R Lab 2

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Roadmap

- RStudio server, R Style
- tidyverse
- T-test

Advanced programming for data science

tidyverse

"The tidyverse is an opinionated collection of R packages designed for data science. All packages share an underlying design philosophy, grammar, and data structures."

The core tidyverse includes the packages that you're likely to use in everyday data analyses. As of tidyverse 1.2.0, the following packages are included in the core tidyverse:

- magrittr: offers a set of operators which make your code more readable
- dplyr: a grammar of data manipulation
- ggplot2:a system for declaratively creating graphics
- tidyr: a set of functions that help you get to tidy data
- readr: provides a fast and friendly way to read rectangular data
- purrr: enhances R's functional programming (FP) toolkit by providing a complete and consistent set of tools for working with functions and vectors
- tibble: a modern re-imagining of the data frame
- stringr: a cohesive set of functions designed to make working with strings as easy as possible
- forcats: provides a suite of useful tools that solve common problems with factors

magrittr

The magrittr does the following:

- structuring sequences of data operations left-to-right (as opposed to from the inside and out)
- avoiding nested function calls
- minimizing the need for local variables and function definitions
- making it easy to add steps anywhere in the sequence of operations

You can think about the following sequence of actions - find key, unlock car, start car, drive to school, park.

Expressed as a set of nested functions in R pseudocode this would look like:

```
park(drive(start_car(find("keys")), to="campus"))
```

Writing it out using pipes give it a more natural (and easier to read) structure:

```
find("keys") %>%
    start_car() %>%
    drive(to = "campus") %>%
    park()
```

Approaches

Basic piping x %>% f is equivalent to f(x) x %>% f(y) is equivalent to f(x, y) x %>% f %>% g %>% h is equivalent to h(g(f(x)))

The argument placeholder

```
x \%\% f(y, .) is equivalent to f(y, x) x \%\% f(y, z = .) is equivalent to f(y, z = x)
```

dplyr - A Grammar of Data Manipulation

dplyr is based on the concepts of functions as verbs that manipulate data frames.

Single data frame functions / verbs:

- - filter(): filter rows by condition(s)
- - slice(): filter rows using index(es)
- - select(): select columns by name
- - rename(): rename variables
- - arrange(): reorder rows
- - mutate(): add new variables
- - distinct(): filter for unique rows
- - sample_n() / sample_frac(): randomly sample rows
- - summarise(): reduce variables to values
- - ... (many more)

CEO Data Analysis

Read CEO data

```
# set working directory
setwd("~/PS630-R-Lab/lab-2") # change to your own working directory
# read dta (Stata)
ceo <- read_dta("./CEOSAL2.DTA") # read CEO dataset using haven</pre>
```

filter() - filter by condition(s)

```
ceo %>% filter(age > 50)
## # A tibble: 139 x 15
               age college grad comten ceoten sales profits mktval lsalary
##
      salary
##
       <dbl> <dbl>
                      <dbl> <dbl>
                                    <dbl>
                                           <dbl> <dbl>
                                                          <dbl>
                                                                 <dbl>
                                                                          <dbl>
         379
                                                                           5.94
##
   1
                51
                          1
                                1
                                        9
                                               3
                                                    169
                                                             40
                                                                  1100
    2
         651
                55
                          1
                                0
                                       22
                                              22
                                                  1100
                                                            -54
                                                                  1000
                                                                           6.48
##
                                               7 19000
##
   3
        1067
                64
                          1
                                1
                                        7
                                                            614
                                                                  3900
                                                                           6.97
   4
                          1
                                0
                                                    536
                                                                           6.85
##
         945
                59
                                       35
                                              10
                                                             24
                                                                   623
##
   5
        1261
                63
                          1
                                1
                                       32
                                               8
                                                  4800
                                                            191
                                                                  2100
                                                                           7.14
##
   6
        1094
                          1
                                1
                                       39
                                               5
                                                  2900
                                                            230
                                                                  3900
                                                                           7.00
                64
```

```
## 7
                                                1200
                                                                        6.40
         601
                               1
                                     26
                                                           34
                                                                 533
##
   8
         355
                66
                         1
                               0
                                     39
                                             8
                                                 560
                                                           8
                                                                 477
                                                                        5.87
        1200
                                                                        7.09
##
   9
                72
                         1
                               0
                                     37
                                            37
                                                 796
                                                           35
                                                                 678
         697
                                     25
                                                8200
                                                          234
                                                                5700
                                                                        6.55
## 10
                51
                         1
                               0
                                              1
## # ... with 129 more rows, and 5 more variables: lsales <dbl>,
     lmktval <dbl>, comtensq <dbl>, ceotensq <dbl>, profmarg <dbl>
ceo %>% filter(age == 50, salary > 1000 )
## # A tibble: 2 x 15
     salary age college grad comten ceoten sales profits mktval lsalary
##
      <dbl> <dbl>
                    <dbl> <dbl> <dbl>
                                        <dbl> <dbl>
                                                      <dbl>
                                                              <dbl>
## 1
       1301
               50
                                    19
                                           15 1800
                                                         130
                                                               1600
                                                                       7.17
                                                               2200
                                                                       7.04
## 2
       1142
               50
                                            3 2600
                                                         166
                        1
                              1
                                    11
## # ... with 5 more variables: lsales <dbl>, lmktval <dbl>, comtensq <dbl>,
## # ceotensq <dbl>, profmarg <dbl>
```

slice() - first 10 columns

```
ceo %>% slice(1:10)
## # A tibble: 10 x 15
               age college grad comten ceoten sales profits mktval lsalary
##
      salarv
                                                          <dbl>
##
       <dbl> <dbl>
                      <dbl> <dbl>
                                   <dbl> <dbl> <dbl>
                                                                  <dbl>
                                                                           <dbl>
##
   1
        1161
                 49
                          1
                                 1
                                        9
                                                2 6200
                                                            966
                                                                  23200
                                                                           7.06
##
         600
                                                    283
                                                                  1100
                                                                           6.40
    2
                 43
                          1
                                 1
                                       10
                                               10
                                                              48
##
    3
         379
                                                                   1100
                 51
                          1
                                 1
                                        9
                                                3
                                                    169
                                                              40
                                                                           5.94
##
   4
         651
                 55
                          1
                                 0
                                       22
                                               22 1100
                                                            -54
                                                                   1000
                                                                           6.48
##
    5
         497
                 44
                          1
                                 1
                                        8
                                               6
                                                    351
                                                             28
                                                                    387
                                                                           6.21
##
    6
        1067
                 64
                          1
                                 1
                                        7
                                               7 19000
                                                            614
                                                                   3900
                                                                           6.97
##
   7
         945
                 59
                          1
                                 0
                                       35
                                               10
                                                    536
                                                             24
                                                                    623
                                                                           6.85
##
                                       32
   8
        1261
                 63
                          1
                                 1
                                                8
                                                   4800
                                                             191
                                                                   2100
                                                                           7.14
##
   9
         503
                 47
                          1
                                        4
                                                4
                                                    610
                                                              7
                                                                    454
                                                                           6.22
                                 1
        1094
                                       39
                                                5 2900
                                                            230
                                                                   3900
## 10
                 64
                          1
                                 1
                                                                           7.00
## # ... with 5 more variables: lsales <dbl>, lmktval <dbl>, comtensq <dbl>,
       ceotensq <dbl>, profmarg <dbl>
```

slice() - last 5 columns

```
ceo %>% slice((n()-4):n())
## # A tibble: 5 x 15
              age college grad comten ceoten sales profits mktval lsalary
     salary
      <dbl> <dbl>
                     <dbl> <dbl>
                                  <dbl>
                                         <dbl> <dbl>
                                                         <dbl>
                                                                         5.58
## 1
        264
               63
                                     42
                                              3
                                                  334
                                                            43
                                                                  480
                         1
                               0
## 2
        185
               58
                                     39
                                              1
                                                  766
                                                            49
                                                                  560
                                                                         5.22
                         1
                               0
## 3
        387
               71
                         1
                               1
                                     32
                                             13
                                                  432
                                                            28
                                                                  477
                                                                         5.96
## 4
       2220
                                     18
                                                  277
                                                           -80
                                                                         7.71
               63
                         1
                               1
                                             18
                                                                  540
## 5
        445
               69
                                     23
                                              0
                                                  249
                                                            31
                                                                  828
                                                                         6.10
                         1
                               0
## # ... with 5 more variables: lsales <dbl>, lmktval <dbl>, comtensq <dbl>,
     ceotensq <dbl>, profmarg <dbl>
```

select() - select columns

```
ceo %>% select(salary, profmarg)
## # A tibble: 177 x 2
##
      salary profmarg
##
       <dbl>
                 <dbl>
##
    1
        1161
                 15.6
          600
                 17.0
##
    2
##
    3
          379
                 23.7
                 -4.91
##
    4
         651
##
    5
          497
                  7.98
        1067
                  3.23
##
    6
    7
         945
                  4.48
##
##
    8
        1261
                  3.98
##
    9
         503
                  1.15
        1094
                  7.93
## 10
## # ... with 167 more rows
select() - exclude columns
ceo %>% select(-salary, -profmarg)
## # A tibble: 177 x 13
##
        age college grad comten ceoten sales profits mktval lsalary lsales
##
               <dbl> <dbl>
                             <dbl>
                                     <dbl> <dbl>
                                                     <dbl>
                                                            <dbl>
                                                                     <dbl>
##
    1
          49
                                  9
                                          2 6200
                                                       966
                                                            23200
                                                                      7.06
                                                                              8.73
                    1
                          1
##
    2
          43
                    1
                          1
                                 10
                                        10
                                              283
                                                        48
                                                              1100
                                                                      6.40
                                                                              5.65
    3
                                  9
                                              169
                                                        40
                                                              1100
                                                                      5.94
                                                                              5.13
##
          51
                    1
                                         3
                          1
##
    4
          55
                                 22
                                        22
                                             1100
                                                       -54
                                                             1000
                                                                      6.48
                                                                              7.00
                   1
                                  8
                                              351
##
    5
          44
                    1
                                         6
                                                        28
                                                              387
                                                                      6.21
                                                                              5.86
                          1
##
    6
          64
                   1
                                  7
                                         7 19000
                                                       614
                                                             3900
                                                                      6.97
                                                                              9.85
                          1
    7
##
          59
                    1
                          0
                                 35
                                        10
                                              536
                                                        24
                                                               623
                                                                      6.85
                                                                              6.28
##
    8
          63
                                 32
                                          8
                                             4800
                                                       191
                                                              2100
                                                                      7.14
                                                                              8.48
                    1
                          1
    9
          47
                                                         7
                                                               454
                                                                      6.22
                                                                              6.41
##
                                  4
                                          4
                                              610
                    1
                          1
          64
                                 39
                                             2900
                                                       230
                                                              3900
                                                                      7.00
                                                                              7.97
## 10
                    1
                          1
                                          5
## # ... with 167 more rows, and 3 more variables: lmktval <dbl>,
       comtensq <dbl>, ceotensq <dbl>
ceo %>% select(-c(salary, profmarg))
## # A tibble: 177 x 13
##
        age college grad comten ceoten sales profits mktval lsalary lsales
##
      <dbl>
               <dbl> <dbl>
                             <dbl>
                                     <dbl> <dbl>
                                                     <dbl>
                                                            <dbl>
                                                                      <dbl>
##
    1
                                  9
                                             6200
                                                       966
                                                            23200
                                                                      7.06
                                                                              8.73
          49
                   1
                                          2
                          1
##
    2
          43
                   1
                                 10
                                        10
                                              283
                                                        48
                                                              1100
                                                                      6.40
                                                                              5.65
                          1
##
    3
                                                        40
                                                                      5.94
          51
                   1
                          1
                                  9
                                          3
                                              169
                                                             1100
                                                                              5.13
                                 22
                                        22
                                                                              7.00
##
    4
          55
                   1
                          0
                                             1100
                                                       -54
                                                             1000
                                                                      6.48
##
    5
          44
                    1
                          1
                                  8
                                         6
                                              351
                                                        28
                                                              387
                                                                      6.21
                                                                              5.86
##
    6
         64
                   1
                          1
                                 7
                                         7 19000
                                                       614
                                                              3900
                                                                      6.97
                                                                              9.85
    7
          59
                          0
                                              536
                                                                              6.28
##
                    1
                                 35
                                        10
                                                        24
                                                              623
                                                                      6.85
                                           4800
##
    8
          63
                    1
                                 32
                                          8
                                                       191
                                                              2100
                                                                      7.14
                                                                              8.48
                          1
                                              610
                                                         7
                                                               454
##
    9
          47
                    1
                          1
                                  4
                                                                      6.22
                                                                              6.41
```

```
5 2900
                   1
                         1
                                39
                                                     230
                                                           3900
                                                                    7.00
                                                                           7.97
## # ... with 167 more rows, and 3 more variables: lmktval <dbl>,
     comtensq <dbl>, ceotensq <dbl>
select() - ranges
ceo %>% select(salary:college)
## # A tibble: 177 x 3
##
      salary
               age college
##
       <dbl> <dbl>
                      <dbl>
##
   1
        1161
                 49
##
   2
         600
                 43
##
   3
         379
                 51
                          1
         651
##
   4
                 55
                          1
##
   5
         497
                 44
##
        1067
                 64
   6
         945
##
   7
                 59
                          1
        1261
                          1
##
   8
                 63
##
   9
         503
                 47
                          1
## 10
        1094
                 64
                          1
## # ... with 167 more rows
select() - excluse ranges
ceo %>% select(-c(salary:college))
## # A tibble: 177 x 12
       grad comten ceoten sales profits mktval lsalary lsales lmktval comtensq
##
##
             <dbl>
                     <dbl> <dbl>
                                    <dbl>
                                           <dbl>
                                                    <dbl>
                                                           <dbl>
                                                                    <dbl>
                                                                              <dbl>
##
   1
          1
                  9
                         2 6200
                                      966
                                           23200
                                                     7.06
                                                            8.73
                                                                    10.1
                                                                                 81
##
   2
                 10
                             283
                                       48
                                            1100
                                                     6.40
                                                            5.65
                                                                     7.00
                                                                                100
          1
                        10
                                                                     7.00
##
   3
                 9
                         3
                             169
                                       40
                                            1100
                                                     5.94
                                                            5.13
                                                                                81
          1
##
    4
          0
                 22
                        22
                            1100
                                      -54
                                            1000
                                                     6.48
                                                            7.00
                                                                     6.91
                                                                                484
##
   5
                 8
                             351
                                       28
                                             387
                                                     6.21
                                                            5.86
                                                                     5.96
          1
                         6
                                                                                 64
##
   6
          1
                 7
                         7 19000
                                      614
                                            3900
                                                     6.97
                                                            9.85
                                                                     8.27
                                                                                 49
##
    7
          0
                 35
                        10
                             536
                                       24
                                             623
                                                     6.85
                                                            6.28
                                                                     6.43
                                                                               1225
                            4800
                                      191
                                            2100
##
   8
          1
                 32
                         8
                                                     7.14
                                                            8.48
                                                                     7.65
                                                                               1024
##
   9
                             610
                                              454
                                                     6.22
                                                            6.41
          1
                 4
                                        7
                                                                     6.12
                                                                                 16
## 10
                 39
                         5 2900
                                      230
                                            3900
                                                     7.00
                                                            7.97
                                                                     8.27
                                                                               1521
## # ... with 167 more rows, and 2 more variables: ceotensq <dbl>,
```

rename() - change column names

profmarg <dbl>

#

```
names(ceo)

## [1] "salary" "age" "college" "grad" "comten" "ceoten"

## [7] "sales" "profits" "mktval" "lsalary" "lsales" "lmktval"

## [13] "comtensq" "ceotensq" "profmarg"
```

```
ceo_new <- ceo %>% rename(profit_margin = profmarg)
names(ceo_new)
    [1] "salary"
                          "age"
                                                             "grad"
##
                                            "college"
##
    [5] "comten"
                          "ceoten"
                                            "sales"
                                                             "profits"
    [9] "mktval"
##
                                                             "lmktval"
                          "lsalary"
                                            "lsales"
## [13] "comtensq"
                          "ceotensq"
                                            "profit_margin"
arrange() - sort data
ceo %>%
  # filter if age is larger than 50
  filter(age > 50) %>%
  # sort by age and then salary
  arrange(age,salary)
## # A tibble: 139 x 15
##
      salary
                age college grad comten ceoten sales profits mktval lsalary
##
                                             <dbl> <dbl>
       <dbl> <dbl>
                       <dbl> <dbl>
                                     <dbl>
                                                            <dbl>
                                                                    <dbl>
                                                                             <dbl>
##
    1
         246
                 51
                           1
                                  0
                                         8
                                                 8
                                                      78
                                                               13
                                                                      458
                                                                              5.51
         379
##
    2
                 51
                           1
                                  1
                                         9
                                                 3
                                                     169
                                                               40
                                                                     1100
                                                                              5.94
##
         541
                                        30
                                                    1400
                                                               82
                                                                     1200
                                                                              6.29
    3
                 51
                           1
         697
                                        25
                                                    8200
                                                                     5700
##
    4
                 51
                           1
                                  0
                                                 1
                                                              234
                                                                              6.55
        1487
##
    5
                 51
                           1
                                  0
                                         3
                                                 3 22200
                                                              182
                                                                     2800
                                                                              7.30
##
         483
                                                   1000
                                                               35
    6
                 52
                           1
                                  1
                                        18
                                                14
                                                                      548
                                                                              6.18
                                                                      889
##
    7
         515
                 52
                           1
                                  1
                                        27
                                                 1
                                                    1100
                                                               51
                                                                              6.24
##
         552
                 52
                                  0
                                        30
                                                    2800
                                                              308
                                                                     3500
                                                                              6.31
    8
                           1
                                                 1
         704
                                         6
                                                                      903
##
    9
                 52
                           1
                                  1
                                                 6
                                                      50
                                                                8
                                                                              6.56
         999
                 52
                           1
                                  0
                                        28
                                                     159
                                                               21
                                                                      398
                                                                              6.91
## 10
                                                17
## # ... with 129 more rows, and 5 more variables: lsales <dbl>,
       lmktval <dbl>, comtensq <dbl>, ceotensq <dbl>, profmarg <dbl>
ceo %>%
  # filter if age is larger than 50
  filter(age > 50) %>%
  # sort by age (descend)
  arrange(desc(age),salary)
## # A tibble: 139 x 15
##
      salary
                age college grad comten ceoten sales profits mktval lsalary
       <dbl> <dbl>
                       <dbl> <dbl>
                                     <dbl>
                                             <dbl> <dbl>
                                                            <dbl>
##
                                                                   <dbl>
                                                                             <dbl>
##
    1
         425
                 86
                           1
                                        13
                                                13
                                                       36
                                                               11
                                                                      644
                                                                              6.05
                                  1
##
    2
         396
                 80
                           1
                                  0
                                        58
                                                28
                                                     513
                                                               53
                                                                      963
                                                                              5.98
##
         300
                 77
                           0
                                  0
                                        45
                                                26
                                                    6900
                                                              483
                                                                     4700
                                                                              5.70
    3
        1946
                                                                     8000
##
    4
                 73
                           1
                                  0
                                        25
                                                21
                                                    7800
                                                              484
                                                                              7.57
                                                24
##
    5
         971
                 72
                                        33
                                                    1400
                                                               69
                                                                      609
                                                                             6.88
                           1
                                  1
##
    6
        1200
                 72
                           1
                                  0
                                        37
                                                37
                                                     796
                                                               35
                                                                      678
                                                                             7.09
##
    7
         387
                 71
                           1
                                  1
                                        32
                                                13
                                                     432
                                                               28
                                                                      477
                                                                              5.96
##
    8
        1675
                 71
                           0
                                  0
                                        31
                                                12
                                                     674
                                                              115
                                                                     1200
                                                                              7.42
##
    9
                                                      29
                                                                      390
         174
                 69
                           1
                                  0
                                        13
                                                13
                                                                6
                                                                              5.16
## 10
         445
                 69
                           1
                                        23
                                                 0
                                                     249
                                                               31
                                                                      828
                                                                              6.10
     ... with 129 more rows, and 5 more variables: lsales <dbl>,
       lmktval <dbl>, comtensq <dbl>, ceotensq <dbl>, profmarg <dbl>
```

mutate() - modify columns

```
ceo %>%
  # add a new variable salary_l: log(salary)
  mutate(salary_l = log(salary)) %>%
  # select salary and salary_l
  select(salary, salary_1, lsalary)
## # A tibble: 177 x 3
##
      salary salary_l lsalary
##
       <dbl>
                <dbl>
                        <dbl>
##
   1
        1161
                 7.06
                         7.06
                 6.40
    2
         600
                         6.40
##
##
   3
         379
                 5.94
                         5.94
                 6.48
##
   4
         651
                         6.48
##
   5
         497
                 6.21
                         6.21
##
        1067
                 6.97
                         6.97
   6
        945
                 6.85
##
   7
                         6.85
        1261
                 7.14
                         7.14
##
  8
                 6.22
## 9
        503
                         6.22
## 10
        1094
                 7.00
                         7.00
## # ... with 167 more rows
distinct() - find unique rows
ceo %>%
  select(age, ceoten) %>%
  distinct() %>%
  arrange(age, ceoten)
## # A tibble: 147 x 2
##
        age ceoten
##
      <dbl> <dbl>
##
   1
         33
         38
                 3
##
   2
##
    3
         39
                 3
         39
##
   4
                 8
   5
         40
                 1
                 5
##
   6
         40
##
   7
                11
         40
##
  8
         41
                 2
## 9
         42
                12
         43
                 2
## 10
## # ... with 137 more rows
sample_n() sampling rows
ceo %>% sample_n(100)
## # A tibble: 100 x 15
##
               age college grad comten ceoten sales profits mktval lsalary
       <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
```

```
733
                                                                 778
                                                                         6.60
##
  1
                60
                               0
                                      8
                                                  347
                                                           18
##
  2
         585
                60
                         1
                               1
                                      36
                                             10 1700
                                                           33
                                                                 449
                                                                         6.37
         491
##
   3
                43
                               1
                                      21
                                              2
                                                  561
                                                           54
                                                                 521
                                                                         6.20
        1268
                                      20
                                                1100
                                                           47
                                                                2500
                                                                         7.15
##
   4
                47
                         1
                               0
##
   5
        1067
                64
                         1
                               1
                                      7
                                              7 19000
                                                          614
                                                                3900
                                                                         6.97
##
  6
        1162
                58
                         1
                               0
                                                3800
                                                          226
                                                                1800
                                                                         7.06
                                     24
                                              6
##
   7
         449
                         1
                               0
                                     31
                                              1
                                                  661
                                                           37
                                                                 538
                                                                         6.11
                56
         379
                                                           40
                                                                1100
                                                                         5.94
## 8
                51
                         1
                               1
                                      9
                                              3
                                                  169
## 9
         834
                61
                         1
                               1
                                      32
                                              0
                                                 7600
                                                          364
                                                                 5300
                                                                         6.73
## 10
         581
                54
                               0
                                      19
                                             19
                                                  408
                                                           23
                                                                 403
                         1
                                                                         6.36
## # ... with 90 more rows, and 5 more variables: lsales <dbl>,
       lmktval <dbl>, comtensq <dbl>, ceotensq <dbl>, profmarg <dbl>
```

summarise() - summarize data

Tabulate Data by grad

```
# creat your own contingency table
ceo_tab = ceo %>%
  # define subgroups
  group_by(grad) %>%
  # provide summary statistic: # of obs, min, max
  summarize(n = n(),
            mean = mean(salary,na.rm = T),
            sd = var(salary,na.rm = T) %>% sqrt(.),
            min = min(salary,na.rm = T),
            max = max(salary,na.rm = T))
ceo_tab
## # A tibble: 2 x 6
     grad
                               min
               n mean
                          sd
     <dbl> <int> <dbl> <dbl> <dbl> <dbl> <dbl>
        0
              83 868.
                        675.
                               174
## 2
         1
              94 864.
                        501.
                               100 2265
```

Using xtable() to export

```
xtable(ceo_tab)
```

% latex table generated in R 3.5.1 by xtable 1.8-3 package % Thu Sep 12 16:14:47 2019

	grad	n	mean	sd	min	max
1	0.00	83	867.73	675.22	174.00	5299.00
2	1.00	94	864.21	501.39	100.00	2265.00

T-test

Tabulate your data

```
# creat your own table
tab <- ceo %>%
 # define subgroups
 group_by(grad) %>%
 # provide summary statistic: # of obs, min, max
 summarize(n = n(),
           mean = mean(profmarg,na.rm = T),
           sd = var(profmarg,na.rm = T) %>% sqrt(.),
           min = min(profmarg,na.rm = T),
           max = max(profmarg,na.rm = T))
tab
## # A tibble: 2 x 6
   grad n mean
                         sd
                             {\tt min}
    <dbl> <int> <dbl> <dbl> <dbl> <dbl>
      0 83 6.71 8.23 -48.1 23.9
## 1
        1
             94 6.16 23.3 -203.
```

Construct T-statistic

$$t = \frac{\bar{X}_t - \bar{X}_c}{\hat{\sigma}_{\bar{X}_t - \bar{X}_c}}$$

where:

$$\hat{\sigma}_{\bar{X_t} - \bar{X_c}} = \sqrt{\frac{\hat{\sigma}_{\bar{X_t}}}{n_t} + \frac{\hat{\sigma}_{\bar{X_c}}}{n_c}}$$

```
# number of observations
n_c <- tab$n[1]
n_t <- tab$n[2]

# mean
mean_c <- tab$mean[1]
mean_t <- tab$mean[2]

# standard deviation
sd_c <- tab$sd[1]
sd_t <- tab$sd[2]

# compute sigma
signma_tc <- sqrt(sd_c^2/n_c + sd_t^2/n_t)</pre>
```

```
# compute t-statistic
t_test <- (mean_t - mean_c)/ signma_tc
t_test</pre>
```

[1] -0.2138428

The degrees of freedom

R uses Welch DoF, which is estimated as follows:

$$\nu_{W} = \frac{\left(\frac{s_{t}^{2}}{n_{t}} + \frac{s_{c}^{2}}{n_{c}}\right)^{2}}{\frac{s_{t}^{4}}{n_{r}^{2}\nu_{t}} + \frac{s_{c}^{4}}{n_{c}^{2}\nu_{c}}}$$

```
# numerator
num = (sd_t^2/n_t + sd_c^2/n_c)^2

# denominator
den = sd_t^4/( (n_t^2) * (n_t - 1)) + sd_c^4/( (n_c^2) * (n_c - 1))

# degrees of freedom
dof = num/den
dof
```

[1] 118.4336

Confidence Interval

$$CI = (\bar{X} - t^* * \hat{\sigma}_{\bar{X}_t - \bar{X}_c}, \bar{X} + t^* * \hat{\sigma}_{\bar{X}_t - \bar{X}_c})$$

where $\sigma_{\bar{X}_t - \bar{X}_c}$ is the estimated standard error, t^* is the critical value of t for the desired level of confidence.

```
mean_dif <- mean_t mean_dif
```

```
## [1] 0.5494467
```

```
critical_t <- qt(0.05/2, dof)
mean_dif - critical_t*signma_tc</pre>
```

```
## [1] 5.637355
mean_dif + critical_t*signma_tc
```

[1] -4.538462

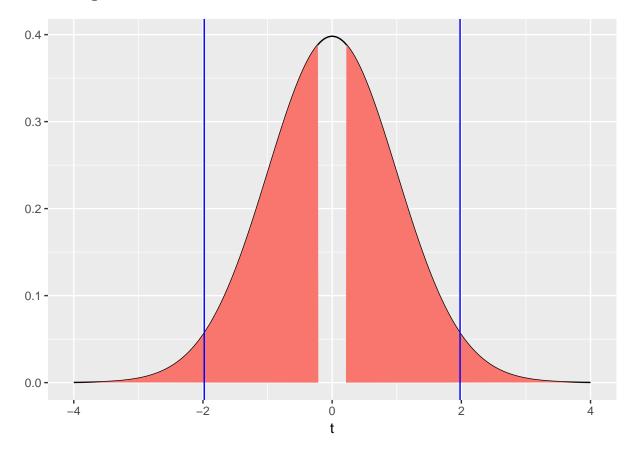
P value

$$|T| > t_{1-\alpha/2,\nu}$$

```
2*pt(-abs(t_test), df = dof) # pt() is the distribution function of t Distribution
```

[1] 0.8310373

Visualizing P value



T-test using t.test

```
##
## Welch Two Sample t-test
##
## data: profmarg by grad
## t = 0.21384, df = 118.43, p-value = 0.831
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -4.538462 5.637355
## sample estimates:
## mean in group 0 mean in group 1
## 6.711907 6.162460
```