

SI 650/EECS 549 - Information Retrieval

Assignment 1 Solution

Due Sunday, Oct. 8th, 23:59 EDT.

Please submit as pdf attachment via Canvas.

General discussion encouraged, but everyone should come up with the solution independently. If you received help from anyone, you should list the name(s) on the top of your submission.

1. Document Ranking and Evaluation [20 points]

Suppose we have a query with **a total of 10 relevant documents** in a collection of 100 documents. A system has retrieved 16 documents whose relevance status is

[++, -, ++, -, +, +, -, -, ++, +, -, -, ++, -, +]

in the order of ranking. A + or ++ indicates that the corresponding document is relevant, while a - indicates that the corresponding document is non-relevant.

- A. [10 points] Compute the precision, recall, F_1 score, and the mean average precision (MAP).
- B. [10 points] Consider ++ as the corresponding document being highly relevant ($r_i = 2$), while + indicates somewhat relevant ($r_i = 1$), - being non-relevant ($r_i = 0$). For the two rest relevant documents, treat them as somewhat relevant ($r_i = 1$) Calculate the Cumulative Gain (CG) at rank 10, Discounted Cumulative Gain (DCG) at rank 10, and Normalized Cumulative Gain (NDCG), at rank 10. Use \log_2 for the discounting function.

Solution

A precision = $8/16 = 0.5$, recall = $8/10 = 0.8$, $F_1 = (2 * 0.5 * 0.8) / (0.5 + 0.8) = 8/13 = 0.615$, $MAP = [1 + (2/3) + (3/5) + (2/3) + (1/2) + (6/11) + (1/2) + (1/2)] / 10 = 0.498$

B $CG@10 = 2 + 0 + 2 + 0 + 1 + 1 + 0 + 0 + 0 + 2 = 8$

$DCG@10 = 2 + 2/\log_2(3) + 1/\log_2(5) + 1/\log_2(6) + 2/\log_2(10) = 4.681$

$IDCG@10 = 2 + 2/\log_2(2) + 2/\log_2(3) + 2/\log_2(4) + 1/\log_2(5) + 1/\log_2(6) + 1/\log_2(7) + 1/\log_2(8) + 1/\log_2(9) + 1/\log_2(10) = 8.385$

$NDCG@10 = 4.681/8.385 = 0.558$

2. Probabilistic Reasoning and Bayes Rule [40 points]

Alice lost her phone a week ago. When she finally got a new phone with a replaced SIM card, she found she got a thousand new messages, many of which are just spam. She wanted to filter out the spam. To her sadness, she lost the contacts as well and could not know which messages are from her friends.

Luckily, Alice attended SI650 and decided to filter the messages in a Bayesian way. She went through 12 messages and noted down 4 observations for each message in Table 1.

- (1) Y: whether the message is Spam (1 for yes, 0 for no);
- (2) H: whether the sender's number is local (1 for yes, 0 for no);
- (3) U: whether the message has an URL link (1 for yes, 0 for no);
- (4) L: whether the message is long (1 for having more than 40 characters, 0 otherwise).

Table 1: Sample observations of the messages

Y	H	U	L
1	1	1	1
1	1	1	0
1	1	1	0
0	1	0	0
0	1	1	1
1	0	1	0
1	0	1	1
0	0	0	0
0	0	1	0
0	0	1	1
0	0	0	0
1	1	0	0

Alice wants to build a filter with these observations. Now in terms of probabilistic reasoning, we can formulate the question as evaluating the conditional probability $P(Y \mid H, U, L)$, we say that the message is a spam if $P(Y = 1 \mid H, U, L) > P(Y = 0 \mid H, U, L)$. We make a further conditional independence assumption that $P(H, U, L \mid Y) = P(H \mid Y)P(U \mid Y)P(L \mid Y)$. In other words, we assume that if the status whether a message is a spam is known (i.e., value of Y is known), the values of H , U , and L would be independent to each other.

- A. [6 points] Fill in the following table (Table 2) with conditional probabilities using only the information present in the 12 samples.

Table 2: Conditional Probabilities and Prior

Y	$P(H = 1 \mid Y)$	$P(U = 1 \mid Y)$	$P(L = 1 \mid Y)$	prior $P(Y)$
1	0.667	?	?	?
0	?	?	?	0.5

- B. [8 points] With the independence assumption, use the Bayes formula and the calculated conditional probabilities to compute the probabilities that message M with $H = 0, U = 1, L = 0$ is a spam. That is, compute $P(Y = 1 \mid H = 0, U = 1, L = 0)$ and $P(Y = 0 \mid H = 0, U = 1, L = 0)$. Would you conclude that message M is a spam? Show your computation.
- C. [6 points] Now, compute $P(Y = 1 \mid H = 0, U = 1, L = 0)$ and $P(Y = 0 \mid H = 0, U = 1, L = 0)$ directly from the 12 examples in Table 1, just like what you did in problem A. Do you get the same value as in problem B? Why?
- D. [5 points] Now, ignore Table 1, and consider any possibilities you can fill in Table 2. Are there any constraints on these values that we must respect when assigning these values? In other words, can we fill in Table 2 with 8 arbitrary values between 0 and 1? If not, are there any constraints on some values that we must follow?
- E. [5 points] Can you change your conclusion of problem B (i.e., whether message M is a spam) by only changing the value H (i.e., if the message comes from a local number) in **one** example of Table 1?
- F. [5 points] Note that the conditional independence assumption $P(H, U, L \mid Y) = P(H \mid Y)P(U \mid Y)P(L \mid Y)$ helps simplify the computation of $P(H, U, L \mid Y)$. In particular, with this assumption, we can compute $P(H, U, L \mid Y)$ based on $P(H \mid Y)$, $P(U \mid Y)$, and $P(L \mid Y)$. If we were to specify the values for $P(H, U, L \mid Y)$ directly, what is the minimum number of probability values that we would have to specify in order to fully characterize the conditional probability distribution $P(H, U, L \mid Y)$? Why? Note that all the probability values of a distribution must sum to 1.
- G. [5 points] Explain why the independence assumption $P(H, U, L \mid Y) = P(H \mid Y)P(U \mid Y)P(L \mid Y)$ does not necessarily hold in reality.

Solution

A. Correct answer shown in Table 3. Bold numbers indicate values that the students need to fill.

Table 3: Conditional Probabilities and Prior

Y	$P(H = 1 Y)$	$P(U = 1 Y)$	$P(L = 1 Y)$	prior $P(Y)$
1	0.667	0.833	0.333	0.5
0	0.333	0.5	0.333	0.5

B.

$$\begin{aligned}
 & P(Y = 1 \mid H = 0, U = 1, L = 0) \\
 &= \frac{P(H = 0, U = 1, L = 0 \mid Y = 1)P(Y = 1)}{P(H = 0, U = 1, L = 0 \mid Y = 1)P(Y = 1) + P(H = 0, U = 1, L = 0 \mid Y = 0)P(Y = 0)} \\
 &= \frac{P(H = 0, U = 1, L = 0 \mid Y = 1)}{P(H = 0, U = 1, L = 0 \mid Y = 1) + P(H = 0, U = 1, L = 0 \mid Y = 0)} \\
 &= \frac{P(H = 0 \mid Y = 1)P(U = 1 \mid Y = 1)P(L = 0 \mid Y = 1)}{P(H = 0 \mid Y = 1)P(U = 1 \mid Y = 1)P(L = 0 \mid Y = 1) + P(H = 0 \mid Y = 0)P(U = 1 \mid Y = 0)P(L = 0 \mid Y = 0)} \\
 &= \frac{0.333 \times 0.833 \times 0.667}{0.333 \times 0.833 \times 0.667 + 0.667 \times 0.5 \times 0.667} = 0.455
 \end{aligned}$$

Similarly $P(Y = 0 \mid H = 0, U = 1, L = 0) = 0.545$. $P(Y = 1 \mid H = 0, U = 1, L = 0) < P(Y = 0 \mid H = 0, U = 1, L = 0)$, we conclude that M is not a spam.

C. Reading from the table, among 2 entries with $H = 0, U = 1, L = 0$, one has $Y = 1$ and one has $Y = 0$. Therefore, both $P(Y = 1 \mid H = 0, U = 1, L = 0)$ and $P(Y = 0 \mid H = 0, U = 1, L = 0)$ are 0.5. The calculation in (B) relies on the assumption of conditional independence, which may not hold.

D. $P(Y = 1) + P(Y = 0) = 1$

E. Changing one row with $Y = 1, H = 1$ to $Y = 1, H = 0$, or changing one row with $Y = 0, H = 0$ to $Y = 0, H = 1$ can change our conclusion.

F. We would need 14 values. (7 for $P(H, U, L \mid Y = 1)$ and 7 for $P(H, U, L \mid Y = 0)$.)

G. This is an open ended question. Answers are acceptable as long as they indicate that two attributes are associated. E.g. Messages with urls are usually longer.

3. Text Data Analyses [40 points]

In this exercise, we are going to get our hands dirty and play with some data in the wild. Download two collections from Canvas, `ehr.txt` and `medhelp.txt`. The first collection are sampled electronic health records (de-identified) released in TREC CDS 2016, with 90 documents in total. The second collection are sampled forum posts downloaded from MedHelp, with 180 documents in total. In both files, each line represents a document. You can also find a stopword list in `stoplist.txt`.

A handy toolkit is the NLTK package (<http://www.nltk.org/>). You may also choose other NLP toolkits.

(1) [10 points] Tokenize the text (e.g. use the `nltk.word_tokenize()` function in the NLTK package) and compute the frequency of words. Then, plot the frequency distribution of words in each collection after the removal of the stopwords: x-axis - word frequency (number of times a word appears in the collection); y-axis - proportion of words with this frequency. Plot the distributions on a log-log scale. Does each plot look like a power-law distribution? Are the two distributions similar or different?

(2) [15 points] Now compare the two collections more rigorously. Report the following properties of each collection. Can you explain these differences based on the nature of the two collections? (20 points) (You can use the `nltk.pos_tag()` function of the NLTK package for part of speech tagging.)

- (a) frequency of stopwords (percentage of the word occurrences that are stopwords.);
- (b) percentage of capital letters;
- (c) average number of characters per word;
- (d) percentage of nouns, adjectives, verbs, adverbs, and pronouns;
- (e) the top 10 nouns, top 10 verbs, and top 10 adjectives.

(3) [10 points] We would like to summarize each document with a few words. However, picking the most frequently used words in each document would be a bad idea, since they are more likely to appear in other document as well. Instead, we pick the words with the highest TF-IDF weights in each document.

In this problem, term frequency (TF) and inverse document frequency (IDF) are defined as:

$$TF(t, d) = \log(c(t, d) + 1)$$
$$IDF(t) = 1 + \log(N/k).$$

$c(t, d)$ is the frequency count of term t in doc d , N is the total number of documents in the collection, and k is the document frequency of term t in the collection.

For each of the first 10 documents in the EHR collection, print out the 5 words that have the highest TF-IDF weights.

(4) [5 points] As discussed in the class, TF-IDF is a common way to weight the terms in each document. It can also be easily calculated from the inverted index, since TF can be obtained from the postings and IDF can be summarized as a dictionary. Could you think of another weighting that cannot be calculated directly from inverted index? What is the advantage of such a weighting?

Hint 1: You can find a tutorial of `nltk.word_tokenize()` and `nltk.pos_tag()` in the NLTK book chapter 3 and 5: <http://www.nltk.org/book/ch03.html> and <http://www.nltk.org/book/ch05.html>. There is also a simple tutorial of NLTK at <http://www.slideshare.net/japerk/nltk-in-20-minutes>. Just use the simple, default settings.)

Hint 2: You may find a lot of decision to make: Should I lower-case the words? Should I use stemmer? What to do with the punctuations? There is not always right and wrong, different answers are accepted. But you should write down clearly how you process the data in each parts and explain your decisions.

Solution

- (1) Both plot should look like a power-law distribution and is similar. Notice that the x-axis or y-axis should be correctly marked in the log scale. The x-axis should marks 10, 100, 1000 (exponentially increasing number), etc.
- (2) Depending on different pre-processing, such as lowercasing all words, stemming, stopword removal, handling special tokens like punctuations and numbers, the exact answers might be different. However, students should not only report the numbers, but also compare and explain the difference.
 - (a) stopwords: EHR < Forum
 - (b) % of capital letters: EHR > Forum
 - (c) word length: EHR slightly larger than Forum
 - (d) EHR has more n., adj., less v., adv., and pron.

(e) lists may vary. Since POS tagging tools are not perfect, it is fine to have weird words or symbols in the list. (e.g. “[” categorized as noun.)

(4) The results I got are. It might vary depending on the pre-processes.

```
['melanotic', 'frank', 'nqwmi', 'quantity', 'readmitted']  
['snap', 'hip', 'leg', 'falling', 'arthroplasty']  
['hypotension', 'group', 'eventually', 'lightheadedness', 'regarding']  
['fracture', 'c2', 'fall', 'nursing', 'sustained']  
['statuspost', 'replacement', 'valve', 'bioprosthesis', 'atrial']  
['stools', 'stricture', 'pes', 'cramping', 'transfusion']  
['tests', 'quadrant', 'ascites', 'gtt', 'dark']  
['reglan', 'ago', 'menstrual', 'ivf', 'shot']  
['delivery', 'gm', 'labor', '678', 'magnesium']  
['ef', 'varices', 'dysfunction', 'cardiomyopathy', '55yo']
```

(4) Possible answers include:

- Weighting based on contextual information. A word may get more weight if it cooccur with certain words.
- Weighting based on topics (topic modeling). A word in the document that have similar meaning to a query word should get more weight since they are of the same topic.
- Weighting based on word embeddings. A word is first mapped to a high dimensional vector and then weighted according to its values on each of the dimension.