



FINITE ELEMENTS SOLUTION OF THE FIBER-MATRIX INTERFACE CRACK: EFFECTS OF MESH REFINEMENT AND DOMAIN SIZE

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Outline

The Fiber-Matrix Interface Problem in Fiber Reinforced Polymer Laminates

- Mark Company C
- Micromechanical modeling
- Preliminary Results & Perspectives
- Conclusions & Outlook
- Appendices & References









The Fiber-Matrix Interface Problem in FRPC Objectives & Approach Micromechanical modeling Intralaminar Transverse Cracking

■ THE FIBER-MATRIX INTERFACE PROBLEM IN FRPC

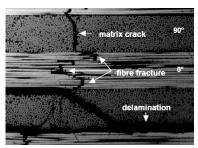






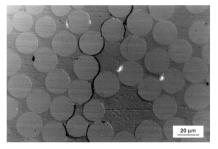
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Intralaminar Transverse Cracking





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(b) By Prof. Dr. E. K. Gamstedt, KTH, SE.

For a visual definition of intralaminar transverse cracking.



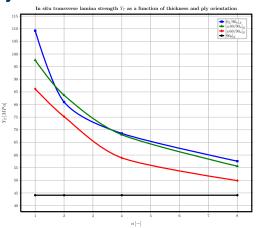






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The Thin Ply Effect



Measurements of in-situ transverse strength from D. L. Flaggs & M. H. Kural, 1982 [1].















Micromechanical modeling





Objectives 9 Appressh

Objectives & Approach

Objectives

 Investigate the influence of volume fraction, thin ply thickness and bounding plies' thicknesses on crack initiation

Objectives & Approach

To infere a relationship like

$$\textit{G}_{*\textit{c}} = \textit{G}_{*\textit{c}}\left(\theta_{\textit{debond}}, \Delta\theta_{\textit{debond}}, \textit{E}_{(\cdot\cdot)}, \nu_{(\cdot\cdot)}, \textit{G}_{()}, \textit{VF}_{\textit{f}}, \textit{t}_{\textit{ply}}, \frac{t_{\textit{ply}}}{t_{\textit{bounding plies}}}\right)$$

Approach

- Design and categorization of different Representative Volume Elements (RVEs)
- Automated generation of RVEs geometry and FEM model
- Finite Element Simulation (in Abagus)







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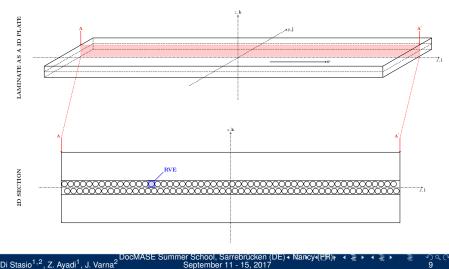






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From macro to micro





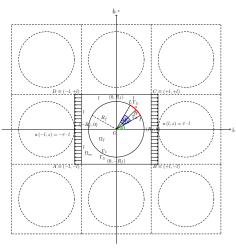






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Representative Volume Elements (RVEs)



- ✓ 2D space
- ✓ Linear elastic materials
- ✓ Displacement control
- \checkmark Dirichlet-type boundary conditions
- ✓ Linear elastic fracture mechanics
- ✓ Contact interaction









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Mesh Design and Generation

Why a good mesh is fundamental

- 1. Geometric discretization has a strong effect on non-linear FEM simulations
- 2. Damage is a process that implies changes in geometry, i.e. generation of surfaces and domain splitting
- 3. Fracture mechanics quantities depends on the local mesh topology and refinement

4-step procedure for mesh generation

- The boundary is generated patching analytical parameterizations
- 2. The boundary is split into a set of 4 corners (c_i) and 4 edges (e_i)
- 3. Interior nodes are created applying transfinite interpolation using multi-dimensional linear Lagrangian interpolants

$$P_1(x, p_j) = \sum_{j=1}^n p_j \prod_{k=1}^n \frac{x - x_k}{x_j - x_k} \quad P_2(x, y, p_j, q_j) = P_1(x, p_j) \otimes P_1(y, q_j)$$

$$r(\xi,\eta) = P_1(\xi,e_2,e_4) + P_1(\eta,e_1,e_3) - P_2(\xi,\eta,c_1,c_2,c_3,c_4)$$

4. The mesh is smoothed applying elliptic mesh generation

$$g^{11}\underline{r}_{,\mathcal{E}\mathcal{E}} + 2g^{12}\underline{r}_{,\mathcal{E}\mathcal{D}} + g^{22}\underline{r}_{,nn} = 0$$

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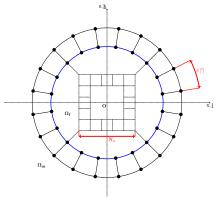






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Angular discretization



Angular discretization at fiber/matrix interface: $\delta = \frac{360^{\circ}}{4N_{\circ}}$.

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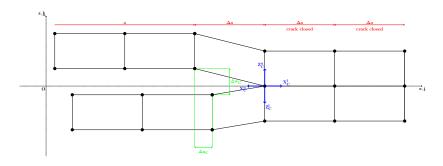






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Virtual Crack Closure Technique (VCCT)



$$G_I = \frac{Z_C \Delta w_C}{2B\Delta a}$$
 $G_{II} = \frac{X_C \Delta u_C}{2B\Delta a}$ \iff In-house routine and Abaqus

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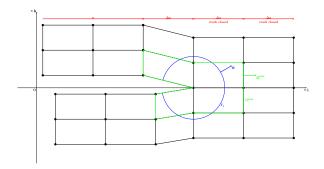






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J-integral evaluation



$$J_{i} = \lim_{\varepsilon \to 0} \int_{\Gamma_{-}} \left(W\left(\Gamma\right) n_{i} - n_{j} \sigma_{jk} \frac{\partial u_{k}\left(\Gamma, X_{i}\right)}{\partial X_{i}} \right) d\Gamma \Longleftrightarrow ^{*} \text{CONTOUR INTEGRAL in Abaqus}$$

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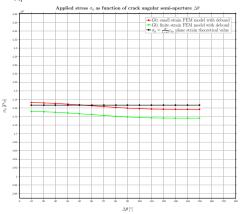






The Fiber-Matrix Interface Problem in FRPC Objectives & Approach Micromechanical modeling Results Conclusions σ_0 and G_0 Finite strain and small strain formulations

$$\sigma_0$$
 for $V f_f = 0.001$, $\frac{L}{B_f} \sim 28$ and $\delta = 0.4^\circ$



In red small strain FEM, in green finite strain FEM, in black $\sigma_0 = \frac{E}{1-\epsilon^2} \varepsilon$.

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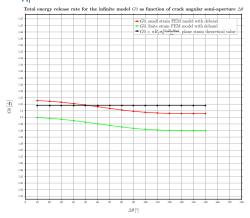






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$$G_0$$
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In red small strain FEM, in green finite strain FEM, in black G_0 calculated assuming $\sigma_0 = \frac{E}{1-\epsilon} \varepsilon$.

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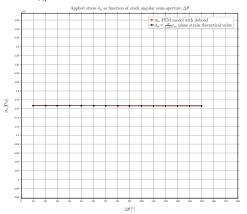






The Fiber-Matrix Interface Problem in FRPC Objectives & Approach Micromechanical modeling Results Conclusions σ_0 and G_0 Finite strain and small strain formulations

$$\sigma_0$$
 for $Vf_f=0.000079$, $\frac{L}{R_f}\sim 100$ and $\delta=0.4^\circ$



In red small strain FEM, in black $\sigma_0 = \frac{E}{1-\epsilon^2} \varepsilon$.



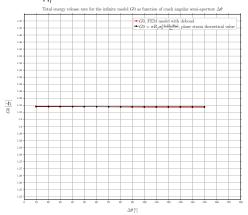






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$$G_0$$
 for $Vf_f=0.000079$, $\frac{L}{R_t}\sim 100$ and $\delta=0.4^\circ$



In red small strain FEM, in black G_0 calculated assuming $\sigma_0 = \frac{E}{1 - L^2} \varepsilon$.



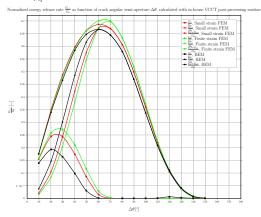






The Fiber-Matrix Interface Problem in FRPC Objectives & Approach Micromechanical modeling Results Conclusions σ_0 and G_0 Finite strain and small strain formulations

$$\frac{G_{(\cdot \cdot \cdot)}}{G_0}$$
 for $V_f=0.001$, $\frac{L}{B_f}\sim 28$ and $\delta=0.4^\circ$



In red small strain FEM, in green finite strain FEM, in black BEM results.



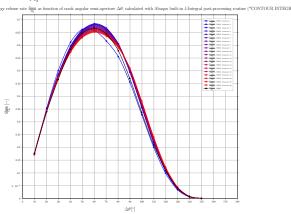






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$$\frac{G_{(\cdot \cdot \cdot)}}{G_0}$$
 for $V_f=0.001$, $\frac{L}{B_f}\sim 28$ and $\delta=0.4^\circ$, small strain formulation



Fading from blue to red J-Integrals evaluated at contours at increasing distance from the crack tip, in black BEM results.

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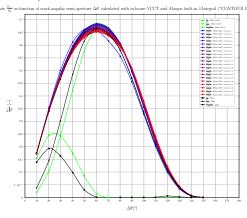






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Fading from blue to red J-Integrals evaluated at contours at increasing distance from the crack tip, in green evaluation with in-house VCCT routine, in black BEM results.

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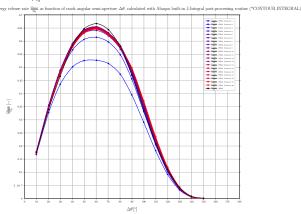






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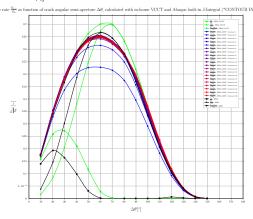






The Fiber-Matrix Interface Problem in FRPC Objectives & Approach Micromechanical modeling Results Finite strain and small strain formulations

$$\frac{G_{(\cdot,\cdot)}}{G_0}$$
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Fading from blue to red J-Integrals evaluated at contours at increasing distance from the crack tip, in green evaluation with in-house VCCT routine, in black BEM results.







Micromechanical modeling Conclusions







Micromechanical modeling



Results



Conclusions

Conclusions & Outlook

Conclusions

- 2D micromechanical models have been developed to investigate crack initiation in thin ply laminates
- A numerical procedure has been devised and implemented to automatize the creation of FEM models
- Analyses for $VF_f \rightarrow 0$ (matrix dominated RVE) conducted to validate the model with respect to previous literature

Outlook

- Investigate the dependence on VF_f , t_{ply} , $\frac{t_{ply}}{t_{bounding plies}}$ and different material systems
- Study numerical performances with respect to model's parameters
- Repeat for different RVEs and compare











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Spread Tow Technology: Implications

- Strong reduction in ply's thickness and weight
- Reduction in laminate's thickness and weight
- Higher fiber volume fraction and more homogeneous fiber distribution
- Ply thickness to fiber diameter ratio decreases of at least 1 order of magnitude, from > 100 to ≤ 10
- Increased load at damage onset and increased ultimate strength, in particular for transverse cracking

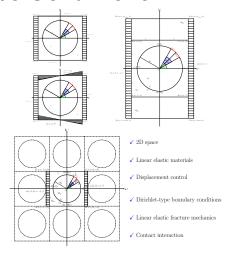








RVEs: Variations on a Theme





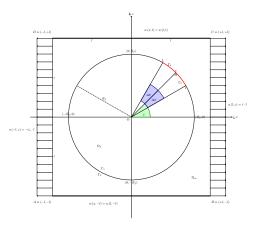






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RVEs: First Variation on a Theme



Isolated RVE with zero vertical displacement BC.

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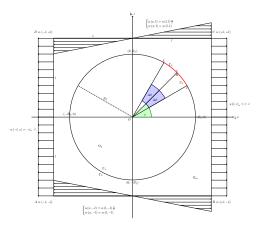






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RVEs: Second Variation on a Theme



Isolated RVE with homogeneous displacement BC.

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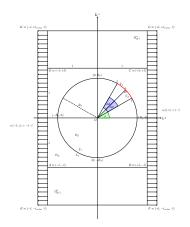






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RVEs: Third Variation on a Theme



Bounded RVE.

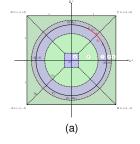


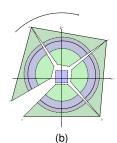


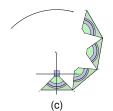


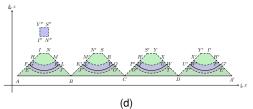


Topological transformation











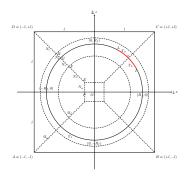




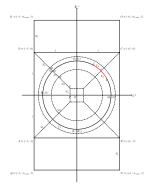
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Mesh parameters









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Finite Element Model in Abaqus

Method

ABAQUS/STD static analysis + VCCT + J-integral.

Type

Static, i.e. no inertial effects. Relaxation until equilibrium.

Elements

CPE4/CPE8

Interface

Tied surface constraint & contact mechanics

Input variables

 R_f , V_f , material properties, interface properties.

Control variables

 θ , $\Delta\theta$, $\bar{\varepsilon}_X$.

Output variables

Stress field, crack tip stress, stress intensity factors, energy release rates, a.





Evaluation of G_0

$$G_0 = \pi R_f \sigma_0^2 \frac{1 + k_m}{8G_m} \tag{1}$$

$$k_m = 3 - 4\nu_m \tag{2}$$

$$\sigma_0^{undamaged} = \frac{E_m}{1 - \nu_m^2} \varepsilon_{xx} \tag{3}$$

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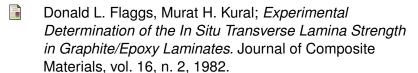




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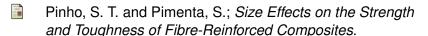








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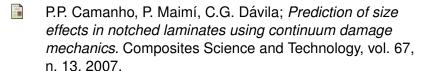








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