
**11-442 / 11-642 / 11-742:
Search Engines**

Diversity

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Topic Outline

- **Introduction**
- **Diversity Evaluation Metrics**
- **Implicit Methods**
 - Maximum Marginal Relevance (MMR)
 - Learning to Rank for diversification
- **Explicit Methods**
 - Query intents (subtopics) discovery
 - xQuAD
 - PM-2

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Explicit Query Intents

Some diversification methods assume that query intents are known

- Query intents are explicit

How can query intents be known?

- Analysis of search logs (covered in a few weeks)

How can this problem be studied without search logs?

- Query intents provided by TREC (which got them from Bing)
- Query intents inferred from commercial search engine suggestions

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Explicit Query Intents: The TREC Web Track Diversity Task

The 2009-2014 TREC Web Tracks had a diversity task

- Intended to encourage research on diversification

Each year, 50 information needs were created

- Most information needs had multiple intents
 - Ambiguous: Unrelated interpretations of the query
 - Faceted: Related interpretations of the query
- Information needs with multiple intents had two types of intents
 - Navigational
 - Informational

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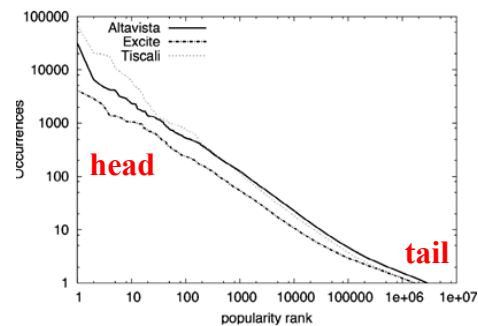
Explicit Query Intents: TREC Information Needs

Queries were manually chosen from Bing's search log

- Picked from median queries (by frequency)
 - Head queries are too easy
 - Tail queries are too rare

Subtopic generation process

- Cluster Bing's query log,
- Manually pick queries from top clusters



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Explicit Query Intents: TREC Information Needs

Topic 15, type=ambiguous

- **Query:** espn sports
- **Description:** I'm looking for various sports scores and information from the ESPN Sports site.
- **Subtopic, type=nav:** The ESPN Sports home page.
- **Subtopic, type=inf:** College football and basketball scores.
- **Subtopic, type=inf:** NBA basketball standings.
- **Subtopic, type=inf:** Baseball scores and information on upcoming live broadcast games.
- **Subtopic, type=inf:** Information on NASCAR races.
- **Subtopic, type=inf:** Fantasy football leagues.

nav: navigational
inf: informational

(<http://trec.nist.gov/data/web/09/wt09.topics.full.xml>)

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Explicit Query Intents: TREC Information Needs

Topic 1, type=faceted

nav: navigational
inf: informational

- **Query:** obama family tree
- **Description:** Find information on President Barack Obama's family history, including genealogy, national origins, places and dates of birth, etc.
- **Subtopic, type=nav:** Find the TIME magazine photo essay "Barack Obama's Family Tree".
- **Subtopic, type=inf:** Where did Barack Obama's parents and grandparents come from?
- **Subtopic, type=inf:** Find biographical information on Barack Obama's mother.

(<http://trec.nist.gov/data/web/09/wt09.topics.full.xml>)

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Explicit Query Intents: TREC Information Needs

Note the two types of topics

- **Ambiguous:** Unrelated interpretations of the query
 - E.g., “michael jordan”, “avp”, “espn sports”
- **Faceted:** Related interpretations of the query
 - E.g., “carnegie mellon university”, “arizona game and fish”, “obama family tree”

Different types might require different methods

- TREC hoped to focus attention on this problem
- A difficult problem, mostly ignored by researchers (so far)

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Explicit Query Intents: TREC Information Needs

In TREC evaluations, the search engine does not know the multiple intents for an information need

- It sees only the query, e.g., “espn sports”
- The assessor knows the different intents
 - Used to form relevance assessments

What information can your search engine use to diversify the ranking?

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Explicit Query Intents: Commercial Search Engines

Google and Bing provide suggested and related queries

- Probably they indicate common search intents

Query suggestions

Related queries

espn	espn s	espn sports
espn	espn scores	espn sports center
espn3	espn sports	espn sportsnation
espn fantasy	espn soccer	espn sports science
espn mlb	espn schedule	

Searches related to espn sports

espn boxing	espn soccer
fox sports	espn sports golf
espn sports live	yahoo sports
espn scores	cbs sports

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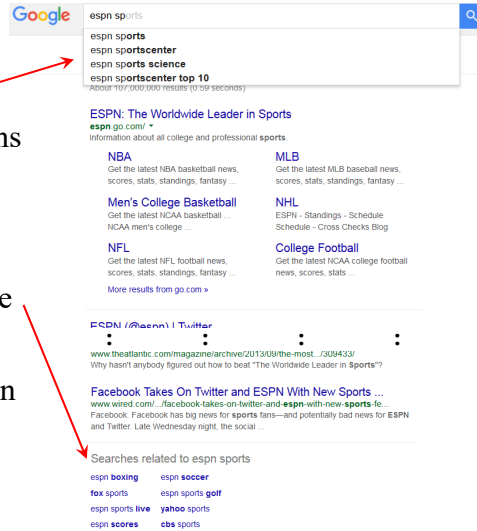
Explicit Query Intents: Commercial Search Engines

Suggested queries

- Appear at the top of the page
- Often prefix-oriented suggestions
 - High precision, low recall

Related queries

- Appear at the bottom of the page
- A wider range of suggestions
 - Higher recall, lower precision



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Explicit Query Intents: Commercial Search Engines

Suggested and related queries produced by three web search engines

Search Engine	Query Type	Avg # of Queries	Avg Query Length	Avg # of Matched Pages
A	related	7.4	2.9	10.4 M
	suggested	6.7	3.0	8.6 M
B	related	9.7	2.6	10.3 M
	suggested	9.3	3.3	7.1 M
C	related	15.9	1.8	18.1 M
	suggested	8.9	3.3	9.5 M

- An average of 14-25 short suggested and related queries

(Santos, et al., 2010)

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Explicit Query Intents: Automatic Generation

How can query intents be generated without a query log?

- Only large search companies have large query logs
- Even Google doesn't have much information about tail queries

This topic is challenging for several reasons

- Query intents are very personal
 - Different people have different interpretations
- There are many possible subtopics
 - Which ones does the gold standard want?
- There are many types of subtopics
 - E.g. ambiguous vs. facets vs. tasks
- Which ones does the gold standard want?

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Explicit Query Intents: Automatic Generation

Many methods have been proposed

- Common ideas
 - Cluster top retrieved documents
 - » By text, URL, keywords, etc.
 - Topic modeling on top retrieved documents
 - Pick diversified terms from search result page using existing document summarization tools
- None of them are convincing
 - E.g., not nearly as effective as Google suggestions
- Still an open research topic

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xQuAD

eXplicit Query Aspect Diversification (xQuAD)

- **Inputs**
 - An initial ranking
 - A set of query intents (e.g., from search engine suggestions)
- **Observation:** A single document may cover multiple intents
 - More likely to be true for faceted queries
- **Key idea:** Select documents that satisfy as many uncovered intents as possible
 - Provide maximum coverage and minimum redundancy
 - MMR did this implicitly – xQuAD does it explicitly

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(Santos, et al., 2010)
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xQuAD

xQuAD(q, R, τ, λ)

```
1  $S \leftarrow \emptyset$ 
2 while  $|S| < \tau$  do
3    $d^* \leftarrow \arg \max_{d \in R \setminus S} (1 - \lambda) P(d|q) + \lambda P(d, \bar{S}|q)$ 
4    $R \leftarrow R \setminus \{d^*\}$ 
5    $S \leftarrow S \cup \{d^*\}$ 
6 end while
7 return  $S$ 
```

Relevance **Diversity**

Remove d^* from the initial ranking
Add d^* to the diversified ranking

R : Initial ranking (produced by some other method)

S : Diversified ranking (initially empty)

τ : Desired length of diversified ranking

λ : Balance between relevance and diversity

(Santos, et al., 2010)

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Diversity Notation Alert

Earlier lectures defined q_i as the i^{th} term of query q

- q : search engines course
- q_2 : 'engines'

This lecture defines q_i as the i^{th} intent of query q

- q : michael jordan
- q_2 : The Berkeley professor Michael Jordan

This is how notation is used in most of the published work

- I'm sorry – don't be confused

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xQuAD

xQuAD's selection criteria: $(1 - \lambda) P(d|q) + \lambda P(d, \bar{S}|q)$
Relevance Diversity

Make some assumptions

- A query q has intents specified by subqueries $\{q_1, \dots, q_k\}$
- Independence assumptions

xQuAD's diversity component becomes:

$$P(d, \bar{S}|q) = \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

↑

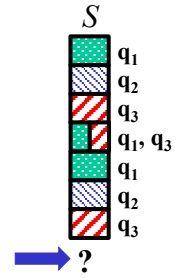
Intent weight

↑

Score of d for intent q_i

⏟

How well S already covers intent q_i



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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank_{init}

$d_1, 0.70$

$d_2, 0.69$

$d_3, 0.68$

$d_4, 0.67$

$d_5, 0.66$

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank_{init}	q₁	q₂
d ₁ , 0.70,	0.7,	0.2

$p(q_i|q)=0.5$

 $d_2, 0.69, 0.8, 0.1$ $d_3, 0.68, 0.6, 0.3$ $d_4, 0.67, 0.2, 0.7$ $d_5, 0.66, 0.3, 0.8$

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank_{init} **q₁** **q₂**
d₁, 0.70, 0.7, 0.2

$p(q_i|q)=0.5$

d ₂ , 0.69,	0.8,	0.1
------------------------	------	-----

$$d_3, 0.68, 0.6, 0.3$$
$$d_4, 0.67, 0.2, 0.7$$

$d_5, 0.66, 0.3, 0.8$

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank _{init}	q ₁	q ₂	xQuAD Scores	p(q _i q)=0.5 λ=0.4
d ₁ , 0.70,	0.7,	0.2	0.6×0.70 + 0.4×[½×0.7 + ½×0.2] = 0.600	
d ₂ , 0.69,	0.8,	0.1	0.6×0.69 + 0.4×[½×0.8 + ½×0.1] = 0.594	
d ₃ , 0.68,	0.6,	0.3	0.6×0.68 + 0.4×[½×0.6 + ½×0.3] = 0.588	
d ₄ , 0.67, 0.2,		0.7	0.6×0.67 + 0.4×[½×0.2 + ½×0.7] = 0.582	
d ₅ , 0.66, 0.3,		0.8	0.6×0.66 + 0.4×[½×0.3 + ½×0.8] = 0.616	

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank _{init}	q ₁	q ₂	rank _{div}	p(q _i q)=0.5 λ=0.4
d ₁ , 0.70,	0.7,	0.2	d ₅	
d ₂ , 0.69,	0.8,	0.1		
d ₃ , 0.68,	0.6,	0.3		
d ₄ , 0.67, 0.2,		0.7		
d ₅ , 0.66, 0.3,		0.8		

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank _{init}	q ₁	q ₂	rank _{div}	xQuAD Scores
d ₁ , 0.70,	0.7,	0.2	d ₅	0.6×0.70 + 0.4×[½×0.7(1-0.3) + ½×0.2(1-0.8)] = 0.526
d ₂ , 0.69,	0.8,	0.1		0.6×0.69 + 0.4×[½×0.8(1-0.3) + ½×0.1(1-0.8)] = 0.530
d ₃ , 0.68,	0.6,	0.3		0.6×0.68 + 0.4×[½×0.6(1-0.3) + ½×0.3(1-0.8)] = 0.504
d ₄ , 0.67,	0.2,	0.7		0.6×0.67 + 0.4×[½×0.2(1-0.3) + ½×0.7(1-0.8)] = 0.458
d ₅ , 0.66,	0.3,	0.8		

p(q_i|q)=0.5
λ=0.4

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank _{init}	q ₁	q ₂	rank _{div}
d ₁ , 0.70,	0.7,	0.2	d ₅
d ₂ , 0.69,	0.8,	0.1	d ₂
d ₃ , 0.68,	0.6,	0.3	
d ₄ , 0.67,	0.2,	0.7	
d ₅ , 0.66,	0.3,	0.8	

p(q_i|q)=0.5
λ=0.4

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xQuAD Example:				
$(1 - \lambda) P(d q) + \lambda \sum_{q_i \in Q} \left[P(q_i q) P(d q_i) \prod_{d_j \in S} (1 - P(d_j q_i)) \right]$				
rank _{init}	q ₁	q ₂	rank _{div}	xQuAD Scores
d ₁ , 0.70,	0.7,	0.2	d ₅	0.6×0.70 + 0.4×[½×0.7(1-0.3)(1-0.8) + ½×0.2(1-0.8)(1-0.1)] = 0.4468
d ₂ , 0.69,	0.8,	0.1	d ₂	
d ₃ , 0.68,	0.6,	0.3		0.6×0.68 + 0.4×[½×0.6(1-0.3)(1-0.8) + ½×0.3(1-0.8)(1-0.1)] = 0.4356
d ₄ , 0.67,	0.2,	0.7		0.6×0.67 + 0.4×[½×0.2(1-0.3)(1-0.8) + ½×0.7(1-0.8)(1-0.1)] = 0.4328
d ₅ , 0.66,	0.3,	0.8		

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xQuAD Example:				
$(1 - \lambda) P(d q) + \lambda \sum_{q_i \in Q} \left[P(q_i q) P(d q_i) \prod_{d_j \in S} (1 - P(d_j q_i)) \right]$				
rank _{init}	q ₁	q ₂	rank _{div}	
d ₁ , 0.70,	0.7,	0.2	d ₅	
d ₂ , 0.69,	0.8,	0.1	d ₂	
d ₃ , 0.68,	0.6,	0.3	d ₁	
d ₄ , 0.67,	0.2,	0.7		
d ₅ , 0.66,	0.3,	0.8		

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xQuAD Example:				
$(1 - \lambda) P(d q) + \lambda \sum_{q_i \in Q} \left[P(q_i q) P(d q_i) \prod_{d_j \in S} (1 - P(d_j q_i)) \right]$				
rank _{init}	q ₁	q ₂	rank _{div}	xQuAD Scores
d ₁ , 0.70,	0.7,	0.2	d ₅	
d ₂ , 0.69,	0.8,	0.1	d ₂	
d ₃ , 0.68,	0.6,	0.3	d ₁	0.6×0.68 + 0.4×[$\frac{1}{2}$ ×0.6(1-0.3)(1-0.8)(1-0.7) + $\frac{1}{2}$ ×0.3(1-0.8)(1-0.1)(1-0.2)] = 0.4217
d ₄ , 0.67,	0.2,	0.7		0.6×0.67 + 0.4×[$\frac{1}{2}$ ×0.2(1-0.3)(1-0.8)(1-0.7) + $\frac{1}{2}$ ×0.7(1-0.8)(1-0.1)(1-0.2)] = 0.4238
d ₅ , 0.66,	0.3,	0.8		

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xQuAD Example:				
$(1 - \lambda) P(d q) + \lambda \sum_{q_i \in Q} \left[P(q_i q) P(d q_i) \prod_{d_j \in S} (1 - P(d_j q_i)) \right]$				
rank _{init}	q ₁	q ₂	rank _{div}	
d ₁ , 0.70,	0.7,	0.2	d ₅	
d ₂ , 0.69,	0.8,	0.1	d ₂	
d ₃ , 0.68,	0.6,	0.3	d ₁	
d ₄ , 0.67,	0.2,	0.7	d ₄	
d ₅ , 0.66,	0.3,	0.8		

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xQuAD Example:

$$(1 - \lambda) P(d|q) + \lambda \sum_{q_i \in Q} \left[P(q_i|q) P(d|q_i) \prod_{d_j \in S} (1 - P(d_j|q_i)) \right]$$

rank _{init}	q ₁	q ₂	rank _{div}
d ₁ , 0.70,	0.7,	0.2	d ₅
d ₂ , 0.69,	0.8,	0.1	d ₂
d ₃ , 0.68,	0.6,	0.3	d ₁
d ₄ , 0.67,	0.2,	0.7	d ₄
d ₅ , 0.66,	0.3,	0.8	

p(q_i|q)=0.5
λ=0.4

Repeat until all documents
in the initial ranking
are added to
the diversified ranking

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xQuAD Behavior

xQuAD prefers documents that satisfy multiple intents

rank_{init}

d₁, 0.70

d₂, 0.69

d₃, 0.68

d₄, 0.67

d₅, 0.66

d₆, 0.65

d₇, 0.64

d₈, 0.63

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xQuAD Behavior

$$p(q_i|q)=0.5$$
$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

rank _{init}	q ₁	q ₂
d ₁ , 0.70,	0.7,	0.1
d ₂ , 0.69,	0.7,	0.2
d ₃ , 0.68,	0.4,	0.5
d ₄ , 0.67,	0.5,	0.4
d ₅ , 0.66,	0.5,	0.5
d ₆ , 0.65,	0.5,	0.5
d ₇ , 0.64,	0.1,	0.7
d ₈ , 0.63,	0.1,	0.9

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xQuAD Behavior

$$p(q_i|q)=0.5$$
$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

rank _{init}	q ₁	q ₂
d ₁ , 0.70,	0.7,	0.1
d ₂ , 0.69,	0.7,	0.2
d ₃ , 0.68,	0.4,	0.5
d ₄ , 0.67,	0.5,	0.4
d ₅ , 0.66,	0.5,	0.5
d ₆ , 0.65,	0.5,	0.5
d ₇ , 0.64,	0.1,	0.7
d ₈ , 0.63,	0.1,	0.9

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xQuAD Behavior

$$p(q_i|q)=0.5$$

$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

	rank _{init}	q ₁	q ₂	rank ₁
d ₁	0.70,	0.7,	0.1	0.580
d ₂	0.69,	0.7,	0.2	0.594
d ₃	0.68,	0.4,	0.5	0.588
d ₄	0.67,	0.5,	0.4	0.582
d ₅	0.66,	0.5,	0.5	0.596
d ₆	0.65,	0.5,	0.5	0.590
d ₇	0.64,	0.1,	0.7	0.544
d ₈	0.63,	0.1,	0.9	0.578

Selecting
the first
document

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xQuAD Behavior

$$p(q_i|q)=0.5$$

$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

	rank _{init}	q ₁	q ₂	rank ₁	rank ₂
d ₁	0.70,	0.7,	0.1	0.580	0.500
d ₂	0.69,	0.7,	0.2	0.594	0.504
d ₃	0.68,	0.4,	0.5	0.588	0.498
d ₄	0.67,	0.5,	0.4	0.582	0.492
d ₅	0.66,	0.5,	0.5	0.596	
d ₆	0.65,	0.5,	0.5	0.590	0.490
d ₇	0.64,	0.1,	0.7	0.544	0.464
d ₈	0.63,	0.1,	0.9	0.578	0.478

Selecting
the second
document

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xQuAD Behavior

$$p(q_i|q)=0.5$$

$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

	rank _{init}	q ₁	q ₂	rank ₁	rank ₂	rank ₃
d ₁	0.70,	0.7,	0.1	0.580	0.500	0.449
d ₂	0.69,	0.7,	0.2	0.594	0.504	
d ₃	0.68,	0.4,	0.5	0.588	0.498	0.460
d ₄	0.67,	0.5,	0.4	0.582	0.492	0.449
d ₅	0.66,	0.5,	0.5	0.596		
d ₆	0.65,	0.5,	0.5	0.590	0.490	0.445
d ₇	0.64,	0.1,	0.7	0.544	0.464	0.443
d ₈	0.63,	0.1,	0.9	0.578	0.478	0.453

Selecting
the third
document

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xQuAD Behavior

$$p(q_i|q)=0.5$$

$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

	rank _{init}	q ₁	q ₂	rank ₁	rank ₂	rank ₃	rank ₄
d ₁	0.70,	0.7,	0.1	0.580	0.500	0.449	0.437
d ₂	0.69,	0.7,	0.2	0.594	0.504		
d ₃	0.68,	0.4,	0.5	0.588	0.498	0.460	
d ₄	0.67,	0.5,	0.4	0.582	0.492	0.449	0.427
d ₅	0.66,	0.5,	0.5	0.596			
d ₆	0.65,	0.5,	0.5	0.590	0.490	0.445	0.419
d ₇	0.64,	0.1,	0.7	0.544	0.464	0.443	0.414
d ₈	0.63,	0.1,	0.9	0.578	0.478	0.453	0.416

Selecting
the fourth
document

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xQuAD Behavior

$$p(q_i|q)=0.5$$

$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

	rank _{init}	q ₁	q ₂	rank ₁	rank ₂	rank ₃	rank ₄	rank ₅
d ₁	0.70,	0.7,	0.1	0.580	0.500	0.449	0.437	
d ₂	0.69,	0.7,	0.2	0.594	0.504			
d ₃	0.68,	0.4,	0.5	0.588	0.498	0.460		
d ₄	0.67,	0.5,	0.4	0.582	0.492	0.449	0.427	0.419
d ₅	0.66,	0.5,	0.5	0.596				
d ₆	0.65,	0.5,	0.5	0.590	0.490	0.445	0.419	0.411
d ₇	0.64,	0.1,	0.7	0.544	0.464	0.443	0.414	0.410
d ₈	0.63,	0.1,	0.9	0.578	0.478	0.453	0.416	0.411

Selecting
the fifth
document

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xQuAD Behavior

$$p(q_i|q)=0.5$$

$$\lambda=0.4$$

xQuAD prefers documents that satisfy multiple intents

	rank _{init}	q ₁	q ₂	rank ₁	rank ₂	rank ₃	rank ₄	rank ₅
d ₁	0.70,	0.7,	0.1	0.580	0.500	0.449	0.437	
d ₂	0.69,	0.7,	0.2	0.594	0.504			
d ₃	0.68,	0.4,	0.5	0.588	0.498	0.460		
d ₄	0.67,	0.5,	0.4	0.582	0.492	0.449	0.427	0.419
d ₅	0.66,	0.5,	0.5	0.596				
d ₆	0.65,	0.5,	0.5	0.590	0.490	0.445	0.419	0.411
d ₇	0.64,	0.1,	0.7	0.544	0.464	0.443	0.414	0.410
d ₈	0.63,	0.1,	0.9	0.578	0.478	0.453	0.416	0.411

q₂ is covered by mediocre documents that also cover q₁, so d₇ and d₈ don't get promoted

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xQuAD

Santos, et al investigated three methods of weighting queries

- Uniform weights: $1 / |Q|$
- A method similar to the CRCS resource ranking algorithm
 - In a later lecture we will cover ReDDE, a similar algorithm
 - Related to the number of top-ranked documents q_i matches
- Based on the relative number of documents it matches in a commercial search engine
 - $n_w(q_i)$ on an earlier slide

Uniform was the most effective on TREC 2009 data

- Perhaps because TREC intents are all weighted equally

(Santos, et al., 2010)

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xQuAD

Effectiveness when using TREC intents (the gold standard)

	α -NDCG			IA-P		
	@5	@10	@100	@5	@10	@100
BM25	0.159	0.186	0.288	0.075	0.071	0.059
+MMR	0.120	0.150	0.224	0.056	0.058	0.039
+Q-Filter	0.159	0.186	0.286	0.075	0.071	0.057
+IA-Select	0.110	0.119	0.180	0.043	0.037	0.023
+xQuAD _u	0.208	0.227	0.324	0.080	0.075	0.056
DPH	0.198	0.212	0.304	0.109	0.106	0.062
+MMR	0.195	0.211	0.303	0.105	0.103	0.062
+Q-Filter	0.198	0.212	0.303	0.109	0.106	0.060
+IA-Select	0.148	0.157	0.203	0.077	0.071	0.023
+xQuAD _u	0.208	0.243	0.334	0.097	0.096	0.061

Initial ranking

Initial ranking

ClueWeb09-B (50 queries from 2009)

(Santos, et al., 2010)

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xQuAD

Searches related to espn sports

espn boxing espn soccer
fox sports espn sports golf
espn sports live yahoo sports
espn scores cbs sports

Effectiveness when using search engine queries as intents

		related sub-queries					
		α -NDCG			IA-P		
	WSE	@5	@10	@100	@5	@10	@100
BM25		0.159	0.186	0.288	0.075	0.071	0.059
+xQuAD _u	A	0.154	0.184	0.282	0.070	0.072	0.057
+xQuAD _u	B	0.154	0.182	0.279	0.073	0.076	0.054
+xQuAD _u	C	0.161	0.182	0.285	0.076	0.076	0.057
DPH		0.198	0.212	0.304	0.109	0.106	0.062
+xQuAD _u	A	0.164	0.189	0.288	0.086	0.083	0.056
+xQuAD _u	B	0.186	0.205	0.295	0.090	0.082	0.057
+xQuAD _u	C	0.206	0.209	0.307	0.108	0.090	0.062

Initial ranking

Initial ranking

ClueWeb09-B (50 queries from 2009)

Related queries (from web search engines A, B, and C) provide little benefit

(Santos, et al., 2010)

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xQuAD

espn
espn s
espn scores
espn sports
espn fantasy
espn soccer
espn schedule
espn sports
espn sports center
espn sportsnation
espn sports science

Effectiveness when using search engine queries as intents

		suggested sub-queries					
		α -NDCG			IA-P		
	WSE	@5	@10	@100	@5	@10	@100
BM25		0.159	0.186	0.288	0.075	0.071	0.059
+xQuAD _u	A	0.171	0.186	0.291	0.082	0.071	0.053
+xQuAD _u	B	0.129	0.158	0.261	0.065	0.067	0.052
+xQuAD _u	C	0.163	0.184	0.287	0.084	0.069	0.053
DPH		0.198	0.212	0.304	0.109	0.106	0.062
+xQuAD _u	A	0.215	0.222	0.313	0.108	0.088	0.055
+xQuAD _u	B	0.162	0.189	0.281	0.088	0.085	0.055
+xQuAD _u	C	0.201	0.236	0.320	0.093	0.092	0.059

Initial ranking

Initial ranking

ClueWeb09-B (50 queries from 2009)

Suggested queries (from some engines) are more effective

(Santos, et al., 2010)

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xQuAD

Effectiveness when using search engine queries (Bing) as intents

S_q		ERR-IA				α -nDCG			
		@20	-	=	+	@20	-	=	+
DPH		0.253				0.364			
+MMR		0.253 ^{oo}	55	30	60	0.367 ^{o∇}	56	28	61
+PC	BS	0.256 ^{▲o}	25	58	62	0.375 ^{▲∇}	29	55	61
+IA-Select	DZ	0.250 ^{oo}	67	12	66	0.356 ^{o∇}	70	12	63
+xQuAD	BS	<u>0.281^o</u>	40	24	81	<u>0.402[▲]</u>	37	24	84
LeToR	LambdaMART	0.337				0.464			
+MMR		0.338 ^{oo}	69	20	56	0.466 ^{oo}	69	20	56
+PC	BS	0.339 ^{▲o}	27	52	66	0.472 ^{▲o}	32	45	68
+IA-Select	DZ	0.217 ^{▼▼}	93	13	39	0.329 ^{▼▼}	98	13	34
+xQuAD	BS	<u>0.351[△]</u>	43	24	78	<u>0.479[▲]</u>	42	23	80

Initial ranking

Initial ranking

(ClueWeb09-B, 145 TREC queries from 2009-2011)

(Santos, et al., 2010)

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xQuAD

xQuAD characteristics

- Requires a set of explicit query intents
- Allows a single document to satisfy multiple query intents
 - Those documents are more likely to be ranked highly
- The diversified ranking covers each intent equally
 - Weighting is possible, but uniform weights were best
- Each query q requires running queries q and $\{q_1, \dots, q_k\}$
 - 7-10 queries in Santos, et al's experiments
 - Thus a little expensive computationally
- One of the more effective methods available today

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Topic Outline

- Introduction
- Diversity Evaluation Metrics
- Implicit Methods
 - Maximum Marginal Relevance (MMR)
 - Learning to Rank for diversification
- **Explicit Methods**
 - Query intents (subtopics) discovery
 - xQuAD
 - PM-2

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PM-2

Proportionality Model 2 (PM-2)

- **Inputs**
 - An initial ranking
 - A set of query intents (e.g., from search engine suggestions)
- **Observation:** A high Recall algorithm for discovering query intents would find many rare or unpopular intents
 - They shouldn't get equal coverage in a diversified ranking
- **Key idea:** The number of documents for each subtopic should be proportional to each subtopic's popularity
 - Minimizes redundancy
 - Coverage of subtopics may better match a person's expectation

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(Dang and Croft, 2012)
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PM-2

PM-2 is an adaptation of the Sainte-Laguë method of assigning proportional representation in elections

- It is a greedy algorithm
- At each rank r
 - Select the query intent q_i that must be covered next to maintain proportional coverage of intents in the ranking
 - Select a document d that covers intent q_i
 - » And, maybe also covers other query intents
 - Remove d from the initial ranking R
 - Assign d to the diversified ranking S

A document may cover multiple intents to varying degrees

(Dang and Croft, 2012)
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PM-2

$$\forall i, v_i = \frac{\text{Diversified Ranking Size}}{\text{Number Of Intents}}, s_i = 0$$

for all $s \in S$

$$\forall q_i \in Q, qt[i] = \frac{v_i}{2s_i + 1}$$

$$i^* = \arg \max_i qt[i]$$

$$d^* = \arg \max_{d_j \in R} (\lambda qt[i^*]p(d_j|q_{i^*}) + (1 - \lambda) \sum_{i \neq i^*} qt[i]p(d_j|q_i))$$

$$S = S \cup \{d^*\}$$

$$R = R \setminus \{d^*\}$$

$$\forall q_i \in Q, s_i = s_i + \frac{p(d^*|q_i)}{\sum_{q_j \in Q} p(d^*|q_j)}$$

end for

v_i : desired ranks in S for q_i
 s_i : ranks in S assigned to q_i now

s : a rank in S to be filled

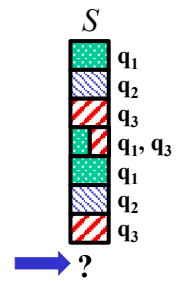
Priority of each intent now

i^* : The intent to cover now

Covers q_{i^*}

Also covers other intents

Update coverage of each intent



(Dang and Croft, 2012)
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$$V(i, n_i) = \frac{\text{Desired Ranking Size}}{\text{Number of Items}} - n_i = 0$$

$$\text{for all } i \in I$$

$$v_{q_i} \in Q, v_{q_i} = \frac{n_i}{|Q| + 1}$$

$$r^* = \arg\max_{q \in Q} v_{q_i}$$

$$d^* = \arg\max_{q \in Q} (v_{q_i} \cdot \ln(d_i(n_i)) + (1 - \lambda) \sum_{q \in Q} v_{q_i} \ln(d_i(n_i)))$$

$$S = S \cup \{d^*\}$$

$$R = R \cup \{d^*\}$$

$$v_{q_i} \in Q, n_i = n_i + \frac{d^*(n_i)}{\sum_{q \in Q} d^*(n_i)}$$

$$\text{end for}$$

PM-2 Example

rank _{init}	q ₁	q ₂
d ₁ , 0.70,	0.7,	0.2
d ₂ , 0.69,	0.8,	0.1
d ₃ , 0.68,	0.6,	0.3
d ₄ , 0.67,	0.2,	0.7
d ₅ , 0.66,	0.3,	0.8

Initialization

Example assumptions

- $p(q_i|q)=0.5$
- Ranking depth=8

v[1] = 0.5×8 = 4 “votes”
v[2] = 0.5×8 = 4

s[1] = 0 “ranks (slots) assigned so far”
s[2] = 0

λ=0.6

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$$V(i, n_i) = \frac{\text{Desired Ranking Size}}{\text{Number of Items}} - n_i = 0$$

$$\text{for all } i \in I$$

$$v_{q_i} \in Q, v_{q_i} = \frac{n_i}{|Q| + 1}$$

$$r^* = \arg\max_{q \in Q} v_{q_i}$$

$$d^* = \arg\max_{q \in Q} (v_{q_i} \cdot \ln(d_i(n_i)) + (1 - \lambda) \sum_{q \in Q} v_{q_i} \ln(d_i(n_i)))$$

$$S = S \cup \{d^*\}$$

$$R = R \cup \{d^*\}$$

$$v_{q_i} \in Q, n_i = n_i + \frac{d^*(n_i)}{\sum_{q \in Q} d^*(n_i)}$$

$$\text{end for}$$

PM-2 Example

rank _{init}	q ₁	q ₂
d ₁ , 0.70,	0.7,	0.2
d ₂ , 0.69,	0.8,	0.1
d ₃ , 0.68,	0.6,	0.3
d ₄ , 0.67,	0.2,	0.7
d ₅ , 0.66,	0.3,	0.8

Quotient scores

qt[1] = 4 / (2×0+1) = 4
qt[2] = 4 / (2×0+1) = 4

i* = 1 “selected intent”

λ=0.6

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$$V_i, n_i = \frac{\text{Discretized Ranking Size}}{\text{Number Of Items}} \dots n_i = 0$$
 for all $i \in I$

$$v_{ij} \in [0, \varphi(i)] = \frac{r_{ij}}{n_i + 1}$$

$$r^i = \argmax_j \varphi(i)$$

$$d^i = \argmax_{j \in I} (v_{ij}^2 \ln(d_j/n_i) + (1 - v_{ij}) \sum_{k \in I} v_{ik} \ln(d_k/n_i))$$

$$S = S \cup \{d^i\}$$

$$R = R \cup \{d^i\}$$

$$v_{ij} \in [0, n_i] = n_i + \frac{d^i(r_{ij}^2)}{d_j + d^i(r_{ij}^2)}$$
 end for

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	PM2 Scores
$d_1, 0.70,$	0.7	0.2	$0.6 \times 4 \times 0.7 + 0.4 \times 4 \times 0.2 = 2.00$
$d_2, 0.69,$	0.8	0.1	$0.6 \times 4 \times 0.8 + 0.4 \times 4 \times 0.1 = 2.08$
$d_3, 0.68,$	0.6	0.3	$0.6 \times 4 \times 0.6 + 0.4 \times 4 \times 0.3 = 1.92$
$d_4, 0.67,$	0.2	0.7	$0.6 \times 4 \times 0.2 + 0.4 \times 4 \times 0.7 = 1.60$
$d_5, 0.66,$	0.3	0.8	$0.6 \times 4 \times 0.3 + 0.4 \times 4 \times 0.8 = 2.00$

$\lambda=0.6$

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$$V_i, n_i = \frac{\text{Discretized Ranking Size}}{\text{Number Of Items}} \dots n_i = 0$$
 for all $i \in I$

$$v_{ij} \in [0, \varphi(i)] = \frac{r_{ij}}{n_i + 1}$$

$$r^i = \argmax_j \varphi(i)$$

$$d^i = \argmax_{j \in I} (v_{ij}^2 \ln(d_j/n_i) + (1 - v_{ij}) \sum_{k \in I} v_{ik} \ln(d_k/n_i))$$

$$S = S \cup \{d^i\}$$

$$R = R \cup \{d^i\}$$

$$v_{ij} \in [0, n_i] = n_i + \frac{d^i(r_{ij}^2)}{d_j + d^i(r_{ij}^2)}$$
 end for

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	Slots assigned
$d_1, 0.70,$	0.7	0.2	d_2 $s[1] += 0.8/(0.8+0.1) = 0.89$ $s[2] += 0.1/(0.8+0.1) = 0.11$
$d_2, 0.69,$	0.8	0.1	
$d_3, 0.68,$	0.6	0.3	
$d_4, 0.67,$	0.2	0.7	
$d_5, 0.66,$	0.3	0.8	

$\lambda=0.6$

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```

// Iterative Ranking Step
// Number of Iterations:  $n_1, n_2 = 0$ 
for all  $i \in I$ 
     $q_i \leftarrow 0, q_i^* \leftarrow \frac{n_1}{n_1 + n_2}$ 
     $r_i^* \leftarrow \arg\max_j q_j^*$ 
     $r_i^* \leftarrow \arg\max_{j \in I} (q_j^* \cdot \ln(d_j(n_i)) + (1 - \lambda) \sum_{k \in I} q_k \cdot \ln(d_k(n_i)))$ 
     $r_i \leftarrow r_i^* \setminus \{r_i^*\}$ 
     $R \leftarrow R \cup \{r_i^*\}$ 
     $q_i \leftarrow 0, q_i = n_1 + \frac{r_i^* \cdot \ln(d_i(n_i))}{\sum_{j \in I} q_j^* \cdot \ln(d_j(n_i))}$ 
end for

```

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	rank_{div}
$d_1, 0.70,$	0.7,	0.2	d_2
$d_2, 0.69,$	0.8,	0.1	
$d_3, 0.68,$	0.6,	0.3	
$d_4, 0.67,$	0.2,	0.7	
$d_5, 0.66,$	0.3,	0.8	

$\lambda=0.6$

Quotient scores

$qt[1] = 4 / (2 \times 0.89 + 1) = 1.44$ “quotients (priorities)”

$qt[2] = 4 / (2 \times 0.11 + 1) = 3.27$

$i^* = 2$ “selected intent”

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```

// Iterative Ranking Step
// Number of Iterations:  $n_1, n_2 = 0$ 
for all  $i \in I$ 
     $q_i \leftarrow 0, q_i^* \leftarrow \frac{n_1}{n_1 + n_2}$ 
     $r_i^* \leftarrow \arg\max_j q_j^*$ 
     $r_i^* \leftarrow \arg\max_{j \in I} (q_j^* \cdot \ln(d_j(n_i)) + (1 - \lambda) \sum_{k \in I} q_k \cdot \ln(d_k(n_i)))$ 
     $r_i \leftarrow r_i^* \setminus \{r_i^*\}$ 
     $R \leftarrow R \cup \{r_i^*\}$ 
     $q_i \leftarrow 0, q_i = n_1 + \frac{r_i^* \cdot \ln(d_i(n_i))}{\sum_{j \in I} q_j^* \cdot \ln(d_j(n_i))}$ 
end for

```

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	rank_{div}
$d_1, 0.70,$	0.7,	0.2	d_2
$d_2, 0.69,$	0.8,	0.1	
$d_3, 0.68,$	0.6,	0.3	
$d_4, 0.67,$	0.2,	0.7	
$d_5, 0.66,$	0.3,	0.8	

$\lambda=0.6$

PM2 Scores

$0.6 \times 3.27 \times 0.2 + 0.4 \times 1.44 \times 0.7 = 0.80$

$0.6 \times 3.27 \times 0.3 + 0.4 \times 1.44 \times 0.6 = 0.93$

$0.6 \times 3.27 \times 0.7 + 0.4 \times 1.44 \times 0.2 = 1.49$

$0.6 \times 3.27 \times 0.8 + 0.4 \times 1.44 \times 0.3 = 1.74$

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```

// Iterated Ranking Step
// Number of Iterations:  $n_i = 0$ 
for all  $i \in I$ 
   $q_i \leftarrow 0$ ,  $q_i^* \leftarrow \frac{r_i}{\sum_{j \in I} r_j}$ 
   $r^* \leftarrow \arg\max_i q_i$ 
   $d^* \leftarrow \arg\max_{d \in D} \{ \sum_{i \in I} q_i^* \ln(d_i / r_i) + (1 - \lambda) \sum_{i \in I} q_i \ln(d_i / r_i) \}$ 
   $S \leftarrow S \cup \{d^*\}$ 
   $R \leftarrow R \setminus \{d^*\}$ 
   $q_i \leftarrow 0$ ,  $r_i \leftarrow r_i + \frac{r_i^* q_i^*}{\sum_{j \in I} r_j^* q_j^*}$ 
end for

```

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	rank_{div}
$d_1, 0.70,$	0.7,	0.2	d_2
$d_2, 0.69,$	0.8,	0.1	d_5
$d_3, 0.68,$	0.6,	0.3	
$d_4, 0.67,$	0.2,	0.7	
$d_5, 0.66,$	0.3,	0.8	

Slots assigned

$\lambda=0.6$

$s[1] += 0.3/(0.3+0.8) = 1.16$
 $s[2] += 0.8/(0.3+0.8) = 0.84$

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```

// Iterated Ranking Step
// Number of Iterations:  $n_i = 0$ 
for all  $i \in I$ 
   $q_i \leftarrow 0$ ,  $q_i^* \leftarrow \frac{r_i}{\sum_{j \in I} r_j}$ 
   $r^* \leftarrow \arg\max_i q_i$ 
   $d^* \leftarrow \arg\max_{d \in D} \{ \sum_{i \in I} q_i^* \ln(d_i / r_i) + (1 - \lambda) \sum_{i \in I} q_i \ln(d_i / r_i) \}$ 
   $S \leftarrow S \cup \{d^*\}$ 
   $R \leftarrow R \setminus \{d^*\}$ 
   $q_i \leftarrow 0$ ,  $r_i \leftarrow r_i + \frac{r_i^* q_i^*}{\sum_{j \in I} r_j^* q_j^*}$ 
end for

```

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	rank_{div}
$d_1, 0.70,$	0.7,	0.2	d_2
$d_2, 0.69,$	0.8,	0.1	d_5
$d_3, 0.68,$	0.6,	0.3	
$d_4, 0.67,$	0.2,	0.7	
$d_5, 0.66,$	0.3,	0.8	

Quotient scores

$\lambda=0.6$

$qt[1] = 4 / (2 \times 1.16 + 1) = 1.20$ “quotients (priorities)”
 $qt[2] = 4 / (2 \times 0.84 + 1) = 1.49$

$i^* = 2$ “selected intent”

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```

// Iterated Ranking Step
// Number of Iterations: n_i = 0
for all i < I
    v_{i,1} < 0, v_{i,2} = \frac{r_i}{\sum_{j=1}^2 r_j}
    r' = argmax_j v_{i,j}
    d' = argmax_{j \in \{1,2\}} (v_{i,j} \cdot \ln(d_j / h_i)) + (1 - \lambda) \sum_{j \in \{1,2\}} v_{i,j} \ln(d_j / h_i)
    S = S \cup \{d'\}
    R = R \setminus \{d'\}
    v_{i,1} < 0, v_{i,2} = \frac{r_i}{\sum_{j \in R} r_j}
end for

```

PM-2 Example

rank _{init}	q ₁	q ₂	rank _{div}	PM2 Scores
d ₁ , 0.70,	0.7,	0.2	d ₂	0.6×1.49×0.2 + 0.4×1.20×0.7 = 0.52
d ₂ , 0.69,	0.8,	0.1	d ₅	
d ₃ , 0.68,	0.6,	0.3		0.6×1.49×0.3 + 0.4×1.20×0.6 = 0.56
d ₄ , 0.67,	0.2,	0.7		0.6×1.49×0.7 + 0.4×1.20×0.2 = 0.72
d ₅ , 0.66,	0.3,	0.8		

λ=0.6

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```

// Iterated Ranking Step
// Number of Iterations: n_i = 0
for all i < I
    v_{i,1} < 0, v_{i,2} = \frac{r_i}{\sum_{j=1}^2 r_j}
    r' = argmax_j v_{i,j}
    d' = argmax_{j \in \{1,2\}} (v_{i,j} \cdot \ln(d_j / h_i)) + (1 - \lambda) \sum_{j \in \{1,2\}} v_{i,j} \ln(d_j / h_i)
    S = S \cup \{d'\}
    R = R \setminus \{d'\}
    v_{i,1} < 0, v_{i,2} = \frac{r_i}{\sum_{j \in R} r_j}
end for

```

PM-2 Example

rank _{init}	q ₁	q ₂	rank _{div}	Slots assigned
d ₁ , 0.70,	0.7,	0.2	d ₂	s[1] = 1.16+0.2/(0.2+0.7) = 1.38 s[2] = 0.84+0.7/(0.2+0.7) = 1.62
d ₂ , 0.69,	0.8,	0.1	d ₅	
d ₃ , 0.68,	0.6,	0.3	d ₄	
d ₄ , 0.67,	0.2,	0.7		
d ₅ , 0.66,	0.3,	0.8		

λ=0.6

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$$V_i, n_i = \frac{\text{Desired Ranking Size}}{\text{Number of Intents}}, n_i = 0$$

$$\text{for all } i \in I$$

$$w_{ij} \in [0, 1], w_{ij} = \frac{r_{ij}}{r_{ij} + 1}$$

$$r^* = \arg\max_i w_{ij}$$

$$d^* = \arg\max_{i \in I} (w_{ij} \cdot \ln(d_{ij}/n_i) + (1 - \lambda) \sum_{i \in I} w_{ij} \cdot \ln(d_{ij}/n_i))$$

$$S = S \cup \{d^*\}$$

$$R = R \cup \{d^*\}$$

$$w_{ij} \in [0, 1], w_{ij} = \frac{r_{ij}^*}{r_{ij}^* + 1}$$

$$\text{end for}$$

PM-2 Example

rank _{init}	q ₁	q ₂	rank _{div}	Quotient scores	λ=0.6
d ₁ , 0.70,	0.7,	0.2	d ₂	qt[1] = 4 / (2×1.38+1) = 1.06 qt[2] = 4 / (2×1.62+1) = 0.95	<div>“quotients (priorities)”</div> <div>“selected intent”</div>
d ₂ , 0.69,	0.8,	0.1	d ₅	i* = 1	
d ₃ , 0.68,	0.6,	0.3	d ₄		
d ₄ , 0.67,	0.2,	0.7			
d ₅ , 0.66,	0.3,	0.8			

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$$V_i, n_i = \frac{\text{Desired Ranking Size}}{\text{Number of Intents}}, n_i = 0$$

$$\text{for all } i \in I$$

$$w_{ij} \in [0, 1], w_{ij} = \frac{r_{ij}}{r_{ij} + 1}$$

$$r^* = \arg\max_i w_{ij}$$

$$d^* = \arg\max_{i \in I} (w_{ij} \cdot \ln(d_{ij}/n_i) + (1 - \lambda) \sum_{i \in I} w_{ij} \cdot \ln(d_{ij}/n_i))$$

$$S = S \cup \{d^*\}$$

$$R = R \cup \{d^*\}$$

$$w_{ij} \in [0, 1], w_{ij} = \frac{r_{ij}^*}{r_{ij}^* + 1}$$

$$\text{end for}$$

PM-2 Example

rank _{init}	q ₁	q ₂	rank _{div}	PM2 Scores	λ=0.6
d ₁ , 0.70,	0.7,	0.2	d ₂	0.6×1.06×0.7 + 0.4×0.95×0.2 = 0.52	
d ₂ , 0.69,	0.8,	0.1	d ₅		
d ₃ , 0.68,	0.6,	0.3	d ₄	0.6×1.06×0.6 + 0.4×0.95×0.3 = 0.50	
d ₄ , 0.67,	0.2,	0.7			
d ₅ , 0.66,	0.3,	0.8			

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$$V_i, n_i = \frac{\text{Diversified Ranking Score}}{\text{Number of Items}}, n_i = 0$$

$$\text{for all } i \in I$$

$$V_{q_1} \in Q, q_1(i) = \frac{n_i}{n_i + 1}$$

$$r^* = \arg \max_i q_1(i)$$

$$d^* = \arg \max_{d \in D} (V_{q_1}(d) \cdot \ln(d_1(n_i)) + (1 - \lambda) \sum_{w \in W} w(d_1(n_i)))$$

$$S = S \cup \{d^*\}$$

$$R = R \cup \{d^*\}$$

$$V_{q_1} \in Q, n_i = n_i + \frac{d^*(d_1(n_i))}{|S| \cdot q_1(d^*)}$$

$$\text{end for}$$

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	rank_{div}
$d_1, 0.70,$	0.7,	0.2	d_2
$d_2, 0.69,$	0.8,	0.1	d_5
$d_3, 0.68,$	0.6,	0.3	d_4
$d_4, 0.67,$	0.2,	0.7	d_1
$d_5, 0.66,$	0.3,	0.8	

Slots assigned

$\lambda=0.6$

$s[1] = 1.38 + 0.7 / (0.7 + 0.2) = 2.16$

$s[2] = 1.62 + 0.2 / (0.7 + 0.2) = 1.84$

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$$V_i, n_i = \frac{\text{Diversified Ranking Score}}{\text{Number of Items}}, n_i = 0$$

$$\text{for all } i \in I$$

$$V_{q_1} \in Q, q_1(i) = \frac{n_i}{n_i + 1}$$

$$r^* = \arg \max_i q_1(i)$$

$$d^* = \arg \max_{d \in D} (V_{q_1}(d) \cdot \ln(d_1(n_i)) + (1 - \lambda) \sum_{w \in W} w(d_1(n_i)))$$

$$S = S \cup \{d^*\}$$

$$R = R \cup \{d^*\}$$

$$V_{q_1} \in Q, n_i = n_i + \frac{d^*(d_1(n_i))}{|S| \cdot q_1(d^*)}$$

$$\text{end for}$$

PM-2 Example

$\text{rank}_{\text{init}}$	q_1	q_2	rank_{div}
$d_1, 0.70,$	0.7,	0.2	d_2
$d_2, 0.69,$	0.8,	0.1	d_5
$d_3, 0.68,$	0.6,	0.3	d_4
$d_4, 0.67,$	0.2,	0.7	d_1
$d_5, 0.66,$	0.3,	0.8	

$\lambda=0.6$

Repeat until all documents
in the initial ranking
are added to
the diversified ranking

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xQuAD vs PM-2

xQuAD picks a document that covers multiple intents

- Give higher weight to intents that need coverage

PM2 picks the intent that most needs to be covered

- Then it picks a document that covers that intent
- There is extra credit for covering other intents, too

$\text{rank}_{\text{init}}$	q_1	q_2	rank_p	rank_x
$d_1, 0.70,$	0.7	0.2	d_2	d_5
$d_2, 0.69,$	0.8	0.1	d_5	d_2
$d_3, 0.68,$	0.6	0.3	d_4	d_1
$d_4, 0.67,$	0.2	0.7	d_1	d_4
$d_5, 0.66,$	0.3	0.8	d_3	d_3

Notice the choices that each algorithms makes

$$\lambda_p=0.6, \lambda_x=0.4$$

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xQuAD vs PM-2

xQuAD picks a document that covers multiple intents

- Give higher weight to intents that need coverage

PM2 picks the intent that most needs to be covered

- Then it picks a document that covers that intent
- There is extra credit for covering other intents, too

$\text{rank}_{\text{init}}$	q_1	q_2	rank_p	rank_x
$d_1, 0.70,$	0.7	0.1	d_2	d_5
$d_2, 0.69,$	0.7	0.2	d_8	d_2
$d_3, 0.68,$	0.4	0.5	d_5	d_3
$d_4, 0.67,$	0.5	0.4	d_6	d_1
$d_5, 0.66,$	0.5	0.5	d_1	d_4
$d_6, 0.65,$	0.5	0.5	d_7	d_6
$d_7, 0.64,$	0.1	0.7	d_4	d_7
$d_8, 0.63,$	0.1	0.9	d_3	d_8

Notice the choices that each algorithms makes

$$\lambda_p=0.6, \lambda_x=0.4$$

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PM-2

Dang and Croft use uniform weighting of query intents

- Santos, et al found it to be most effective

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PM-2

How well does it work?

		α -NDCG	Win/Loss	ERR-IA	Prec-IA
Sub-topics			WT-2009		
	Query-likelihood	0.2979		0.1953	0.1146
	MMR	0.2963	16/19	0.1922	0.1221
	xQuAD	0.3300 _{Q,M}	23/15	0.2207 _{Q,M}	0.1190
	PM-1	0.3076	18/17	0.2027	0.1140
	PM-2	0.3473^P	19/19	0.2407^P	0.1197
Suggestions	Query-likelihood	0.2875		0.1895	0.1095
	MMR	0.2926	16/15	0.1919	0.1108
	xQuAD	0.2995	14/19	0.1973	0.1089
	PM-1	0.2870	16/18	0.1830	0.0929 ^x
	PM-2	0.3200	17/19	0.2139	0.1123^P
	WT-2009 Best (uogTrDYCcsB) [10]	0.3081	N/A	0.1922	N/A

ClueWeb09-B (50 queries from 2009)

Evaluated at 50 documents (e.g., α -NDCG@50)

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(Dang and Croft, 2012)
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PM-2

How well does it work?

		α -NDCG	Win/Loss	ERR-IA	Prec-IA
			WT-2010		
Sub-topics	Query-likelihood	0.3236		0.2081	0.1713
	MMR	0.3349 _Q	19/14	0.2161	0.1740
	xQuAD	0.4074 _{Q,M}	29/14	0.2671 _{Q,M}	0.2028
	PM-1	0.4323 _{Q,M} ^X	32/13	0.3071 _{Q,M} ^X	0.1827
	PM-2	0.4546 _{Q,M} ^{X,P}	34/10	0.3271 _{Q,M} ^X	0.2030
Suggestions	Query-likelihood	0.3268		0.2131	0.1730
	MMR	0.3361 _Q	17/14	0.2206	0.1746
	xQuAD	0.3582 _{Q,M}	31/6	0.2372 _{Q,M}	0.1785
	PM-1	0.3664 _{Q,M} ^X	25/15	0.2409	0.1654
	PM-2	0.4374 _{Q,M} ^{X,P}	33/10	0.3087 _{Q,M} ^{X,P}	0.1841
WT-2010 Best (uogTrB67xS) [11]		0.4178	N/A	0.2980	N/A

ClueWeb09-B (50 queries from 2010)

Evaluated at 50 documents (e.g., α -NDCG@50)

(Dang and Croft, 2012)
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PM-2

PM-2 characteristics

- Requires a set of explicit query intents
- Allows a single document to satisfy multiple query intents
 - Those documents are more likely to be ranked highly
- The diversified ranking covers each intent proportionally
 - Weighting is possible, but uniform weights were best
- Each query q requires running queries q and $\{q_1, \dots, q_k\}$
 - Presumably 7-10 queries in Dang & Croft's experiments
 - Thus a little expensive computationally
- Relative performance vs. xQuAD depends on detailed datasets and explicit topics.

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Implicit vs. Explicit Diversification Algorithms

Explicit methods are more effective than MMR, but they need to know query intents

- Obtaining intents from web search engines is unsatisfying
 - Reliance on another organization
 - Perhaps the query suggestions don't work well for your task

R-LeToR works the best with supervision

- xQuAD and PM-2 are both unsupervised (but they have extra information – intents)

Ideally, we want the best characteristics of each method

- No need for external resources
- Make use of subtopics when available
- Fully utilize supervision

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Summary

Methods of identifying query intents

- Commercial search engine suggestions
 - Query suggestions > related queries
- Still an open problem
 - Very hard without search log

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Summary

Diversification algorithms

- Maximum Marginal Relevance (MMR)
- Relational Learning to Rank (R-LeToR)
- xQuAD
- PM-2

Characteristics

- MMR: Implicit, unsupervised, penalizes redundancy
- R-LeToR: Implicit, supervised, features to model redundancy
- xQuAD: Explicit, unsupervised, penalizes redundancy
- PM-2: Explicit, unsupervised, enforces proportionality

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Summary

Performance: $R\text{-LeToR} > PM\text{-2} \approx xQuAD > MMR$

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Topic Outline

- **Introduction**
- **Diversity Evaluation Metrics**
- **Implicit Methods**
 - Maximum Marginal Relevance (MMR)
 - Learning to Rank for diversification
- **Explicit Methods**
 - Query intents (subtopics) discovery
 - xQuAD
 - PM-2

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For More Information

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