

# Growth of transverse cracks from multiple adjacent debonds: debond-debond interaction between rows of partially debonded fibers in UD composites

Luca Di Stasio<sup>a,b</sup>, Janis Varna<sup>b</sup>, Zoubir Ayadi<sup>a</sup>

<sup>a</sup>*Université de Lorraine, EEIGM, IJL, 6 Rue Bastien Lepage, F-54010 Nancy, France*

<sup>b</sup>*Luleå University of Technology, University Campus, SE-97187 Luleå, Sweden*

---

## Abstract

Models of Repeating Unit Cell (RUC) are developed to represent different Representative Volume Elements (RVEs) of UD composites of infinite size. Several damage states are studied in the form of different geometrical configurations of partially debonded and fully bonded fibers. It is found that the energetically most favorable cases for fiber/matrix interface crack (debond) growth are those where debonds grow on vertically (i.e. along thickness direction) aligned fibers. A maximum of Energy Release Rate (ERR) magnification is found when the vertically aligned partially debonded fibers are also contiguous.

*Keywords:* Polymer-matrix Composites (PMCs), Transverse Failure, Debonding, Finite Element Analysis (FEA)

---

## 1. Introduction

Transverse cracks (or micro- or matrix cracks) represents one of the very first damage mechanism appearing in a Fiber Reinforced Polymer Composite (FRPC). A full understanding of the factors determining its onset and propagation could lead to structural improvements aimed to delay, suppress and possibly control transverse cracking in order to increase the energy absorbing capabilities of polymer composites. Early microscopic observations determined that onset of transverse cracking coincides with the appearance of fiber-matrix interface cracks (also called debonds), which grow along the arc direction of the

10 fiber until a critical size, then kink out of the interface and coalesce with other  
 debonds to form what is macroscopically seen as a transverse crack [1].  
 Analytical models of a single partially debonded fiber in an infinite matrix were  
 firstly solved by Perlman and Sih [2], who provided the solution in terms of  
 stress and displacement fields, and Toya [3], who analyzed the energy release  
 15 rate at the crack tip. Numerical treatment of the problem soon followed, in par-  
 ticular with the Boundary Element Method (BEM) solution by Paris et al. [4].  
 The numerical analysis of the single fiber model allowed first to understand the  
 importance of crack face contact in the mechanics of fiber-matrix debonding [5],  
 confirming earlier results regarding the straight bi-material interface [6]. Fiber-  
 20 matrix debonding was thus investigated in models of a single fiber embedded  
 in an effectively infinite matrix under remote tension [4] and remote compres-  
 sion [7]. Residual thermal stresses were also analyzed [8]. The effect of a second  
 nearby fiber was furthermore studied under the effect of different uniaxial and  
 biaxial tensile and compressive loads [9, 10, 11, 12]. Debond growth in a hexag-  
 25 onal cluster of fibers embedded in an effectively homogenized UD composite was  
 investigated by Zhuang et al. [13]. The interaction of two debonds facing each  
 other on two nearby fibers was addressed in [14] for a cluster of fibers immersed  
 in a homogenized UD, while models of kinking were developed for a single fiber  
 in an infinite matrix [15] and a cluster of fibers in a homogenized UD [16].  
 30 According to the observations presented in [1], multiple debonds grow at the  
 same time on a series of fibers roughly aligned along the thickness direction  
 of the laminate; they then kink and coalesce to form a transverse crack. If a  
 few studies of kinking [15, 16] and linking of debonds [14] are present in the  
 literature, it seems that no attention has still been paid to the effect on debond  
 35 growth of the presence of multiple debonds on (vertical or horizontal) rows of  
 fibers, i.e. the stage that precedes kinking, coalescence and the appearance  
 of a macroscopic transverse crack. It is this issue that we want to address in  
 this paper. By means of Representative Volume Elements (RVEs) with symme-  
 try or coupling conditions on all its boundaries, three different configurations  
 40 of debonds appearing in a UD composite with a regular microstructure under

transverse tension are studied: first, the case of multiple vertical (i.e. along the thickness direction) rows of partially debonded fibers; second, the case of multiple horizontal (i.e. along the loading direction) rows of partially debonded fibers; finally, the case of partially debonded fibers appearing after the same  
45 number of fully bonded fibers along the vertical and horizontal direction.

## 2. RVE models & FE discretization

### 2.1. Introduction & Nomenclature

We focus in this article on debond growth in unidirectional (UD) composites subjected to in-plane transverse tensile loading. In particular, the interaction  
50 between debonds is studied through the development of models of Repeating Unit Cells (RUC) of laminates (see Fig. 1 to Fig. 3). Only the central fiber in the RUC cell is in a damaged state in the form of a debond. The composite RUC is repeating both in the in-plane transverse direction and in the composite thickness direction; it thus corresponds to an infinite composite which models,  
55 in a limiting case, the behavior of a thick UD composite (free surfaces very far from the debonds). According to the proposed RUC design, the composite with debonds is considered as a sequence of stacked damaged and undamaged fiber rows, with each row having only one fiber in the thickness direction. Given that all the RUCs are characterized by a regular microstructure with fibers orga-  
60 nized in a square-packing arrangement, they are as well Representative Volume Elements (RVE) of composites with a specific spatial distribution of debonds. In order to facilitate the treatment of models, let us introduce the in-plane coordinates  $x$  and  $y$ , where  $x$  is in the transverse direction of the UD composite ( $z$  is consequently the through-the-thickness direction). Two considerations lie  
65 at the basis of the chosen RVE models. First, upon application of a load in the  $x$ -direction, the strain response in the  $y$ -direction is small due to the very small minor Poisson's ratio of the UD composite. Second, debonds are considered to be significantly longer in the fiber longitudinal direction than in the arc direction. We therefore use 2D models under the assumption of plane strain and

70 defined in the  $x - z$  section of the composite. The analysis presented applies to long debonds and focuses on understanding the mechanisms of growth along the arc direction. Transverse tensile strain is applied to the composites in the form of a constant displacement in the  $x$ -direction along the vertical boundary of the RUC as shown in Figures 1 to 4. As models are distinguished by the number of rows of fibers and by the spacing between debonds along the vertical and horizontal directions, the corresponding RUCs can be categorized based on the number  $n$  of fibers in the horizontal direction and  $k$  in the vertical direction. Vertical displacement coupling is always applied along the free surfaces. Thus, we introduce the common notation  $n \times k - coupling$  to denote a RUC with  $n \times k$  fibers and kinematic coupling applied to it. In Section 2.2, a detailed account of the selected combinations of  $n$ ,  $k$ , and boundary conditions is provided as well as a description of the corresponding models of damaged composite.

## 2.2. Models of Representative Volume Element (RVE)

The model shown in Fig. 1 represents an infinite UD laminate in which debonds appear regularly every  $n^{th}$  undamaged fiber in horizontal fiber rows and fiber rows containing damaged fibers appear every  $k^{th}$  row of only undamaged fibers. The model is used to study the interaction between debonds appearing at regular but potentially different intervals along the horizontal and vertical direction, measured in terms of fully bonded (undamaged) fibers present between them. By changing the value of parameters  $n$  and  $k$  (number of fibers respectively in the horizontal and vertical direction) different distribution of debonds can be investigated: from isolated debonds far apart from each other (early stages of damage) to a UD with all the fibers partially debonded (an unphysical limit case). The model of Fig. 1 is referred to as  $n \times k - coupling$ .

95 Models in Figures 2 and 3 represent instead a UD composite with respectively vertical lines and horizontal rows of partially debonded fibers repeating at the regular intervals respectively in the horizontal and vertical direction, measured respectively in terms of vertical lines and horizontal rows of fully bonded (undamaged) fibers. According to the nomenclature introduced in Sec-

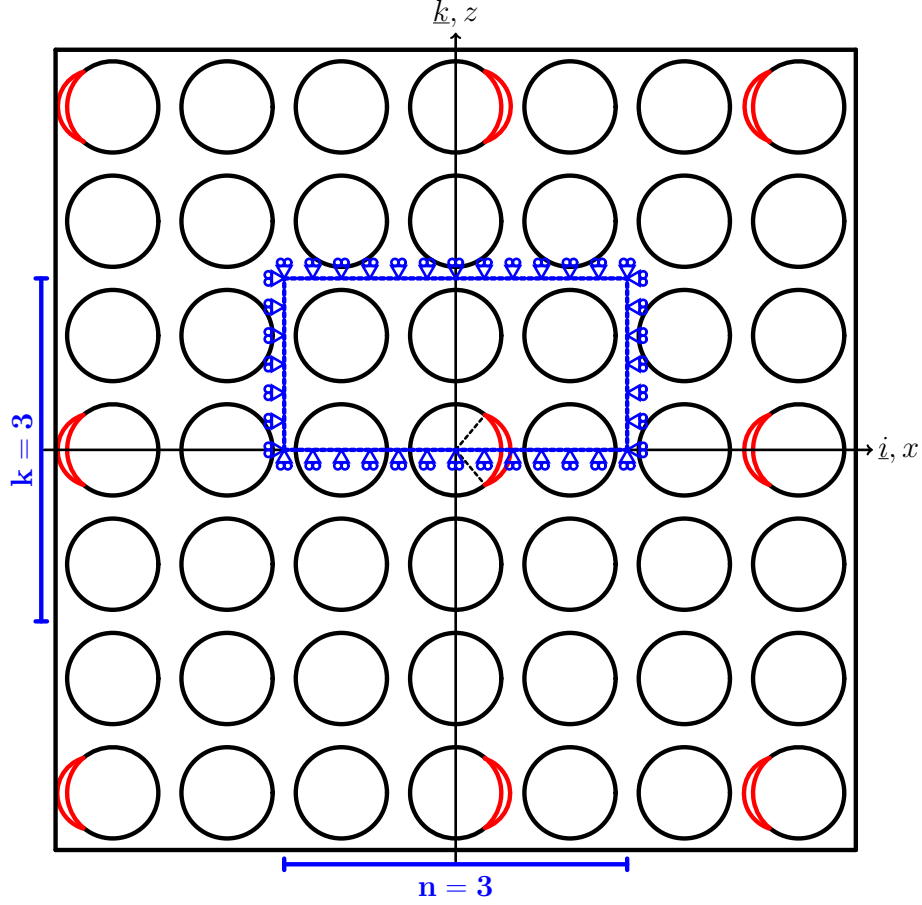


Figure 1: Rows of fibers with debonds repeating at different distances along the horizontal direction and rows with debonded fibers repeating at different distances along the vertical direction: models  $n \times k$  – coupling.

tion 2.1, these two models are identified respectively by  $n \times 1$  – coupling and  $1 \times k$  – coupling.

Model  $n \times 1$  – coupling in Figure 2 is studied to investigate the interaction of debonds in a configuration that represents, although in an idealized form, the stage preceding coalescence of debonds and formation of macroscopic transverse cracks.

On the other hand, model  $n \times 1$  – coupling in Figure 3 addresses a configuration of debonds that has not been observed in in-situ analyses of UD composites

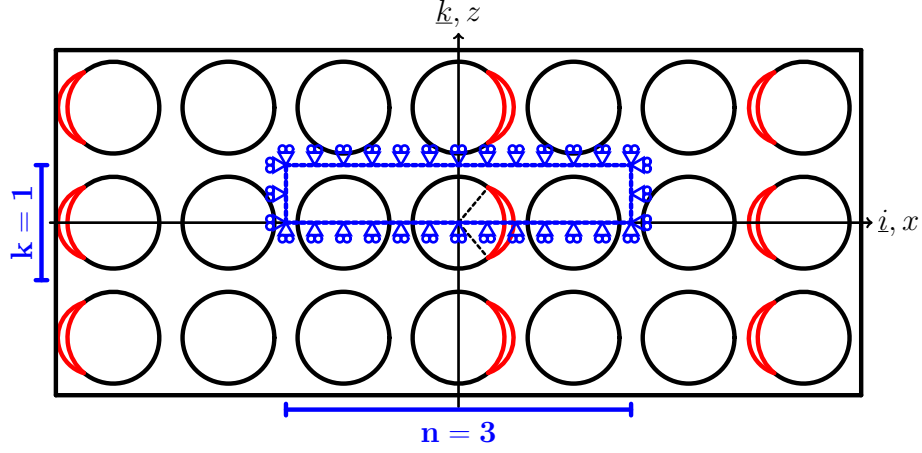


Figure 2: Vertical lines of fibers with debonds repeating at different distances along the horizontal direction: models  $n \times 1$  – *coupling*.

in transverse tension and can thus be deemed unphysical, but has nonetheless the potential to shed light on debonds' interaction mechanisms that makes this configuration unobservable.

### 2.3. Finite Element (FE) discretization

Discretization and analysis of RUCs is performed with the Finite Element Method (FEM) within the Abaqus environment, a commercial FEM software [17]. Length  $l$  and height  $h$  of the model are respectively determined by the number of fibers  $n$  in the horizontal direction and  $k$  across the thickness (see Sec. 2.2) according to Eq. 1:

$$l = 2nL \quad h = kL; \quad (1)$$

where  $2L$  is the length of a one-fiber unit, see Fig. 4, and  $L$  is defined as a function of the fiber volume fraction  $V_f$  and the fiber radius  $R_f$  according to

$$L = \frac{R_f}{2} \sqrt{\frac{\pi}{V_f}}. \quad (2)$$

$R_f$  is assumed to be the same for every fiber and equal to  $1 \mu m$ . The choice of the previous value is not dictated by physical considerations but for

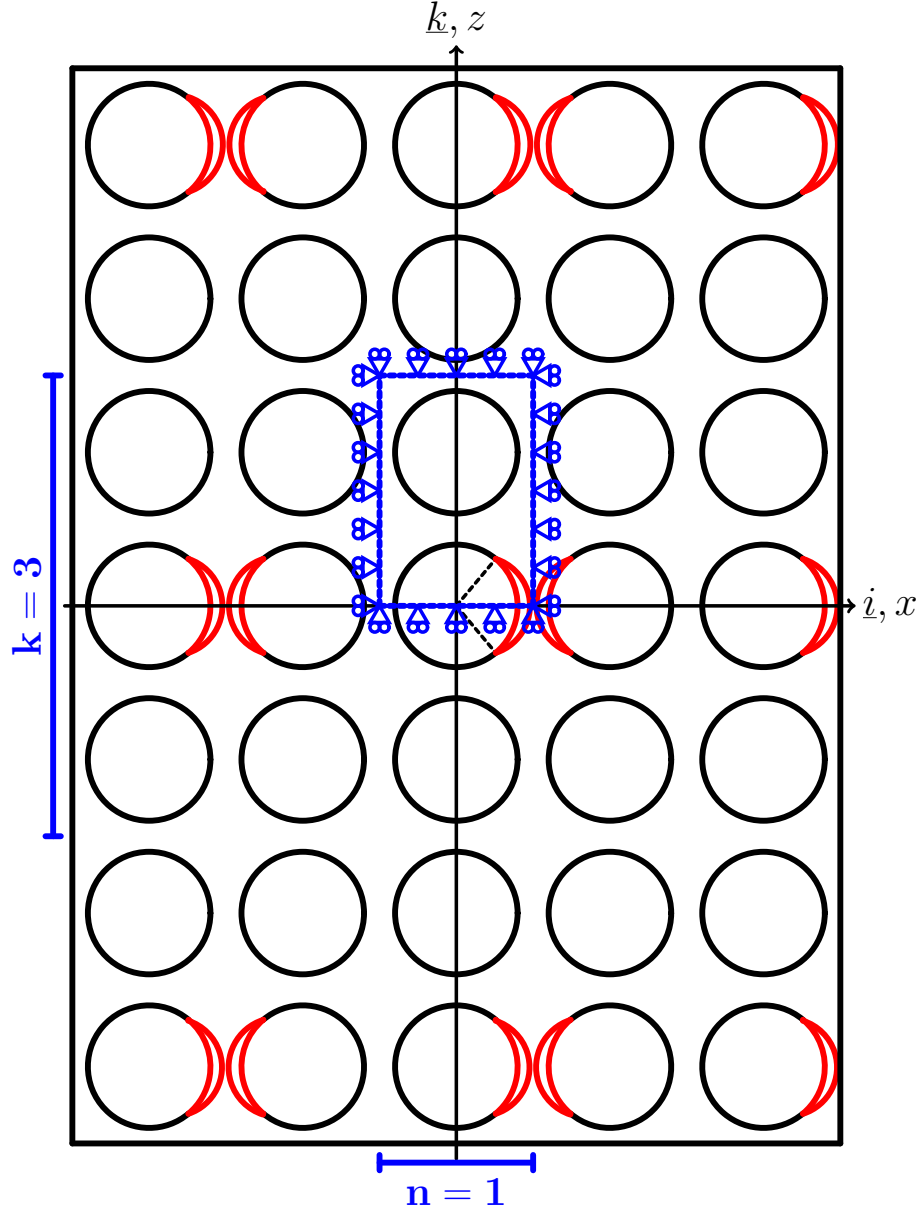


Figure 3: Horizontal rows of fibers with debonds repeating at different distances along the vertical direction: models  $1 \times k$  – coupling.

simplicity. It is thus useful to remark here that, in a linear elastic solution as the one considered in the present work, the ERR is proportional to the geometrical

dimensions of the model and, consequently, recalculation of the ERR for fibers of any size requires a simple multiplication. Notice also that relationships in  
125 Eqs. 1 and 2 imply that the local and global  $V_f$  are everywhere equal.

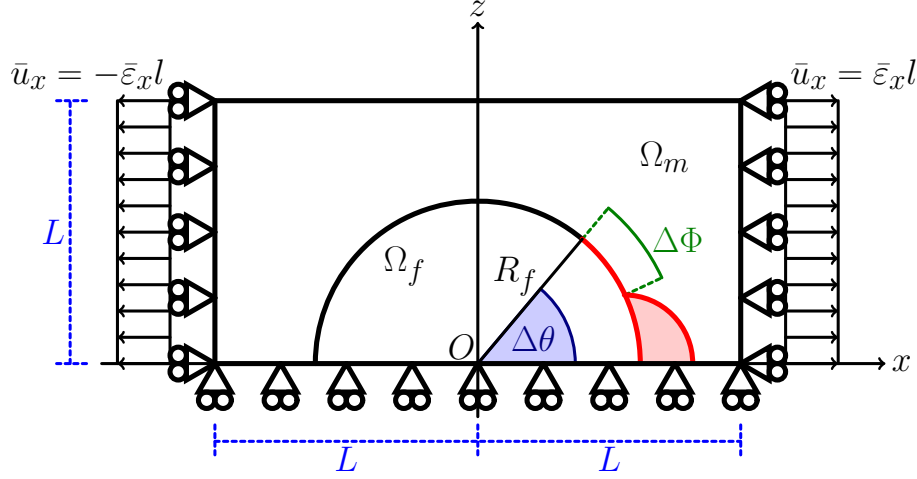


Figure 4: Schematic of the model with its main parameters.

The debond is placed symmetrically with respect to the  $x$  axis (see Fig. 4) and it is characterized by an angular size of  $\Delta\theta$  (making the full debond size equal to  $2\Delta\theta$ ). For large debond sizes (at least  $\geq 60^\circ - 80^\circ$ ), a region  $\Delta\Phi$  of variable size appears at the crack tip where the crack faces are in contact with  
130 each other but free to slide relatively to each other. In order to model crack faces motion in the contact zone, frictionless contact is considered between the two crack faces to allow free sliding and avoid interpenetration. Symmetry with respect to the  $x$  axis is applied on the lower boundary and coupling of vertical displacement on the upper boundary. Kinematic coupling on the  $x$ -displacement  
135 is applied along the left and right sides of the RUC in the form of a constant  $x$ -displacement  $\pm\bar{\varepsilon}_x l$ , corresponding to transverse strain  $\bar{\varepsilon}_x$  equal to 1%.

Meshing of the model is accomplished with second order, 2D, plane strain triangular (CPE6) and quadrilateral (CPE8) elements. A regular mesh of 8-node ( $2^{nd}$  order rectangular) elements with almost unitary aspect ratio is enforced at  
140 the crack tip in order to ensure the convergence of the ERR. The angular size



Table 1: Summary of the mechanical properties of fiber and matrix.  $E$  stands for Young’s modulus,  $\mu$  for shear modulus and  $\nu$  for Poisson’s ratio.

<b>Material</b>	$E$ [GPa]	$\mu$ [GPa]	$\nu$ [–]
Glass fiber	70.0	29.2	0.2
Epoxy	3.5	1.25	0.4

$\delta$  of an element in the crack tip neighborhood is always equal to  $0.05^\circ$ . The crack faces are modeled as element-based surfaces and a small-sliding contact pair interaction with no friction is imposed between them. The Mode I, Mode II and total Energy Release Rates (ERRs) (respectively referred to as  $G_I$ ,  $G_{II}$  and  $G_{TOT}$ ) are the main result of FEM simulations; they are evaluated using the VCCT [18] implemented in a in-house Python routine and, for  $G_{TOT}$  only, the J-integral [19] is calculated by use of the Abaqus built-in command. A glass fiber-epoxy UD composite is treated in the present work, and it is assumed that their response lies always in the linear elastic domain. The material properties of glass fiber and epoxy are reported in Table 1. Validation is performed with respect to the results reported in [15, 11], which were obtained with the Boundary Element Method (BEM) for a model of a single fiber with a symmetric debond placed in an infinite matrix. As discussed in more detail in [20], the agreement between FEM (present work) and BEM [15, 11] solutions is good and the difference between the two does not exceed 5%. This provides us with a level of uncertainty with which we can analyze the significance of observed trends: any relative difference in ERR between different RUCs smaller than 5% cannot be reliably distinguished from numerical uncertainty and its discussion should thus be avoided.

### 3. Results & Discussion

#### 3.1. Interaction between isolated debonds in infinite UD composites

The effect on Mode I and Mode II ERR of the interaction between debonds appearing at regular distances (in terms of fully bonded fibers) in the horizontal

and vertical directions (models  $n \times k$  – coupling) is shown respectively in Figure 5 and Figure 6. It can be observed that it is the distance between debonds in the horizontal direction that presents a relevant effect on ERR: the number of fully bonded fibers between consecutive debonds in the vertical direction has a negligible influence on Mode I and a very modest effect, below or at the limit of the 5% accuracy of the model, on Mode II.

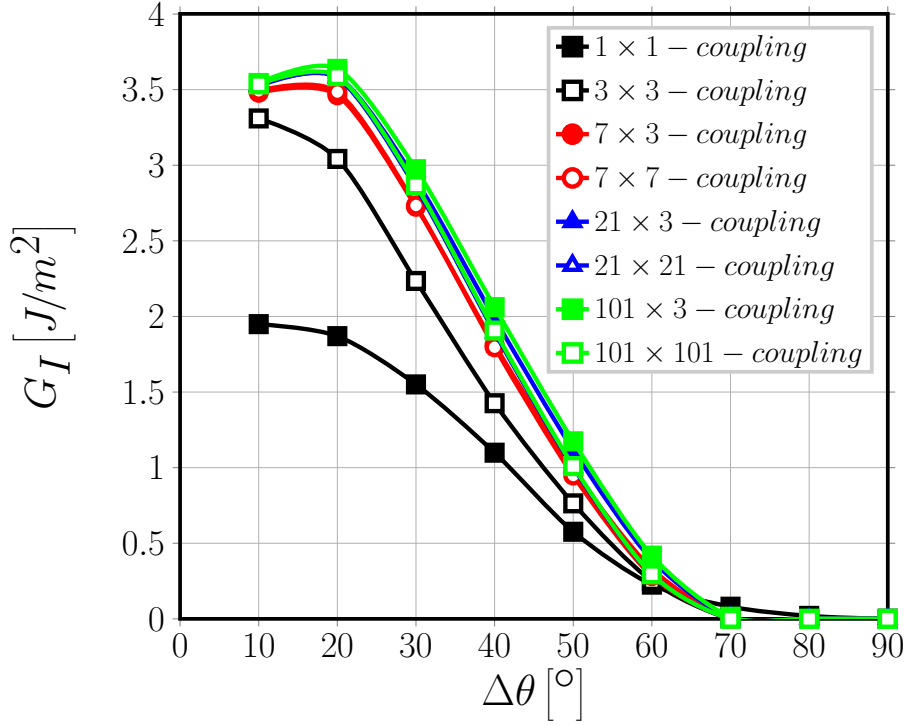


Figure 5: Effect of debond-debond interaction in infinite UD composites on Mode I ERR: models  $n \times k$  – coupling.  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

On the other hand, increasing the number of fully bonded fibers between debonds in the horizontal direction leads to a significant increase in both Mode I and Mode II ERR, due to the magnification of the  $x$ -strain in the crack tip neighborhood [20]. A critical distance (in terms of undamaged fibers) at which a non-interacting solution can be observed is apparent for Mode I (Figure 5). Given that Mode II ERR for models  $21 \times 3$  – coupling,  $21 \times 21$  – coupling,

$101 \times 3 - \text{coupling}$  and  $101 \times 101 - \text{coupling}$  is in a  $\leq 5\%$  range with respect to each other and thus their difference is not significant taking into account model accuracy, it can be argued that also in Mode II a critical distance exists at which a non-interacting solution appears.

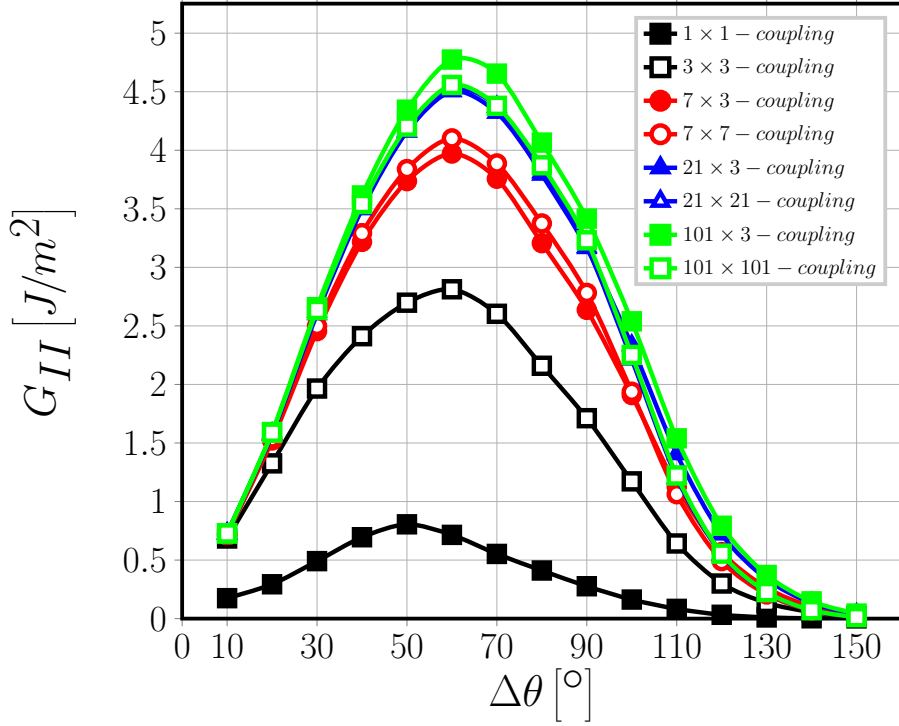


Figure 6: Effect of debond-debond interaction in infinite UD composites on Mode II ERR: models  $n \times k - \text{coupling}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

### 3.2. Debond-debond interaction between horizontal rows of partially debonded fibers in infinite UD composites

The results presented in Figures 7 and 8 for respectively Mode I and Mode II ERR of models  $1 \times k - \text{coupling}$  confirm the observations presented in Section 3.1. Models  $1 \times k - \text{coupling}$  represents the RVE of an infinite UD composite with horizontal fiber rows that appear at regular intervals (measured in terms of fully bonded fibers) and in which fibers are all partially debonded (see Fig. 3

for reference).

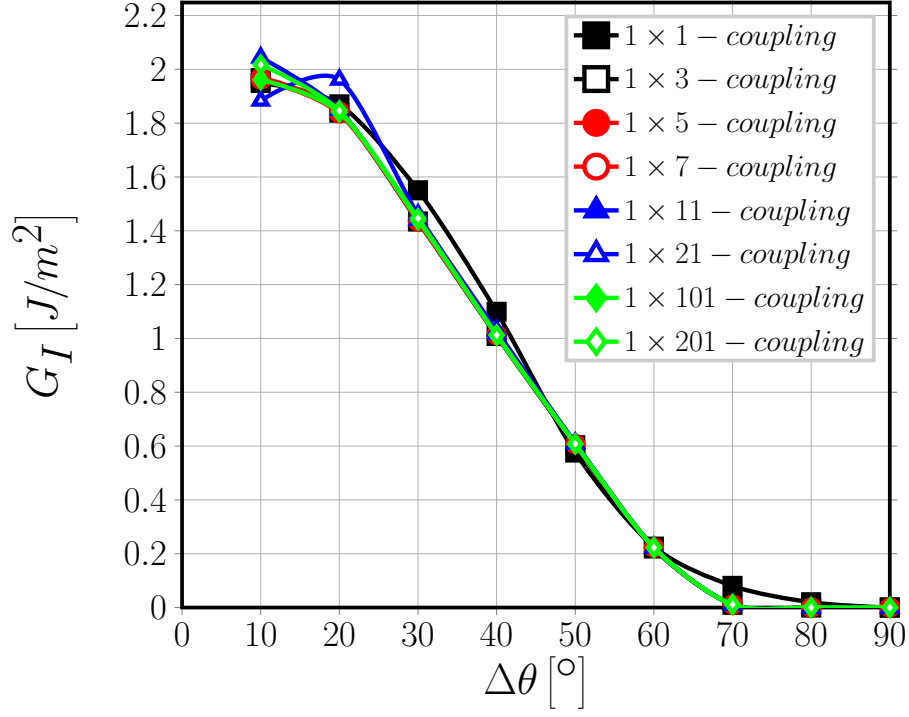


Figure 7: Effect of debond-debond interaction in infinite UD composites on Mode I ERR: models  $1 \times k - \text{coupling}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

Varying the number  $k$  of undamaged fibers between fiber rows of only partially debonded fibers does not have any effect on ERR, neither in Mode I (Figure 7) nor in Mode II (Figure 8). The observations of Sec. 3.1 are thus confirmed: it is the presence of fully bonded fibers only in the horizontal direction, i.e. the loading direction, that affects the debond ERR through  $x$ -strain magnification.

### 3.3. Debond-debond interaction between vertical lines of partially debonded fibers in infinite UD composites

Figures 9 and 10 report respectively Mode I and Mode II ERR for models  $1 \times k - \text{coupling}$ , which correspond to the RVEs of UD composites with vertical

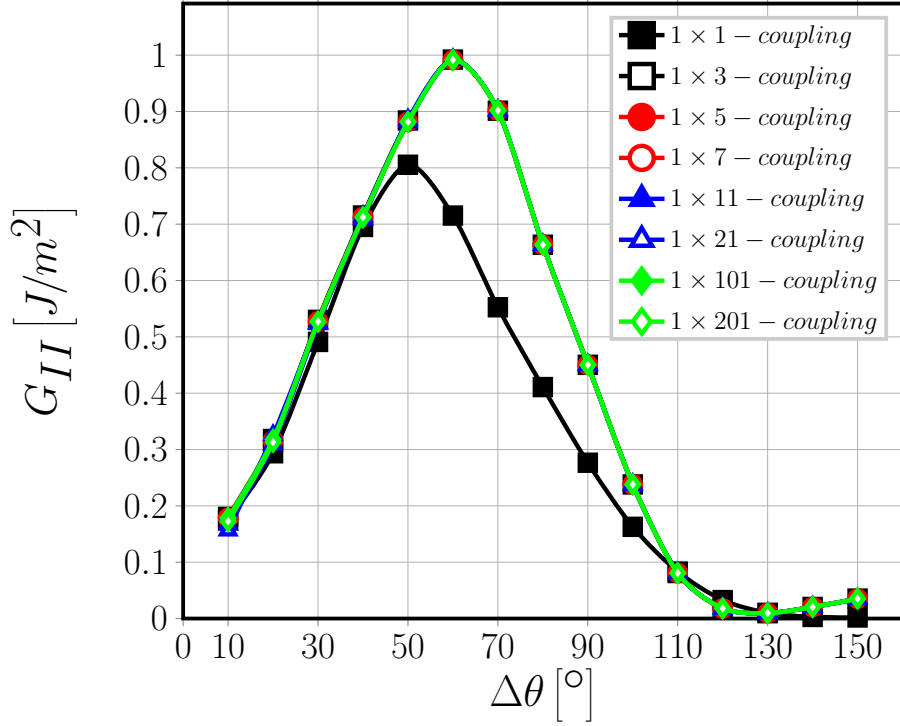


Figure 8: Effect of debond-debond interaction in infinite UD composites on Mode II ERR: models  $1 \times k$  – coupling.  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

lines of partially debonded fibers appearing at regular intervals (in terms of undamaged fibers) in the horizontal direction (see Fig. 2 for reference).

200 As it can be expected from the discussion of Sec. 3.1 and Sec. 3.2, increasing the number of fully bonded fibers between two consecutive lines of partially debonded fibers is responsible for significant increases in both Mode I and Mode II ERR.

205 However, comparison of Fig. 9 with Fig. 7 and of Fig. 9 with Fig. 7 provides an additional interesting result: the presence of fully bonded fibers between debonds appearing on vertically aligned fibers reduces both  $G_I$  and  $G_{II}$ . On the other hand, for the same horizontal distance between debonded fibers, the energetically most favorable configuration is achieved when debonds are contiguous along the vertical direction. Two further effects can be observed: the

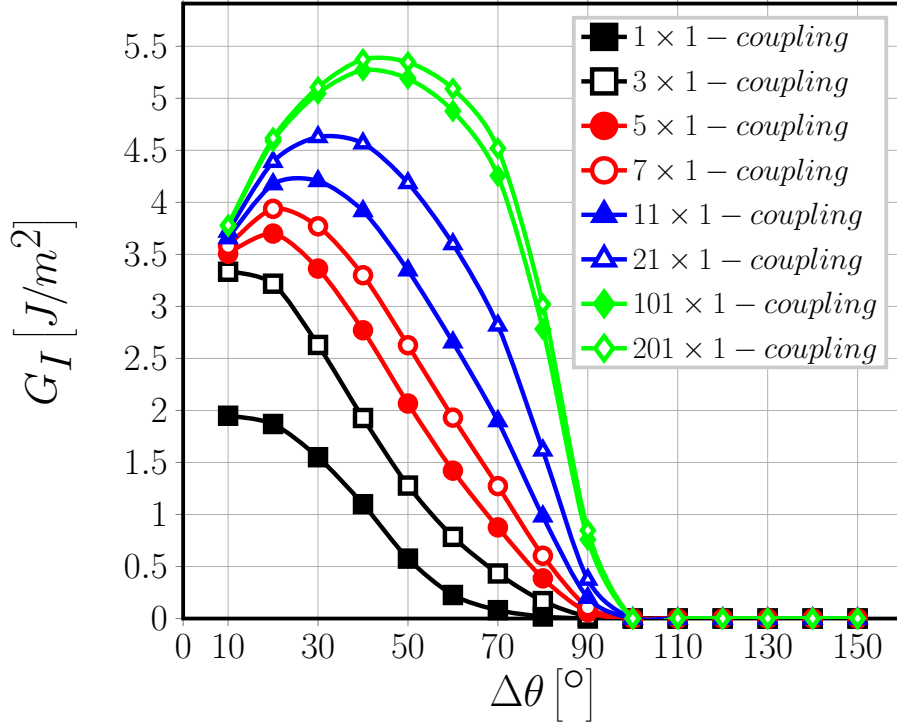


Figure 9: Effect of debond-debond interaction in infinite UD composites on Mode I ERR: models  $n \times 1 - coupling$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

onset of the contact zone is delayed up to a debond size of  $\sim 100^\circ$  (Fig. 9); the peak value of  $G_{II}$  is shifted to a debond size of up to  $90^\circ$  (Fig. 10). Thus, larger debonds are in general favored. This behavior can be related to the local deformation of the matrix. Between two vertically aligned debonds, the matrix strip between the two partially debonded fibers has, locally, both the lower and the upper surface free to deform. Due to Poisson's effect, the two surfaces move towards each other, imposing an opening displacement on the crack tip. This in turn favors Mode I and delays the onset of the contact zone. Furthermore, taking into account that fibers are more rigid than the surrounding matrix, when the fiber on top of the debonded one is undamaged (fully bonded), the  $x$ -displacement field in the matrix is restrained by the requirement of continuity at the interface. When instead another partially debonded fiber is present,

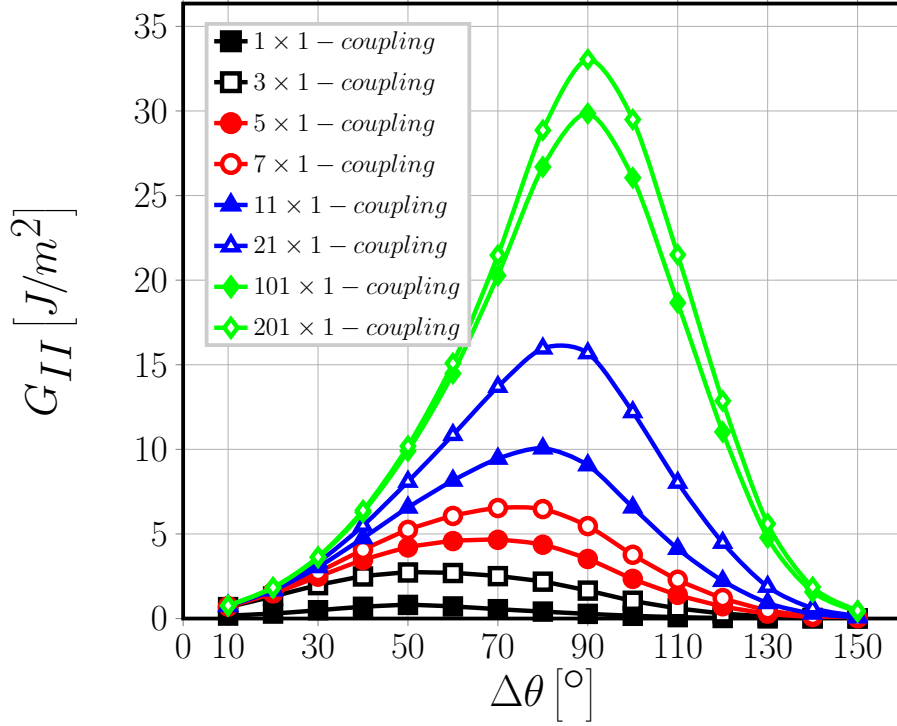


Figure 10: Effect of debond-debond interaction in infinite UD composites on Mode II ERR: models  $n \times 1 - coupling$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

a matrix strip is created with an upper and lower free surfaces, i.e. detached from the upper and lower fibers. The displacement field in this matrix strip is thus not restrained by the more rigid fibers and a magnification effect of the  $x$ -strain takes place. This in turn causes an increase in  $G_I$  for smaller debonds (the  $x$ -displacement is the major component of the crack opening displacement at the crack tip) and in  $G_{II}$  for larger ones (the  $x$ -displacement is the major component of the crack shear displacement at the crack tip).

#### 4. Conclusions & Outlook

Different models of infinite UD composites have been studied with different configurations of multiple interacting debonds in order to investigate their effect of Mode I and Mode II Energy Release Rate.

Building upon the observations made in the previous section, several conclusions can be drawn about the growth of debonds in UD composites:

- 235     • at given strain level, multiple debonds can appear on not consecutive vertically-aligned fibers;
- at a given strain level, the vertical lines of fibers on which debonds grow are determined by the horizontal distance from pre-existing debonds;
- a minimum non-interactive distance exists for the Energy Release Rate;
- 240     • when spacing between vertical lines of debonds is lower than the minimum non-interactive distance, the ERR decreases;
- thus, conversely, when spacing between vertical lines of debonds is lower than the minimum non-interactive distance, higher levels of strain are needed to grow debonds;
- 245     • growth of debonds appearing on contiguous vertically-aligned fibers is energetically the most favorable;
- larger debonds are favored on contiguous vertically aligned partially debonded fibers.

## Acknowledgements

250     Luca Di Stasio gratefully acknowledges the support of the European School of Materials (EUSMAT) through the DocMASE Doctoral Programme and the European Commission through the Erasmus Mundus Programme.

## References

- 255     [1] J. E. Bailey, A. Parvizi, On fibre debonding effects and the mechanism of transverse-ply failure in cross-ply laminates of glass fibre/thermoset composites, *Journal of Materials Science* 16 (3) (1981) 649–659. doi: 10.1007/bf02402782.



- 260 [2] A. Perlman, G. Sih, Elastostatic problems of curvilinear cracks in bonded dissimilar materials, *International Journal of Engineering Science* 5 (11) (1967) 845–867. doi:10.1016/0020-7225(67)90009-2.
- [3] M. Toya, A crack along the interface of a circular inclusion embedded in an infinite solid, *Journal of the Mechanics and Physics of Solids* 22 (5) (1974) 325–348. doi:10.1016/0022-5096(74)90002-7.
- 265 [4] F. París, J. C. Caño, J. Varna, The fiber-matrix interface crack — a numerical analysis using boundary elements, *International Journal of Fracture* 82 (1) (1996) 11–29. doi:10.1007/bf00017861.
- [5] J. Varna, F. París, J. C. Caño, The effect of crack-face contact on fiber/matrix debonding in transverse tensile loading, *Composites Science and Technology* 57 (5) (1997) 523–532. doi:10.1016/s0266-3538(96)00175-3.
- 270 [6] M. Comninou, The interface crack, *Journal of Applied Mechanics* 44 (4) (1977) 631. doi:10.1115/1.3424148.
- [7] E. Correa, E. Gamstedt, F. París, V. Mantič, Effects of the presence of compression in transverse cyclic loading on fibre–matrix debonding in uni-  
275 directional composite plies, *Composites Part A: Applied Science and Manufacturing* 38 (11) (2007) 2260–2269. doi:10.1016/j.compositesa.2006.11.002.
- [8] E. Correa, V. Mantič, F. París, Effect of thermal residual stresses on matrix failure under transverse tension at micromechanical level: A numerical and  
280 experimental analysis, *Composites Science and Technology* 71 (5) (2011) 622–629. doi:10.1016/j.compscitech.2010.12.027.
- [9] E. Correa, F. París, V. Mantič, Effect of the presence of a secondary transverse load on the inter-fibre failure under tension, *Engineering Fracture Mechanics* 103 (2013) 174–189. doi:10.1016/j.engfracmech.2013.02.026.

- 285 [10] E. Correa, F. París, V. Mantič, Effect of a secondary transverse load on the inter-fibre failure under compression, *Composites Part B: Engineering* 65 (2014) 57–68. doi:10.1016/j.compositesb.2014.01.005.
- [11] C. Sandino, E. Correa, F. París, Numerical analysis of the influence of a nearby fibre on the interface crack growth in composites under transverse  
290 tensile load, *Engineering Fracture Mechanics* 168 (2016) 58–75. doi:10.1016/j.engfracmech.2016.01.022.
- [12] C. Sandino, E. Correa, F. París, Interface crack growth under transverse compression: nearby fibre effect, in: *Proceeding of the 18<sup>th</sup> European Conference on Composite Materials (ECCM-18)*, 2018.
- 295 [13] L. Zhuang, A. Pupurs, J. Varna, R. Talreja, Z. Ayadi, Effects of inter-fiber spacing on fiber-matrix debond crack growth in unidirectional composites under transverse loading, *Composites Part A: Applied Science and Manufacturing* 109 (2018) 463–471. doi:10.1016/j.compositesa.2018.03.031.
- 300 [14] J. Varna, L. Q. Zhuang, A. Pupurs, Z. Ayadi, Growth and interaction of debonds in local clusters of fibers in unidirectional composites during transverse loading, *Key Engineering Materials* 754 (2017) 63–66. doi:10.4028/www.scientific.net/kem.754.63.
- [15] F. París, E. Correa, V. Mantič, Kinking of transversal interface cracks  
305 between fiber and matrix, *Journal of Applied Mechanics* 74 (4) (2007) 703. doi:10.1115/1.2711220.
- [16] L. Zhuang, R. Talreja, J. Varna, Transverse crack formation in unidirectional composites by linking of fibre/matrix debond cracks, *Composites Part A: Applied Science and Manufacturing* 107 (2018) 294–303.  
310 doi:10.1016/j.compositesa.2018.01.013.
- [17] Simulia, Providence, RI, USA, ABAQUS/Standard User’s Manual, Version 6.12 (2012).

- [18] R. Krueger, Virtual crack closure technique: History, approach, and applications, *Applied Mechanics Reviews* 57 (2) (2004) 109. doi:10.1115/1.1595677.
- [19] J. R. Rice, A path independent integral and the approximate analysis of strain concentration by notches and cracks, *Journal of Applied Mechanics* 35 (2) (1968) 379. doi:10.1115/1.3601206.
- [20] L. D. Stasio, J. Varna, Z. Ayadi, Energy release rate of the fiber/matrix interface crack in ud composites under transverse loading: debond-debond and debond-free boundary interactions, submitted to *Theoretical and Applied Fracture Mechanics*.