Effect of uniform distributions of bonded and debonded fibers on the growth of the fiber/matrix interface crack in UD laminates with different fiber contents under transverse loading

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Abstract

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1. Introduction

1. We start with a few lines devoted to the spread tow technology and thin plies: what they are, what can be done, what are the possible applications.
2. By quoting the relevant references, we report on the observation that one of the main beneficial mechanisms in thin ply is the retardation of transverse crack propagation. We then enlarge by reporting the microscopical observations by Saito, in which debonds where also observed. We observe that available microscopic observations are just a few and mainly in 2D.
3. Propagation of transverse cracks has been widely investigated both analytically and numerically
4. Initiation at the level of fiber/matrix interface is instead a less researched subject.

5. cohesive elements are a possible choice, but have some drawbacks, which makes a LEFM approach valuable
6. With regard to LEFM studies of laminates under transverse loading, models can be found in the literature about: the single fiber in infinite matrix under different mode of loading, the effect of adjacent fibers on a fiber in infinite matrix under different mode of loading, the single fiber in an equivalent composite in transverse tension, the effect of adjacent fibers on a fiber in an equivalent composite in transverse tension.
7. For initiation of transverse cracking at the fiber/matrix interface in UD laminates under transverse tension, there is thus a gap regarding: the effect of fiber volume fraction; the interaction of debonded and bonded fibers in micro-structured assemblies, i.e. no homogenization. This article addresses these two points.
8. We conclude the introduction with a summary of the article's structure.

2. RVE models & FE discretization

2.1. Introduction & Nomenclature

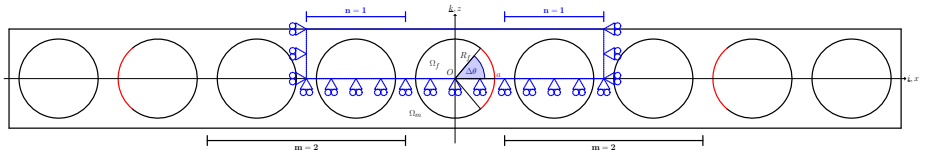
In order to investigate the interaction between debonds in UD composites, we developed different models of laminates in which the only damage present is represented by the fiber/matrix interface crack. All of these Representative Volume Elements feature regular microstructures with fibers placed according to a square-packing tiling. As the very high longitudinal modulus of UD composites and cross-ply laminates ensures that the y-strain due to loading in the x-direction is small, we consider only 2D models under the assumption of plane strain, defined in the $x - z$ section of the laminate. Consequently, debonds are considered to be significantly longer in the fiber direction than in the arc direction. The analysis presented thus applies to long debonds, of which we are interested in understanding the mechanisms of growth along its arc direction. The UD composites are further supposed to be subjected to transverse tension, applied along the x direction in the pictures. As the models are differentiated

by the number of layers of fibers and by the spacing between debonds along the vertical and horizontal directions, the corresponding Repeating Unit Cells (RUCs) can be distinguished from each other based on the number n of fibers in the horizontal direction and k in the vertical direction. Furthermore, the upper surface can be either free or coupling can be applied. We thus introduce the common notation $n \times k - free$ and $n \times k - coupling$ to denote a RUC with $n \times k$ fibers and, respectively, a free upper surface or coupling applied to it. The correspondence between specific combinations of particular choices of n, k and upper boundary conditions and representative models of laminate are detailed in Section 2.2.

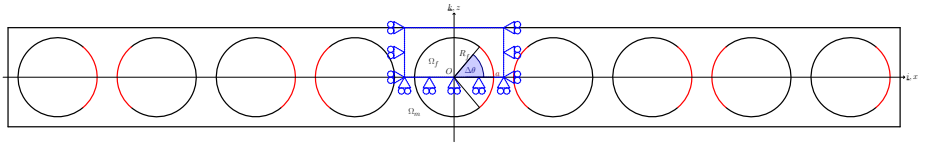
2.2. Models of Representative Volume Element (RVE)

The first two models feature, as shown in Fig. 1, a UD laminate with only one layer of fibers across its thickness. This is quite an extreme model from the microstructural point of view; however, it allows to focus the analysis on the interaction between debonds placed along the direction of the load. Furthermore, as the upper surface is considered free, the interaction is stronger in this case than in any other, making the predictions of this model rather conservative. In retrospective, if only 20 years ago such a model would have been considered too abstracted from the physical reality, the recent advancements in the spread tow technology make this approach appealing also for practical considerations.

In the first version of the model laminate, Fig. 1a, debonds appear in the laminate on every $(m+1)^{th}$ fiber on alternating sides of the partially debonded fiber. The symmetries of the model allow the use of a Repeating Unit Cell (RUC), which corresponds to the Representative Volume Element (RVE) of this microstructure, with a central debonded fiber and $\frac{m}{2}$ fiber(s) on each side. It is highlighted by blue lines in 1a. Following the notation introduced in Section 2.1, we will refer to this model as $(m+1) \times 1 - free$, where $n = (m+1), k = 1$. In the second version of the single-layer-of-fibers model, 1b, a debond appears on each fiber on alternating sides and the corresponding RUC has only one debonded fiber. We will refer to this model as $1 \times 1 - free$, where $n = k = 1$.



(a) Single layer of fibers with a debond appearing every m fibers.



(b) Single layer of fibers with debonds appearing on each fiber.

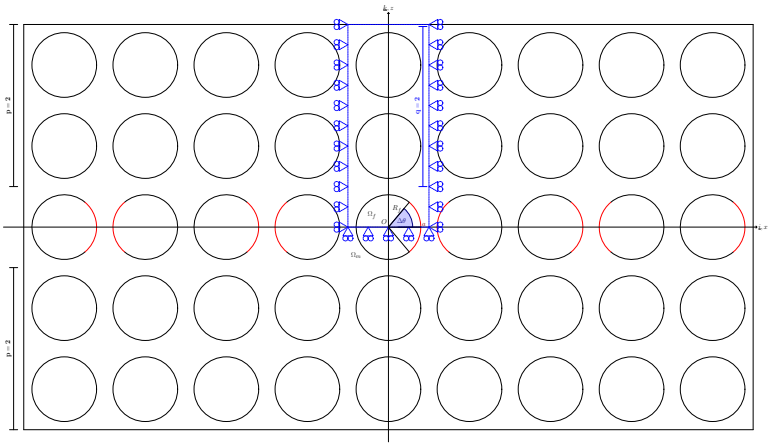
Figure 1: Models of UD laminates with a single layer of fibers and debonds repeating at different distances. The corresponding repeating element (RVE) is highlighted in blue.

The second set of models considers instead laminates with multiple layers of fibers across the thickness: a finite number of layers in the first two models (2a and 2b); an infinite number in the model of Fig. 3. In the first representative laminate (Fig. 2a), all the fibers in the central layer are debonded. The UD is made by $2p+1$ layers of fibers across the thickness, corresponding to a RUC with $p+1$ fibers in the z direction. This model will be referred to in the following as $1 \times (p+1) - free$, where $n = 1, k = (p+1)$. In the second model (Fig. 2b), a debond appear every $(m+1)^{th}$ fiber in the central line of fibers in a laminate with $2p+1$ layers. The corresponding RUC has thus $\frac{m}{2}$ fiber(s) on each side and p above the partially debonded fiber. We will refer to this model as $(m+1) \times (p+1) - free$, where $n = (m+1), k = (p+1)$.

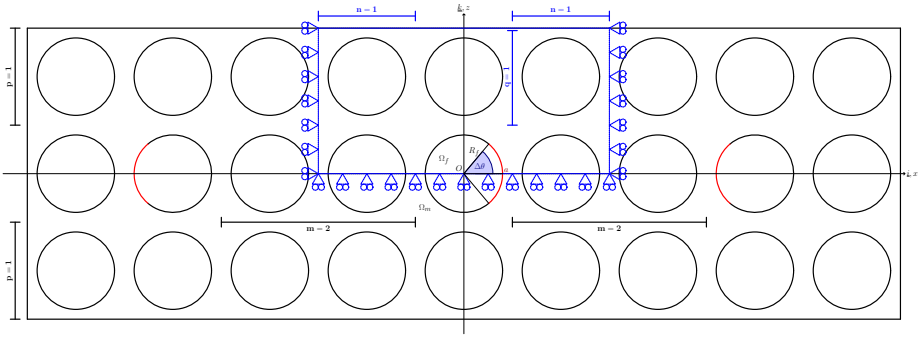
Finally, the last model considers an UD composite with an infinite number of partially debonded fibers. The corresponding RUC is made by a single partially debonded fiber and kinematic coupling conditions applied to the upper boundary. This model is referred to as $1 \times 1 - coupling$, where $n = k = 1$.

2.3. Finite Element (FE) discretization

Each RUC is discretized using the Finite Element Method (FEM) within the Abaqus environment, a commercial FEM package [1]. The length l and height h



(a) Multiple layers of fibers with debonds appearing on each fiber beloging to the central layer.



(b) Mutiple layers of fibers with a debond appearing every m fibers within the central layer.

Figure 2: Models of UD laminates with different layers of fibers and debonds repeating at different distances. The corresponding repeating element (RVE) is highlighted in blue.

of the model (see Fig. 4a) are determined by number of fibers n in the horizontal direction and k across the thickness (see 2.2) according to Eq. 1:

$$l = 2nL \qquad h = (2k-1)\,L; \tag{1}$$

where the reference length L is defined as a function of the fiber volume fraction V_f and the fibers' radius according to

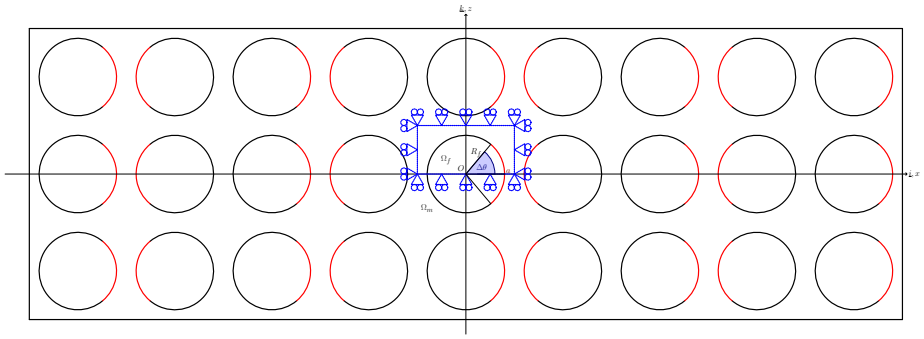
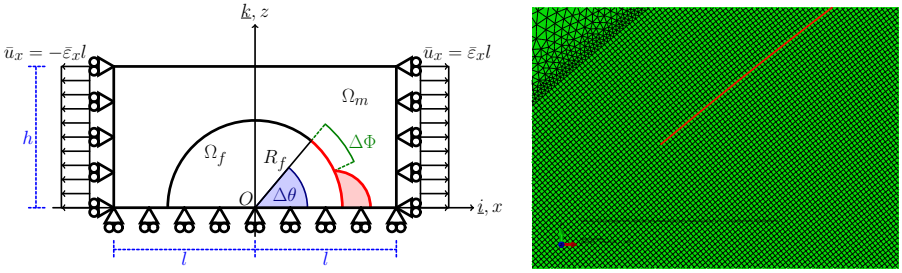


Figure 3: Model of UD laminates with an infinite number of layers of fibers and debonds appearing on each fiber. The corresponding repeating element (RVE) is highlighted in blue.

$$L = \frac{R_f}{2}\sqrt{\frac{\pi}{V_f}}. \tag{2}$$

The fibers' radius R_f is assumed to be the same for each fiber present n the model and equal to $1\mu m$. The relationships in Eqs. 1 and 2 thus ensure that the local and global V_f are everywhere equal.



(a) Schematic of the model with its main parameters.

(b) Mesh near the crack tip. Crack's faces shown in red.

Figure 4: Details and main parameters of the Finite Element model.

The debond is placed symmetrically with respect to the x axis (in red in 4a) and has an angular size of $\Delta\theta$ (the full debond's size is thus $2\Delta\theta$). For high debond's sizes ($\geq 60° - 80°$), a region of variable size $\Delta\Phi$ appears at the crack tip in which the crack's faces are in contact and slide on each other. Due to its appearance, frictionless contact is considered between the two crack's faces

to allow free slipping and avoid interpenetration. Symmetry with respect to the x axis is applied on the lower boundary and kinematic coupling on the left and right sides. The upper boundary is in general free, except for the model $1 \times 1 - coupling$ (Fig. 3) which requires kinematic coupling also on the upper side. Constant transverse strain $\bar{\varepsilon}$ equal to 1% is applied to the right and left sides by means of an imposed displacement of, respectively, $\pm\bar{\varepsilon}l$.

Table 1: Summary of the mechanical properties of fiber and matrix.

Material	$E\,[GPa]$	$G\,[GPa]$	$\nu\,[-]$
Glass fiber	70.0	29.2	0.2
Epoxy	3.5	1.25	0.4

The model is meshed using second order, 2D, plane strain triangular (CPE6) and rectangular (CPE8) elements. A regular mesh of quadrilateral elements with an almost unitary aspect ratio is required at the crack tip, as shown in Fig. 4b. The angular size δ of an element in the crack tip region is always equal to 0.05°. The mode I, mode II and total Energy Release Rates (ERRs) represent the main output of the FEM analysis; they are evaluated using the VCCT technique [2] implemented in a custom Python routine and, for the total ERR, the J-integral [3] by application of the Abaqus built-in functionality. A glass fiber-epoxy system is considered in every model, and it is assumed that their response lies always in the linear elastic domain. The properties used are listed in Table 1.

2.4. Validation of the model

The model is validated in Fig. 5 against the results reported in [4], obtained with the Boundary Element Method (BEM) for a single fiber with a symmetric debond placed in an infinite matrix. This situation is modeled using the *free* RVE with $V_f = 0.0079\%$, which corresponds to a RUC's length and height of ~ 100.

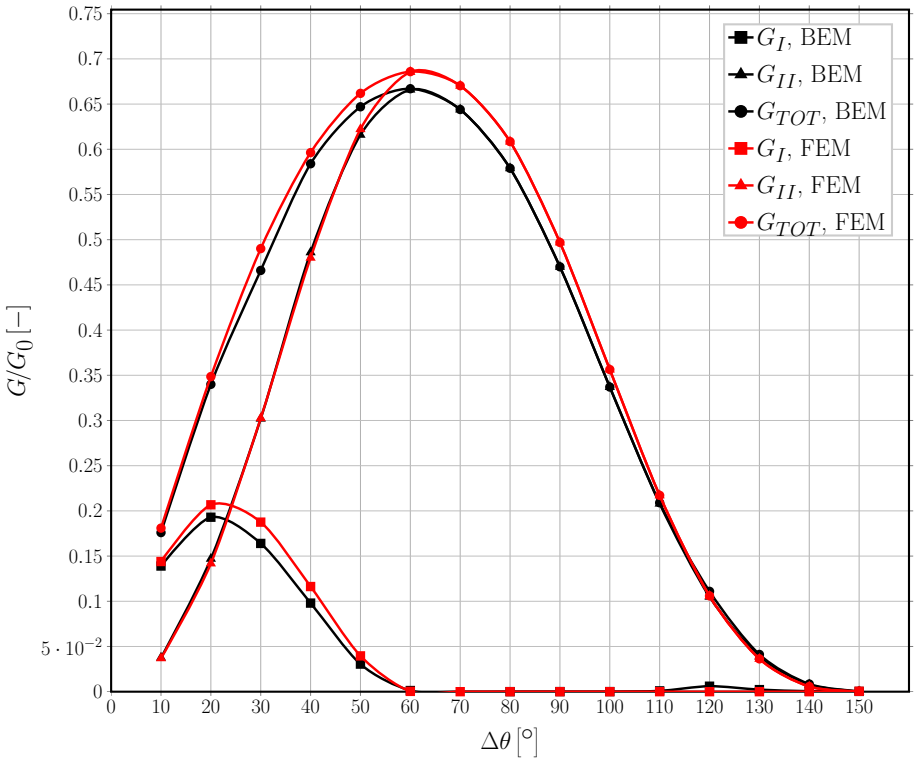


Figure 5: Validation of the single fiber model for the infinite matrix case with respect to the BEM solution in [4].

To allow for a comparison, the results are normalized following [4] with respect to a reference Energy Release Rate G_0 defined as

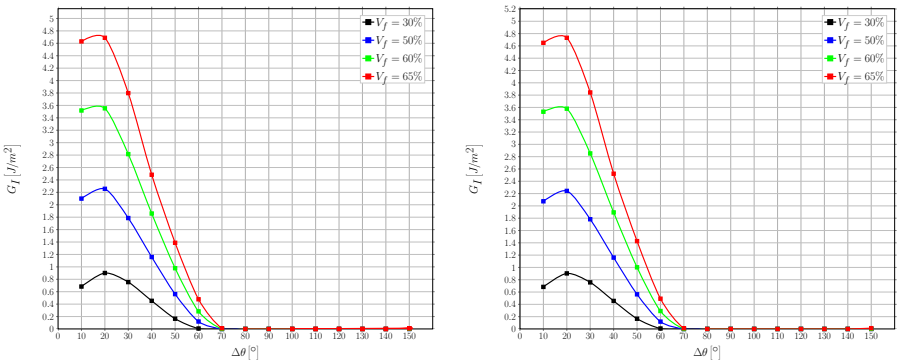
$$G_0 = \frac{1 + k_m}{8\mu_m} \sigma_0^2 \pi R_f \tag{3}$$

where μ is the shear modulus, k is the Kolosov's constant defined as $3 - 4\nu$ for plane strain conditions, R_f is the fiber radius and the pedix m refers to the properties of the matrix. σ_0 is the stress at the boundary, computed as the average of the stress extracted at each boundary node along the right side (arithmetic average as nodes are equispaced by design along both the left and right sides).

3. Results & Discussion

3.1. Effect of Fiber Volume Fraction

As shown in Figs. 6 and 7, respectively for mode I and mode II, the fiber content has a drastic effect on the Energy Release Rate at the crack tip of the fibre/matrix interface crack. The effect of four levels of fiber volume fraction are compared, 30%, 50%, 60% and 65%, on two microstructural models: a D6H0V11L (a debond every 6^{th} fiber in the central layer of an UD with 11 layers of fibers), Figs. 6a and 7a, and a D11H0V21L (a debond every 11^{th} fiber in the central layer of an UD with 21 layers of fibers), Figs. 6b and 7b.



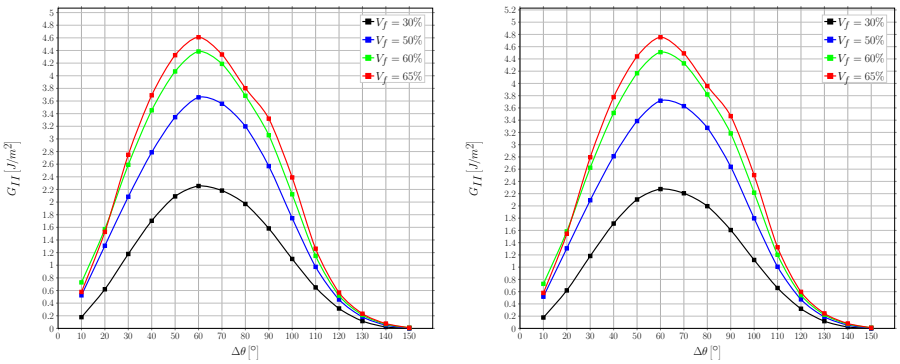
(a) 5 fibers each side, 5 above.

(b) 10 fibers each side, 10 above.

Figure 6: A view of the effect of fiber volume fraction on Mode I ERR in two exemplificative models.

Comparison of Fig. 6a with 6b, and of Fig. 7a with 7b, indicates that there exists a specific effect of the fiber content, independent of the microstructure. For mode I, Fig. 6, the maximum value of the ERR is increased by ~ 5.2 times when V_f changes from 30% to 65% in both models. The debond's size for which the peak value occurs remains unchanged at 20°, but for 60% and 65% the value at 10° and at 20° are almost identical, approximately creating a plateau and thus making the growth of small debonds ($\leq 20°$) in mode I unstable. Furthermore, increasing the fiber volume fraction delays the onset of the contact zone, which corresponds in 6 to the first value of $\Delta\theta$ for which G_I is equal to zero. For

$V_f = 30\%$, the contact zone first appears for a debond of 60°, similarly to what happens in the single fiber in infinite matrix model (Fig. 5). For higher fiber contents, the contact zone's onset is delayed to a debond's size equal to 70°.



(a) 5 fibers each side, 5 above. (b) 10 fibers each side, 10 above.

Figure 7: A view of the effect of fiber volume fraction on Mode II ERR in two exemplificative models.

For mode II, Fig. 6, the maximum value of the ERR is increased by ~ 2.1 times when V_f changes from 30% to 65% in both models. The effect is thus similar to mode I, but with a significantly lower magnitude. As for mode I, the debond's size for which the peak value occurs remains unchanged, at 60° for mode II. The shape of the curve remains instead unchanged, thus no effect on the stability of mode II with respect to debond's size can be observed. It is worthwhile to notice, however, that the ratio of mode II to mode I peak values is $\frac{max(G_{II})}{max(G_I)} \sim \frac{2.2}{0.9} \sim 2.4$ for $V_f = 30\%$, while it is $\sim \frac{4.7}{4.7} \sim 1$ for $V_f = 65\%$ in both models. Given that the peaks occur at different debond's sizes, for which the value of the other ERR is very small or even close to zero, this means that the increase in fiber content creates a long range of very close values of total ERR, and thus has a global destabilizing effect on the debond's growth.

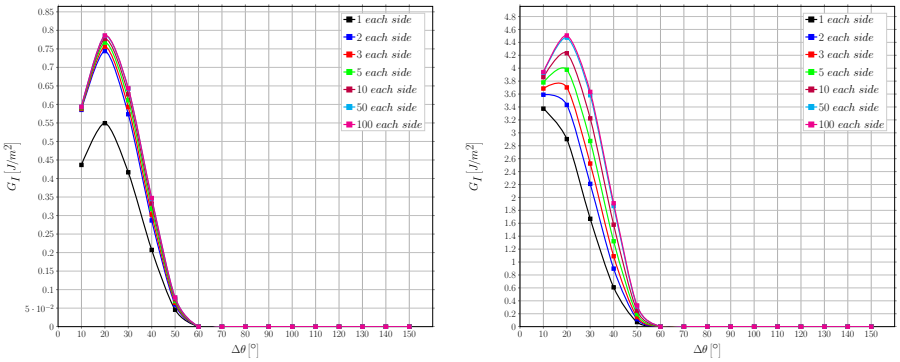
The general incresing trends observed in Figs. 6 and 7 are related to the fact that, given that the global and local V_f are everywhere identical in the models presented, an increase in fiber content corresponds to a decrease in the average distance between fibers. Thus, the relaxation of the stress and strain fields in the

matrix domain occurs over smaller lengths causing higher values at the crack tip. The difference in relative magnification between mode I and mode II and the delay in the contact zone's onset are instead due to the interplay between two different mechanisms, both caused by the ordered microstructural arrangement of the model. In the models considered, a fully bonded fiber is always placed along the horizontal direction, aligned with the partially debonded fiber and exactly in front of the debond. By increasing V_f, the former moves closer to the latter and this causes a magnification of the x-strain at the crack tip. For small debonds ($\leq 20° - 30°$), the crack tip is approximately normal to the x-direction and thus an increase in ε_x causes an increase in G_I. On the other hand, for large debonds ($\geq 70° - 80°$) the crack growth is almost aligned with the x-axis, thus a magnification in the x-strain translates into an increase of mode II ERR. However, this increasing effect on G_{II} is counteracted by the presence of a fully bonded fiber along the vertical direction, aligned with the partially debonded one. As fibers are more rigid than the sourrounding matrix, the presence of the former will restrain horizontal displacements, thus hampering strong increases in G_{II} for large debonds. Furthermore, due to the mismatch in the Poisson's ratios, the fully bonded fiber placed above generates an upward-directed component of the vertical displacement field in the matrix, which tends to open the debond and causes the delay in the contact zone's onset. The interplay between these mechanisms is governed by the average inter-fiber distance and, in turn, by the fiber volume fraction.

3.2. Interaction between debonds in UD laminates with a single layer of fibers

The interaction of debonds appearing at regular intervals in UD composites with a single layer of fibers is studied for mode I (Fig. 8) and mode II (Fig. 9) and fiber content equal to 30% (Figs. 8a and 9a) and 60% (Figs. 8b and 9b). The models treated are $D3H0V1L$, $D5H0V1L$, $D7H0V1L$, $D11H0V1L$, $D21H0V1L$, $D101H0V1L$ and $D201H0V1L$, corresponding respectively to a debond every 3^{rd}, 5^{th}, 7^{th}, 11^{th}, 21^{st}, 101^{st} and 201^{st} fiber (Fig. 1a). Given that the upper surface of the UD is left free, the interaction is stronger than in any other

case and the results of this section are thus the most conservative in terms of debond's growth. From both 8 and 9, it can be seen that the presence of a debond decreases the strain magnification effect discussed in Sec. 3.1 and thus reduces the value of the ERR.

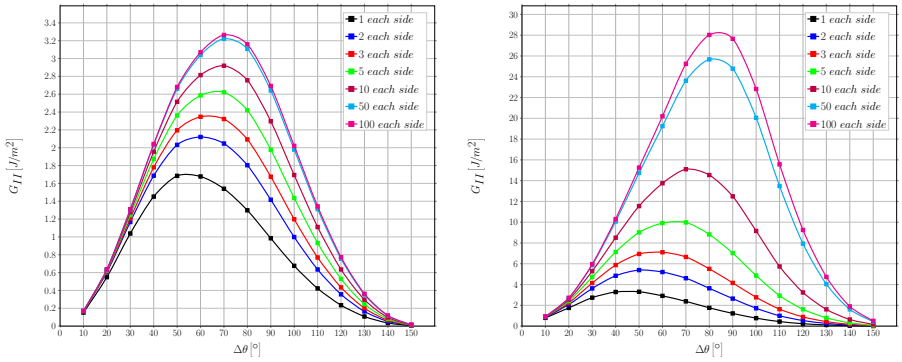


(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 8: Effect of the interaction between debonds appearing at regular intervals on Mode I ERR in an UD with a single layer of fibers at different levels of fiber volume fraction V_f.

For mode I, the presence of a free surface, and inversely the absence of a fully bonded fiber along the vertical direction, implies the absence of the counteracting upward-oriented vertical component of the displacement field due to the mismatch in Poisson's ratios. This in turn translates into the constancy of the value of $\Delta\theta$ corresponding to contact zone's onset, always equal to 60°. For $V_f = 30\%$, mode I is reduced going from a debond placed every 5^{th} fiber to every 3^{th} fiber. Larger spacing does not seem to have a sizable effect. Similarly, at 60% no difference can be seen between the case of a debond placed every 101^{th} and every 201^{th} fiber. These observations suggest the existence of characteristic distance dependent on the fiber volume fraction which governs the interaction between debonds.

Without costraint on the upper surface, the strain magnification effect creates larger displacements in the x-direction, which increase mode II for larger debonds. When debonds are far apart, the series of rigid elements (constituted by fully bonded fibers and their sorronding matrix) creates higher x-strains,



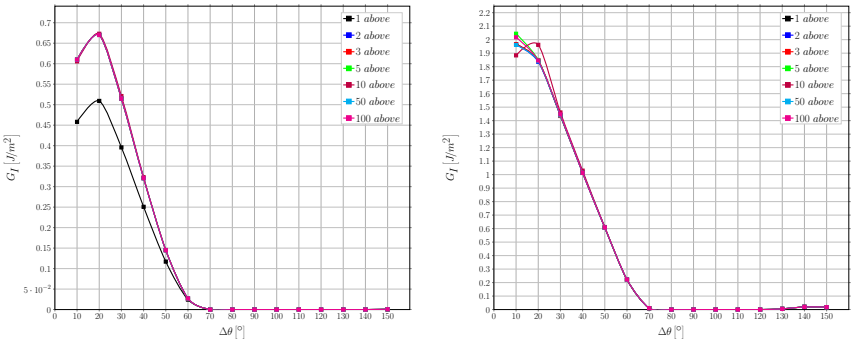
(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 9: Effect of the interaction between debonds appearing at regular intervals on Mode II ERR in a single-ply laminate with a single layer of fibers at different levels of fiber volume fraction V_f.

which in turn generates higher tangential displacements at the crack tip for larger debonds. Conversely, when debonds are closer, the strain concentration is reduced and the tangential component at the crack tip decreases for large $\Delta\theta$. This is the mechanism behind the change in the value of $\Delta\theta$ for which the peak of G_{II} occurs: from 70° to 50° at 30%, and from 80° to 40° at 60% going from the higher to the smaller spacing of debonds. Differently from mode I, the presence of a characteristic distance is harder to establish. For $V_f = 30\%$ (Fig. 9a), it seems reasonable to establish it at around 100 fully bonded fibers between each debond. For $V_f = 60\%$ (Fig. 9b), the difference between models $D101H0V1L$ and $D201H0V1L$ is still sizable, thus preventing the establishment of such characteristic distance. It is possible to observe, however, that the change between $D101H0V1L$ and $D201H0V1L$ is significantly smaller than between $D21H0V1L$ and $D101H0V1L$ ($2\left[\frac{J}{m^2}\right]$ vs $11\left[\frac{J}{m^2}\right]$), thus suggesting the existence of the characteristic distance outside the range studied.

3.3. Influence of layers of fully bonded fibers on debond's growth in a line of debonded fibers located at mid-thickness

The effect of the presence of layers of fully bonded fibers on debond's growth in a line of partially debonded fibers located at mid-thickness in UD composites is studied for mode I (Fig. 10) and mode II (Fig. 11) and fiber content equal to 30% (Figs. 10a and 11a) and 60% (Figs. 10b and 11b). The models treated are $D1H0V3L$, $D1H0V5L$, $D1H0V7L$, $D1H0V11L$, $D1H0V21L$, $D1H0V101L$ and $D1H0V201L$, corresponding to a debond every 1^{st} fiber in the horizontal direction, in a UD composites with respectively 3, 5, 7, 11, 21, 101 and 201 layers of fibers (Fig. 2a).



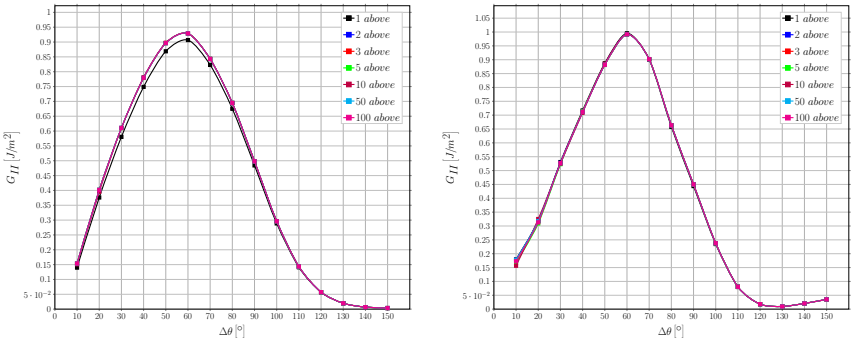
(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 10: Influence of layers of fully bonded fibers on debond's growth in Mode I ERR in a centrally located line of debonded fibers at different levels of fiber volume fraction V_f.

3.4. Interaction between debonds in UD laminates with multiple layers of fibers

Finally models that are closer to real laminates and are more complex (2 parameters: number of fibers along the horizontal direction, number of layers in the vertical one). G_I in Fig. 12, G_{II} in Fig. 13.

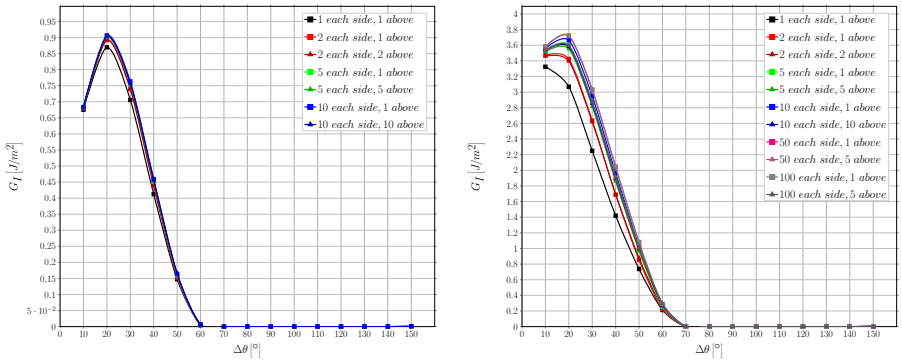
One graphic for each V_f (30%,50%,60%,65%), one curve for some selected case of fibers on top and on the side. Hypothesis of selected cases ([n. on side, n. on top]): [1,1], [2,1], [2,2], [5,1], [5,5], [10,1], [10,10], [50,1], [50,10], [100,1],



(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 11: Influence of layers of fully bonded fibers on debond's growth in Mode II ERR in a centrally located line of debonded fibers at different levels of fiber volume fraction V_f.

[100,10]

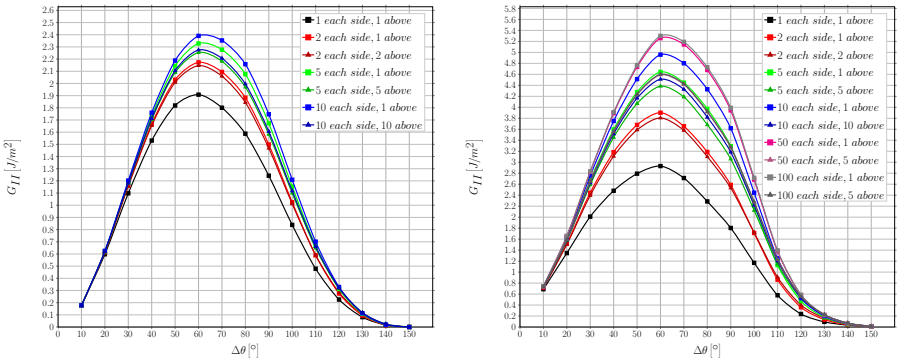


(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 12: Effect of the interaction between debonds appearing at regular intervals on Mode I ERR in a single-ply laminate with multiple layers of fibers at different levels of fiber volume fraction V_f.

3.5. Comparison with the single fiber model with equivalent boundary conditions

We compare the previous results with the corresponding models of single fibers with equivalent BC. We draw conclusions on the possibility of using a single fiber with equivalent BCs. By remembering the actual ply configurations



(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 13: Effect of the interaction between debonds appearing at regular intervals on Mode II ERR in a single-ply laminate with multiple layers of fibers at different levels of fiber volume fraction V_f.

the repeating elements are modeling, and observing that in the vertical direction no significant effect related to the presence of debonded or bonded fiber can be found, we conclude that debonds appearing in fibers aligned in the vertical direction are energetically equivalent, and thus different configurations of debonded/bonded fibers along the vertical direction have the same probability. It is thus likely, from the energetic point of view, that debonds form at the same time along fibers aligned vertically. G_I in Fig. 14 and Fig. 16, G_{II} in Fig. 15 and Fig. 17.

One graphic for each V_f (30%,50%,60%,65%), one curve for single fiber with BC + some selected case of fibers on top and on the side. Hypothesis of selected cases ([n. on side, n. on top]): [1,1], [2,1], [2,2], [5,1], [5,5], [10,1], [10,10]

4. Conclusions & Outlook

Acknowledgements

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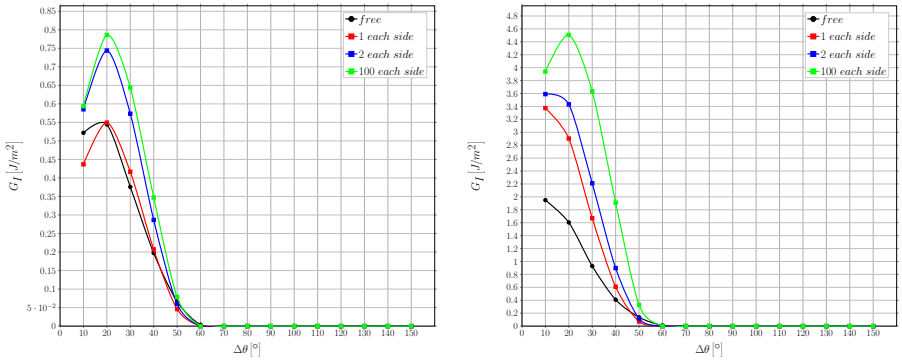
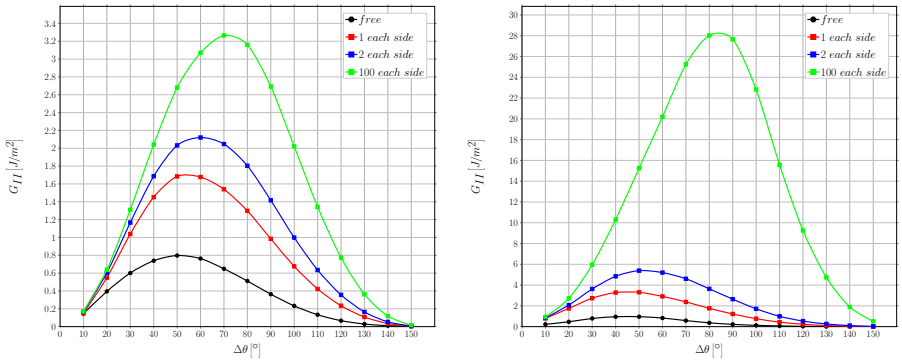


(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 14: Comparison of Mode I ERR between the single fiber model with free upper boundary and the multiple fibers model with fibers only on the side at different levels of fiber volume fraction V_f.



(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 15: Comparison of Mode II ERR between the single fiber model with free upper boundary and the multiple fibers model with fibers only on the side at different levels of fiber volume fraction V_f.

European Commission through the Erasmus Mundus Programme.

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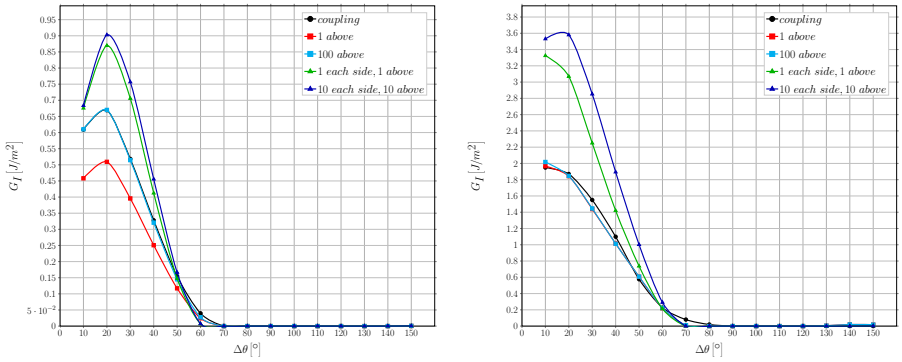
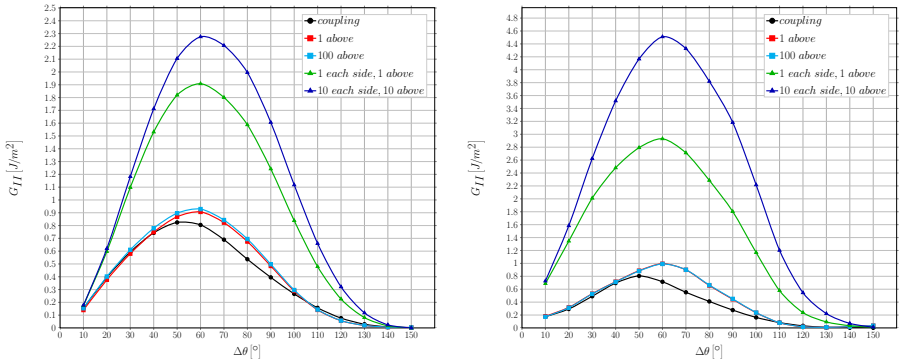


(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 16: Comparison of Mode I ERR between the single fiber model with coupling conditions along the upper boundary and the multiple fibers model with fibers above and both above and on the side at different levels of fiber volume fraction V_f.



(a) $V_f = 30\%$. (b) $V_f = 60\%$.

Figure 17: Comparison of Mode II ERR between the single fiber model with coupling conditions along the upper boundary and the multiple fibers model with fibers above and both above and on the side at different levels of fiber volume fraction V_f.

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