

Energy release rate of fiber/matrix interface crack growth in cross-ply laminates under transverse loading: effect of the $0^\circ/90^\circ$ interface and of 0° layer thickness

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Abstract

Models of Representative Volume Elements (RVEs) of cross-ply laminates with different geometric configurations and damage states are studied. Debond growth is characterized by the estimation of the Mode I and Mode II Energy Release Rate (ERR) using the Virtual Crack Closure Technique (VCCT). It is found that the presence of the $0^\circ/90^\circ$ interface and the thickness of the 0° layer have no effect, apart from laminates with *ultra-thin* 90° plies where it is however modest. The present analysis support the claim that debond growth is not affected by the ply-thickness effect.

Keywords: Polymer-matrix Composites (PMCs), Fibre/matrix bond, Debonding, Finite Element Analysis (FEA)

1. Introduction

Since the development of the *spread tow* technology or “FUKUI method” [1], significant efforts have been directed toward the characterization of *thin-ply* laminates [2, 3, 4, 5, 6, 7, 8, 9, 10, 11] and their application to mission-critical structures in the aerospace sector [12].

At the lamina level, the use of *thin-ply*s leads to more regular and homogeneous microstructures [6, 9]. Measurements of ply level properties (tensile and compressive modulus, Poisson’s ratio, ultimate tensile strength, tensile onset of damage, interlaminar shear strength) on Uni-Directional (UD) specimens ($[0_m^\circ]$

10 and $[90_m^\circ]$) revealed no remarkable difference with average properties available in
 the literature for the same type of fiber, nor showed any particular dependence
 on the ply thickness [9]. Only an increase of the ultimate compressive strength
 in the fiber direction was observed with very thin plies (~ 4 fiber diameters),
 although with very scattered values. The authors claim the increase to be due
 15 to the fiber arrangement's increased regularity which prevents the onset of fiber
 microbuckling [9]. A number of researchers [2, 3, 4] has reported improvements
 in fatigue life with the use of *thin-ply*s, which are explained as a consequence of
 delayed propagation of free edge delaminations and intralaminar cracks. Several
 researchers have analyzed the effect of *thin-ply*s on damage development under
 20 static [3, 4, 5, 6, 7, 8, 9], fatigue [2, 3, 4, 5, 9] and impact loadings [3, 4, 5, 9]. It
 seems apparent that *thin-ply* laminates possess an increased ability to delay, and
 in some cases even suppress, the onset and propagation of intralaminar cracks
 (called often transverse or matrix or micro-cracks).

The first stage in the appearance of transverse cracks is known to be the occur-
 25 rence of fiber/matrix interface cracks (also referred to as debonds), which grow
 along the fiber arc direction, then kink out of the interface and coalesce forming
 a transverse crack [13]. Different approaches have been applied to model the
 initiation and growth of debonds. The Cohesive Zone Model (CZM) has been
 used to mimic the propagation of debonds along fiber interfaces; coupled with
 30 a failure criterion for the matrix, it has provided simulations of the growth of
 transverse cracks starting from a virgin material [14, 15, 16, 17]. The main
 advantages of this approach are the possibility to observe the development of
 a simulated crack path and to record a load-displacement curve to compare
 with experimental measurement. However, various observations cast a doubt
 35 about the applicability of the CZM: the bi- (for 2D models) and tri- (in 3D)
 axiality of the matrix stress state in the inter-fiber region that is linked with a
 cavitation-like failure of the polymer [18]; the locality and mode dependency of
 the interface failure [19]; the problematic use at the microscopic level of prop-
 erties measured in UD specimens at the laminate level [15]. A second approach
 40 that obviates these drawbacks is the application of Linear Elastic Fracture Me-

chanics (LEFM) arguments to the study of debond growth. The analysis focuses
 on the evaluation of Mode I and Mode II Energy Release Rate (ERR) at the
 crack tip by means of the Virtual Crack Closure Technique (VCCT) [20] or
 the J-Integral method [21]. The stress and strain field, required for the ERR
 45 computation, can be solved by application of different methodologies such as
 analytical solutions [22], the Boundary Element Method (BEM) [23] or the Fi-
 nite Element Method (FEM) [24]. This approach presents nonetheless some
 limitations: it describes propagation of the debond and not its initiation; the
 role of friction in the contact zone is still an open issue; consensus is still lack-
 50 ing on a proper criterion for crack propagation in mixed mode. Finite fracture
 mechanics [25] is one way to address the initiation problem. Different studies
 have followed the LEFM approach and analyzed models of one or two fibers
 in an effectively infinite matrix [26, 27, 28, 29, 30] and of an hexagonal clus-
 ter of fibers in an effectively infinite homogenized UD composite [31, 24]. The
 55 problem of debond growth along the fiber-matrix interface in a cross-ply lam-
 inate has been only addressed very recently in [32, 33], where authors embed
 a single partially debonded fiber in an effectively infinite homogenized 90° ply
 bounded by homogenized 0° layers. Thus, the effect of debond-debond inter-
 action and of the relative proximity of a $0^\circ/90^\circ$ interface on debond ERR in
 60 cross-ply laminates is yet to be addressed. The present work is devoted to this
 problem. Models of Repeating Unit Cells (RUCs) are developed to represent
 laminates with different degrees of damage in the 90° ply (here only in the form
 of debonds). The number of fully bonded fibers across the thickness of the 90°
 ply is varied in order to investigate the effect of the proximity of the $0^\circ/90^\circ$
 65 interface. The thickness of the bounding 0° layers is also used as a parameter
 of the study. The stress and strain fields are solved with the Finite Element
 Method in Abaqus [34] and the debond (crack) is characterized by its Mode I
 and Mode II ERR calculated with the VCCT.

2. RVE models & FE discretization

2.1. Introduction & nomenclature

In the present work, we investigate debond development under in-plane longitudinal tension in $[0_{m \cdot k \cdot 2L}^\circ, 90_{k \cdot 2L}^\circ, 0_{m \cdot k \cdot 2L}^\circ]$ laminates. The interaction between debonds in the presence of an interface with a stiff layer is studied with the use of different Repeating Unit Cells (RUCs) (see Figures 1 and 2 in Sec. 2.2), in which only the central fiber is partially debonded. Repetition of the composite RUC occurs along the in-plane laminate 0° -direction (corresponding to specimen axial direction and RUC horizontal direction in Figures 1 and 2), thus representing a cross-ply laminate with a thin or even ultra-thin 90° ply in the middle.

All the RUCs present regular microstructures with fibers placed according to a square-packing configuration characterized by the repetition of the same one-fiber unit cell of size $2L \times 2L$, where L is a function of the fiber volume fraction V_f and the fiber radius according to

$$L = \frac{R_f}{2} \sqrt{\frac{\pi}{V_f}}. \quad (1)$$

Each fiber in the model has the same radius R_f , equal to $1 \mu m$. This specific value has no physical meaning per se and it has been selected for simplicity. It is useful to observe that, in a linear elastic solution as the one described in the present article, the ERR is proportional to the geometrical dimensions of the model and thus re-evaluation of the ERR for fibers of any size requires just a multiplication. Furthermore, it is worth to point out that V_f is the same in the one-fiber unit and in the overall RUC, i.e. no clustering of fibers is considered. The thickness of the 90° ply depends on the number k of fiber rows present across the thickness (the vertical or z direction in Figures 1 and 2) according to

$$t_{90^\circ} = k \cdot 2L. \quad (2)$$

On the other hand, the thickness of 0° layers can be assigned freely as a multiple of the 90° ply thickness as

$$t_{0^\circ} = m \cdot t_{90^\circ} \quad (3)$$

95 where m is an arbitrary integer. Thus, the thickness ratio m represents one additional parameter for the investigation.

In the following, let us consider in-plane coordinates x and y , and assume that the laminate 0° -direction is aligned with the x -axis. In the presence of a load in the x -direction, the strain in the y -direction is small, due to the very small
100 Poisson's ratio of the laminate. Debonds are present only in the 90° layer and are considered to be significantly longer in the fiber direction than in the arc direction [35]. Therefore we use 2D models under the assumption of plane strain, defined in the $x - z$ section of the composite. The study presented in this paper thus applies to long debonds and its focus is on understanding the mechanisms
105 of growth along their arc direction. The laminates are assumed to be subject to tensile strain, which is applied in the form of a constant displacement in the x -direction along both vertical boundaries of the RUC as shown in Figure 3.

We assume damage to be present only in the central “row” of fibers of the 90° layer in the form of multiple debonds appearing at different regular intervals
110 along the loading (horizontal) direction. The number of fibers n present in the horizontal direction of the RUC (Figures 1 and 2) controls the distance, in terms of fully bonded fibers, between consecutive debonds: if the RUC has n fibers in the horizontal direction, two consecutive debonds are separated by $n - 1$ undamaged fibers. The RUCs considered are thus Representative Volume
115 Elements (RVEs) of cross-ply laminates with a certain distribution of debonds in the middle 90° layer.

In summary, the models are differentiated by: first, the spacing between debonds along the horizontal direction in the 90° layer, which corresponds to the number n of fibers in the RUC's horizontal direction; second, the thickness of the middle
120 90° ply measured in terms of the number k of fiber rows in the vertical direction; third, the factor m which provides the thickness of 0° layers as a multiple of the 90° ply thickness. It thus seems natural to introduce a common notation

for the RUCs as $n \times k - m \cdot t_{90^\circ}$.

An additional family of RUCs is considered to study the effect of equivalent
125 boundary conditions, which is constituted by only one partially debonded fiber.
Homogenized 0° layers are not present. The application of coupling of horizontal
displacements u_x along the right and left sides allows for repetition along the
horizontal direction. When the upper boundary of the RUC is left free, we
define the $1 \times 1 - free$ model. If coupling of the vertical displacements u_z is
130 applied to the upper boundary, we define instead the $1 \times 1 - coupling$ model. In
the case a linear distribution of the horizontal displacement u_x is applied to the
upper boundary, the model is referred to as $1 \times 1 - H$. Finally, when the linear
distribution of the horizontal displacement u_x is superimposed to the condition
of coupling of the vertical displacements u_z on the upper boundary, we have
135 the $1 \times 1 - coupling + H$. Further details about this family of RUCs and the
corresponding laminate RVE can be found in [36].

2.2. Description of modelled Representative Volume Elements (RVEs)

The first family of Representative Volume Elements (RVEs) is represented
in Figure 1. It represents a set of $[0_{m \cdot k \cdot 2L}^\circ, 90_{k \cdot 2L}^\circ, 0_{m \cdot k \cdot 2L}^\circ]$ laminates with an
140 ultra-thin 90° layer, constituted by a single row of fibers across the thickness.
Debonds appear at regular intervals measured in terms of number $n - 1$ of fully
bonded fibers present between them, which in turn correspond to the number
of fibers along the horizontal direction of the RVE as highlighted in Fig. 1.
They are thus the $n \times 1 - m \cdot t_{90^\circ}$ models, where $m = 1, 10$ and n is an integer
145 ≥ 1 ($n = 1$ corresponds to the case of a debond appearing on all the fibers in
the central 90° layer). These models are geometrically extreme, but allow to
focus on the interaction between debonds and the inter-ply $0^\circ/90^\circ$ interface.
Furthermore, the *spread tow* technology is today capable of producing cross-ply
laminates with the central 90° layer thickness only 4–5 times the fiber diameter,
150 as shown for example in [6], which may in future give practical relevance even
to such extreme case.

The second set of models considers instead cross-ply laminates with a central

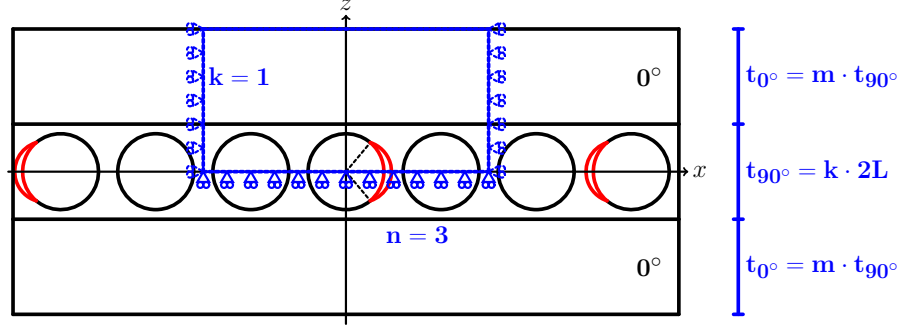


Figure 1: Models of $[0^{\circ}_{m \cdot k \cdot 2L}, 90^{\circ}_{k \cdot 2L}, 0^{\circ}_{m \cdot k \cdot 2L}]$ laminates with an ultra-thin 90° layer, where the 90° ply is made up by a single “row” of fibers. Debonds are repeating at different distances, measured in terms of the number $n-1$ of fully bonded fibers appearing between two consecutive debonds. $2L$ is the thickness of one-fiber row.

90° ply of variable thickness, measured in terms of number k of fiber rows “stacked” in the vertical direction in Figure 2. Once again, debonds appear in the central row only at regular intervals measured in terms of number $n - 1$ of fully bonded fibers present between them, as highlighted in Fig. 2. These models are thus the $n \times k - m \cdot t_{90^{\circ}}$ models, where $m = 1, 10$, $k > 1$ and n is an integer ≥ 1 ($n = 1$ corresponds to the case of a debond appearing on all fibers of the central fiber row in the 90° layer).

By increasing the number n of fibers in the horizontal direction in the RUC, decreasing levels of damage (debonds spaced further apart and the interaction between debonds becomes less important) are considered to be present in the laminate. By increasing the number k of fiber rows, the thickness of the 90° layer is increased and the effect of the relative proximity of the inter-ply $0^{\circ}/90^{\circ}$ interface can thus be studied. Finally, by increasing the factor m , the thickness of the 0° layers is increased for a given thickness of the 90° , which allows the investigation of the 0° ply-block effect [37].

2.3. Finite Element (FE) discretization

The RUCs are discretized and solved with the Finite Element Method (FEM) using the commercial FEM package Abaqus [34]. The total length and height

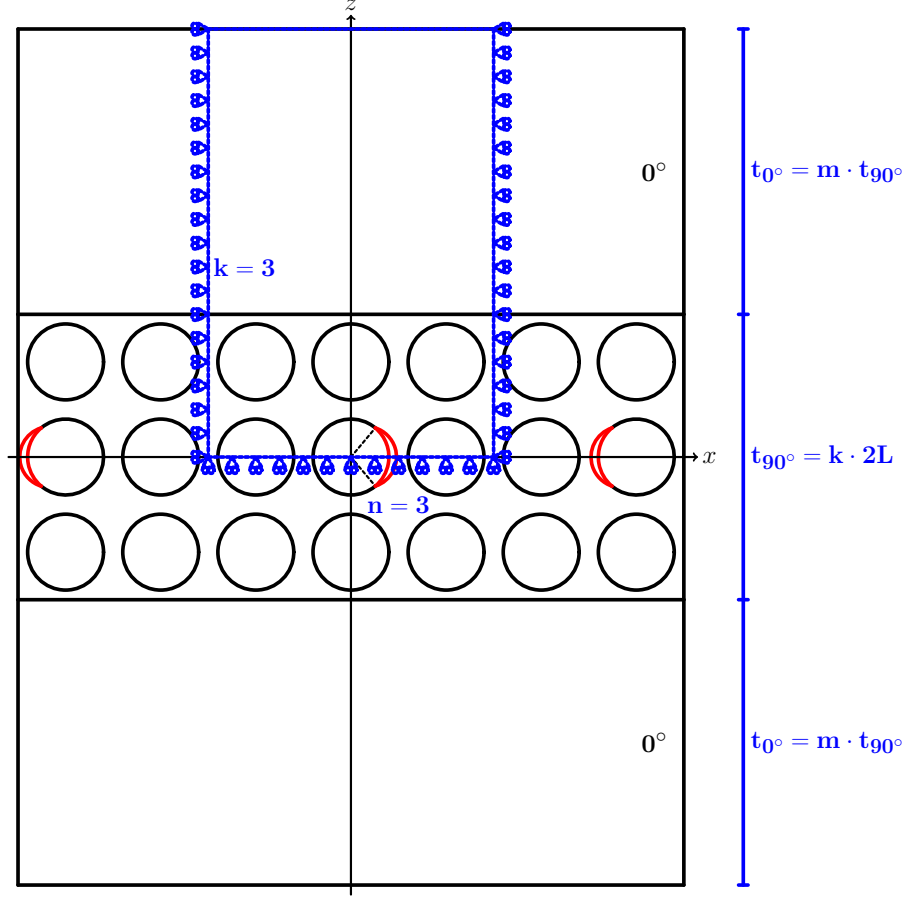


Figure 2: Models of $[0_{m \cdot k \cdot 2L}^\circ, 90_{k \cdot 2L}^\circ, 0_{m \cdot k \cdot 2L}^\circ]$ laminates with a 90° layer of variable thickness, determined by the number k of “rows” of fibers along the vertical direction. Debonds are repeating at different distances along the horizontal direction, measured in terms of the number $n - 1$ of fully bonded fibers appearing between two consecutive debonds. $2L$ is the thickness of one-fiber row.

of a RUC are determined by the number of fibers n in the horizontal direction, the number of fiber rows k across the thickness and the thickness ratio m (see Sec. 2.1 and Sec. 2.2).

The debond appears symmetrically with respect to the x axis (see Fig. 3) and we characterize it with the angular size $\Delta\theta$ (the full debond size is thus $2\Delta\theta$). In the case of large debond sizes ($\geq 60^\circ - 80^\circ$), a region of size $\Delta\Phi$ to be

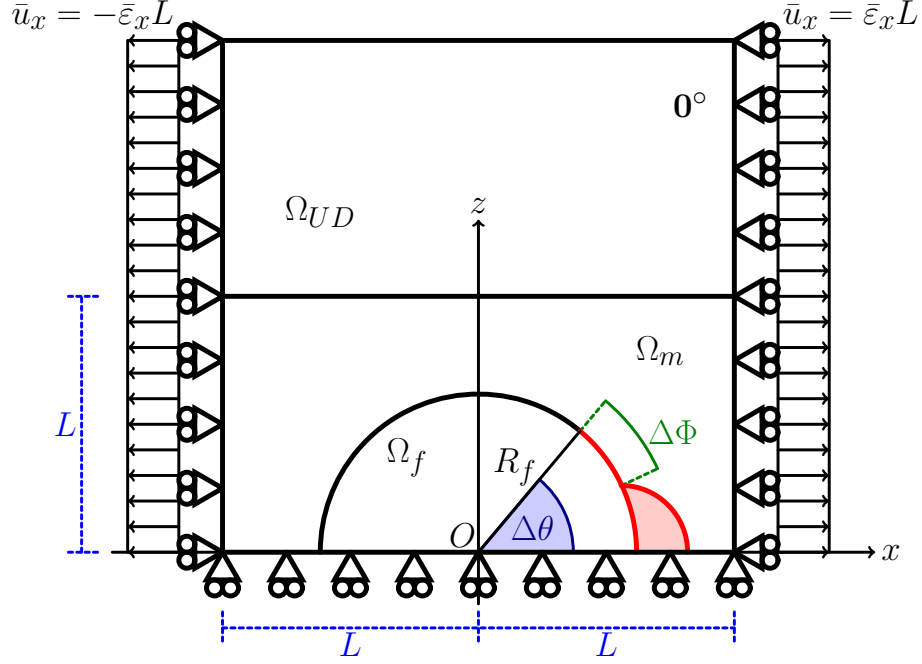


Figure 3: Schematic of the model with its main parameters.

determined by the solution itself appears at the crack tip. In this region, called the *contact zone*, the crack faces are in contact and slide on each other. Due to existence of the contact zone, frictionless contact is considered between the two crack faces to avoid interpenetration and allow free sliding. Symmetry with respect to the x axis is applied on the lower boundary. Kinematic coupling on the x -displacement is applied along the left and right boundaries of the model in the form of a constant x -displacement $\pm \bar{\varepsilon}_x l$, corresponding to transverse strain $\bar{\varepsilon}_x$ equal to 1%.

Table 1: Summary of mechanical properties of fiber, matrix and UD layer.

| Material | V_f [%] | E_L [GPa] | E_T [GPa] | G_{LT} [GPa] | ν_{LT} [-] | ν_{TT} [-] |
|-------------|-----------|-------------|-------------|----------------|----------------|----------------|
| Glass fiber | - | 70.0 | 70.0 | 29.2 | 0.2 | 0.2 |
| Epoxy | - | 3.5 | 3.5 | 1.25 | 0.4 | 0.4 |
| UD | 60.0 | 43.442 | 13.714 | 4.315 | 0.273 | 0.465 |

185 The FEM model is discretized using second order, 2D, plane strain triangular
 (CPE6) and rectangular (CPE8) elements. In the crack tip neighborhood, a
 refined regular mesh of quadrilateral elements with almost unitary aspect ratio
 is needed to ensure a correct evaluation of the ERR. The angular size δ of an
 element in this refined region close to the crack tip is by design equal to 0.05° .
 190 The crack faces are modeled as element-based surfaces with a frictionless small-
 sliding contact pair interaction. The Mode I, Mode II and total Energy Release
 Rates (ERRs) (respectively G_I , G_{II} and G_{TOT}) represent the main result of
 the numerical analysis. They are computed using the VCCT [20] implemented
 in a custom Python routine. Glass fiber and epoxy are considered throughout
 195 this article, and it is assumed that their response always lies in the linear elastic
 domain. The effective UD properties are computed using Hashin's Concentric
 Cylinder Assembly model [38] with the self-consistency scheme for the out-of-
 plane shear modulus of Christensen [39]. The properties used are listed in
 Table 1. The model was validated with respect to BEM results of [40, 29];
 200 considerations about the order of accuracy can be found in [36].

3. Results & Discussion

3.1. *Effect of the proximity of the $0^\circ/90^\circ$ interface and of the thickness of the 0° layer on debond ERR*

We first focus our attention on the model $1 \times 1 - m \cdot t_{90^\circ}$, which represents
 205 a particular case of the family $n \times 1 - m \cdot t_{90^\circ}$. It corresponds to a cross-
 ply laminate in which the central 90° ply is constituted by only one fiber row,
 in which each fiber possesses a debond appearing on alternating sides. The
 model thus represents an extreme idealization, in the sense that: first, the
 central 90° layer is the thinnest that can be conceived, which allows us to
 210 investigate the direct effect of the proximity of the $0^\circ/90^\circ$ interface on debond
 ERR; second, a very particular damage state is present for which every fiber
 is partially debonded from the surrounding matrix, corresponding to the most
 severe damage state that can occur in the 90° ply when considering debonds as

the only mechanism of damage. We are thus focusing on the presence of the
 215 $0^\circ/90^\circ$ interface and on the thickness of the 0° layer, by considering the ratio
 $m = \frac{t_{0^\circ}}{t_{90^\circ}}$ of ply thicknesses as a free parameter.

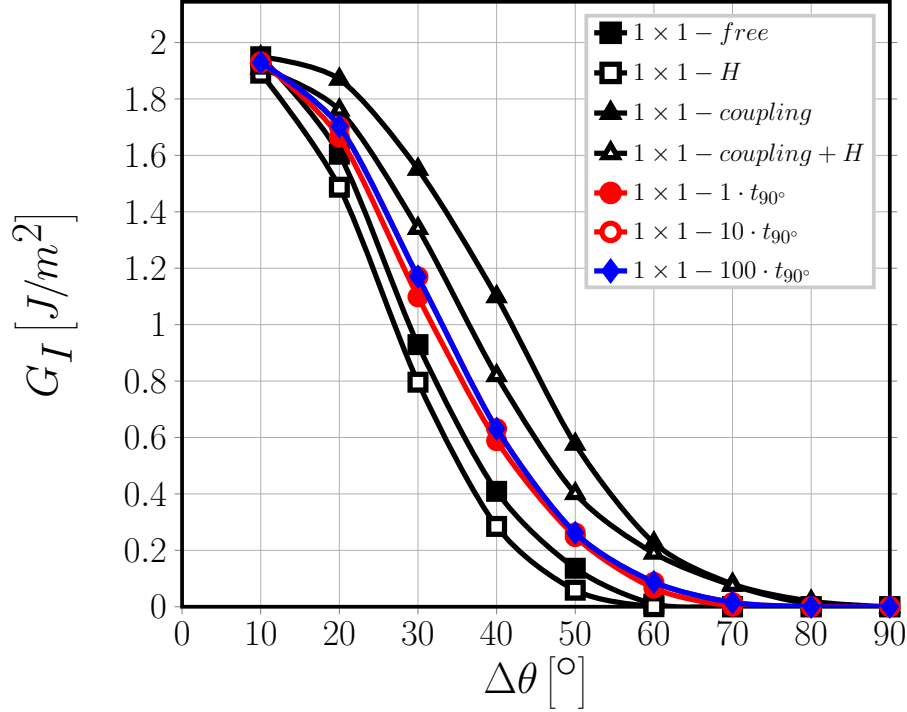


Figure 4: Effect of the proximity of the $0^\circ/90^\circ$ interface and of the thickness of the 0° layer on Mode I ERR: models $1 \times 1 - free$, $1 \times 1 - H$, $1 \times 1 - coupling$, $1 \times 1 - coupling + H$ and $1 \times 1 - m \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

In Figures 4 and 5 it is possible to observe respectively the Mode I and Mode
 II ERR for models $1 \times 1 - m \cdot t_{90^\circ}$ with $m = 1, 10, 100$. Mode I ERR is practically
 unaffected by the 0° layer thickness, only a marginal increase $\leq 1\%$ can be seen
 220 when m is increased from 1 to 10. No further observable change is present when
 m is increased to 100. Moreover, the contact zone onset, which corresponds to
 the first value of $\Delta\theta$ such that $G_I = 0$, is always equal to 70° irrespective of
 the value of m . A more remarkable, albeit small, effect of the 0° layer thickness
 can be observed for Mode II when m is increased from 1 to values ≥ 10 . For

225 open cracks, i.e. when no contact zone is present and thus $\Delta\theta$ is smaller than 70° , increasing the 0° layer thickness causes a reduction of Mode II ERR; while for closed cracks, when a contact zone is present and $\Delta\theta > 70^\circ$, the increase in thickness leads to an increase in ERR.

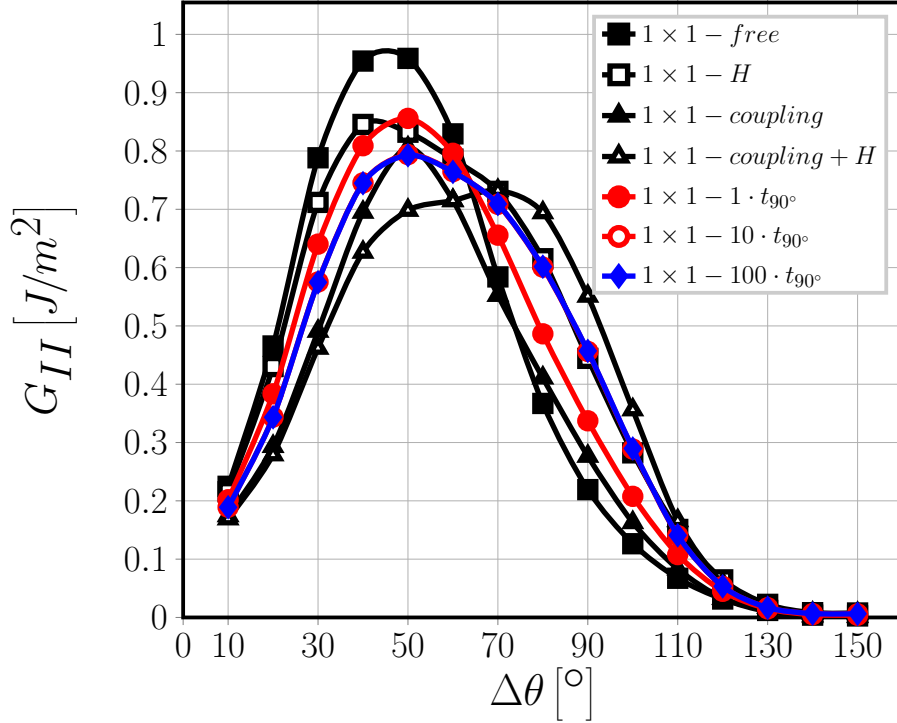


Figure 5: Effect of the proximity of the $0^\circ/90^\circ$ interface and of the thickness of the 0° layer on Mode II ERR: models $1 \times 1 - free$, $1 \times 1 - H$, $1 \times 1 - coupling$, $1 \times 1 - coupling + H$ and $1 \times 1 - m \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

230 In order to understand the interaction mechanism between the $0^\circ/90^\circ$ interface and the debond, Mode I and Mode II ERR are reported respectively in Figures 4 and 5 for models $1 \times 1 - free$, $1 \times 1 - H$, $1 \times 1 - coupling$ and $1 \times 1 - coupling + H$. These RUCs all present equivalent boundary conditions and it is here useful to recall their characteristics: in model $1 \times 1 - free$ the upper boundary is left free; coupling conditions on the vertical displacements u_z are applied to the upper boundary in model $1 \times 1 - coupling$; in model

$1 \times 1 - H$ a linearly distributed horizontal displacement u_x is applied to the upper boundary; in model $1 \times 1 - coupling + H$ coupling conditions on the vertical displacements u_z and a linearly distributed horizontal displacement u_x are imposed together on the upper boundary.

240 Observing Figure 4, it is possible to notice that the values of G_I for the $1 \times 1 - free$ and the $1 \times 1 - coupling$ models represent respectively a lower and an upper bound for the $1 \times 1 - m \cdot t_{90^\circ}$ RVEs: this is true with respect to the value of G_I as well as of contact zone onset (60° for $1 \times 1 - free$, 70° for $1 \times 1 - m \cdot t_{90^\circ}$, 80° for $1 \times 1 - coupling$). When a linearly distributed horizontal displacement u_x is
 245 applied to the upper boundary, providing the $1 \times 1 - H$ and $1 \times 1 - coupling + H$ models from the $1 \times 1 - free$ and the $1 \times 1 - coupling$ models, G_I decreases with respect to the “parent” models while the value of $\Delta\theta$ at contact zone onset remains unchanged (60° for $1 \times 1 - free$ and $1 \times 1 - H$, 80° for $1 \times 1 - coupling$ and $1 \times 1 - coupling + H$). Moreover, it is possible to observe that the values
 250 of G_I of $1 \times 1 - coupling + H$ are much closer to but always greater than those of $1 \times 1 - m \cdot t_{90^\circ}$ RVEs, thus constituting a more representative upper bound for the latter.

Analogous considerations can be drawn with regard to Mode II (see Fig. 5). For small debonds, $\Delta\theta \leq 30^\circ$, no significant difference in G_{II} can be seen between
 255 $1 \times 1 - free$ and $1 \times 1 - H$ and between $1 \times 1 - coupling$ and $1 \times 1 - coupling + H$. With respect to $1 \times 1 - m \cdot t_{90^\circ}$ RVEs, the first pair ($1 \times 1 - free$ and $1 \times 1 - H$) represents the lower bound while the second pair ($1 \times 1 - coupling$ and $1 \times 1 - coupling + H$) the upper bound. For $30^\circ < \Delta\theta \leq 60^\circ$, $1 \times 1 - H$ and $1 \times 1 - coupling + H$ provide significantly lower values of G_{II} than respectively
 260 $1 \times 1 - free$ and $1 \times 1 - coupling$. G_{II} values of $1 \times 1 - H$ are very close to $1 \times 1 - m \cdot t_{90^\circ}$, even coincident for $\Delta\theta = 60^\circ$. On the other hand, G_{II} values of $1 \times 1 - coupling$ are very close to $1 \times 1 - m \cdot t_{90^\circ}$ with $m \geq 10$ and even coincident for $\Delta\theta = 50^\circ$. For $60^\circ < \Delta\theta \leq 110^\circ$, the situation changes. $1 \times 1 - free$ and $1 \times 1 - coupling$ provides values of G_{II} close to each other, even coincident for
 265 $\Delta\theta = 70^\circ$. values of G_{II} of $1 \times 1 - H$ and $1 \times 1 - coupling + H$ are significantly larger than both $1 \times 1 - free$ and $1 \times 1 - coupling$. Furthermore, G_{II} values of

$1 \times 1 - H$ coincide with those of $1 \times 1 - m \cdot t_{90^\circ}$ with $m \geq 10$. Mode II ERR of $1 \times 1 - 1 \cdot t_{90^\circ}$ is instead close, but not coincident, to that of $1 \times 1 - coupling$. For $\Delta\theta > 110^\circ$, G_{II} is the same for all models and reaches 0 at a debond size of around 130° , showing that no further growth is possible for such large debonds. These results help to understand the effect of the $0^\circ/90^\circ$ interface on debond ERR. The presence of the stiff homogenized 0° layer causes the matrix placed relatively far from the fiber (close to the interface) to contract much less than it would do in the presence of a free surface due to its relatively high Poisson's ratio. Furthermore, the presence of the $0^\circ/90^\circ$ interface induces a more homogeneous x -displacement field all over the matrix domain. For small debonds ($\Delta\theta < 60^\circ - 70^\circ$), it causes a concurrent increase of G_I and decrease of G_{II} . For small debonds in fact, the Crack Opening Displacement at the crack tip

$$COD \sim \cos(\Delta\theta)u_x + \sin(\Delta\theta)u_z, \quad (4)$$

which governs Mode I according to

$$G_I = \lim_{\Delta a \rightarrow 0} \frac{1}{a} \int_a^{\Delta a} \sigma_I(\xi) COD(\xi) d\xi, \quad (5)$$

is mostly due to the global x -displacement field:

$$COD \sim \cancel{\cos(\Delta\theta)} \overset{\sim 1 \text{ for } \Delta\theta \rightarrow 0}{u_x} + \cancel{\sin(\Delta\theta)} \overset{\sim 0 \text{ for } \Delta\theta \rightarrow 0}{u_z}, \quad (6)$$

which increases in the presence of the $0^\circ/90^\circ$ interface. The Crack Sliding Displacement at the crack tip

$$CSD \sim -\sin(\Delta\theta)u_x + \cos(\Delta\theta)u_z, \quad (7)$$

which governs Mode II according to

$$G_{II} = \lim_{\Delta a \rightarrow 0} \frac{1}{a} \int_a^{\Delta a} \sigma_{II}(\xi) CSD(\xi) d\xi, \quad (8)$$

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is linked to the global vertical displacement field due to Poisson's effect:

$$CSD \sim \cancel{-\sin(\Delta\theta)} \xrightarrow{\sim 0 \text{ for } \Delta\theta \rightarrow 0} u_x + \cancel{\cos(\Delta\theta)} \xrightarrow{\sim 1 \text{ for } \Delta\theta \rightarrow 0} u_z \sim \nu u_x, \quad (9)$$

effect that is lower in the presence of a 0° layer instead of a free surface thanks to the stiffness of the former. This causes also the delay in the onset of the contact zone. For large debonds ($\Delta\theta > 60^\circ - 70^\circ$) instead, after the onset of the contact zone, the situation reverses:

$$COD \sim \cancel{\cos(\Delta\theta)} \xrightarrow{\sim 0 \text{ for } \Delta\theta \rightarrow 1} u_x + \cancel{\sin(\Delta\theta)} \xrightarrow{\sim 1 \text{ for } \Delta\theta \rightarrow 0} u_z \sim \nu u_x < 0, \quad (10)$$

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i.e. the faces are in contact, while

$$CSD \sim \cancel{-\sin(\Delta\theta)} \xrightarrow{\sim 1 \text{ for } \Delta\theta \rightarrow 0} u_x + \cancel{\cos(\Delta\theta)} \xrightarrow{\sim 0 \text{ for } \Delta\theta \rightarrow 0} u_z. \quad (11)$$

Thus, the increase in magnitude of the global x -displacement field leads to an increase in the crack sliding displacement component at the crack tip and thus in Mode II ERR.

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The local bending stiffness of the 0° ply seems also to be playing a role. In the presence of a free surface, the matrix in the 90° ply contracts significantly more than the fibers due to the mismatch in Poisson's ratios, thus leading to a higher overall contraction of the composite in the inter-fibers regions than above the fibers. This results in a very curved surface, which follows roughly the fibers' curvature. For small debonds ($\Delta\theta < 60^\circ - 70^\circ$), this translates into higher values of the vertical displacement field and thus an increase in Mode II ERR. For large debonds ($\Delta\theta > 60^\circ - 70^\circ$), the curvature of the material around the fiber corresponds to lower values of the horizontal displacement and thus a reduction of G_{II} . In the presence of a 0° layer, such deformation is prevented by the bending stiffness of the latter: Mode II ERR decreases for small debonds and increases for large ones. However, as a relatively thin 0° layer such as

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the one in $1 \times 1 - 1 \cdot t_{90^\circ}$ possesses a lower bending stiffness and thus matrix deformation is able to locally bend the interface, Mode II ERR presents a profile close to $1 \times 1 - H$ for small debonds (curved surface but more homogeneous x -displacement) and to $1 \times 1 - free$ for large ones (locally curved surface). For thicker 0° layers, the increased bending stiffness prevents the curvature of the interface and Mode II ERR becomes closer to $1 \times 1 - coupling$ for small debonds (reduced Poisson's effect) and to $1 \times 1 - H$ for large ones (increased horizontal displacement due to locally straight surface).

3.2. Effect of the proximity of the $0^\circ/90^\circ$ interface and of the thickness of the 0° layer on non-interactive debonds in a one-fiber row 90° ply

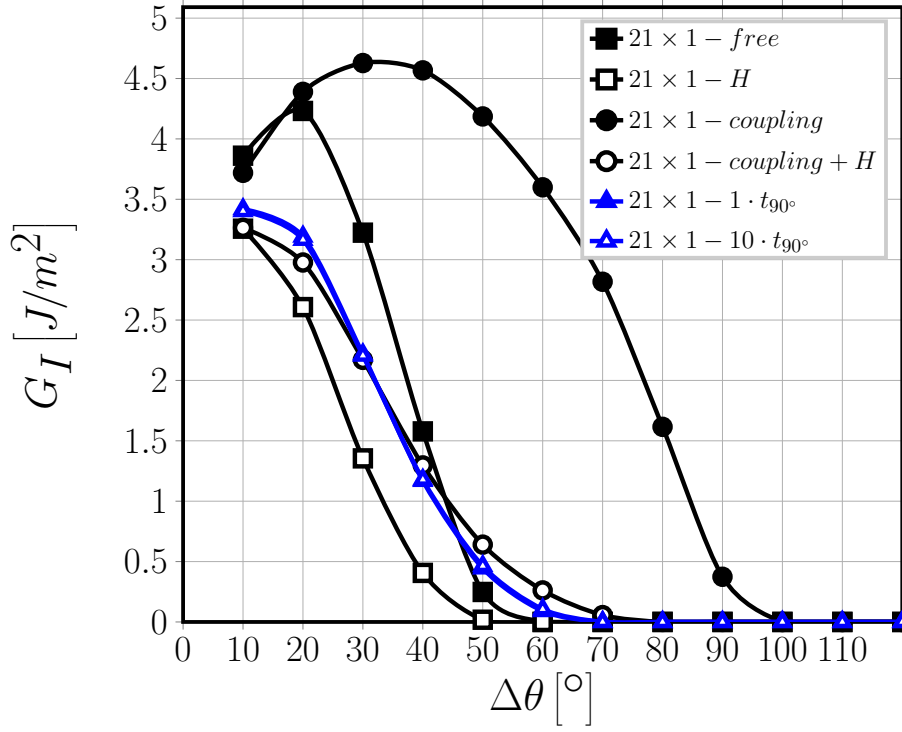


Figure 6: Effect of the presence of the 0° layer on Mode I ERR of non-interactive debonds: models $21 \times 1 - free$, $21 \times 1 - H$, $21 \times 1 - coupling$, $21 \times 1 - coupling + H$, $21 \times 1 - 1 \cdot t_{90^\circ}$ and $21 \times 1 - 10 \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

We turn now our attention to models $n \times 1 - m \cdot t_{90^\circ}$, which correspond to a

cross-ply laminate in which the central 90° ply is constituted by only one fiber row where multiple partially debonded fibers are present, located at a distance of $n - 1$ fully bonded fibers from each other, and debonds appear on alternating sides of consecutive damaged fibers (see Figure 1). This class of models allows to study the effect of the presence of the 0° layer and of its thickness on non-interactive debonds. As observed in a previous work [36], the presence of fully bonded fibers between partially debonded ones in the loading has a strong effect on debond ERR and controls the interaction between debonds. When n is increased, both Mode I and Mode II increase: the addition of stiffer elements, in the form of fully bonded fibers, increase the magnitude of the horizontal displacement field u_x at the crack tip and thus causes higher values of ERR (see Equations 4, 5, 7 and 8). When looked from this perspective, i.e. moving from the most to the least severe state of damage, this effect is referred to as “strain magnification” [36]. From the opposite perspective, from the least to most severe damage state, we talk about “crack shielding” [36, 41]: an increasing number of debonds correspond to an increasing number of discontinuities in the horizontal displacement field u_x , which causes a reduction of the magnitude of displacements and strains and thus of ERR. There seems to exist a characteristic distance, measured in terms of fully bonded fibers, above which a change in the number of undamaged fibers affects only marginally, or even not all, debond ERR. This distance, generally $n \sim 20$, marks the transition between a non-interactive solution ($n > 20$) and an interactive one ($n < 20$). The “strain magnification” effect thus represents the transition from the interactive to the non-interactive solution, while the “crack shielding” effect the transition from the non-interactive to the interactive solution. If in Sec. 3.1 we studied the effect of the proximity of the $0^\circ/90^\circ$ interface and of the thickness of the 0° layer on interactive debonds ($1 \times 1 - \dots$), we analyze in the present section the effect of the $0^\circ/90^\circ$ interface and of the 0° layer thickness on non-interactive debonds ($n \times 1 - \dots$ with $n > 20$).

Comparing Fig. 6 with Fig. 4 and Fig. 7 with Fig. 5, it is possible to observe how increasing the number of fully bonded fibers between consecutive debonds

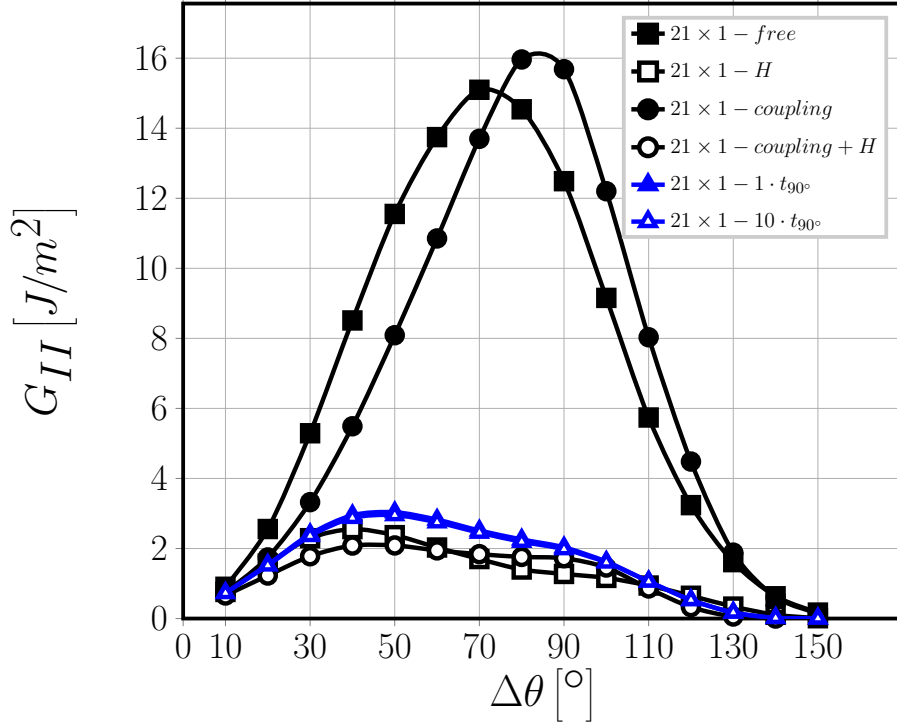


Figure 7: Effect of the presence of the 0° layer on Mode II ERR of non-interactive debonds: models $21 \times 1 - free$, $21 \times 1 - H$, $21 \times 1 - coupling$, $21 \times 1 - coupling + H$, $21 \times 1 - 1 \cdot t_{90^\circ}$ and $21 \times 1 - 10 \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

in the loading leads to an increase in Mode I and Mode II ERR. The peak G_I increases from $1.93 \left[\frac{J}{m^2} \right]$ in $1 \times 1 - 1 \cdot t_{90^\circ}$ to $3.42 \left[\frac{J}{m^2} \right]$ in $21 \times 1 - 1 \cdot t_{90^\circ}$, while the peak G_{II} from $0.86 \left[\frac{J}{m^2} \right]$ to $3.04 \left[\frac{J}{m^2} \right]$. The value of $\Delta\theta$ at contact zone onset remains instead the same (70°).

The effect of the 0° layer thickness is instead non-existent: values of both G_I and G_{II} are coincident for $21 \times 1 - 1 \cdot t_{90^\circ}$ and $21 \times 1 - 10 \cdot t_{90^\circ}$.

In agreement with the introductory considerations of this section and the results in [36], it is possible to observe in Figures 6 and 7 that $21 \times 1 - free$ and $21 \times 1 - coupling$, in which the horizontal displacement u_x is left unconstrained, show both the highest values of Mode I and Mode II ERR as well as the maximum increase with respect to the interactive case ($1 \times 1 - free$ and $1 \times 1 - coupling$).

When a linearly distributed horizontal displacement is applied to the upper
360 boundary, thus constraining the magnitude of the strain magnification effect,
both the values of Mode I and Mode II ERR as well as their increase with
respect to the interactive case are significantly reduced. Interestingly, $21 \times 1 -$
coupling + H represents, when considering both Mode I and Mode II ERR, the
best approximation to the results of $21 \times 1 - m \cdot t_{90^\circ}$ using equivalent boundary
365 conditions. The $0^\circ/90^\circ$ interface, by remaining straight (coupling conditions
on the vertical displacements) and controlling the magnitude of the horizontal
displacement (applied linearly distributed horizontal displacement), acts against
the strain magnification effect and reduces debond ERR. It seems reasonable
to conclude that debond growth is favored (i.e. higher ERR) in the presence of
370 strain or stress concentrations (as for example in the presence of a free surface
or only coupling conditions on the vertical displacement), while more uniform
strain and stress fields as those created by the proximity of the $0^\circ/90^\circ$ interface
reduce both Mode I and Mode II ERR and prevent debond growth.

3.3. *Effect of the presence of fiber rows with no damage on the debond- $0^\circ/90^\circ$ 375 interface interaction*

After having investigated the effect of the proximity of the $0^\circ/90^\circ$ interface
and of the thickness of the 0° layer on debond ERR for different cases of debond-
debond interaction in the same fiber row, we address in this section the effect
of the presence of fiber rows with only fully bonded fibers on the interaction
380 between debonds and the $0^\circ/90^\circ$ interface. In other words, we are separating
the debond from the $0^\circ/90^\circ$ interface by inserting rows of fully bonded fibers
in between, thus increasing the distance to the interface. We consider only the
case $m = 1$, i.e. $t_{0^\circ} = t_{90^\circ}$, given that increasing the 0° layer thickness does not
result in any remarkable effect on ERR as shown in Sec. 3.1 and Sec. 3.2.

385 Following the same philosophy of Sec. 3.1 and Sec. 3.2, we analyze the effect
of the presence of fiber rows with no damage on debond ERR: first, when the
central fiber row possesses only partially debonded fibers, representing the most
severe damage state for these RUCs and the solution for interactive debonds

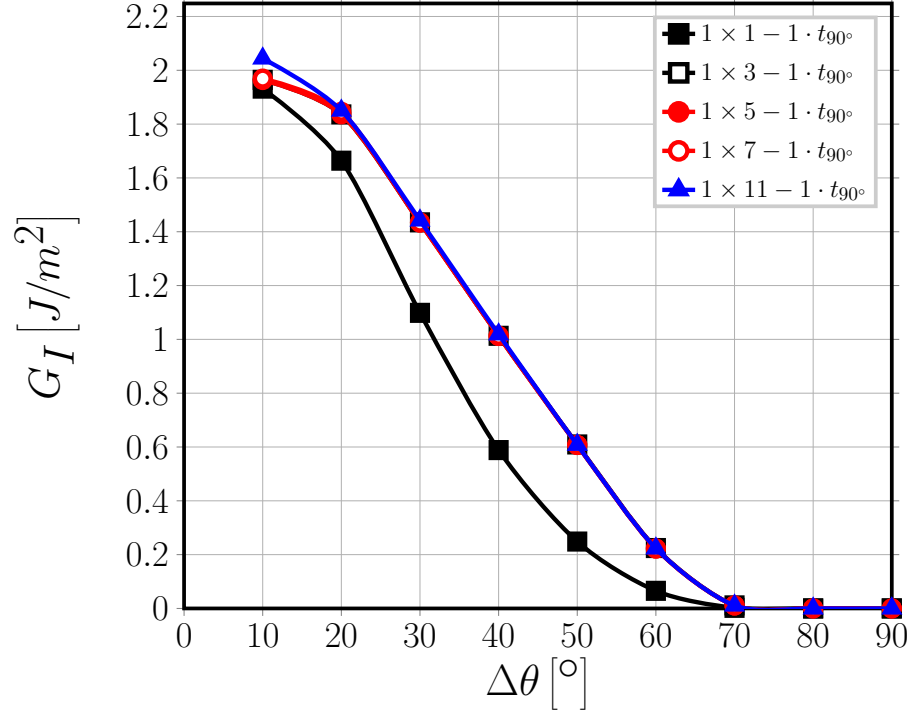


Figure 8: Effect of the presence of undamaged fiber rows in the 90° layer on debond- $0^\circ/90^\circ$ interface interaction for Mode I ERR: models $1 \times k - free$ and $1 \times k - 1 \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

(models $1 \times k - 1 \cdot t_{90^\circ}$ in Figures 8 and 9); afterwards, the case of debonds
 390 separated by fully bonded fibers in the central fiber row, corresponding to the
 least severe state of damage and to the solution for non-interactive debonds
 (models $21 \times k - 1 \cdot t_{90^\circ}$ in Figures 10 and 11).

Observation of Fig. 8, Fig. 9, Fig. 10 and Fig. 11 reveals that no difference
 can be seen in Mode I and Mode II ERR by increasing the number k of rows with
 395 undamaged fibers when $k \geq 3$, which means that debond ERR does not change
 once at least 1 row of undamaged fibers is present between the debond and the
 $0^\circ/90^\circ$ interface. A significant change is visible only when $k = 1$, which means
 that no row of fibers with no damage is present between the debond and the
 $0^\circ/90^\circ$ interface. This change, from $k \geq 3$ to $k = 1$, is in particular a reduction

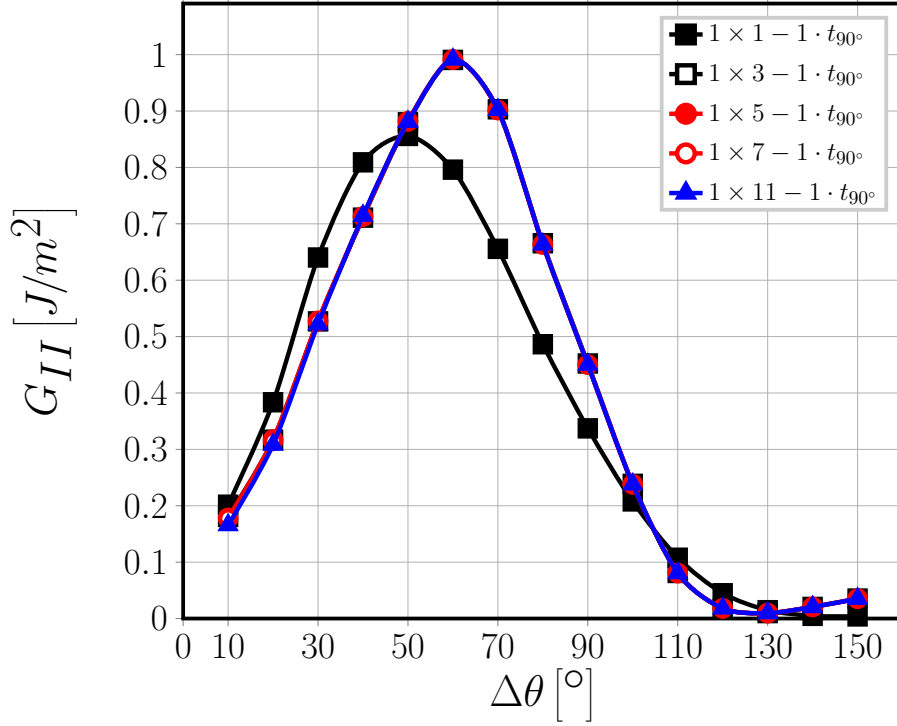


Figure 9: Effect of the presence of undamaged fiber rows in the 90° layer on debond- $0^\circ/90^\circ$ interface interaction for Mode II ERR: models $1 \times k - free$ and $1 \times k - 1 \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

of both G_I and G_{II} . The results of Figures 8, 9, 10 and 11 imply that the mechanisms of debond- $0^\circ/90^\circ$ interface interaction described in Sec. 3.1 and Sec. 3.2 are actually very localized and that debond ERR is affected by the presence of the $0^\circ/90^\circ$ interface only when no fully bonded fiber is placed in between. Given that the number k of fibers in the RUC vertical direction corresponds to the thickness of the 90° ply measured in terms of rows of fibers present through its thickness, the results here presented point to another conclusion: the ply-thickness effect does not seem to apply to debond growth, unless an *ultra-thin* ply constituted by only one fiber row ($k = 1$) is considered.

Analogous results can be found in [32, 33], where the authors investigate the ply-thickness effect on debond growth using: first, a single centrally-placed

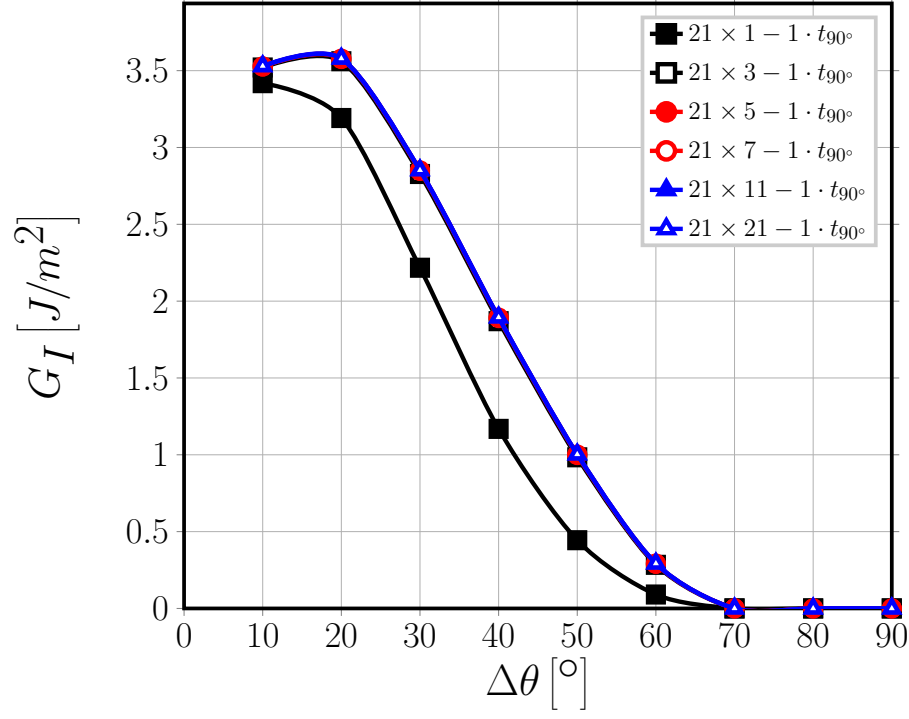


Figure 10: Effect of the presence of undamaged fiber rows in the 90° layer on debond- $0^\circ/90^\circ$ interface interaction for Mode I ERR: models $n \times k - free$ and $n \times k - 1 \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

partially debonded fiber with surrounding matrix corresponding to $V_f = 55\%$, embedded from all sides in a homogenized 90° ply bounded by homogenized 0° layers; second, one partially debonded fiber placed in the center and a second partially debonded fiber placed at an angle θ_2 with respect to the horizontal direction with surrounding matrix corresponding to $V_f = 55\%$, embedded from all sides in a homogenized 90° ply bounded by homogenized 0° layers. The thickness of the 0° layer is chosen as reference and a $[0_p^\circ, 90_{r,p}^\circ]_S$ laminate is considered. Carbon-epoxy and glass-epoxy systems are both studied. The thickness of the 90° ply, $t_{90^\circ} = r \cdot t_{0^\circ}$, varies from $r = 3$ (thick 90° ply, > 100 fiber diameters) to $r = 0.1$ (thin 90° ply, $\sim 4 - 5$ fiber diameters). No measurable ply-thickness effect is observed. Experimental support to the claim that the ply-thickness

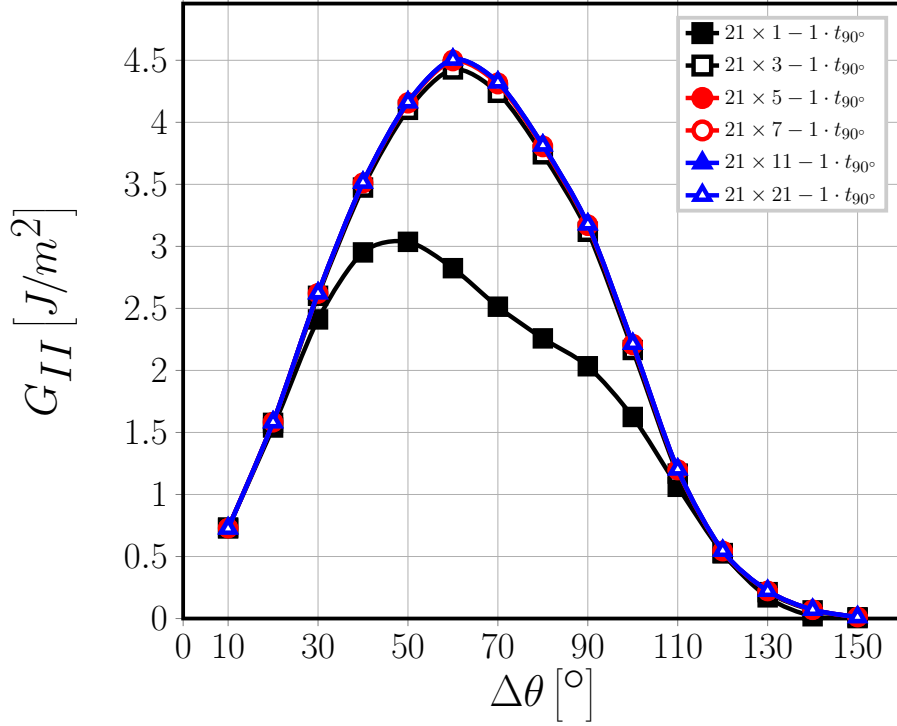


Figure 11: Effect of the presence of undamaged fiber rows in the 90° layer on debond- $0^\circ/90^\circ$ interface interaction for Mode II ERR: models $n \times k - free$ and $n \times k - 1 \cdot t_{90^\circ}$. $V_f = 60\%$, $\varepsilon_x = 1\%$.

effect has no influence on debond growth can be also found in the literature, in [6]. The authors conducted *in-situ* observations of edge micro-cracks with an optical microscope on $[0_2^\circ, 90_n^\circ, 0_2^\circ]$ carbon fiber-epoxy laminates with $n = 1, 2, 4$,
425 corresponding to a 90° ply thickness of respectively $40 [\mu m]$ ($\sim 6 - 8$ fiber diameters), $80 [\mu m]$ ($\sim 12 - 16$ fiber diameters) and $160 [\mu m]$ ($\sim 24 - 32$ fiber diameters). For $n = 1$, i.e. the case of a very thin 90° ply, isolated debonds appear at a lower value of the applied strain than in thicker plies (at 0.4% vs 0.7%) while coalescence of debonds is suppressed and no transverse crack can
430 be observed even at a strain of 1.5% . The ply-thickness effect was thus observed in [6] for transverse cracks, i.e. coalescence of debonds was delayed to higher strains and even suppressed, but not for debond growth. The analysis presented

in this article brings new arguments to the claim that the ply-thickness effect does not influence the growth of debonds.

435 4. Conclusions

Different models of Repeating Unit Cell, representing different cross-ply laminates, have been studied in order to study the effect of the presence of the 0° layer and of its thickness on debond Energy Release Rate for interactive and non-interactive debonds. In order to investigate the mechanisms of the debond-
440 $0^\circ/90^\circ$ interface interaction, Mode I and Mode II ERR of cross-ply RUCs are compared with those of RUCs with equivalent boundary conditions on the upper boundary: a free boundary; coupling conditions on the vertical displacements; an applied linear distribution of the horizontal displacement; coupling conditions on the vertical displacements superimposed to an applied linear distribution of
445 the horizontal displacement. It has been found that:

- by forcing the $0^\circ/90^\circ$ interface to remain approximately straight and controlling the magnitude of the horizontal displacements in the composite (and thus in the 90° ply), the presence of the 0° layer causes more homogeneous distributions of horizontal and vertical displacements, reducing
450 the ERR at the debond crack tip;
- the thickness of the 0° layer does not affect the Energy Release Rate, except for a marginal change when $t_{0^\circ} = t_{90^\circ}$ in the case of interactive debonds;
- no difference in ERR is seen when one or more rows of fibers with no
455 damage are present between the debond and the $0^\circ/90^\circ$ interface, a change is observed only no row of undamaged fibers is present between the debond and the $0^\circ/90^\circ$ interface;
- no effect of the 90° layer thickness, measured in terms of number k of rows of fibers, is observed when $k \geq 3$, a reduction in ERR takes place only
460 when the thickness is reduced to only one fiber row ($k = 1$).

The results reported in this article strengthen the claim that the ply-thickness effect does not influence the growth of debonds, as previously suggested in the literature [6, 17, 32, 33].

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