HANDOUT 3

JIASU WANG

- 1. Explain the following terms: Linear combination, Span, vector equation, matrix equation, homogeneous linear system, Nonhomogeneous system.
- 2. How to determine if v is in the span of v_1, \dots, v_m ? If v is in the span of v_1, \dots, v_m , how to find a_1, \dots, a_m such that $v = \sum_i a_i v_i$? (See example below.)
- 3. Determine if **b** is a linear combination of $\mathbf{a}_1, \mathbf{a}_2$ and \mathbf{a}_3 . If so, write down the linear combination.

(1)
$$\mathbf{a}_1 = \begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix}, \mathbf{a}_2 = \begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}, \mathbf{a}_3 = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}, \mathbf{b} = \begin{bmatrix} -7 \\ 3 \\ -2 \end{bmatrix}$$

- 4. Solve the following system of equation: $\begin{bmatrix} 1 & 0 & 2 \\ -2 & 5 & 0 \\ 2 & 5 & 8 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 17 \\ 4 \\ 72 \end{bmatrix}.$
- 5. Find the parametric equation of the line through **a** parallel to **b**.

(2)
$$\mathbf{a} = \begin{bmatrix} 7 \\ 2 \end{bmatrix}, \mathbf{b} = \begin{bmatrix} 3 \\ -4 \end{bmatrix}.$$

6. Find the parametric equation of the line through **a** and **b**.

(3)
$$\mathbf{a} = \begin{bmatrix} 7 \\ 2 \end{bmatrix}, \mathbf{b} = \begin{bmatrix} 3 \\ -4 \end{bmatrix}.$$

Takeaway:

- The parametric equation of the line through **a** parallel to **b**: $\mathbf{x} = \mathbf{a} + t\mathbf{b}$.
- The parametric equation of the line through **a** and **b**: $\mathbf{x} = t\mathbf{a} + (1-t)\mathbf{b}$.