(r: Var, x: Var, y: Var) \mathbf{r} = \mathbf{x} + \mathbf{y}
rel DivExp(r: Var, x: Var, y: Var) \mathbf{r} = \mathbf{x} / \mathbf{y}
```

Computed Lattices:

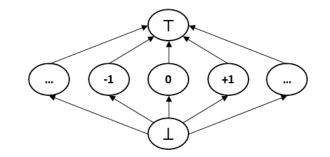


Lattice Definition



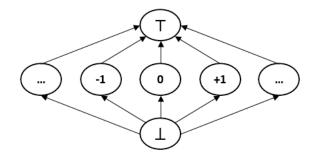
```
enum Constant {
   case Top,
   case Cst(Int),
   case Bot
}
```

Lattice Definition

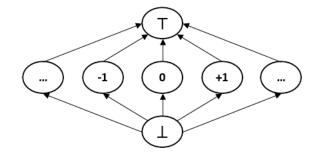


And define lub and glb in similar way...

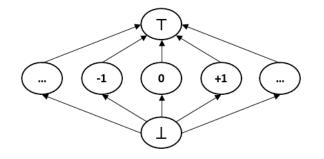
Analysis Rules



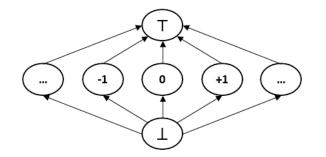
Transfer Function



Example: Finding Bugs



Filter Function



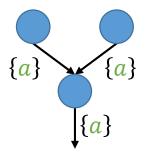
Experiments

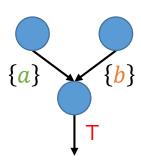
We have expressed three analyses in Flix:

- The Strong Update Analysis [Lhoták and Chung]
- The IFDS algorithm [Reps, Horwitz, and Sagiv]
 - Instantiated with the Alias-Set analysis [Naeem and Lhoták]
- The IDE algorithm [Sagiv, Reps, and Horwitz]

Strong Update Analysis

- Hybrid points-to analysis for C programs:
 - flow-sensitive for singleton points-to sets.
 - *flow-insensitive* for everything else.





Strong Update Analysis

```
\begin{array}{l} \ell: p = \&a \\ \ell: p = q \\ \ell: p = q \\ \ell: *p = q \\ \forall a \in pt(p) \cdot pt(q) \sqsubseteq su[\underline{\ell}](a) \\ \forall a \in pt(p) \cdot pt(q) \subseteq pt(a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq pt(p) \\ \ell: p = *q \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq pt(p) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p = *q \\ \forall a \in pt(q) \cdot ptsu[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p \in su[\overline{\ell}](a) \\ \ell: p \in su[\overline{\ell}](a) \subseteq su[\overline{\ell}](a) \\ \ell: p \in su[\overline{\ell}](a) \subseteq su[\overline{\ell}
```

Strong Update Analysis

```
Pt(p, a) :- AddrOf(p, a).
                                                          [AddrOf]
Pt(p, a) := Copy(p, q), Pt(q, a).
                                                          [Copy]
SUAfter(1, a, Single(b)) :-
                                                          [Store]
  Store(1, p, q), Pt(p, a), Pt(q, b).
PtH(a, b) := Store(1, p, q), Pt(p, a), Pt(q, b).
                                                          [Load]
Pt(p, b) := Load(1, p, q), Pt(q, a), PtSU(1, a, b).
SUBefore(12, a, t) :- CFG(11, 12), SUAfter(11, a, t).
                                                          [CFlow]
SUAfter(1, a, t) :- SUBefore(1, a, t), Preserve(1, a).
                                                          [Preserve]
PtSU(1, a, b) :- PtH(a, b), SUBefore(1, a, t), filter(t, b).
```

IFDS & IDE

Inter-procedural context-sensitive dataflow analyses:

- expressed as graph reachability problems.
- Interprocedural Finite Distributive Subset (IFDS)
 - pure graph reachability.
- Inteprocedural Distributive Environments (IDE)
 - IFDS with composition of micro-functions along the path.
- Anecdotally, these algorithms are hard to understand.

IFDS

```
declare PathEdge, WorkList, SummaryEdge: global edge set
               algorithm Tabulate(G_{IP}^{\#})
               begin

Let (N^\#, E^\#) = G_{IP}^\#
                  PathEdge := \{\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle \}

WorkList := \{\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle \}

SummaryEdge := \emptyset
              \begin{array}{l} \text{cosminus}_{\lambda \in \mathcal{Y}}(\mathbb{R}^n) = \mathcal{N} \text{ } \textbf{do} \\ \text{ for each } n \in \mathcal{N} \text{ } \textbf{do} \\ \lambda_n := |d_2 \in D \mid \exists d_1 \in (D \cup \{\textbf{0}\}) \text{ such that } \langle s_{proc} g_{(n)}, d_1 \rangle \rightarrow \langle n, d_2 \rangle \in \text{ PathEdge } \} \text{ } \textbf{do} \\ \text{ } \textbf{do} \end{array}
               procedure Propagate(e)
               if e ∉ PathEdge then Insert e into PathEdge; Insert e into WorkList fi
              procedure ForwardTabulateSLRPs()
begin
while WorkList ≠ Ø do
                        Select and remove an edge \langle s_p, d_1 \rangle \rightarrow \langle n, d_2 \rangle from WorkList
                        switch n
                           \begin{aligned} & \text{case } n \in Call_p: \\ & \text{for each } d_3 \text{ such that } \langle n, d_2 \rangle \rightarrow \langle s_{culledProc(n)}, d_3 \rangle \in E^* \text{ do} \\ & \text{Propagate}(\langle s_{culledProc(n)}, d_3 \rangle \rightarrow \langle s_{culledProc(n)}, d_3 \rangle) \end{aligned}
[13]
[14]
[15]
[16]
[17]
[18]
[19]
[20]
                                  for each d_3 such that \langle n, d_2 \rangle \rightarrow \langle returnSite(n), d_3 \rangle \in (E^s \cup SummaryEdge) do Propagate(\langle s_p, d_1 \rangle \rightarrow \langle returnSite(n), d_3 \rangle)
                              end case
                            case n = e_p:

for each c \in callers(p) do

for each d_a, d_a such that \langle c, d_a \rangle \rightarrow \langle s_p, d_1 \rangle \in E^s and \langle e_p, d_2 \rangle \rightarrow \langle returnSite(c), d_3 \rangle \in E^s do

if \langle c, d_a \rangle \rightarrow \langle returnSite(c), d_3 \rangle \rightarrow \langle s_p, d_1 \rangle \in E^s and \langle e_p, d_2 \rangle \rightarrow \langle returnSite(c), d_3 \rangle \in E^s do

insert \langle c, d_a \rangle \rightarrow \langle returnSite(c), d_3 \rangle into Summary Edge then
[21]
[22]
[23]
[24]
[25]
[26]
[27]
[28]
[29]
[30]
[31]
[32]
                                                   for each d_3 such that \langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle c, d_4 \rangle \in PathEdge do
Propagate(\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle returnSite(c), d_5 \rangle)
                               end case
[33]
[34]
[35]
[36]
[37]
                              case n \in (N_p - Call_p - \{e_p\}):

for each \langle m, d_3 \rangle such that \langle n, d_2 \rangle \rightarrow \langle m, d_3 \rangle \in E^\# do
                                          Propagate(\langle s_p, d_1 \rangle \rightarrow \langle m, d_3 \rangle)
   end case
end switch
od
end
```

IDE

```
{\bf procedure}\ {\bf Forward Compute Jump Functions SLRPs ()}
                for all (s_p, d'), (m, d) such that m occurs in procedure p and d', d \in D \cup \{\Lambda\} do
                JumpFn(\langle s_p, d' \rangle \to \langle m, d \rangle) = \lambda l. \top od
for all corresponding call-return pairs (c, r) and d', d \in D \cup \{\Lambda\} do
  [2]
[3]
                     SummaryFn(\langle c, d' \rangle \rightarrow \langle r, d \rangle) = \lambda l. \top od
  [4]
[5]
[6]
[7]
                 PathWorkList := \{ \langle s_{main}, \Lambda \rangle \rightarrow \langle s_{main}, \Lambda \rangle \}
                JumpFn((s_{main}, \Lambda) \rightarrow (s_{main}, \Lambda)) := id
while PathWorkList \neq \emptyset do
                      Select and remove an item \langle s_p, d_1 \rangle \rightarrow \langle n, d_2 \rangle from PathWorkList
  [8]
[9]
[10]
                       let f = JumpFn(\langle s_p, d_1 \rangle \rightarrow \langle n, d_2 \rangle)
                       switch(n)
  [11]
                            case n is a call node in p, calling a procedure q:
  [12]
                                for each d_3 such that (n, d_2) \rightarrow (s_q, d_3) \in E^{\sharp} do
  [13]
                                    Propagate (\langle s_q, d_3 \rangle \rightarrow \langle s_q, d_3 \rangle, id) od
  [14]
                                let r be the return-site node that corresponds to n
  [15]
[16]
                                for each d_3 such that e = \langle n, d_2 \rangle \rightarrow \langle r, d_3 \rangle \in E^{\sharp} do
                                    Propagate(\langle s_n, d_1 \rangle \rightarrow \langle r, d_3 \rangle, EdgeFn(e) o f) od
  [17]
[18]
[19]
[20]
                                for each d_3 such that f_3 = SummaryFn(\langle n, d_2 \rangle \rightarrow \langle r, d_3 \rangle) \neq \lambda l. T do
                                     Propagate(\langle s_p, d_1 \rangle \rightarrow \langle r, d_3 \rangle, f_3 \circ f) od endcase
                             case n is the exit node of p:
                                for each call node c that calls p with corresponding return-site node r do
  [21]
[22]
[23]
[24]
[25]
[26]
[27]
                                     for each d_4, d_5 such that (c, d_4) \rightarrow (s_p, d_1) \in E^{\sharp} and (e_p, d_2) \rightarrow (r, d_5) \in E^{\sharp} do
                                         let f_4 = EdgeFn(\langle c, d_4 \rangle \rightarrow \langle s_p, d_1 \rangle) and
                                                f_5 = EdgeFn(\langle e_p, d_2 \rangle \rightarrow \langle r, d_5 \rangle) and
                                                f' = (f_5 \circ f \circ f_4) \sqcap SummaryFn(\langle c, d_4 \rangle \rightarrow \langle r, d_5 \rangle)
                                         If f' \neq SummaryFn(\langle c, d_4 \rangle \rightarrow \langle r, d_5 \rangle) then
                                           SummaryFn(\langle c, d_4 \rangle \rightarrow \langle r, d_5 \rangle) := f'
                                            let s_q be the start node of c's procedure
  [28]
[29]
                                           \text{for each } d_3 \text{ such that } f_3 = JumpFn(\langle s_q, d_3 \rangle \to \langle c, d_4 \rangle) \neq \lambda l. \top \text{ do}
                                              Propagate((s_q, d_3) \rightarrow (r, d_5), f' \circ f_3) od fl od od endcase
  [30]
                             default:
                                  for each \langle m, d_3 \rangle such that \langle n, d_2 \rangle \rightarrow \langle m, d_3 \rangle \in E^{\sharp} do
                                     Propagate((s_p, d_1) \rightarrow (m, d_3), EdgeFn((n, d_2) \rightarrow (m, d_3)) \circ f) od endcase
   procedure Propagate(e, f)
             begin
                 let f' = f \sqcap JumpFn(e)
                if f' \neq JumpFn(e) then
                     JumpFn(e) := f'
                    Insert e into PathWorkList fl
             end
procedure ComputeValues()
       begin

/* Phase II(i) */

for each n^{\sharp} \in N^{\sharp} do val(n^{\sharp}) := \top od
           val((s_{main}, \Lambda)) := \bot

NodeWorkList := \{(s_{main}, \Lambda)\}

while NodeWorkList \neq \emptyset do
                 Select and remove an exploded-graph node (n, d) from NodeWorkList
                 switch(n)
                     case n is the start node of p:
for each c that is a call node inside p do
                            for each d' such that f' = JumpFn((n, d) \rightarrow (c, d')) \neq M.T do

PropagateValue((c, d'), f'(val((s_p, d)))) od od endcase
                     case n is a call node in p, calling a procedure q: for each d' such that (n,d) \rightarrow (s_q,d') \in E^q do PropagateValue((s_q,d'), EdgeFn((n,d) \rightarrow (s_q,d'))(val((n,d)))) od endcase
                 end switch od
                Phase II(ii) */
            f Prase I(ii) f for each node n, in a procedure p, that is not a call or a start node do for each d', d such that f' = JumpFn(⟨sp, d') → ⟨n, d⟩) ≠ λl. T do val(⟨n, d⟩) := val(⟨n, d⟩) ∩ f'(val(⟨sp, d'⟩)) od od
 procedure PropagateValue(n!, v)
       begin

let v' = v \cap val(n^{\sharp})

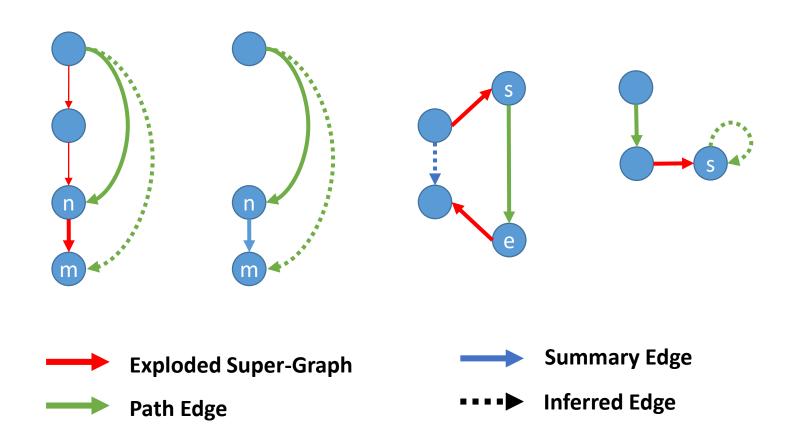
if v' \neq val(n^{\sharp}) then

val(n^{\sharp}) := v'
              Insert nº into Node WorkList fi
```

IFDS

- Input: the exploded super-graph.
 - The super-graph is the inter-procedural CFG.
 - The exploded super-graph is a copy of the CFG for each analysis element (in the distributive subset).
- Output: Path Edges + Summary Edges.

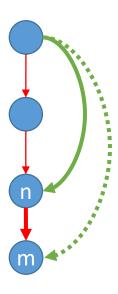
IFDS – Graphical Formulation



IFDS

(node, element)-pair

```
PathEdge(d1, m, d3):-
  PathEdge(d1, n, d2),
  CFG(n, m),
  d3 <- eshIntra(n, d2).</pre>
```



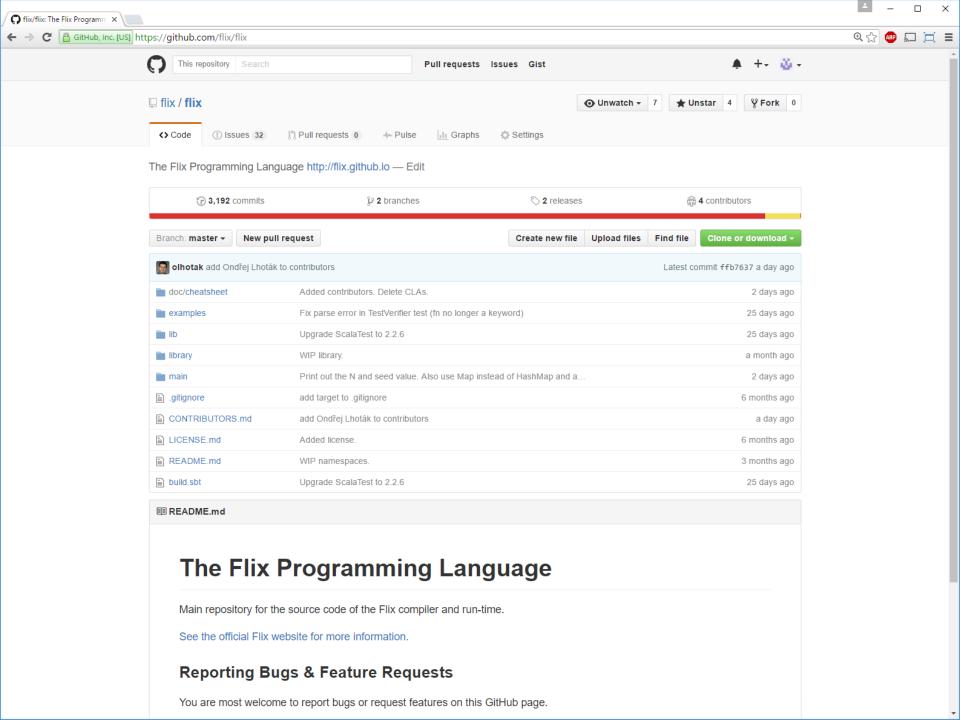
- The CFG is represented as a tabulated relation.
- The exploded super-graph (eshIntra) must be represented as a *function computed on-demand*.

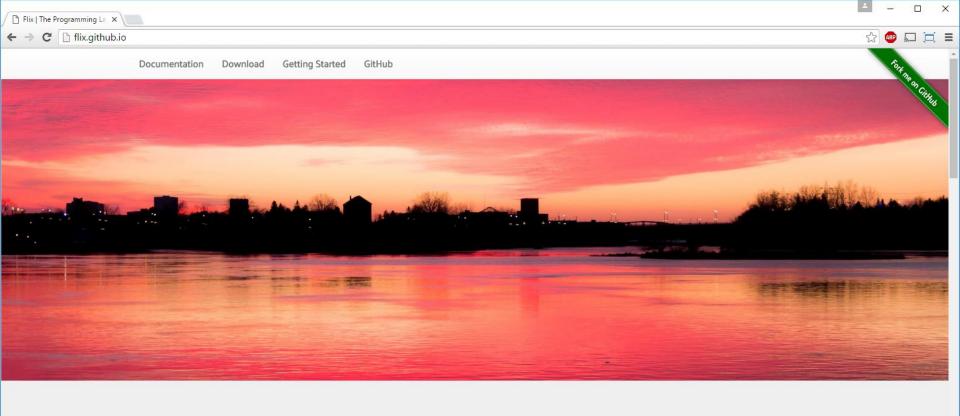
IFDS

```
PathEdge(d1, m, d3):-
    CFG(n, m),
    PathEdge(d1, n, d2),
    d3 \leftarrow eshIntra(n, d2).
PathEdge(d1, m, d3):-
    CFG(n, m),
    PathEdge(d1, n, d2),
    SummaryEdge(n, d2, d3).
PathEdge(d3, start, d3):-
    PathEdge(d1, call, d2),
    CallGraph(call, target),
    EshCallStart(call, d2, target, d3),
    StartNode(target, start).
SummaryEdge(call, d4, d5):-
    CallGraph(call, target),
    StartNode(target, start),
    EndNode(target, end),
    EshCallStart(call, d4, target, d1),
    PathEdge(d1, end, d2),
    d5 <- eshEndReturn(target, d2, call).</pre>
EshCallStart(call, d, target, d2) :-
    PathEdge( , call, d),
    CallGraph(call, target),
    d2 <- eshCallStart(call, d, target).</pre>
Result(n, d2):-
    PathEdge(_, n, d2).
```

IDE

```
JumpFn(d1, m, d3, comp(long, short)) :-
   CFG(n, m),
    JumpFn(d1, n, d2, long),
    (d3, short) <- eshIntra(n, d2).
JumpFn(d1, m, d3, comp(caller, summary)) :-
   CFG(n, m),
    JumpFn(d1, n, d2, caller),
   SummaryFn(n, d2, d3, summary).
JumpFn(d3, start, d3, identity()) :-
    JumpFn(d1, call, d2, _),
    CallGraph(call, target),
    EshCallStart(call, d2, target, d3, _),
   StartNode(target, start),
SummaryFn(call, d4, d5, comp(comp(cs, se), er)):-
   CallGraph(call, target),
   StartNode(target, start),
    EndNode(target, end),
    EshCallStart(call, d4, target, d1, cs),
    JumpFn(d1, end, d2, se),
    (d5, er) <= eshEndReturn(target, d2, call).</pre>
EshCallStart(call, d, target, d2, cs) :-
    JumpFn(_, call, d, _),
    CallGraph(call, target),
    (d2, cs) <= eshCallStart(call, d, target).</pre>
InProc(p, start) := StartNode(p, start).
InProc(p, m) := InProc(p, n), CFG(n, m).
Result(n, d, apply(fn, vp)) :-
    ResultProc(proc, dp, vp),
    InProc(proc, n),
    JumpFn(dp, n, d, fn).
ResultProc(proc, dp, apply(cs, v)) :-
    Result(call, d, v),
    EshCallStart(call, d, proc, dp, cs).
```





Flix. Functional. Logical.

The elegance of functional programming with the conciseness of logic programming.

Think SQL, but on steroids.

Recent News

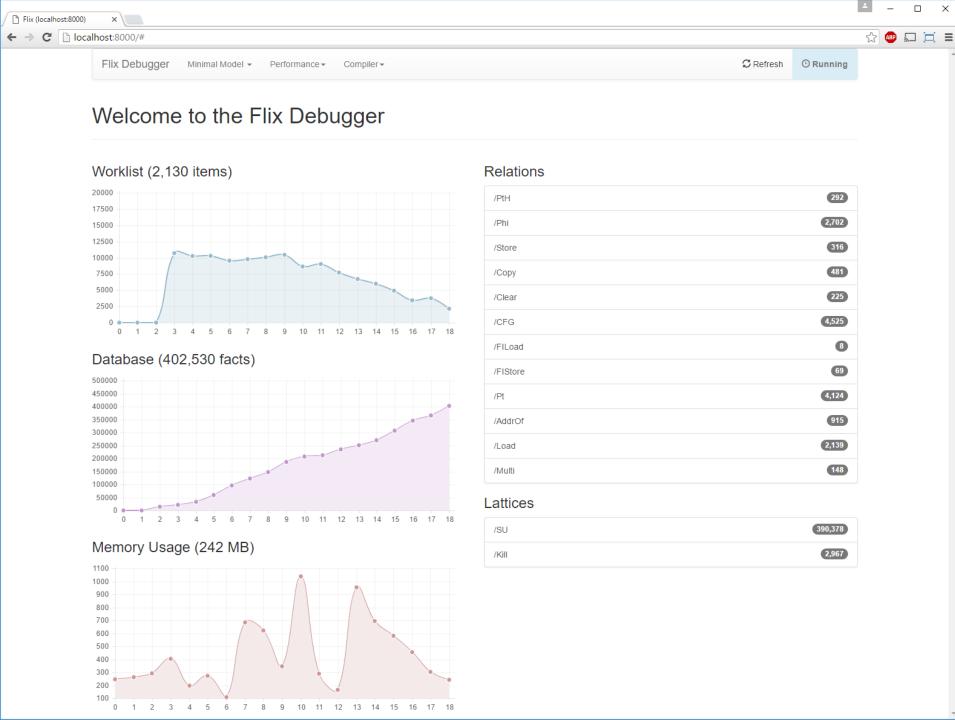
- 2016-06-10 The first preview version of Flix is now available! Note that Flix is still under heavy development and some aspects of the languages are expected to change.
- 2016-06-10 The paper From Datalog to Flix: A Declarative Language for Fixed Points on Lattices is

Get Started with Flix

Requires the Java Runtime Environment 1.8

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Documentation





© Running

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Compiler ▼

Performance ▼

 ${\mathcal Z}$ Refresh

Performance / Rules

Flix Debugger Minimal Model -

← → C 🗋 localhost:8000/#

The table shows the number of miliseconds spent in evaluation of each rule.

Location	Rule	Hits	Total Time (msec)	Latency (msec/op)	Throughput (ops/msec)
SUopt.flix:102:1	SU(12,a,t) :- CFG(11, 12), $SU(11,a,t)$, $killNot(a, k)$, $Kill(12,k)$.	918,300	18,582 msec	0.0202 msec/op	49 ops/msec
SUopt.flix:86:1	$Pt(p,b) \ :- \ Load(l,p,q), \ Pt(q,a), \ filter(t, \ b), \ PtH(a,b), \ SU(l,a,t).$	930,051	3,745 msec	0.0040 msec/op	248 ops/msec
SUopt.flix:101:1	SU(12,a,t) :- CFG(11, 12), SU(11,a,t), Multi(a).	915,193	3,245 msec	0.0035 msec/op	282 ops/msec
SUopt.flix:112:1	SU(l,a,f(b)) :- Clear(l), PtH(a,b).	810	784 msec	0.9679 msec/op	1 ops/msec
SUopt.flix:118:1	Kill(1, top(42)) :- Phi(1,_,_).	1	133 msec	133.0000 msec/op	0 ops/msec
SUopt.flix:79:1	SU(1,a,f(b)) :- Store(1,p,q), $Pt(p,a)$, $Pt(q,b)$.	28,099	62 msec	0.0022 msec/op	453 ops/msec
SUopt.flix:81:1	PtH(a,b) :- Store(1,p,q), Pt(p,a), Pt(q,b).	28,099	50 msec	0.0018 msec/op	562 ops/msec
SUopt.flix:87:1	$Pt(p,b)$:- $FILoad(p,q,_)$, $Pt(q,a)$, $PtH(a,b)$.	14,859	27 msec	0.0018 msec/op	550 ops/msec
SUopt.flix:82:1	PtH(a,b) :- FIStore(p,q,_), Pt(p,a), Pt(q,b).	28,099	25 msec	0.0009 msec/op	1,124 ops/msec
SUopt.flix:74:1	Pt(p,a) :- $Copy(p,q)$, $Pt(q,a)$.	14,050	23 msec	0.0016 msec/op	611 ops/msec
SUopt.flix:70:1	Pt(p,a) :- AddrOf(p,a).	1	17 msec	17.0000 msec/op	0 ops/msec
SUopt.flix:117:1	<pre>Kill(l,f(b)) :- Store(l,p,q), Pt(p,b).</pre>	14,050	14 msec	0.0010 msec/op	1,004 ops/msec

What's in the paper: MATH

- From Datalog to Flix semantics:
 - explains the relationship between Datalog and Flix.
 - develops the model-theoretic semantics of Flix.
- Presents semi-naïve evaluation for Flix:
 - the basis for efficient Datalog and Flix solvers.
- Experimental results and details of analyses:
 - the Strong Update analysis, and
 - the IFDS Alias-Set analysis.

Summary: Flix!

- A new declarative and functional programming language for fixed point computations on lattices.
- Inspired by Datalog and extended with lattices and monotone transfer/filter functions.
- Implementation freely available:

http://github.com/flix

Documentation and more information:

http://flix.github.io

Thank You!

