11-442 / 11-642 / 11-742: Search Engines

Best-Match Retrieval: VSM, BM25

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1

#### Introduction



#### Until now, we have focused on exact-match retrieval models

- <u>Unranked Boolean</u> and <u>Ranked Boolean</u>
- Used widely in industry until about 1990
- Still an important form of retrieval in many situations

#### Today's lecture introduces **best-match** retrieval models

- Easier for many people to use
- Often more accurate
- Considered the state-of-the-art today in many situations

2

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#### Introduction



#### We started by examining exact match Boolean retrieval models

- Documents either <u>match</u> or <u>do not match</u> the query
- Unranked Boolean, Ranked Boolean

### <u>Best match</u> retrieval models calculate <u>how well</u> a document d<sub>i</sub> satisfies the information need I expressed by a query Q

- Ideally expressed as Satisfy  $(I, d_i)$  or  $p(d_i | I)$
- More often expressed as Similarity  $(Q, d_i)$  or  $p(d_i | Q)$
- Many documents match the query to some degree (partial match)

#### The search result is a ranked list of documents

• "Best first"

3

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3

#### Introduction

# Most best match retrieval models treat the document as a vector or distribution of term weights • A set of index terms

- The "bag of words"
- A weight for each index term
  - "term weights"

#### There is less agreement on ...

- How to treat the query
- How to rank documents

Docume	nt
	Waink

Term	Weight
camera	0.09551
image	0.07303
picture	0.06180
up	0.04494
movie	0.04494
like	0.03933
mode	0.03933
software	0.03933
red	0.03371
digital	0.02809
eye	0.02809
shutter	0.02809
sony	0.02809
-	

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#### **Best Match Retrieval Models**

#### What distinguishes different best-match models?

- The theory
  - Important to scientists, but maybe not to practitioners
- How term weights are calculated
  - Most models use the same statistics (tf, df, doclen, numdocs)
- How <u>similarity</u> between query and document is calculated
- Whether the retrieval model can handled <u>structured queries</u>

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5

#### Introduction



#### This unit covers several best-match retrieval models

- Vector space retrieval model (VSM)
- Probabilistic retrieval models (BM25)
- Statistical language models (query likelihood)
- Inference networks (Indri)

Each retrieval model is based on a different theory

... however, they have (mostly) similar architectures

#### Disagreement about theory, but agreement about what works

• Don't be confused by the theory – this stuff is simple

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#### **Lecture Outline**

#### Introduction

#### The vector space model (VSM)

- Standard VSM (lnc.ltc)
- Lucene

**BM25** 

7

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#### 7

#### **The Vector Space Retrieval Model**

Representation: Any text can be represented by a term vector

• Examples: Documents, queries, sentences, ....

#### Similarity is determined by distance in a vector space

• There are many ways of measuring this distance

#### Best known vector space systems

- SMART, developed by Gerard Salton, mostly at Cornell
- Lucene's ClassicSimilarity retrieval model

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#### **Vector Space Similarity**

### How similar is the text represented by vectors x and y?

### There are many ways to measure the similarity of two vectors

• Overlap of vectors x and y can be determined by their inner product

$$\sum_{i=1}^{|V|} x_i \cdot y_i$$

• *V* is the vocabulary

01 110181105				
V	X	y	$x_i \cdot y_i$	
apple	0	0	0	
buy	1	0	0	
camera	17	1	17	
dog	0	0	0	
image	13	1	13	
like	7	0	0	
mode	7	0	0	
movie	8	0	0	
up	8	0	0	
zooms	1	1	1	
Total			31	

tf weights

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9

#### **Vector Space Similarity**

#### Overlap measures the similarity of the vocabularies of x and y

• The number of terms they have in common

#### Overlap is a weak similarity metric

- It doesn't normalize for vector length
- All terms are treated as equally important

#### Does overlap favor any of these conditions?

- Two long pieces of text with overlapping vocabularies
- Two short pieces of text with overlapping vocabularies
- One long and one short piece of text with overlapping vocabularies

10

#### **Cosine Similarity**

#### Many similarity functions have been developed

- Inner product, Dice coefficient, Jackard coefficient,

. . .

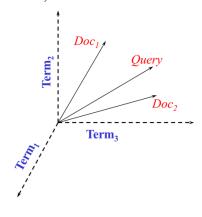
Cosine correlation is the most popular

The <u>cosine of the angle between two vectors</u> is determined by scaling for document length

$$\frac{\sum_{i=1}^{|V|} x_i \cdot y_i}{\sqrt{\sum_{i=1}^{|V|} x_i^2}} \sqrt{\sum_{i=1}^{|V|} y_i^2}$$

Length of vector y

11



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11

### **Cosine Similarity**

#### tf weights

V	X	y	$\mathbf{x_i} \cdot \mathbf{y_i}$
apple	0	0	0
buy	1	0	0
camera	17	1	17
dog	0	0	0
image	13	1	13
like	7	0	0
mode	7	0	0
movie	8	0	0
up	8	0	0
zooms	1	1	1
Total			31

#### Length of x:

$$\sqrt{1^2 + 17^2 + 13^2 + \dots + 1^2} = 26.19$$

#### Length of y:

$$\sqrt{1^2 + 1^2 + 1^2} = 1.73$$

#### **Sim** (x, y):

$$\frac{31}{26.19 \times 1.73} = \frac{31}{45.33} = 0.68$$

12

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#### **Vector Coefficients**

#### Vector coefficients (term weights) determine each term's effect

• The vector space model <u>does not specify</u> how to set term weights

#### **Some common considerations:**

- Document term weight: Importance of the term in this document
- Collection term weight: Importance of the term in this collection
- Length normalization: Compensate for varying document lengths

#### Naming convention for term weight functions: DCL.DCL

- First triple is document vector, second triple is query vector
- n=none (no weighting on that factor)
- Example: lnc.ltc

13

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#### **Document Term Weights (D)**

#### How should the importance of term t in document d be represented?

• How well does term *t* describe <u>document *d*</u>?

#### Some common choices

- Binary weight?
- Term frequency (tf)?
- Some function of term frequency?
- ...

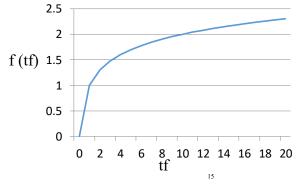
14

#### **Document Term Weights (D)**

What characteristics are required in a term weighting function?

- A monotonic function
- Term frequency scaled by document length?

• Saturation?



One popular choice

tf log(tf+1) 1 0.69

2 1.10 1.39

4 1.61

1.79

1.95

15

#### **Collection Term Weights (C): Inverse Document Frequency (idf)**

How should the importance of term *t* in the collection be represented?

- Observation: Terms that occur in many documents in the collection are less useful for discriminating among documents (i.e., separating relevant and non-relevant sets)
- The most common choice is inverse document frequency (idf)

Some common forms of idf

$$idf = log \frac{N}{df}$$
  $idf = log \frac{N+1}{df}$   $idf = log \left(\frac{N}{df}\right) + 1$ 

Standard form (Know this)

To avoid idf=0

To avoid idf=0

N: # documents in corpus df: # documents

containing t

The three formulas produce similar (but not identical) rankings

#### lnc.ltc

**Inc.ltc:** A popular combination of term weights and similarity metric

- •"l": document term weight = log(tf) + 1
- •"t": collection term weight = log (N / df)

•"c": cosine length normalization  $\sqrt{\sum_{w_i}^2}$ 

- •"n": weight = 1.0 (i.e., none)
- For example:

e:  $\frac{\sum d_i \cdot q_i}{\sqrt{\sum d_i^2} \cdot \sqrt{\sum q_i^2}} = \frac{\sum (\log(tf) + 1) \cdot \left( (\log(qtf) + 1) \log \frac{N}{df} \right)}{\sqrt{\sum (\log(tf) + 1)^2} \cdot \sqrt{\sum \left( (\log(qtf) + 1) \log \frac{N}{df} \right)^2}}$ Cosine similarity metric "document length ormalization" "query length normalization"

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Know this

**17** 

#### Inc.ltc

Why does Inc.ltc put idf in the query term weight?

• Originally, idf represented the term's importance to the query

Different vector space systems may have it anywhere

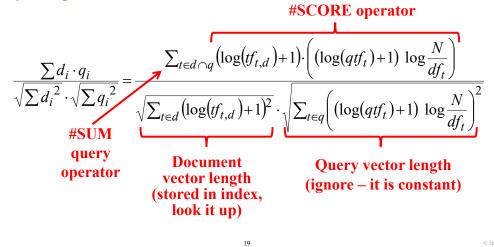
Query	Document	
log (N / df)		Query term weight
	log (N / df)	<b>Document term weight</b>
sqrt (log (N / df))	sqrt (log (N / df))	One policy for both vectors
log(N/df)	log(N/df)	Double idf weighting (idf <sup>2</sup> )

There is no good theory to guide setting vector space weights

18

#### **Vector Space Implementation**

It is easy to implement lnc.ltc



19

#### **Boolean Queries**

The vector space is based on the <u>similarity of two vectors</u> ... do query operators fit within the vector space framework?

AND, OR, and NOT have vector space implementations

- 'p-norm' operators
  - Score combinations that mimic the effects of Boolean operators
- I rarely see anyone use them, so we don't cover them

What about proximity operators?

20

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### **Vector Space Similarity: Query Operators Such As NEAR/n**

### Remember that some query operators can be viewed as <u>dynamically creating</u> indexing terms

- The operator produces an inverted list containing df, tf, ...
- E.g., NEAR/n, UW/n, SYNONYM (...), ...
- Thus, the vector space can handle them just like other terms

#### How does this affect document length normalization?

- Standard practice is to ignore it
- Just compute length over unigrams

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#### Lucene

#### Lucene's ClassicSimilarity uses a two-step retrieval process

- 1. Use a Boolean query to form a set of documents
  - E.g., Unranked Boolean AND
  - "Fuzzy" Boolean is also an option
- 2. Use a vector space retrieval algorithm to rank the set

22

#### Lucene

#### Each document can have a query-independent weight

• E.g., PageRank

#### **Documents are composed of fields**

- Each field is an independent text representation
  - I.e., a distinct vector space or bag of words
- Each field can have a query-independent weight
  - E.g., so that Title is more important than Body
  - Field weights are assigned when the index is built
    - » Just look them up from the index when evaluating the query

23

#### A Simplified View of Lucene's ClassicSimilarity Ranker

#### Lucene uses a modified vector space algorithm

- A simplified view is RSV (d,q) = weight  $(d) \times coordinationMatch <math>(d,q) \times cosine (d,q)$ 
  - weight(d): Query-independent importance of d (e.g., PageRank)
  - coordinationMatch (d,q): % of query terms that match d
  - cosine (d,q):

$$\frac{\sum d_i \cdot q_i}{\sqrt{\sum d_i^2} \cdot \sqrt{\sum q_i^2}} = \frac{\sum \left(\sqrt{tf} \cdot \left(1 + \log \frac{N}{df + 1}\right)\right) \cdot \left(qtf \cdot \left(1 + \log \frac{N}{df + 1}\right)\right)}{\sqrt{\sum \left(\sqrt{tf} \cdot \left(1 + \log \frac{N}{df + 1}\right)\right)^2} \cdot \sqrt{\sum \left(qtf \cdot \left(1 + \log \frac{N}{df + 1}\right)\right)^2}}$$
"document length "query length"

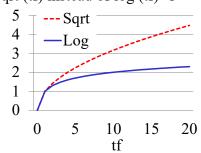
normalization"

normalization"

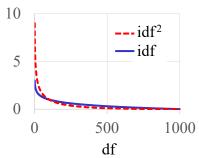
### A Simplified View of Lucene's ClassicSimilarity Ranker

#### Lucene's vector space retrieval model has two important differences from lnc.ltc

• sqrt (tf) instead of log (tf)+1



• idf<sup>2</sup> instead of idf



#### What are the effects?

- Stronger reward for terms that are frequent in this document
- Stronger penalty for terms that are frequent across the corpus

25

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25

### **Vector Space Retrieval Model: Summary**

#### **Standard vector space**

- Each dimension corresponds to a term in the vocabulary
- Vector elements are real-valued, reflecting term importance
- Any vector (document, query, ...) can be compared to any other
- Cosine correlation is the similarity metric used most often
- A <u>best-match</u> retrieval model
  - Unlike the Boolean retrieval model, which was exact-match

26

#### **Vector Space Retrieval Model**

The key idea: Measure similarity among weighted term vectors

• Documents, queries, paragraphs, sentences, ... anything

#### What is missing from the vector space model?

- No guidance about how to set term weights
- No guidance about how to determine similarity
- No method of supporting query-independent weights

#### You can do pretty much anything you want

- Strength: Very flexible, can absorb good ideas from anywhere
- Weakness: Everything is heuristic

27

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27

#### **Lecture Outline**

#### Introduction

The vector space model (VSM)

- Standard VSM (lnc.ltc)
- Lucene

**BM25** 

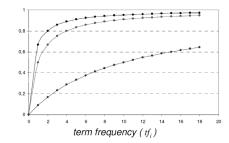
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#### **BM25**

Robertson used inspiration from another (unsuccessful) retrieval model to develop requirements for a tf function

- Zero when tf=0
- Increases monotonically with tf
- Saturates as tf increases
  - Shape depends on parameters

 $tf/(tf+k_1)$  is a good approximation



**Document length normalization** 

• Normalize by

$$(1-b)+b\frac{doclen}{avg\_doclen}$$

(Robertson & Zaragoza, 2007)

29

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#### The BM25 Retrieval Model

The BM25 model

BM25 has been used with many different parameter configurations

- Originally:  $k_1=2$ , b=0.75,  $k_3=0$  (also used in Inquery)
- Usually:  $k_1=1.2$ , b=0.75,  $k_3=0-1000$  $k_1=0.9$ , b=0.40,  $k_3=0-1000$  (large collections)\*

(\* Shane Culpepper, 2014, personal communication)

30

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#### The BM25 model

$$\frac{\sum\limits_{t \in q \cap d} \left(\log \frac{\mathrm{N} - \mathrm{df_t} + 0.5}{\mathrm{df_t} + 0.5}\right) \frac{tf_{\mathrm{t,d}}}{tf_{\mathrm{t,d}} + k_1 \left((1 - b) + b \frac{\mathrm{doclen_d}}{\mathrm{avg\_doclen}}\right)} \frac{(k_3 + 1) \, qtf_{\mathrm{t}}}{k_3 + qtf_{\mathrm{t}}}}{\mathbf{RSJ \ weight}}$$
(idf)
tf weight
user
weight

#### Note the similarities to the vector space

• A saturating tf function tf

• idf df, N

• Document length normalization doclen, avg doclen

• Summation of scores

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31

#### The BM25 Retrieval Model

#### HW2 requires you to think about the effects of parameters

$$\sum_{t \in q \cap d} \left( \log \frac{\mathsf{N} - \mathsf{df}_{\mathsf{t}} + 0.5}{\mathsf{df}_{\mathsf{t}} + 0.5} \right) \frac{t f_{\mathsf{t},\mathsf{d}}}{t f_{\mathsf{t},\mathsf{d}} + k_1 \left( (1 - b) + b \frac{\mathsf{doclen}_{\mathsf{d}}}{\mathsf{avg\_doclen}} \right)} \frac{(k_3 + 1) \, qt f_{\mathsf{t}}}{k_3 + qt f_{\mathsf{t}}}$$

#### What happens when k<sub>3</sub> approaches 0?

- Query term frequency has no effect
  - "apple apple pie" is the same as "apple pie"

$$\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{tf_{t,d}}{tf_{t,d} + k_1 \left( (1 - b) + b \frac{doclen_d}{avg\_doclen} \right)}$$

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HW2 requires you to think about the effects of parameters

$$\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{tf_{t,d}}{tf_{t,d} + k_1 \left( (1 - b) + b \frac{doclen_d}{avg\_doclen} \right)} \frac{(k_3 + 1) qtf_t}{k_3 + qtf_t}$$

#### What happens when k<sub>1</sub> approaches 0?

- Document term frequency has no effect
  - Rare words and repeated query terms dominate

$$\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{(k_3 + 1) qtf_t}{k_3 + qtf_t}$$

33

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33

#### The BM25 Retrieval Model

HW2 requires you to think about the effects of parameters

$$\sum_{t \in q \cap d} \left( \log \frac{\mathsf{N} - \mathsf{df}_\mathsf{t} + 0.5}{\mathsf{df}_\mathsf{t} + 0.5} \right) \frac{tf_\mathsf{t,d}}{tf_\mathsf{t,d} + k_1 \left( (1-b) + b \frac{\mathsf{doclen}_\mathsf{d}}{\mathsf{avg}\_\mathsf{doclen}} \right)} \frac{(k_3 + 1) \, qtf_\mathsf{t}}{k_3 + qtf_\mathsf{t}}$$

#### What happens when b approaches 0?

- Document length is ignored
  - Long documents are more likely to be retrieved

$$\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{tf_{t,d}}{tf_{t,d} + k_1} \frac{(k_3 + 1) qtf_t}{k_3 + qtf_t}$$

34

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This is how BM25 is usually presented, but it contains a flaw

$$\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{tf_{t,d}}{tf_{t,d} + k_1 \left( (1 - b) + b \frac{doclen_d}{avg\_doclen} \right)} \frac{(k_3 + 1) qtf_t}{k_3 + qtf_t}$$

Suppose  $df_t = N/2$ 

- RSJ weight =  $\log \frac{N \frac{N}{2} + 0.5}{\frac{N}{2} + 0.5} = \log \frac{\frac{N}{2} + 0.5}{\frac{N}{2} + 0.5} = \log(1) = 0$
- Matching the term has <u>no effect</u> on the document score

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#### The BM25 Retrieval Model

This is how BM25 is usually presented, but it contains a flaw

$$\sum_{t \in q \cap d} \left( \log \frac{\mathrm{N} - \mathrm{df_t} + 0.5}{\mathrm{df_t} + 0.5} \right) \frac{tf_{\mathrm{t,d}}}{tf_{\mathrm{t,d}} + k_1 \left( (1-b) + b \frac{\mathrm{doclen_d}}{\mathrm{avg\_doclen}} \right)} \frac{(k_3 + 1) \, qtf_{\mathrm{t}}}{k_3 + qtf_{\mathrm{t}}}$$

Suppose  $df_t > N/2$  (e.g., N/2 + 1)

- RSJ weight =  $\log \frac{N (\frac{N}{2} + 1) + 0.5}{(\frac{N}{2} + 1) + 0.5} = \log \frac{\frac{N}{2} + 0.5}{\frac{N}{2} + 1.5} = \log(fraction) < 0$
- Matching a frequent term <u>lowers</u> a document's score

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36

This is how BM25 is usually presented, but it contains a flaw

$$\sum_{t \in q \cap d} \left( \log \frac{N - \mathrm{df_t} + 0.5}{\mathrm{df_t} + 0.5} \right) \frac{tf_{\mathrm{t,d}}}{tf_{\mathrm{t,d}} + k_1 \left( (1 - b) + b \frac{\mathrm{doclen_d}}{\mathrm{avg\_doclen}} \right)} \frac{(k_3 + 1) \, qtf_{\mathrm{t}}}{k_3 + qtf_{\mathrm{t}}}$$

**Robertson's solution** 

- Change the RSJ weight to
  - Jamie's code does this

$$Max \left( 0, \log \frac{N - df_t + 0.5}{df_t + 0.5} \right)$$

(Robertson & Zaragoza, 2007)

37

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**37** 

#### Lucene's BM25 Ranker

#### Recently, Lucene added BM25 ranking

- Standard BM25, except for the RSJ weight
- Lucene adds +1 to prevent negative RSJ weight

Modified RSJ weight

$$\sum_{t \in q \cap d} \left( log \left( 1 + \frac{N - df_t + 0.5}{df_t + 0.5} \right) \right) \frac{tf_{t.d}}{tf_{t.d} + k_1 \left( (1 - b) + b \frac{doclen_d}{doclen_{avg}} \right)} \frac{(k_3 + 1)qtf_t}{k_3 + qtf_t}$$

**Equivalently** 

$$\sum_{t \in q \cap d} \left( log \left( \frac{N+1}{df_t + 0.5} \right) \right) \frac{tf_{t.d}}{tf_{t.d} + k_1 \left( (1-b) + b \frac{doclen_d}{doclen_{avg}} \right)} \frac{(k_3+1)qtf_t}{k_3 + qtf_t}$$

38

(Doug Turnbull — October 16, 2015)

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#### **BM25 Implementation**

**#SCORE** operator

BM25 is easy to implement

• If #SUM,  $qtf_t = 1$ 

• If #WSUM,

 $\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{tf_{t,d}}{tf_{t,d} + k_1 \left( (1 - b) + b \frac{\text{doclen}_d}{\text{avg\_doclen}} \right)} \frac{(k_3 + 1) qtf_t}{k_3 + qtf_t}$ 

#SUM or #WSUM query operator

- Constants (N, avg doclen) are stored in the index look them up
- doclen<sub>d</sub> is stored in the index look it up
- Parameters (b,  $k_1$ ,  $k_3$ ) are stored in the retrieval model look them up

39

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39

#### BM25: Boolean Queries

#### BM25 doesn't support Boolean query operators

• Typically it is used only for unstructured queries

40

#### BM25: Query Operators Such As NEAR/n

### Remember that some query operators can be viewed as <u>dynamically creating</u> indexing terms

- The operator produces an inverted list containing df, tf, ...
- E.g., NEAR/n, UW/n, SYNONYM (...), ...
- Thus, BM25 can handle them just like other terms

#### How does this affect document length normalization (avg\_doclen)?

- Standard practice is to ignore it
- Just compute length over unigrams

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41

## BM25 Implementation: qtf

#### Query term frequency (qtf) seems to confuse many students

- You don't need to worry about it in your homework
  - We will not give you duplicate query terms
  - Your BM25 queries will always have qtf=1
- But, if you want to know how it works...

42

### BM25 Implementation: qtf

#### How is qtf implemented in a search engine?

$$\sum_{t \in q \cap d} \left( \log \frac{N - df_t + 0.5}{df_t + 0.5} \right) \frac{tf_{t,d}}{tf_{t,d} + k_l \left( (1 - b) + b \frac{doclen_d}{avg\_doclen} \right)} \frac{(k_3 + 1) qtf_t}{k_3 + qtf_t}$$

#### Think of BM25 this way



#### User weights are managed by the #WSUM query operator

• E.g., "apple apple pie" → #WSUM (2 apple 1 pie)

43

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43

### **BM25 Implementation:** qtf

#### QrySopWsum implements a query operator that takes weights

- Query: #WSUM (2 apple 1 pi)
- Object:

QrySopWsum
arg\_weights:2 1
args: //

• For the BM25 retrieval model, treat the input values as qtf

The Qry and QrySop ancestor classes don't provide arg weights

- But, a subclass can add elements
- You will do this for Indri in HW2

44

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## BM25 Implementation: qtf

Query term frequency (qtf) seems to confuse many people, so...

Query: #SUM (a b c)

- a: qtf=1
- b: qtf=1
- c: qtf=1

Query: #SUM (a b a)

- a: qtf=2
- b: qtf=1

Easy cases...

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45

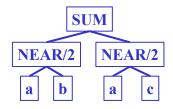
### BM25 Implementation: qtf

**Query:** #SUM (#NEAR/2 (a b) #NEAR/2 (a c))

- #NEAR/2 (a b): qtf=1
- #NEAR/2 (a c): qtf=1
- a, b, and c don't have qtf because they are arguments to NEAR
  - The SUM operator doesn't see them

If confused, think about the parse tree

- A query operator only sees its their children
- It doesn't see its grandchildren



46

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### The BM25 Retrieval Model: Summary

#### **Advantages**

- Motivated by sound probabilistic theory
- Parameters allow it to be tuned to new environments
- Very effective in a wide variety of evaluations

#### **Disadvantages**

- Heuristic tf weighting and document length normalization
- Effects of parameters not immediately obvious tune them for your dataset!

One of the most popular retrieval models for the last 15 years

47

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47

#### **Lecture Outline**

#### Introduction

The vector space model (VSM)

- Standard VSM (lnc.ltc)
- Lucene

**BM25** 

48

#### For Additional Information

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