

Data Science for Economists

Lecture 4: Functions

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Introduction

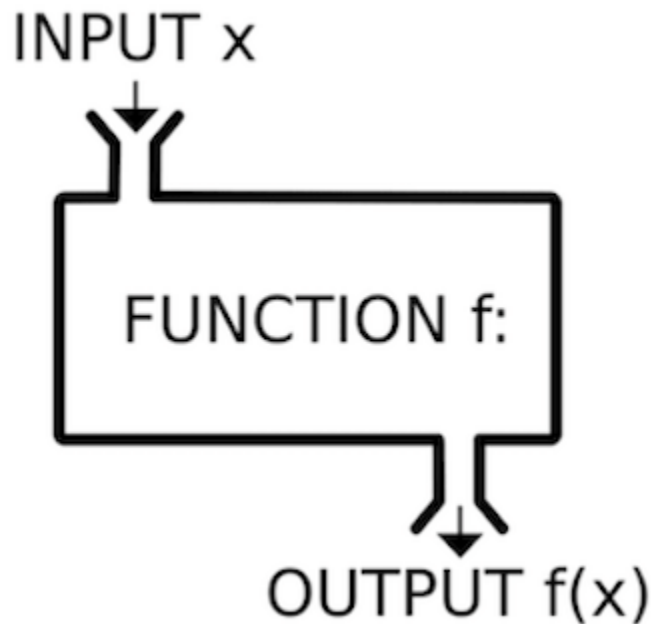
Agenda

Today we will finally officially cover functions.

While we have already used and talked about them quite a lot, there are some things we should go over along with learning how to write our own.

Functions

What is a function? Just like in m



Terminology

- Function: f
- Function input/arguments: x
- Function output: $f(x)$

Motivation

Let's generate a simple data.frame:

```
d = data.frame(x=runif(6),y=rnorm(6),z=rchisq(6,1))
```

Imagine we want to rescale each of these vectors so the minimum value and the maximum in the column is 1. Here is one way we could do this:

```
d$x = (d$x - min(d$x,na.rm=TRUE))/(max(d$x, na.rm=TRUE) - min(d$x,  
d$y = (d$y - min(d$x,na.rm=TRUE))/(max(d$y, na.rm=TRUE) - min(d$y,  
d$z = (d$z - min(d$z,na.rm=TRUE))/(max(d$z, na.rm=TRUE) - min(d$z,  
  
head(d)
```

```
##           x           y           z  
## 1 0.2704415 0.02365953 0.14054315  
## 2 0.8299695 0.04338331 0.54221604  
## 3 0.4060968 0.57550079 0.00000000  
## 4 0.9358038 0.15466332 1.00000000  
## 5 1.0000000 -0.42449921 0.33814069  
## 6 0.0000000 -0.23047777 0.04121895
```

Something's wrong here.

Motivation

Look more closely:

```
d$y = (d$y - min(d$x, na.rm=TRUE))/(max(d$y, na.rm=TRUE) - min(d$y,
```

I accidentally included the minimum from column x as opposed to column y. What we want is this:

```
d$Var = (d$Var - min(d$Var, na.rm=TRUE))/(max(d$Var, na.rm=TRUE) -
```

where we can give R a list of columns and it performs the same process. This is what a function does. Our initial ones will be a little bit simpler than this.

What is a function

Functions in programming are just like functions in math: they take in input and return a unique output.

Functions allow you to put code that you use frequently into a single line.

You should consider writing a function whenever you've copied a block of code more than twice (i.e. you now have three copies of it).

R for Data Science

Using functions appropriately makes for much cleaner code and code w/ less errors.

Functions are verbs; arguments are nouns.

A Trivial Function

```
return_input = function(x){  
  x #return the input as output  
}
```

```
return_input(1)
```

```
## [1] 1
```

```
return_input(letters)
```

```
## [1] "a" "b" "c" "d" "e" "f" "g" "h" "i" "j" "k" "l" "m" "n" "o"
```

```
## [20] "t" "u" "v" "w" "x" "y" "z"
```

```
return_input = function(x){  
  return(x) #this is equivalent, I prefer this  
}
```

```
return_input(1)
```

```
## [1] 1
```

Pythagorean Theorem

```
hypotenuse = function(a,b){  
  sqrt(a^2+b^2)  
}  
hypotenuse(3,4)
```

```
## [1] 5
```

```
hypotenuse(1:5,2:6)
```

```
## [1] 2.236068 3.605551 5.000000 6.403124 7.810250
```

```
hypotenuse(3,1:5)
```

```
## [1] 3.162278 3.605551 4.242641 5.000000 5.830952
```

```
hypotenuse(3:5,1:5) #don't do this
```

```
## Warning in a^2 + b^2: longer object length is not a multiple of  
## length
```

```
## [1] 3.162278 4.472136 5.830952 5.000000 6.403124
```

A Weighted Mean

```
wt_mean = function(x,w){  
  sum(x*w)/sum(w)  
}  
wts = runif(20)  
wt_mean(1:20,wts)
```

```
## [1] 11.99396
```

```
wt_mean = function(x,w){  
  if(length(x)≠length(w)){  
    stop("x and w must be the same length")  
  }  
  sum(x*w)/sum(w)  
}
```

```
wt_mean(1:20,wts[-1])
```

```
## Error in wt_mean(1:20, wts[-1]): x and w must be the same length
```

```
wt_mean(w = wts, x=1:20)
```

```
## [1] 11.99396
```

Default Arguments

In **R** you can define default arguments for functions. Typically you do this for arguments that are used often and you don't want to always pass it to the function.

We've already seen one example of default arguments:

```
rmnorm(1)
```

```
## [1] -0.3200564
```

```
rmnorm(1,mean=0,sd=1)
```

```
## [1] -1.311522
```

To define a default argument, simply add it to the list of arguments with the default value.

```
test_fun = function(x, y=2){  
  x+y  
}  
test_fun(3)
```

```
## [1] 5
```

Default Arguments: Weighted M

```
wt_mean = function(x,w=rep(1,length(x))){  
  # Description: Takes the weighted average of x using weights w  
  # Default w is a vector of 1s the same length as x.  
  
  if(length(x)≠length(w)){  
    stop("x and w must be the same length")  
  }  
  
  sum(x*w)/sum(w)  
}
```

```
wt_mean(1:20)      # my weighted mean fun with equal weights
```

```
## [1] 10.5
```

```
mean(1:20)         # same as my function
```

```
## [1] 10.5
```

```
wt_mean(1:20, wts) # with the random weights
```

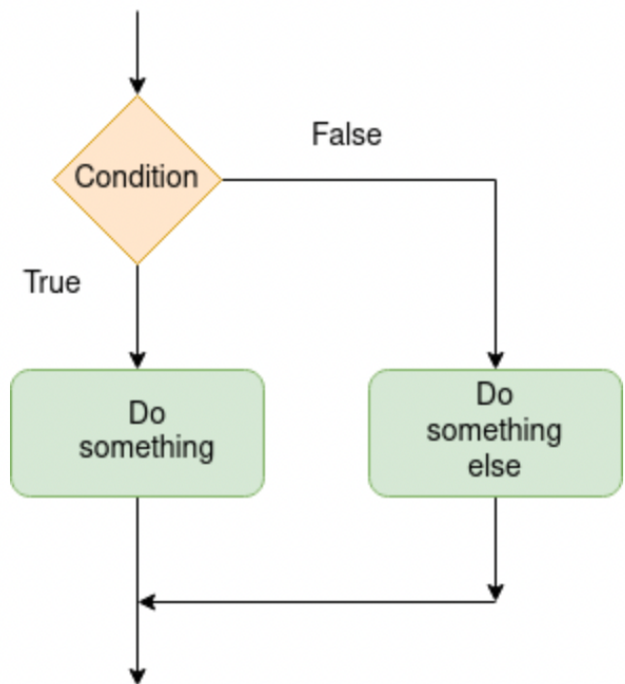
```
## [1] 11.99396
```

Intro to Control Flow

Control flow refers to ways in which we control the order in which code is executed.

The reason we learned the logic above is because we can use logical gates to determine the path our code takes.

Note: for simplicity, taking if statements outside of function definitions on these slides.



if Statements

If statements are the most fundamental aspect of control flow.

If something is true, then the code is executed. Otherwise, the code moves on.

If statements must take a logical as an input: either `TRUE` or `FALSE`.

```
x = 2
if(x < 0){
  print("x is less than 0")
}
```

Notice nothing printed!

```
x = -1
if(x < 0){
  print("x is less than 0")
}
```

```
## [1] "x is less than 0"
```


if, else if, and else

However, sometimes we want to check multiple conditions. We can use `if` statements.

```
x = runif(1,-1,1)
if(x > 0){
  print("x is positive!")
} else if(x < 0){
  print("x is negative!")
} else{
  print("x is 0!")
}
```

```
## [1] "x is negative!"
```

```
x
```

```
## [1] -0.4512327
```

More on if Statements

Let me show you an example of bad code

```
grade = 85 + rnorm(1,sd=5)
if (grade ≥ 90) {
  print(paste0("A ",round(grade)," is an A"))
}
if (grade ≥ 80 & grade < 90) {
  print(paste0("An ",round(grade)," is a B"))
}
```

```
## [1] "An 89 is a B"
```

```
if (grade ≥ 70 & grade < 80) {
  print(paste0("A ",round(grade)," is a C"))
}
if (grade ≥ 60 & grade < 70) {
  print(paste0("A ",round(grade)," is a D"))
}
if(grade < 50){
  print(paste0("A ",round(grade)," is an F"))
}
```

More on if Statements

To write clean code, think smart:

```
if (grade ≥ 90) {  
    print(paste0("A ",round(grade)," is an A"))  
} else if (grade ≥ 80) {  
    print(paste0("A ",round(grade)," is a B"))  
} else if (grade ≥ 70) {  
    print(paste0("A ",round(grade)," is a C"))  
} else if (grade ≥ 60) {  
    print(paste0("A ",round(grade)," is a D"))  
} else{  
    print(paste0("A ",round(grade)," is an F"))  
}
```

```
## [1] "A 89 is a B"
```

More on if Statements

The "else if" and "else" statements must be on the same line as the curly

```
statement = F
if(statement)
{print("It's True!")}
else
{print("It's False!")}
}
```

```
## Error: <text>:5:1: unexpected 'else'
## 4: }
## 5: else
##      ^
```

```
statement = F
if(statement)
{print("It's True!")}
else
{print("It's False!")}
}
```

```
## [1] "It's False!"
```

More on if Statements

If everything fits on one line, that then don't need curly brackets

```
x1 = if(TRUE) 2 else 3  
x2 = if(FALSE) 2 else 3  
c(x1,x2)
```

```
## [1] 2 3
```

Vectorized if Statements

With the standard if statement, R only allows a single logical value to be

- If a vector is supplied, it only takes the first element.

```
vals = c(T,F)
if(vals){
  print("TRUE!")
}
```

```
## Error in if (vals) {: the condition has length > 1
```

To do if else operations with a vector of logicals, use `ifelse()`

```
x = 1:10
ifelse(x %% 2 == 0, "Even", "Odd")
```

```
## [1] "Odd" "Even" "Odd" "Even" "Odd" "Even" "Odd" "Even" "Odd"
```

Test Your Understanding

Take 30 seconds to think about the following, then group up with the people in your neighborhood to discuss:

Using `ifelse()` commands, write a block of code that prints out "the remainder" for each integer 1 to 10 where `r` is the remainder when dividing by 3

Conditions

Sometimes we would like to throw an error, warning, or message while c of the code.

This can be done with the following respective functions: `stop()`, `warni`

```
x = 0
if(x>0){
  print(1/x)
}else if(x<0){
  print(-1/x)
}else{stop("You cannot divide by 0!")}
```

```
## Error in eval(expr, envir, enclos): You cannot divide by 0!
```

```
warning("This is a warning!")
```

```
## Warning: This is a warning!
```

```
message("This is a message!")
```

```
## This is a message!
```


Conditions

- Errors stop code from running. These should be used to prevent something from running.
- Warnings will still allow for code to run, but in most cases, caution should be taken when the warning is triggered.
- Messages can be useful when writing functions to see what is happening.
 - More to come later.

Back to Functions

Default Arguments

```
normalize = function(x, m = mean(x,na.rm=na.rm),s = sd(x,na.rm=na.rm))  
  return((x - m)/s)  
}  
normalize(1:10)
```

```
## [1] -1.4863011 -1.1560120 -0.8257228 -0.4954337 -0.1651446  0.1651446  0.4954337  
## [7]  0.4954337  0.8257228  1.1560120  1.4863011
```

```
normalize(c(1:10,NA))
```

```
## [1] NA NA NA NA NA NA NA NA NA NA NA
```

```
normalize(c(1:10,NA),na.rm=TRUE)
```

```
## [1] -1.4863011 -1.1560120 -0.8257228 -0.4954337 -0.1651446  0.1651446  0.4954337  
## [7]  0.4954337  0.8257228  1.1560120  1.4863011                NA
```

Writing Functions: Good Style

The following are some recommendations for good programming style w

1. Name your functions something descriptive.
 - Remember, they are verbs!
2. Try to foresee errors and incorrect inputs to your functions and provide warnings.
 - This is less important if your functions are only for you.
3. Comment, comment comment!
4. If you write a "family" of functions, try to use similar naming schemes.
5. Scope....

Scope

I've referred to the global environment a lot throughout lectures. In terms of the most general.

However, the environment within a function is a separate, more specific environment. Understanding this difference is important.

Variables in the global environment can be referred to in `R` but variables in a function environment that are not returned *will not* be saved in the global environment.

It is generally frowned upon to refer to too many global variables within a function.

- It also depends on how lazy you're being

Let's see some examples.

Scope Examples

```
y = 2
add_xy = function(x){
  return(x + y)
}
add_xy(3)
```

```
## [1] 5
```

```
my_mean = function(x){
  x_sum = sum(x)
  x_sum/length(x)
}
my_mean(1:10)
```

```
## [1] 5.5
```

```
x_sum
```

```
## Error in eval(expr, envir, enclos): object 'x_sum' not found
```

```
-- return() makes this clearer:
```

```
my_mean = function(x){
```

Advice Regarding Scope

- Variables that are unlikely to change throughout a script are safe to refer to as "global variables."
 - e.g. *N_sim* in a simulation exercise.
- When writing functions, only refer to variables in the global environment as described above. Relying on globals too much is sloppy.
- However, writing functions with too many arguments is also bad practice. Try to find a balance.
- There are ways to save variables created in a function to the global environment (e.g. `assign` or `global` or `assignGlobal` or `globalVariables` or `assignGlobalEnv` or `assignGlobalEnv2` or `assignGlobalEnv3` or `assignGlobalEnv4` or `assignGlobalEnv5` or `assignGlobalEnv6` or `assignGlobalEnv7` or `assignGlobalEnv8` or `assignGlobalEnv9` or `assignGlobalEnv10` or `assignGlobalEnv11` or `assignGlobalEnv12` or `assignGlobalEnv13` or `assignGlobalEnv14` or `assignGlobalEnv15` or `assignGlobalEnv16` or `assignGlobalEnv17` or `assignGlobalEnv18` or `assignGlobalEnv19` or `assignGlobalEnv20` or `assignGlobalEnv21` or `assignGlobalEnv22` or `assignGlobalEnv23` or `assignGlobalEnv24` or `assignGlobalEnv25` or `assignGlobalEnv26` or `assignGlobalEnv27` or `assignGlobalEnv28` or `assignGlobalEnv29` or `assignGlobalEnv30` or `assignGlobalEnv31` or `assignGlobalEnv32` or `assignGlobalEnv33` or `assignGlobalEnv34` or `assignGlobalEnv35` or `assignGlobalEnv36` or `assignGlobalEnv37` or 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`assignGlobalEnv164` or `assignGlobalEnv165` or `assignGlobalEnv166` or `assignGlobalEnv167` or `assignGlobalEnv168` or `assignGlobalEnv169` or `assignGlobalEnv170` or `assignGlobalEnv171` or `assignGlobalEnv172` or `assignGlobalEnv173` or `assignGlobalEnv174` or `assignGlobalEnv175` or `assignGlobalEnv176` or `assignGlobalEnv177` or `assignGlobalEnv178` or `assignGlobalEnv179` or `assignGlobalEnv180` or `assignGlobalEnv181` or `assignGlobalEnv182` or `assignGlobalEnv183` or `assignGlobalEnv184` or `assignGlobalEnv185` or `assignGlobalEnv186` or `assignGlobalEnv187` or `assignGlobalEnv188` or `assignGlobalEnv189` or `assignGlobalEnv190` or `assignGlobalEnv191` or `assignGlobalEnv192` or `assignGlobalEnv193` or `assignGlobalEnv194` or `assignGlobalEnv195` or `assignGlobalEnv196` or `assignGlobalEnv197` or `assignGlobalEnv198` or `assignGlobalEnv199` or `assignGlobalEnv200` or `assignGlobalEnv201` or `assignGlobalEnv202` or `assignGlobalEnv203` or `assignGlobalEnv204` or `assignGlobalEnv205` or `assignGlobalEnv206` or `assignGlobalEnv207` or `assignGlobalEnv208` or `assignGlobalEnv209` or `assignGlobalEnv210` or `assignGlobalEnv211` or `assignGlobalEnv212` or `assignGlobalEnv213` or `assignGlobalEnv214` or `assignGlobalEnv215` or `assignGlobalEnv216` or `assignGlobalEnv217` or `assignGlobalEnv218` or `assignGlobalEnv219` or `assignGlobalEnv220` or `assignGlobalEnv221` or `assignGlobalEnv222` or `assignGlobalEnv223` or `assignGlobalEnv224` or `assignGlobalEnv225` or `assignGlobalEnv226` or `assignGlobalEnv227` or `assignGlobalEnv228` or `assignGlobalEnv229` or `assignGlobalEnv230` or `assignGlobalEnv231` or `assignGlobalEnv232` or `assignGlobalEnv233` or `assignGlobalEnv234` or `assignGlobalEnv235` or `assignGlobalEnv236` or `assignGlobalEnv237` or `assignGlobalEnv238` or `assignGlobalEnv239` or `assignGlobalEnv240` or `assignGlobalEnv241` or `assignGlobalEnv242` or `assignGlobalEnv243` or `assignGlobalEnv244` or `assignGlobalEnv245` or `assignGlobalEnv246` or `assignGlobalEnv247` or `assignGlobalEnv248` or `assignGlobalEnv249` or `assignGlobalEnv250` or `assignGlobalEnv251` or `assignGlobalEnv252` or `assignGlobalEnv253` or `assignGlobalEnv254` or `assignGlobalEnv255` or `assignGlobalEnv256` or `assignGlobalEnv257` or `assignGlobalEnv258` or `assignGlobalEnv259` or `assignGlobalEnv260` or `assignGlobalEnv261` or `assignGlobalEnv262` or `assignGlobalEnv263` or `assignGlobalEnv264` or `assignGlobalEnv265` or `assignGlobalEnv266` or `assignGlobalEnv267` or `assignGlobalEnv268` or `assignGlobalEnv269` or `assignGlobalEnv270` or `assignGlobalEnv271` or `assignGlobalEnv272` or `assignGlobalEnv273` or `assignGlobalEnv274` or `assignGlobalEnv275` or `assignGlobalEnv276` or `assignGlobalEnv277` or `assignGlobalEnv278` or `assignGlobalEnv279` or `assignGlobalEnv280` or `assignGlobalEnv281` or `assignGlobalEnv282` or `assignGlobalEnv283` or `assignGlobalEnv284` or `assignGlobalEnv285` or `assignGlobalEnv286` or 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Returning vs Printing

I have hinted at the difference between returning an object and printing

This distinction matters the most for functions.

When you return an object from a function, that is the only thing that ca

When you print an object, it shows output but does not return the object
unless you also specify it to print.

The best thing I can say to understand the difference is that printing is f
is for the computer!

Let's look at some examples.

Returning vs Printing

```
plus_delta = function(x,delta=1){  
  print(paste0("We are adding ", delta, " to ", x, "!"))  
  x + delta  
}
```

```
plus_delta(5)
```

```
## [1] "We are adding 1 to 5!"
```

```
## [1] 6
```

```
plus_delta(4.5,0.75)
```

```
## [1] "We are adding 0.75 to 4.5!"
```

```
## [1] 5.25
```

Returning vs Printing

```
mult_plus1 = function(x,y){  
  xy = x*y  
  print(xy)  
  xy+1  
}
```

```
mult_plus1(2,3)
```

```
## [1] 6
```

```
## [1] 7
```

```
xy
```

```
## Error in eval(expr, envir, enclos): object 'xy' not found
```

```
out1 = mult_plus1(2,3)
```

```
## [1] 6
```

```
out1
```

```
## [1] 7
```

Returning vs Printing

If the last line of a function is a print statement, will also return the printed characters)

```
mult_plus1 = function(x,y){  
  xy = x*y  
  print(xy+1)  
}
```

```
out2 = mult_plus1(2,3)
```

```
## [1] 7
```

```
out2
```

```
## [1] 7
```

```
class(out2)
```

```
## [1] "numeric"
```

Misc Aspects of Functions

Functions don't have to have arguments.

Functions don't have to return an object.

Functions can only return one object; however, if you're using if statements multiple returns specified. It's just ultimately only one will be used.

You can write functions to take an arbitrary number of inputs using ...

No arguments or Returns

```
say_hello = function(){  
  print("Hello! :)")  
} #notice, nothing is being returned either!!  
  
say_hello()
```

```
## [1] "Hello! :)"
```

```
say_my_name = function(name){  
  print(name)  
}  
  
say_my_name("Drew")
```

```
## [1] "Drew"
```

Conditional Returns

```
is_prime = function(x){  
  if ( x %% 1 != 0 ) stop("x must be an integer!")  
  if ( length(x)!=1 ) stop("x can only be length 1!")  
  if ( x %in% 1:2 ){ # if x is 1 or 2, return FALSE or TRUE  
    return(x == 2)  
  } else { # otherwise, loop through numbers 3 to x  
    num_vec      = 3:x  
    prime_list = 2  
    i            = 1  
    for(n in num_vec){  
      if(sum((n %% prime_list) == 0) == 0){  
        i            = i + 1  
        prime_list[i] = n  
      }  
    }  
    if(x %in% prime_list){ # if x is in list of primes, return TRUE  
      return(TRUE)  
    }else{ # otherwise, return FALSE  
      return(FALSE)  
    }  
  }  
}
```

Conditional Returns

```
primes1to100 = sapply(1:100,is_prime)
names(primes1to100) = 1:100
primes1to100
```

```
##      1      2      3      4      5      6      7      8      9     10     11
## FALSE  TRUE  TRUE FALSE  TRUE FALSE  TRUE FALSE FALSE FALSE  TRUE
##     14     15     16     17     18     19     20     21     22     23     24
## FALSE FALSE FALSE  TRUE FALSE  TRUE FALSE FALSE FALSE  TRUE FALSE
##     27     28     29     30     31     32     33     34     35     36     37
## FALSE FALSE  TRUE FALSE  TRUE FALSE FALSE FALSE FALSE FALSE  TRUE
##     40     41     42     43     44     45     46     47     48     49     50
## FALSE  TRUE FALSE  TRUE FALSE FALSE FALSE  TRUE FALSE FALSE FALSE
##     53     54     55     56     57     58     59     60     61     62     63
##  TRUE FALSE FALSE FALSE FALSE FALSE  TRUE FALSE  TRUE FALSE FALSE
##     66     67     68     69     70     71     72     73     74     75     76
## FALSE  TRUE FALSE FALSE FALSE  TRUE FALSE  TRUE FALSE FALSE FALSE
##     79     80     81     82     83     84     85     86     87     88     89
##  TRUE FALSE FALSE FALSE  TRUE FALSE FALSE FALSE FALSE FALSE  TRUE
##     92     93     94     95     96     97     98     99    100
## FALSE FALSE FALSE FALSE FALSE  TRUE FALSE FALSE FALSE
```

Arbitrary Inputs

```
commas = function( ... ){  
  out = paste( ... ,sep = ", ")  
  out  
}  
  
commas("red","blue", "yellow","green")
```

```
## [1] "red, blue, yellow, green"
```

Any arguments that come after `...` *must have default arguments!*

Next lecture(s): Misc.
