

# Machine Learning and Computational Physics

## Fall 2020

### Assignment 4

Due: October 19<sup>th</sup> 2020, 11:59:59 PM PDT

### Backpropagation of second derivatives

In class notes we recognized that in order to solve higher-order PDEs using deep neural networks we need to evaluate the second derivative of the output layer with respect to the input layer. This can be done by developing a backpropagation algorithm for the second derivatives which relates the second derivative wrt. the output of layer ( $l$ ) to the second derivative wrt. to the output of layer ( $l+1$ ). That is we need a formula like:

$$\frac{\partial^2(\cdot)}{\partial x_k^{(l)} \partial x_i^{(l)}} = \sum_j A_{ikj}^{(l+1)} \frac{\partial(\cdot)}{\partial x_j^{(l+1)}} + \sum_{j,m} B_{ikjm}^{(l+1)} \frac{\partial^2(\cdot)}{\partial x_j^{(l+1)} \partial x_m^{(l+1)}}. \quad (1)$$

Using the notes in the class find an expression for  $A_{ikj}^{(l+1)}$  and  $B_{ikjm}^{(l+1)}$  in terms of the weights of the ( $l+1$ ) layer and the derivatives of the activation function.