

# Energy release rate of the fiber/matrix interface crack growth in $[0_{m \cdot 2l}^{\circ}, 90_l^{\circ}]_S$ laminates under transverse loading: effect of $0^{\circ}/90^{\circ}$ interface

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## Abstract

Models of Representative Volume Elements (RVEs) of cross-ply  $[0_{m \cdot 2l}^{\circ}, 90_l^{\circ}]_S$  laminates with different geometric configurations and damage states are studied. Debond growth is characterized by the estimation of the Mode I and Mode II Energy Release Rate (ERR) using the Virtual Crack Closure Technique (VCCT) and the J-integral. It is found that the presence of the  $0^{\circ}/90^{\circ}$  interface and the thickness of the  $0^{\circ}$  layer have no effect, apart from laminates with *ultra-thin*  $90^{\circ}$  plies where it is however modest. With the exception of cross-ply laminates with an *ultra-thin*  $90^{\circ}$  ply, no difference is found in debond ERR between a UD composite and a cross-ply laminate.

**Keywords:** Polymer-matrix Composites (PMCs), Thin-ply, Transverse Failure, Debonding, Finite Element Analysis (FEA)

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## 1. Introduction

Since the development of the *spread tow* technology or “FUKUI method” [1, 2], significant efforts have been directed toward the characterization of *thin-ply* laminates [3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15] and their application to mission-critical structures in the aerospace sector [16, 17, 18, 19].

At the lamina level, the use of *thin-ply*s leads to more regular and homogeneous microstructures [9, 12]. Measurement of ply level properties (tensile and compressive modulus, Poisson’s ratio, ultimate tensile strength, tensile on-

set of damage, interlaminar shear strength) on UD specimens ( $[0_m^\circ]$  and  $[90_m^\circ]$ )  
10 revealed no remarkable difference with average properties available in the literature for the same type of fiber, nor showed any particular dependence on the ply thickness [12]. Only an increase of the ultimate compressive strength in the fiber direction was observed with very thin plies ( $\sim 4$  fiber diameters), although with very scattered values, which the authors claim to be due to the  
15 fiber arrangement's increased regularity which prevents the onset of fiber microbuckling [12]. A number of researchers [4, 5, 6, 7] has reported improvements in fatigue life with the use of *thin-ply*s, which are explained as a consequence of delayed propagation of free edge delaminations and intralaminar cracks. Several researchers have in fact analyzed the beneficial effect of *thin-ply*s on damage  
20 development under static [3, 6, 7, 8, 9, 10, 11, 12], fatigue [4, 6, 7, 8, 12] and impact loadings [6, 7, 8, 12]. It seems apparent that *thin-ply* laminates possess an increased ability to delay, and in some cases even suppress, the onset and propagation of intralaminar cracks (or transverse or matrix or micro-cracks).  
The first appearance of transverse cracks is known to be characterized by the  
25 occurrence of fiber/matrix interface cracks (also referred to as debonds), which grow along the fiber arc direction, then kink out of the interface and coalesce forming a transverse crack [20]. Different approaches have been applied to model the initiation and growth of debonds. The Cohesive Zone Model (CZM) has been used to mimic the propagation of debonds along fiber interfaces; coupled with a failure criterion for the matrix, it has provided simulations of the  
30 growth of transverse cracks starting from a virgin material [21, 22, 23, 24]. The main advantages of this approach are the possibility to observe the development of a simulated crack path and to record a load-displacement curve to compare with experimental measurement. However, various observations cast a doubt  
35 about the applicability of the CZM: the bi- (for 2D models) and tri- (in 3D) axially of the matrix stress state in the inter-fiber region that is linked with a cavitation-like failure of the polymer [25]; the locality and mode dependency of the interface failure [26]; the problematic use at the microscopic level of properties measured in UD specimens at the laminate level [22]. A second approach

40 that obviates these drawbacks is the application of Linear Elastic Fracture Me-  
 chanics (LEFM) arguments to the study of debond growth. The analysis focuses  
 on the evaluation of Mode I and Mode II Energy Release Rate (ERR) at the  
 crack tip by means of the Virtual Crack Closure Technique (VCCT) [27] or the  
 J-Integral method [28]. The stress and strain field, required for the ERR compu-  
 45 tation, can be solved by application of different methodologies such as analytical  
 solutions [29], the Boundary Element Method (BEM) [30] or the Finite Element  
 Method (FEM) [31]. The limitation of this approach is that it describes prop-  
 agation of the debond, not its initiation. Finite fracture mechanics [32] is one  
 way how to address the initiation problem. Different works have followed the  
 50 LEFM approach and studied models of one or two fibers in an effectively infinite  
 matrix [33, 34, 35, 36, 37] and of an hexagonal cluster of fibers in an effectively  
 infinite homogenized UD composite [38, 31]. The problem of debond growth  
 along the fiber-matrix interface in a cross-ply laminate has been only addressed  
 very recently in [39, 40], where authors embed a single partially debonded fiber  
 55 in an effectively infinite homogenized  $90^\circ$  ply bounded by homogenized  $0^\circ$  lay-  
 ers. Thus, the effect of debond-debond interaction and of the relative proximity  
 of a  $0^\circ/90^\circ$  interface on the debond's ERR in cross-ply laminates is yet to be  
 addressed. The present work is devoted to this problem. Models of Repeating  
 Unit Cells (RUCs) are developed to represent laminates with different degrees  
 60 of damage (here only in the form of debonds). The number of fully bonded  
 fibers across the thickness of the  $90^\circ$  ply is varied in order to investigate the  
 effect of the proximity of the  $0^\circ/90^\circ$  interface. The thickness of the bounding  $0^\circ$   
 layers is also used as a parameter of the study. The stress and strain fields are  
 solved with the Finite Element Method in Abaqus [41] and the debond (crack)  
 65 is characterized by its Mode I and Mode II ERR, calculated with the VCCT  
 and the J-integral method.

## 2. RVE models & FE discretization

### 2.1. Introduction & Nomenclature

In the present work, we investigate debond development under in-plane  
70 transverse tension in  $[0_{m \cdot 2l}^\circ, 90_l^\circ]_S$  laminates, where  $2l$  is the thickness of the  
central  $90^\circ$  layer expressed in terms of the number  $l$  of plies constituting it and  
 $m \cdot 2l$  represents the thickness of the  $0^\circ$  layer as a multiple of the  $90^\circ$  layer  
thickness. The interaction between debonds in the presence of an interface with  
a stiff layer is studied with the use of different Repeating Unit Cells (RUCs)  
75 (see Figures 1 and 2 in Sec. 2.2), in which only the central fiber is partially  
debonded. Repetition of the composite RUC can occur only along the in-plane  
transverse direction, thus representing a cross-ply laminate with a thin or even  
ultra-thin  $90^\circ$  ply in the middle.

The thickness of the  $90^\circ$  ply depends on the number of fibers present across the  
80 thickness (the vertical or  $z$  direction in Figures 1 and 2) and the value of the  
fiber volume fraction  $V_f$ . On the other hand, the thickness of the  $0^\circ$  layers can  
be assigned freely as a multiple of the  $90^\circ$  ply thickness, i.e.  $t_{0^\circ} = m \cdot t_{90^\circ}$  where  
 $m$  is an arbitrary integer. Thus, the thickness ratio  $i$  represents one additional  
parameter for the investigation. In the RUCs proposed, we consider the  $90^\circ$   
85 ply with debonds as a series of stacked damaged and undamaged fiber rows,  
each row with only one fiber in the thickness direction. All the RUCs present  
regular microstructures with fibers placed according to a square-packing con-  
figuration and consequently they are Representative Volume Elements (RVE)  
of cross-ply laminates with a certain distribution of debonds in the middle  $90^\circ$   
90 layer. In the following, let us consider in-plane coordinates  $x$  and  $y$ , where  $x$   
is in the transverse direction of the cross-ply laminate under consideration. In  
the presence of a load in the  $x$ -direction, the strain in the  $y$ -direction is small,  
due to the very small Poisson's ratio of the laminate. Furthermore, debonds are  
considered to be significantly longer in the fiber direction than in the arc direc-  
95 tion [42]. Therefore we use 2D models under the assumption of plane strain,  
defined in the  $x - z$  section of the composite. The study presented in this paper

thus applies to long debonds and its focus is on understanding the mechanisms of growth along their arc direction. The laminates are assumed to be subject to transverse tensile strain, which is applied in the form of a constant displacement in the  $x$ -direction along both vertical boundaries of the RUC as shown in Figure 3.

In summary, the models are differentiated by: first, the spacing between debonds along the horizontal direction in the  $90^\circ$  layer, which corresponds to the number  $n$  of fibers in the RUC's horizontal direction; second, the thickness of the middle  $90^\circ$  ply measured in terms of the number  $k$  of fiber rows; third, the factor  $m$  which provides the thickness of the  $0^\circ$  layers as an integer multiple of the  $90^\circ$  ply thickness. It thus seems natural to introduce a common notation in the presented results as  $n \times k - m \cdot t_{90^\circ}$ . An additional model is considered to study the effect of equivalent boundary conditions. This final model is constituted by only one partially debonded fiber. The application of coupling of horizontal displacements in the form of a constant applied displacement along the right and left sides allows for repetition along the horizontal direction. The presence of coupling of vertical displacements and a linear distribution of horizontal displacements on the bottom and top surfaces models the presence of the interface between the  $90^\circ$  layer and the stiff  $0^\circ$  one. This model is referred to as  $1 \times 1 - H + V$  given that: it has respectively 1 fiber in the horizontal and in the vertical direction; on the top and bottom surfaces, both horizontal (H) and vertical (V) displacements are assigned. Furthermore, two single fiber models similar to  $1 \times 1 - H + V$  are considered in the present work for comparison: the  $1 \times 1 - free$  and  $1 \times 1 - coupling$ . In the first, the upper surface is left free; in the second, vertical displacement coupling is applied to the upper boundary. Further details about these models and the corresponding laminate RVE can be found in [43].

## 2.2. Description of modelled Representative Volume Elements (RVEs)

The first family of Representative Volume Elements (RVEs) is represented in Figure 1. It represents a set of  $[0_{m \cdot 2l}^\circ, 90_l^\circ]_S$  cross-ply laminates with an

ultra-thin  $90^\circ$  layer, constituted by a single row of fibers across the thickness. Debonds appear at regular intervals measured in terms of number  $n - 1$  of fully bonded fibers present between them, which in turn correspond to the number of fibers along the horizontal direction of the RVE as highlighted in Fig. 1.

They are thus the  $n \times 1 - m \cdot t_{90^\circ}$  models, where  $m = 1, 10$  and  $n$  is an integer  $\geq 1$  ( $n = 1$  corresponds to the case of a debond appearing on all the fibers in the central  $90^\circ$  layer). These models are geometrically extreme, but allow to focus on the interaction between debonds and the inter-ply  $0^\circ/90^\circ$  interface.

Furthermore, the *spread tow* technology is today capable of producing cross-ply laminates with the central  $90^\circ$  layer thickness only 4–5 times the fiber diameter, as shown for example in [9], which may in future give practical relevance even to such extreme case.

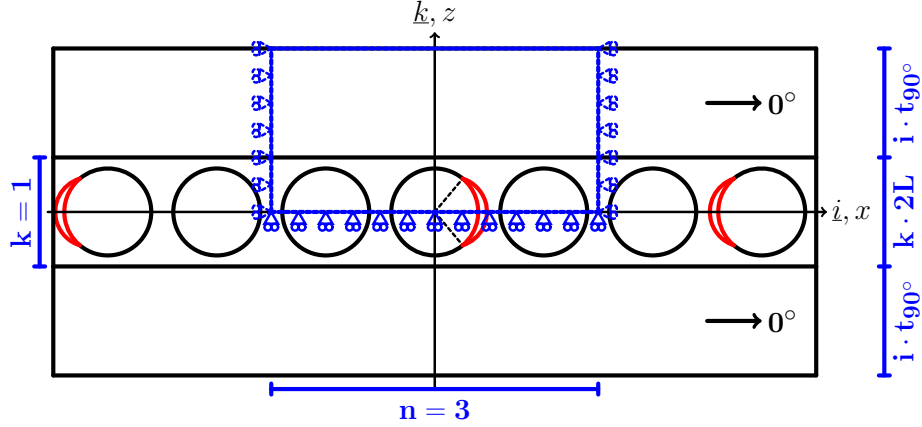


Figure 1: Models of  $[0_{m \cdot 2l}^\circ, 90_l^\circ]_S$  laminates with an ultra-thin  $90^\circ$  layer, where the  $90^\circ$  ply is made up by a single “row” of fibers. Debonds are repeating at different distances, measured in terms of the number  $n - 1$  of fully bonded fibers appearing between two consecutive debonds.

The second set of models considers instead cross-ply laminates with a central  $90^\circ$  ply of variable thickness, measured in terms of number  $k$  of fiber rows appearing in the vertical direction in Figure 2. Once again, debonds appear in the central row only at regular intervals measured in terms of number  $n - 1$  of fully bonded fibers present between them, which in turn correspond to the number of fibers along the horizontal direction of the RUC as highlighted in

Fig. 2. These models are thus the  $n \times k - i \cdot t_{90^\circ}$  models, where  $i = 1, 10$ ,  $k > 1$  and  $n$  is an integer  $\geq 1$  ( $n = 1$  corresponds to the case of a debond appearing on all fibers of the central fiber row in the  $90^\circ$  layer).

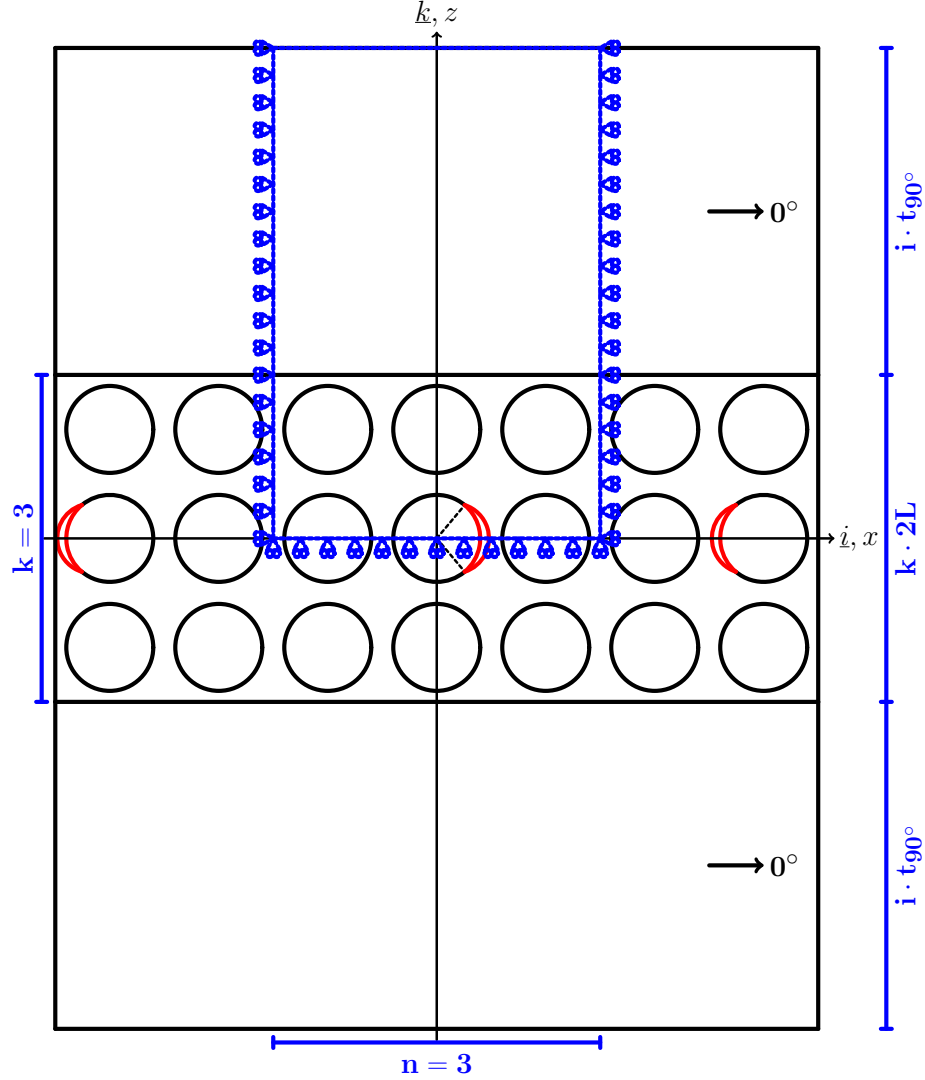


Figure 2: Models of  $[0_{m \cdot 2L}^\circ, 90_i^\circ]_S$  laminates with a  $90^\circ$  layer of variable thickness, determined by the number  $k$  of “rows” of fibers along the vertical direction. Debonds are repeating at different distances along the horizontal direction, measured in terms of the number  $n - 1$  of fully bonded fibers appearing between two consecutive debonds.

By increasing the number  $n$  of fibers in the horizontal direction in the RUC, decreasing levels of damage (debonds spaced further apart and the interaction  
150 between debonds becomes less important) are considered to be present in the laminate. By increasing the number  $k$  of fiber rows, the thickness of the  $90^\circ$  layer is increased and the effect of the relative proximity of the inter-ply  $0^\circ/90^\circ$  interface can thus be studied. Finally, by increasing the factor  $m$ , the thickness of the  $0^\circ$  layers is increased for a given thickness of the  $90^\circ$ , which allows the  
155 investigation of the laminate thickness effect for a given ply thickness [44].

### 2.3. Finite Element (FE) discretization

The RUCs are discretized and solved with the Finite Element Method (FEM) using the commercial FEM package Abaqus [41]. The length  $l$  and height  $h$  of the model are determined by the number of fibers  $n$  in the horizontal direction,  
160 the number of fiber rows  $k$  across the thickness and the thickness ratio  $i$  (see Sec. 2.2) according to Eq. 1:

$$l = 2nL \quad h = (1 + 2i)kL. \quad (1)$$

In Eq. 1,  $2L$  is the length of a one-fiber unit (see Fig. 3), which in turn is as a function of the fiber volume fraction  $V_f$  and the fiber radius according to

$$L = \frac{R_f}{2} \sqrt{\frac{\pi}{V_f}}. \quad (2)$$

Each fiber in the model has the same radius  $R_f$ , equal to  $1 \mu m$ . This specific  
165 value has no physical meaning per se and it has been selected for simplicity. It is useful to observe that, in a linear elastic solution as the one described in the present article, the ERR is proportional to the geometrical dimensions of the model and thus re-evaluation of the ERR for fibers of any size requires just a multiplication. Furthermore, the local and global  $V_f$  are everywhere equal  
170 thanks to the relationships in Eqs. 1 and 2.

The debond appears symmetrically with respect to the  $x$  axis (see Fig. 3) and we characterize it with the angular size  $\Delta\theta$  (the full debond size is thus





Figure 3: Schematic of the model with its main parameters.

$2\Delta\theta$ ). In the case of large debond sizes ( $\geq 60^\circ - 80^\circ$ ), a region of size  $\Delta\Phi$  to be  
determined by the solution itself appears at the crack tip. In this region, called  
175 the *contact zone*, the crack faces are in contact and slide on each other. Due  
to existence of the contact zone, frictionless contact is considered between the  
two crack faces to avoid interpenetration and allow free sliding. Symmetry with  
respect to the  $x$  axis is applied on the lower boundary. The upper boundary  
is free, except for the model  $1 \times 1 - H + V$  which requires on the upper side  
180 kinematic coupling of vertical displacements and applied linearly distributed  
horizontal displacements. Kinematic coupling on the  $x$ -displacement is applied  
along the left and right boundaries of the model in the form of a constant  $x$ -  
displacement  $\pm \bar{\varepsilon}_x l$ , corresponding to transverse strain  $\bar{\varepsilon}_x$  equal to 1%.

The FEM model is discretized using second order, 2D, plane strain triangular  
185 lar (CPE6) and rectangular (CPE8) elements. In the crack tip neighborhood, a  
refined regular mesh of quadrilateral elements with almost unitary aspect ratio

Table 1: Summary of mechanical properties of fiber, matrix and UD layer.  $E$  stands for Young’s modulus,  $\mu$  for shear modulus and  $\nu$  for Poisson’s ratio. Indexes  $L$  and  $T$  stand respectively for *longitudinal* and *transverse*.

Material	$V_f$ [%]	$E_L$ [GPa]	$E_T$ [GPa]	$\mu_{LT}$ [GPa]	$\nu_{LT}$ [–]	$\nu_{TT}$ [–]
Glass fiber	-	70.0	70.0	29.2	0.2	0.2
Epoxy	-	3.5	3.5	1.25	0.4	0.4
UD	60.0	43.442	13.714	4.315	0.273	0.465

is needed to ensure a correct evaluation of the ERR. The angular size  $\delta$  of an element in this refined region close to the crack tip is by design equal to  $0.05^\circ$ . The crack faces are modeled as element-based surfaces with a frictionless small-sliding contact pair interaction. The Mode I, Mode II and total Energy Release Rates (ERRs) (respectively  $G_I$ ,  $G_{II}$  and  $G_{TOT}$ ) represent the main result of the numerical analysis. They are computed using the VCCT [27] implemented in a custom Python routine and the total ERR is obtained from the J-integral [28] evaluation by means of the Abaqus built-in functionality. Glass fiber and epoxy are considered throughout this article, and it is assumed that their response always lies in the linear elastic domain. The effective UD properties are computed using Hashin’s Concentric Cylinder Assembly model [45] with the self-consistency scheme for the out-of-plane shear modulus of Christensen [46]. The properties used are listed in Table 1. The model was validated with respect to BEM results of [47, 36]; considerations about the order of accuracy can be found in [43].

### 3. Results & Discussion

#### 3.1. Effect of the proximity of the $0^\circ/90^\circ$ interface and of the thickness of the $0^\circ$ layer on debond ERR

We first focus our attention on the model  $1 \times 1 - i \cdot t_{90^\circ}$ , which represents a particular case of the family  $n \times 1 - i \cdot t_{90^\circ}$ . It corresponds to a cross-ply laminate in which the central  $90^\circ$  ply is constituted by only one fiber row, in which each fiber

possesses a debond appearing on alternating sides. The model thus represents an extreme idealization, in the sense that: the central  $90^\circ$  layer is the thinnest that can be conceived and cannot actually be produced; second, a very particular damage state is present for which every fiber is partially debonded from the surrounding matrix. However, the first condition allows us to investigate the direct effect of the proximity of the stiff  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface on debond ERR; the second condition prevents the insurgence of strain magnification effects which would be significant in one-fiber-row ply with debonds appearing at regular intervals of fully bonded fibers [43]. The model  $1 \times 1 - i \cdot t_{90^\circ}$  thus isolates the effect of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface. Given that the ratio  $i = \frac{t_{0^\circ}}{t_{90^\circ}}$  is a free parameter, we can furthermore study the effect of the thickness of the  $0^\circ$  layer on debond ERR.

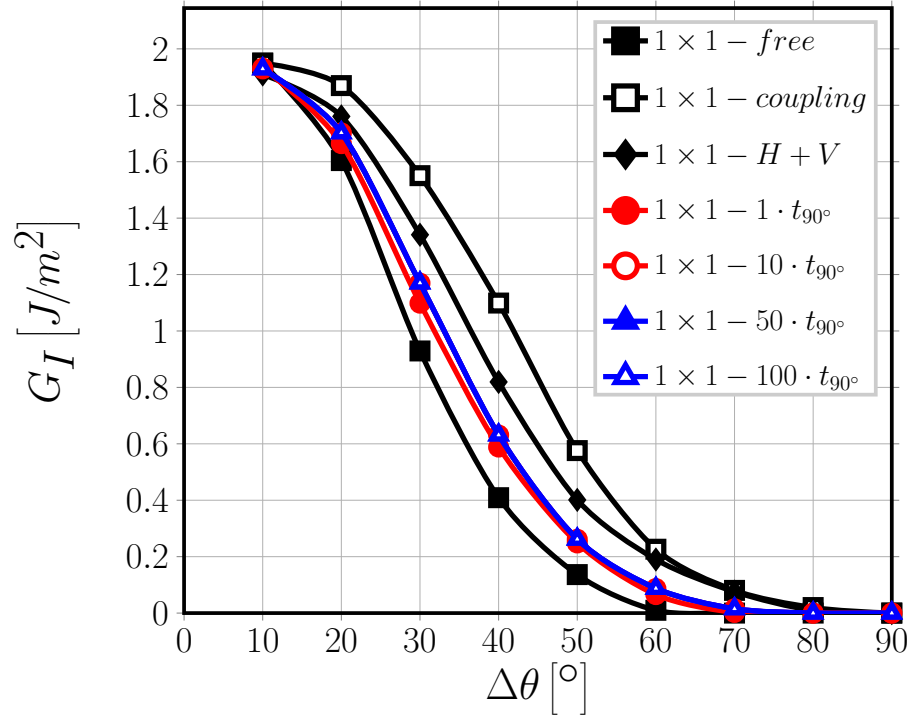


Figure 4: Effect of the proximity of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface and of the thickness of the  $0^\circ$  layer on Mode I ERR: models  $1 \times 1 - free$ ,  $1 \times 1 - coupling$ ,  $1 \times 1 - H + V$  and  $1 \times 1 - i \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

220 In Figures 4 and 5 respectively the Mode I and Mode II ERR are compared  
 between models  $1 \times 1 - i \cdot t_{90^\circ}$  with  $i = 1, 10, 50, 100$  and models  $1 \times 1 - free$ ,  
 $1 \times 1 - coupling$  and  $1 \times 1 - H + V$ . It is worth to remind us of the laminate  
 RVE that correspond to these last three models: model  $1 \times 1 - free$  represents  
 a one-fiber-row UD composite with all the fibers partially debonded; model  
 225  $1 \times 1 - coupling$  corresponds to a UD laminate with an infinite number of fiber  
 rows and all the fibers partially debonded; model  $1 \times 1 - H + V$  represents a  
 cross-ply laminate with one-fiber-row central  $90^\circ$  ply. Observing Figure 4, it is  
 possible to notice that the presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface translates into  
 a modest increase in the value of  $G_I$  with respect to the free surface. For every  
 230 value of the thickness, however, the values of  $G_I$  are lower than those computed  
 with the  $1 \times 1 - coupling$  and  $1 \times 1 - H + V$  models. A more significant effect can  
 be observed in relation to contact zone onset, which is delayed from  $\Delta\theta = 60^\circ$   
 in the presence of a free surface to  $70^\circ$  in the presence of a homogenized  $0^\circ$   
 layer. The maximum delay is however reached with the models with equivalent  
 235 boundary conditions ( $1 \times 1 - coupling$  and  $1 \times 1 - H + V$ ), for which the contact  
 zone onset happens at  $\Delta\theta = 80^\circ$ . No effect of the thickness of the  $0^\circ$  layer on  
 Mode I ERR can be observed.

The presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface causes instead a decrease of  
 Mode II for open debonds ( $\Delta\theta < 60^\circ - 70^\circ$ ) and a decrease for close debonds  
 240 ( $\Delta\theta > 60^\circ - 70^\circ$ ) with respect to the free surface case (see Fig. 5). The trend is  
 the same as the one of the model  $1 \times 1 - H + V$ , but more modest in magnitude.  
 A small effect of the thickness of the  $0^\circ$  layer on Mode II ERR can be noticed  
 in Fig. 5 when the ratio  $i = \frac{t_{0^\circ}}{t_{90^\circ}}$  is increased from 1 to 10. The change between  
 the two follows the same pattern described previously: when the thickness of  
 245 the  $0^\circ$  ply is increased, Mode II decreases for open debonds and increases for  
 closed debonds.

These results help to shed light on the effect of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface  
 on debond ERR. The presence of the stiff homogenized  $0^\circ$  layer causes the  
 matrix placed relatively far from the fiber (close to the left and right sides) to  
 250 contract much less than it would do in the presence of a free surface due to its



Figure 5: Effect of the proximity of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface and of the thickness of the  $0^\circ$  layer on Mode II ERR: models  $1 \times 1 - free$ ,  $1 \times 1 - coupling$ ,  $1 \times 1 - H + V$  and  $1 \times 1 - i \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

relatively high Poisson's ratio. Furthermore, the presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface induces a more homogeneous  $x$ -displacement field all over the matrix domain. This causes a concurrent increase of  $G_I$  and decrease of  $G_{II}$  for small debonds, where the crack opening displacement component at the crack tip (responsible for Mode I) is mostly due to the global  $x$ -displacement field (which increase in the presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface) while the crack shear displacement component at the crack tip (responsible for Mode II) is instead linked to the global vertical displacement field due to Poisson's effect (which is decreasing). This causes also the delay in the onset of the contact zone. For large debonds instead, after the onset of the contact zone, the situation reverses: the magnitude increase of the global  $x$ -displacement field leads to an increase in

the crack shear displacement component at the crack tip and thus in Mode II ERR. By comparing the results for Mode II of models  $1 \times 1 - free$ ,  $1 \times 1 - H + V$  and  $1 \times 1 - i \cdot t_{90^\circ}$  with  $i = 1, 10, 50, 100$  (Fig. 5), it can be argued that the effect of the  $0^\circ$  ply thickness is related to the distance of the free surface: for  $t_{0^\circ} = t_{90^\circ}$  a modest effect of the presence of the upper free surface of the  $0^\circ$  ply is still felt by the debond and the effect of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface previously described is reduced, with the ERR values closer to the  $1 \times 1 - free$  model. When the thickness ratio is increased to 10, the effect disappears. No further change is observed for thicker  $0^\circ$  layers.

### 3.2. Effect of the proximity of the $0^\circ/90^\circ$ $0^\circ/90^\circ$ interface on debond-debond interaction in a single fiber row $90^\circ$ ply

We turn now our attention to the models  $n \times 1 - 1 \cdot t_{90^\circ}$ , which correspond to a cross-ply laminate in which the central  $90^\circ$  ply is constituted by only one fiber row where debonds appear on alternating sides of the damaged fiber at regular intervals of  $n - 1$  fully bonded fibers (see Figure 1). This class of models allows to study the effect of the presence of the  $0^\circ$  layer on debond-debond interaction and, particularly, crack shielding [48, 43].

From Figures 6 and 7 it seems apparent that the effect of the presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface is to reduce the  $x$ -strain magnification caused by the presence of an increasing number of fully bonded fibers between two consecutive debonds. Effects observed in the previous section (Sec. 3.1) are also retrievable in Figures 6 and 7. For Mode I, irrespectively of the number of undamaged fibers between two consecutive debonds, the contact zone onset is shifted by  $\sim 10^\circ$  from  $60^\circ$  in the presence of a free surface to  $70^\circ$  when the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface is present. For Mode II it is possible to observe, especially when debonds are closer to each other, that larger debonds show a slightly higher  $G_{II}$ , as discussed in Sec. 3.1.

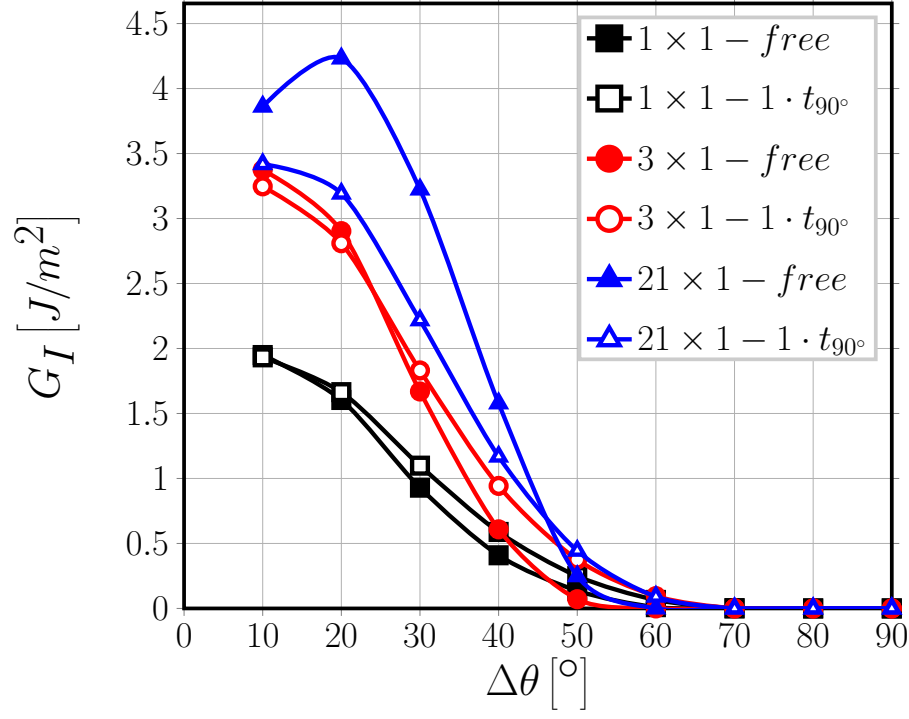


Figure 6: Effect of the presence of the  $0^\circ$  layer on debond-debond interaction for Mode I ERR: models  $n \times 1 - free$  and  $n \times 1 - 1 \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

### 3.3. Effect of the presence of fiber rows with no damage on the debond- $0^\circ/90^\circ$ $0^\circ/90^\circ$ interface interaction

After having investigated the effect of the proximity of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface and of the thickness of the  $0^\circ$  layer on debond ERR and on debond-debond interaction, we address in this section the effect of the presence of fiber rows with only fully bonded fibers inside (and thus no damage) on the interaction between debonds and the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface interaction. To this end, we study the models  $1 \times k - 1 \cdot t_{90^\circ}$ , which represent a cross-ply laminate with the central  $90^\circ$  ply made of  $k$  fiber rows and where all the fibers in the central row are partially debonded. Given that today  $90^\circ$  layers with around 4 – 5 fibers across the thickness are manufacturable thanks to the *thin-ply* technology, this family of models considers a quite realistic geometric configuration of the  $90^\circ$

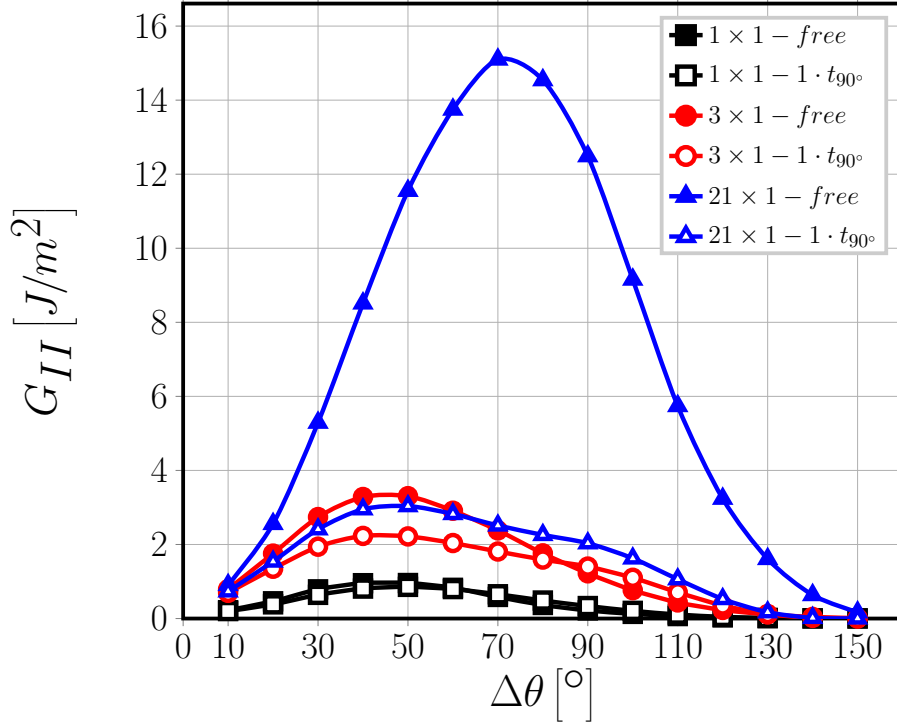


Figure 7: Effect of the presence of the  $0^\circ$  layer on debond-debond interaction for Mode II ERR: models  $n \times 1 - free$  and  $n \times 1 - 1 \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

ply, although ideally organized following a perfect square-packing arrangement. The damage state represents on the other hand quite an extreme idealization: however, the fact that all the fibers in the central row are partially debonded prevents the presence of strain magnification effects.

305 Figures 8 and 9 show clearly that the presence of the  $0^\circ$  ply does not affect in any measurable way the debond ERR neither in Mode I nor in Mode II: there is no difference in  $G_I$   $G_{II}$  between models  $1 \times k - free$  and  $1 \times k - 1 \cdot t_{90^\circ}$ .

310 However, in Figures 8 and 9 the central fiber row of the  $90^\circ$  layer possesses only partially debonded fibers, which represents an extreme damage state. It has been shown that the presence of fully bonded fibers causes a magnification of the  $x$ -strain in the debond neighborhood which leads to an increase in ERR both in one-fiber-row UD [43] and  $90^\circ$  ply in cross-ply laminates (Sec. 3.2). When



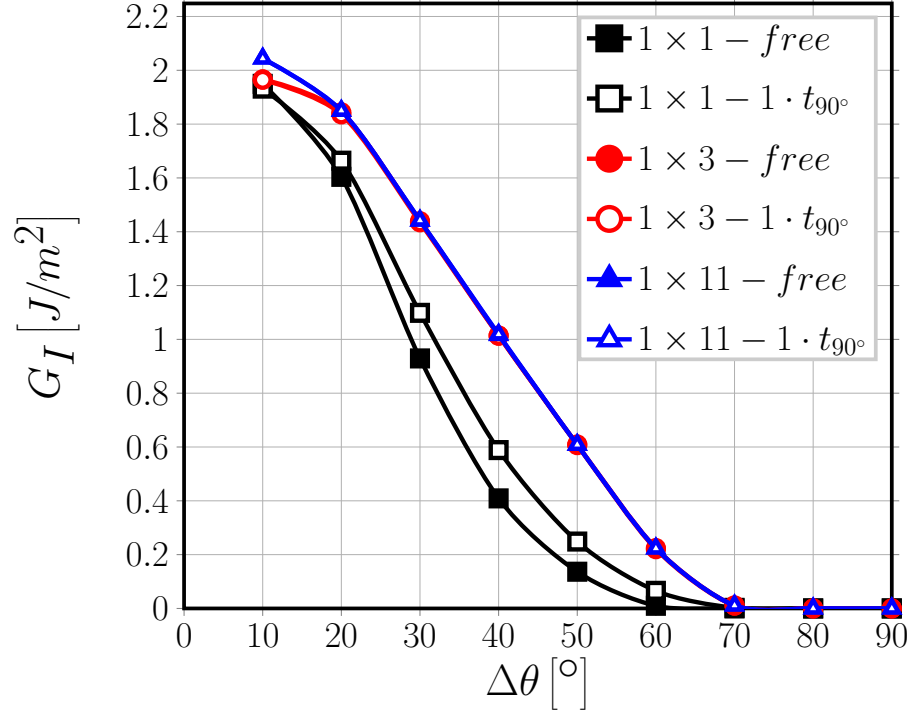


Figure 8: Effect of the presence of undamaged fiber rows in the  $90^\circ$  layer on debond- $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface interaction for Mode I ERR: models  $1 \times k - free$  and  $1 \times k - 1 \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

rows of undamaged fibers are present above and below the fiber row containing the debonds, the presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface has, with respect to the free surface case (corresponding to an extremely thin UD composite), no effect on  $G_I$  and only a small effect on  $G_{II}$ , relevant only for thin  $90^\circ$  plies (see Figures 10 and 11). When present, this effect corresponds to a reduction in Mode II ERR, particularly for debonds further apart (in terms of number of fully bonded fibers between them).

In [39, 40], the authors investigated the existence of scale effects (like the *thin-ply effect*) in the context of the fiber-matrix interface crack using a single partially debonded fiber embedded in a homogenized  $90^\circ$  ply bounded by homogenized  $0^\circ$  layers. They observed the absence of any size effect. The results



Figure 9: Effect of the presence of undamaged fiber rows in the  $90^\circ$  layer on debond- $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface interaction for Mode II ERR: models  $1 \times k - free$  and  $1 \times k - 1 \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

presented in this article confirm their observation and provide a micromechanical explanation (see Sec. 3.1). We have also shown that extremely thin  $90^\circ$  plies (1 – 5 fibers across the thickness) do on the other hand present a magnification effect when fully bonded fibers appear between consecutive aligned debonds. The effect becomes stronger with thinner  $90^\circ$  layers. The only effect of the  $0^\circ$  ply is to reduce the magnification of ERR, which nonetheless takes place. However, this mechanism is not typical of cross-ply laminates, but it can be observed in UD composites as well [43]. It provides a possible mechanical description of the observations presented in [9]: in very thin  $90^\circ$  plies debonds appear at lower strains because the magnification effect is stronger. As more debonds are created, their interaction (crack shielding) causes a reduction in



Figure 10: Effect of the presence of undamaged fiber rows in the  $90^\circ$  layer on debond- $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface interaction for Mode I ERR: models  $n \times k - free$  and  $n \times k - 1 \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

335 ERR which disfavors debond growth.

#### 4. Conclusions & Outlook

Different models of Repeating Unit Cell, representing different representative cross-ply laminates, have been studied in order to study the effect of the presence of the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface and of the thickness of the  $0^\circ$  ply on debond  
340 Energy Release Rate and on crack shielding. It has been found that the presence of the  $0^\circ$  ply causes only a reduction in ERR, especially in Mode II. However, the strain magnification effect due to the presence of fully bonded fibers between two consecutive debonds follows the same pattern previously identified for UD composites. Furthermore, the influence of the  $0^\circ$  layer is strongly mitigated by



Figure 11: Effect of the presence of undamaged fiber rows in the  $90^\circ$  layer on debond- $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface interaction for Mode II ERR: models  $n \times k - free$  and  $n \times k - 1 \cdot t_{90^\circ}$ .  $V_f = 60\%$ ,  $\varepsilon_x = 1\%$ .

the presence of rows of undamaged fibers. Already the presence of 1 row between  
respectively the upper and lower  $0^\circ$  layer and the central fiber row with partially  
debonded fibers causes the computed Mode I and Mode II ERR to adhere closely  
to the results for a UD composite with the same geometrical configuration and  
damage state. The results presented provide an important insight: it appears  
that the behavior of the fiber/matrix interface crack is affected strongly only by  
very close perturbation of the elastic fields. *Thin* and *ultra-thin* plies present  
a peculiar behavior in terms of debond growth because their reduced thickness  
brings the  $0^\circ/90^\circ$   $0^\circ/90^\circ$  interface close enough for the debonds to feel the  
perturbation in the elastic fields. Otherwise, it seems that no difference can  
be found in the mechanism of debond growth between a UD composite and a

cross-ply laminate.

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## References

- [1] K. Kawabe, New spreading technology for carbon fiber tow and its application to composite materials, *Sen'i Gakkaishi* 64 (8) (2008) 262–267. doi:10.2115/fiber.64.p\_262.
- 365 [2] K. Kawabe, H. Sasayama, S. Tomoda, New carbon fiber tow-spread technology and applications to advanced composite materials, *SAMPE Journal* 45 (2) (2008) 6–17.
- [3] H. Sasayama, K. Kawabe, S. Tomoda, I. Ohsawa, K. Kageyama, N. Ogata, Effect of lamina thickness on first ply failure in multidirectionally laminated composites, in: *Proceedings of the 8<sup>th</sup> Japan SAMPE Symposium*, SAMPE, 2003.  
370
- [4] K. Yamaguchi, H. Hahn, The improved ply cracking resistance of thin-ply laminates, in: *Proceedings of the 15<sup>th</sup> International Conference on Composite Materials (ICCM-15)*, SAMPE, 2005.
- 375 [5] S. Tsai, S. Sih, R. Kim, Thin ply composites, in: *Proceedings of 46<sup>th</sup> AIAA/ASME/AHS/ASC Structures, Structural Dynamics & Materials Conference*, 2005.
- [6] S. Sih, R. Kim, K. Kawabe, S. Tsai, Experimental studies of thin-ply laminated composites, *Composites Science and Technology* 67 (6) (2007) 996–1008. doi:10.1016/j.compscitech.2006.06.008.  
380

- [7] T. Yokozeki, Y. Aoki, T. Ogasawara, Experimental characterization of strength and damage resistance properties of thin-ply carbon fiber/toughened epoxy laminates, *Composite Structures* 82 (3) (2008) 382–389. doi:10.1016/j.compstruct.2007.01.015.
- 385 [8] T. Yokozeki, A. Kuroda, A. Yoshimura, T. Ogasawara, T. Aoki, Damage characterization in thin-ply composite laminates under out-of-plane transverse loadings, *Composite Structures* 93 (1) (2010) 49–57. doi:10.1016/j.compstruct.2010.06.016.
- 390 [9] H. Saito, H. Takeuchi, I. Kimpara, Experimental evaluation of the damage growth restraining in 90 layer of thin-ply cfrp cross-ply laminates, *Advanced Composite Materials* 21 (1) (2012) 57–66. doi:10.1163/156855112X629522.
- 395 [10] A. Arteiro, G. Catalanotti, J. Xavier, P. Camanho, Notched response of non-crimp fabric thin-ply laminates, *Composites Science and Technology* 79 (2013) 97–114. doi:10.1016/j.compscitech.2013.02.001.
- [11] A. Arteiro, G. Catalanotti, J. Xavier, P. Camanho, Large damage capability of non-crimp fabric thin-ply laminates, *Composites Part A: Applied Science and Manufacturing* 63 (2014) 110–122. doi:10.1016/j.compositesa.2014.04.002.
- 400 [12] R. Amacher, J. Cugnoni, J. Botsis, L. Sorensen, W. Smith, C. Dransfeld, Thin ply composites: Experimental characterization and modeling of size-effects, *Composites Science and Technology* 101 (2014) 121–132. doi:10.1016/j.compscitech.2014.06.027.
- 405 [13] G. Guillaumet, A. Turon, J. Costa, J. Renart, P. Linde, J. Mayugo, Damage occurrence at edges of non-crimp-fabric thin-ply laminates under off-axis uniaxial loading, *Composites Science and Technology* 98 (2014) 44–50. doi:10.1016/j.compscitech.2014.04.014.

- [14] C. Huang, S. Ju, M. He, Q. Zheng, Y. He, J. Xiao, J. Zhang, D. Jiang, Identification of failure modes of composite thin-ply laminates containing circular hole under tension by acoustic emission signals, *Composite Structures* 206 (2018) 70–79. doi:10.1016/j.compstruct.2018.08.019.
- [15] J. Cugnoni, R. Amacher, S. Kohler, J. Brunner, E. Kramer, C. Dransfeld, W. Smith, K. Scobbie, L. Sorensen, J. Botsis, Towards aerospace grade thin-ply composites: Effect of ply thickness, fibre, matrix and interlayer toughening on strength and damage tolerance, *Composites Science and Technology* 168 (2018) 467–477. doi:10.1016/j.compscitech.2018.08.037.
- [16] J.-B. Moon, M.-G. Kim, C.-G. Kim, S. Bhowmik, Improvement of tensile properties of CFRP composites under LEO space environment by applying MWNTs and thin-ply, *Composites Part A: Applied Science and Manufacturing* 42 (6) (2011) 694–701. doi:10.1016/j.compositesa.2011.02.011.
- [17] Y. H. N. Kim, S. Ko, W.-S. Lay, J. Tian, P. Chang, S. U. Thielk, H.-J. Bang, J. Yang, Effects of shallow biangle, thin-ply laminates on structural performance of composite wings, *AIAA Journal* 55 (6) (2017) 2086–2092. doi:10.2514/1.j055465.
- [18] A. Kopp, S. Stappert, D. Mattsson, K. Olofsson, E. Marklund, G. Kurth, E. Mooij, E. Roorda, The aurora space launcher concept, *CEAS Space Journal* 10 (2) (2017) 167–187. doi:10.1007/s12567-017-0184-2.
- [19] D. A. McCarville, J. C. Guzman, A. K. Dillon, J. R. Jackson, J. O. Birkland, 3.5 Design, Manufacture and Test of Cryotank Components, Elsevier, 2018, pp. 153–179. doi:10.1016/b978-0-12-803581-8.09958-6.
- [20] J. E. Bailey, A. Parvizi, On fibre debonding effects and the mechanism of transverse-ply failure in cross-ply laminates of glass fibre/thermoset composites, *Journal of Materials Science* 16 (3) (1981) 649–659. doi:10.1007/bf02402782.

- [21] V. Kushch, S. Shmegeera, P. Brøndsted, L. Mishnaevsky, Numerical simulation of progressive debonding in fiber reinforced composite under transverse loading, *International Journal of Engineering Science* 49 (1) (2011) 17–29. doi:10.1016/j.ijengsci.2010.06.020.
- 440 [22] L. P. Canal, C. González, J. Segurado, J. LLorca, Intraply fracture of fiber-reinforced composites: Microscopic mechanisms and modeling, *Composites Science and Technology* 72 (11) (2012) 1223–1232. doi:10.1016/j.compscitech.2012.04.008.
- 445 [23] L. Bouhala, A. Makradi, S. Belouettar, H. Kiefer-Kamal, P. Frères, Modelling of failure in long fibres reinforced composites by x-FEM and cohesive zone model, *Composites Part B: Engineering* 55 (2013) 352–361. doi:10.1016/j.compositesb.2012.12.013.
- 450 [24] M. Herráez, D. Mora, F. Naya, C. S. Lopes, C. González, J. LLorca, Transverse cracking of cross-ply laminates: A computational micromechanics perspective, *Composites Science and Technology* 110 (2015) 196–204. doi:10.1016/j.compscitech.2015.02.008.
- [25] L. E. Asp, L. A. Berglund, P. Gudmundson, Effects of a composite-like stress state on the fracture of epoxies, *Composites Science and Technology* 53 (1) (1995) 27–37. doi:10.1016/0266-3538(94)00075-1.
- 455 [26] V. Mantič, Interface crack onset at a circular cylindrical inclusion under a remote transverse tension. application of a coupled stress and energy criterion, *International Journal of Solids and Structures* 46 (6) (2009) 1287–1304. doi:10.1016/j.ijsolstr.2008.10.036.
- 460 [27] R. Krueger, Virtual crack closure technique: History, approach, and applications, *Applied Mechanics Reviews* 57 (2) (2004) 109. doi:10.1115/1.1595677.
- [28] J. R. Rice, A path independent integral and the approximate analysis of



strain concentration by notches and cracks, *Journal of Applied Mechanics* 35 (2) (1968) 379. doi:10.1115/1.3601206.

- 465 [29] M. Toya, A crack along the interface of a circular inclusion embedded in an infinite solid, *Journal of the Mechanics and Physics of Solids* 22 (5) (1974) 325–348. doi:10.1016/0022-5096(74)90002-7.
- [30] F. París, J. C. Caño, J. Varna, The fiber-matrix interface crack — a numerical analysis using boundary elements, *International Journal of Fracture* 470 82 (1) (1996) 11–29. doi:10.1007/bf00017861.
- [31] L. Zhuang, A. Pupurs, J. Varna, R. Talreja, Z. Ayadi, Effects of inter-fiber spacing on fiber-matrix debond crack growth in unidirectional composites under transverse loading, *Composites Part A: Applied Science and Manufacturing* 109 (2018) 463–471. doi:10.1016/j.compositesa.2018.03.031. 475
- [32] M. Muñoz-Reja, L. Távara, V. Mantič, P. Cornetti, Crack onset and propagation at fibre-matrix elastic interfaces under biaxial loading using finite fracture mechanics, *Composites Part A: Applied Science and Manufacturing* 82 (2016) 267–278. doi:10.1016/j.compositesa.2015.09.023.
- 480 [33] E. Correa, V. Mantič, F. París, Effect of thermal residual stresses on matrix failure under transverse tension at micromechanical level: A numerical and experimental analysis, *Composites Science and Technology* 71 (5) (2011) 622–629. doi:10.1016/j.compscitech.2010.12.027.
- [34] E. Correa, F. París, V. Mantič, Effect of the presence of a secondary transverse load on the inter-fibre failure under tension, *Engineering Fracture Mechanics* 485 103 (2013) 174–189. doi:10.1016/j.engfracmech.2013.02.026.
- [35] E. Correa, F. París, V. Mantič, Effect of a secondary transverse load on the inter-fibre failure under compression, *Composites Part B: Engineering* 65 (2014) 57–68. doi:10.1016/j.compositesb.2014.01.005.

- 490 [36] C. Sandino, E. Correa, F. París, Numerical analysis of the influence of a nearby fibre on the interface crack growth in composites under transverse tensile load, *Engineering Fracture Mechanics* 168 (2016) 58–75. doi:10.1016/j.engfracmech.2016.01.022.
- [37] C. Sandino, E. Correa, F. París, Interface crack growth under transverse  
495 compression: nearby fibre effect, in: *Proceeding of the 18<sup>th</sup> European Conference on Composite Materials (ECCM-18)*, 2018.
- [38] J. Varna, L. Q. Zhuang, A. Pupurs, Z. Ayadi, Growth and interaction of debonds in local clusters of fibers in unidirectional composites during transverse loading, *Key Engineering Materials* 754 (2017) 63–66. doi:  
500 10.4028/www.scientific.net/kem.754.63.
- [39] M. Velasco, E. Graciani, L. Távara, E. Correa, F. París, BEM multiscale modelling involving micromechanical damage in fibrous composites, *Engineering Analysis with Boundary Elements* 93 (2018) 1–9. doi:10.1016/j.enganabound.2018.03.012.
- 505 [40] F. París, M. L. Velasco, E. Correa, Micromechanical study on the influence of scale effect in the first stage of damage in composites, *Composites Science and Technology* 160 (2018) 1–8. doi:10.1016/j.compscitech.2018.03.004.
- [41] Simulia, Providence, RI, USA, ABAQUS/Standard User’s Manual, Version  
510 6.12 (2012).
- [42] H. Zhang, M. Ericson, J. Varna, L. Berglund, Transverse single-fibre test for interfacial debonding in composites: 1. experimental observations, *Composites Part A: Applied Science and Manufacturing* 28 (4) (1997) 309–315. doi:10.1016/s1359-835x(96)00123-6.
- 515 [43] L. D. Stasio, J. Varna, Z. Ayadi, Energy release rate of the fiber/matrix interface crack in ud composites under transverse loading: debond-debond

and debond-free boundary interactions, submitted to Theoretical and Applied Fracture Mechanics.

- [44] G. Frossard, J. Cugnoni, T. Gmür, J. Botsis, Mode I interlaminar fracture of carbon epoxy laminates: Effects of ply thickness, *Composites Part A: Applied Science and Manufacturing* 91 (2016) 1–8. doi:10.1016/j.compositesa.2016.09.009.
- [45] Z. Hashin, Analysis of composite materials—a survey, *Journal of Applied Mechanics* 50 (3) (1983) 481. doi:10.1115/1.3167081.
- [46] R. Christensen, K. Lo, Solutions for effective shear properties in three phase sphere and cylinder models, *Journal of the Mechanics and Physics of Solids* 27 (4) (1979) 315–330. doi:10.1016/0022-5096(79)90032-2.
- [47] F. París, E. Correa, V. Mantič, Kinking of transversal interface cracks between fiber and matrix, *Journal of Applied Mechanics* 74 (4) (2007) 703. doi:10.1115/1.2711220.
- [48] I. García, V. Mantič, E. Graciani, Debonding at the fibre–matrix interface under remote transverse tension. one debond or two symmetric debonds?, *European Journal of Mechanics - A/Solids* 53 (2015) 75–88. doi:10.1016/j.euromechsol.2015.02.007.