

GEORGIA INSTITUTE OF TECHNOLOGY
SCHOOL of ELECTRICAL and COMPUTER ENGINEERING
ECE 6254 Fall 2022
Project #2

Assigned: 15 Sep
Due Date: 22 Sep

Please contact the TAs for clarification on the instructions in the assignments.

For all Problems, to get credit you must submit your answers/code on Canvas under “Assignments → Project 2” (submit answers here).

Problem 1

In this problem we will compare the performance of traditional least squares, ridge regression, and the LASSO on a real-world dataset. We will use the “Boston House Prices” dataset which contains the median sale price (as of some point in the 1970’s, when the dataset was created) of owner occupied homes in about 500 different neighborhoods in the Boston area, along with 13 features for each home that might be relevant. These features include factors such as measures of the crime rate; measures of school quality; various measures of density; proximity to things like highways, major employment centers, the Charles River; pollution levels; etc.¹

Follow the same steps as Project 1 to get on the COC-ICE cluster (and assuming you use the conda env ece6254 as defined in Project 1):

- VPN into Georgia Tech (see Slide 7 of the ICE Orientation slides)

<https://faq.oit.gatech.edu/content/how-do-i-get-started-campus-vpn/>

- `ssh <gt-userID>@coc-ice.pace.gatech.edu`
- `module load anaconda3/2020.11`
- `conda activate ece6254`

To get the Boston House Prices dataset in Python

- `conda install -c conda-forge scikit-learn`
- `python`
- `from sklearn.datasets import load_boston`
- `boston = load_boston()`
- `X = boston.data`
- `y = boston.target`

¹See <http://bit.ly/21TueYY> for more details about this dataset.

Problem 1 (cont.)

To judge the quality of each approach, split the dataset into a training set and a testing set. The training set should consist of 400 observations, and use the remaining observations for testing.

Before training any of these algorithms, it is a good idea to “standardize” the data. By this, I mean that you should take each feature (i.e., each column of the matrix \mathbf{X}) and subtract off its mean and divide by the standard deviation to make it zero mean and unit variance. Otherwise, the regularized methods will implicitly be placing bigger penalties on using features which just happen to be scaled to have small variance. You should determine how to “standardize” your training data by appropriately shifting/scaling each feature *using only the training data*, and then apply this transformation to both the training data and the testing data so that your learned function can readily be applied to the test set.

1. First, I would like you to evaluate the performance of least squares. You should implement this yourself using the equation we derived in class. Report the performance of your algorithm in terms of mean-squared error on the test set, i.e.,

$$\frac{1}{n_{\text{test}}} \|\mathbf{y}_{\text{test}} - \mathbf{X}_{\text{test}} \hat{\boldsymbol{\theta}}\|_2^2.$$

2. Next, using the formula derived in class, implement your own version of ridge regression. You will need to set the free parameter λ . You should do this using the training data in whatever manner you like (e.g., via a holdout set) – but you should *not* allow the testing dataset to influence your choice of λ . Report the value of λ selected and the performance of your algorithm in terms of mean-squared error on the test set.
3. Finally, I would like you to evaluate the performance of the LASSO. You do not need to implement this yourself. Instead, you can use scikit-learn’s built in solver via

```
1 from sklearn import linear_model
2 reg = linear_model.Lasso(alpha = ???) # Fill in alpha
3 reg.fit(Xtrain,ytrain)
4 reg.predict(Xtest)
```

Above, `alpha` corresponds to the λ parameter from the lecture notes. As in part (b), you will need to do something principled to choose a good value for this parameter. Report the value of `alpha` used in your code, the performance of your algorithm in terms of mean-squared error, and the number of nonzeros in $\boldsymbol{\theta}$. (You can get $\boldsymbol{\theta}$ via `reg.coef_`.)

Problem 2

In this problem I'd like you to use the following code to generate a dataset to evaluate various approaches to regression in the presence of outliers.

```
1 import numpy as np
2 np.random.seed(2017)
3 n = 100
4 xtrain = np.random.rand(n)
5 ytrain = 0.25 + 0.5*xtrain + np.sqrt(0.1)*np.random.randn(n)
6 idx = np.random.randint(0,100,10)
7 ytrain[idx] = ytrain[idx] + np.random.randn(10)
```

The code above generates training data by selecting random values for the x_i 's, then computing $f(x) = \frac{1}{4} + \frac{1}{2}x$ and adding a small amount of Gaussian noise to each observation. It then follows by creating some “outliers” in the y_i 's by picking 10 random entries and adding a much larger amount of noise to just those elements.

In the problems below, you should find a linear fit to this data. In all of the methods below, there will be one or more parameters to set. You can do this manually using whatever approach you like. (Do not go crazy optimizing these, just tune the parameters until your estimate looks reasonable.)

1. To begin, find a linear fit using the code for ridge regression that you produced in the first problem. Report the value of λ that you selected, and report the slope and intercept of your linear fit.
2. Next, I would like you to find a linear fit using the Huber loss. This can be done via

```
1 from sklearn import linear_model
2 reg = linear_model.HuberRegressor(epsilon = 1.35, alpha=0.001)
3 reg.fit(xtrain.reshape(-1,1),ytrain)
```

You have two parameters to choose here: ϵ (which controls the shape of the loss function and needs to be greater than 1.0) and α (the regularization parameter). Report the values of ϵ and α you selected, and report the slope and intercept of your linear fit (see `reg.intercept_` and `reg.coef_`).