Dulton summary

Steps:

1) The model

$$kc+ = kc1_+ + kc2_+ \tag{3}$$

$$k_1' = k_1' + k_1' + k_2' + k_3' + k_4' + k_5' +$$

$$h_t = M_4 + h_4$$
 (5)

$$kc_{++1} = (1-dc)kc_{+} + iC_{+}$$
 (6)

$$P_{t} = P_{t}^{i} / P_{t}^{c} \tag{6}$$

growth rates Ye & Yi. Ass. Yi > 8c.

HHS max ln C+ - 2hr s.t. C+ + iC+ + ptitt = Wh+ + rC+kc+ + ri+kit Convert Hall-forgenson: rc+= r + de rit= [r+di-gp]P+ Pritt = Prkitty - (1-di) Prkit already in wints of cons! So the Lagrangian is L= ln 4- 2h+ + A. [- Ca - KC++1 - P+ kif+n + w+h+ + (rc++1-dc) kc+ + (ri+ (1-h) +) kif Foxs: $\frac{w_t}{c_t} = \chi$ 1 = BE+ C+ (1C++1+1-dc)

1-BE+ C+ P+1 (P+1 + 1- di)

GE: max Pyber hytab kely kily - with - replicit - nithit

FOLS

 $W_{t} = (1-a-b)bc_{t}hl_{t}^{-a-b}kcl_{t}^{a}kil_{t}^{b} \cdot P_{t}^{c}$ $rc_{t} = abc_{t}hl_{t}^{A-a-b}kcl_{t}^{a}kil_{t}^{b} \cdot P_{t}^{c}$ $ri_{t} = bbc_{t}hl_{t}^{A-a-b}kcl_{t}^{a}kil_{t}^{b} \cdot P_{t}^{c}$

they pay? I quess this one

Google max Ptbit 42+ 1-4-6 kc2+ ki2+ - wr 42-rake2+ - right

FOCS

W= (1-a-b) bir h2+ a-bkc2+ ki2+ pf 1-a-b kc2+ ki2+ pf 1-a-b kc2+ a-1 ki2+ pf

rit= 6. bit hzf-4-b xc2+ a ki2+ b-1 pf

Use P+ = P+ /P+ and let P+=1

W+= (1-a-b) bir h2+ a-bkc2+ ki2+ P+

12+ a bit h2+ 1-a-b ke 2+ a-1 ki2+ P+

rit= 6. bit hz 1-4-b xc2+ a kiz+ b-1 P+

Equilibrium conditions of the model:

$$kc_{+} = ke_{+} + kc_{+}$$
 (3)

$$h_t = M_t + h_{4}$$
 (5)

$$\frac{W_{+}}{G} = \chi \tag{6}$$

Denote by " a growth rates of a variable.

· Loms:
$$\frac{kc+n}{kc+} = (n-dc) + \frac{ic}{kc+} \rightarrow ic = kc = g$$

$$\frac{|ki+1}{k+1} = (1-di) + \frac{it_+}{ki_+} - 3 \quad \hat{i} = \hat{k}i = gi$$

· EEs: rc constant

h constant

• Frisch:
$$= x \rightarrow \hat{y} = \hat{c}$$

So: yc, kc, ic, c, w grow at g gi, ki, it grow at gi rc, h constant

ri, p grow (folk, we'll see why) at gp.
Let's map "endog" growth rates to exog. ones (xc, xi).

$$y\hat{c} = fc + a \cdot k\hat{c} + b \cdot k\hat{i}$$
i.e. $g = fc + a \cdot g + b \cdot gi$

$$g = \frac{1}{1-a} fc + \frac{b}{1-a} gi \qquad (i)$$

$$y_i^2 = y_i + a \cdot k\hat{c} + b \cdot k\hat{i}$$

i.e. $g_i = y_i + a \cdot g + b \cdot g_i$
 $g_i = \frac{1}{1-b}y_i + \frac{q}{1-b}g$ (ii)

In (i):

$$g\left(1 - \frac{ab}{(1-a)(1-b)}\right) = \frac{1-b}{(1-a)(1-b)} g(1 + \frac{b}{(1-a)(1-b)} g(1 + \frac{b}{(1-a)($$

Back in (li)

$$g_i = 1-a-b$$
 γ_i $\alpha(1-b)$ γ_c $+ ab$ γ_i $\alpha(1-b)(1-a-b)$ $\alpha(1-b)(1-a-b)$ $\alpha(1-b)(1-a-b)$

So (I) & (III) say that

- · ye grows at the same rate as be trans bi trans (I)
- yi grows at the same rate as be Ta-6 bita-6 1
- -> 50 everything that grows by g needs to be stationard

& everything that grows by g; needs to be stationarized

I now just need (1), he clahorship blun gp & (Sc, 8i). For that, PTO:

From The ratio of value of outports (following Outton Annex A.) P'yi = re loc2 + ri ki2 + wh2 | Diff with time.

P'yi = re loc2 + ri ki2 + wh2 | Diff with time.

gp + gi - g = d (RHS) } WTS that this = 0. RHS: ln (rc kc2 + ri - ki2 + w h2) - ln(rc kc1+ri ki1+w h1) So gp + gi - g = 0, so: gp=g-gi (I've called this (I) in my work.) Then from PFs we sub in g & gi 9P= 1-6 1c + 6 11 - 9 1c - 1-9 11 - 1-0-6 11 => 9P = re-r. (E) -> 50 everything that grows by gp grows at the Same rate as be and can thus by stationanted by that!

Summany of stationanisation strategy: ("=stationarized)

1.
$$\tilde{X}_t = \frac{X_t}{bc_{t-1}} = \frac{X_t}{bc_{t-1}} = \frac{b}{bc_{t-1}} = \frac{b}{bc_{t-1}} = \frac{b}{bc_{t-1}} = \frac{b}{bc_{t-1}}$$

8.
$$X_{+} = X_{+} = X_{+} = rit, p_{+}$$

$$\frac{bc_{+-1}}{bi_{+-1}}$$

4.
$$X_{t} = \frac{X_{t-1}}{X_{t-1}} = (1+Y_{x})$$
 for $X_{t} = bc_{t}$, bit

And why 1+ x? 3/c the fx (x=c,i) are net growth rates.

(2)

So git = (1+ (i+) h2+ 1-4-6 bezt 12-6

$$\frac{bc_{t+1}}{bc_{t-1}} = \frac{(1-dc)kc_{t} + ic_{t}}{bc_{t}}$$

$$\frac{bc_{t}}{bc_{t-1}} = \frac{b}{bi_{t}} = \frac{b}{bc_{t-1}}$$

$$\frac{bc_{t}}{bc_{t-1}} = \frac{b}{bi_{t-1}}$$

$$\frac{bc_{t-1}}{bc_{t-1}} = \frac{bc_{t}}{bc_{t-1}}$$

$$= \left(\frac{1}{1+8c_{i+1}}\right)^{\frac{1-b}{1-a-b}} \left(\frac{1}{1+8i_{i+1}}\right)^{\frac{b}{1-a-b}}$$

(12):
$$A = \beta E_{+} \frac{C_{+}}{C_{+}} \frac{\beta_{+} A_{+}}{\beta_{+}} \left(\frac{\gamma_{i+} A_{i}}{\beta_{+}} + 1 - d_{i} \right)$$

$$1 = \beta E_{+} \frac{C_{+}}{C_{+}} \frac{G_{+} A_{i}}{G_{+}} \frac{\beta_{+} A_{i}}{\beta_{+}} \frac{bC_{+}}{bC_{+} A_{i}} \left(\frac{\gamma_{i+} A_{i}}{\beta_{i+}} + 1 - d_{i} \right)$$

$$Same as in \frac{bC_{+}}{bC_{+} A_{i}} \frac{bC_{+}}{bC_{+}} \left(\frac{\gamma_{i+} A_{i}}{\beta_{i+}} + 1 - d_{i} \right)$$

$$= \frac{bC_{+}}{bC_{+} A_{i}} \frac{bC_{+}}{bC_{+}}$$

$$= \frac{A + \gamma_{i+} A_{i}}{A + \gamma_{i+} A_{i}}$$

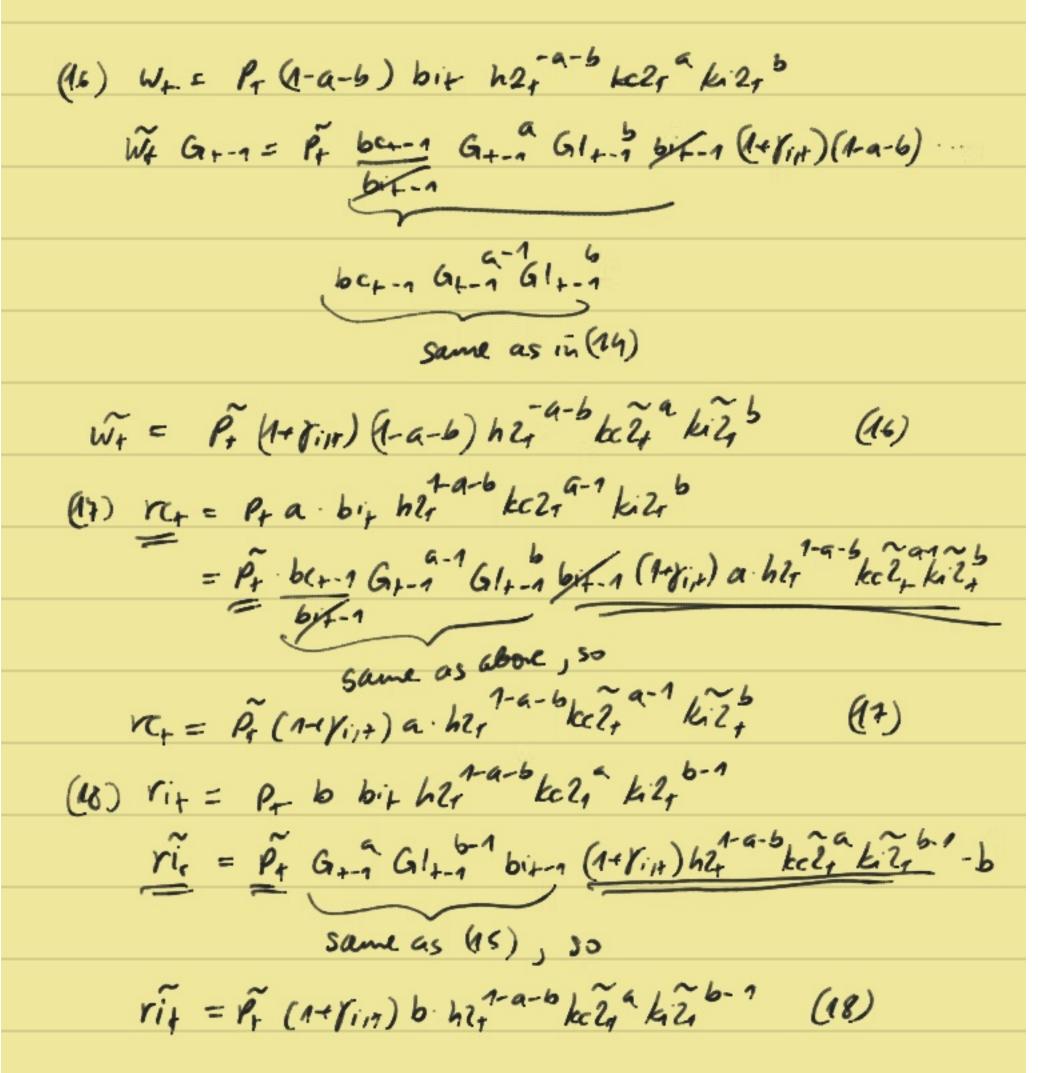
$$1 = \beta E_{1} \frac{C_{1}}{C_{1+1}} \left(\frac{1}{1+\gamma_{i+1}} \right)^{\frac{5}{1-\alpha-b}} \frac{1+\gamma_{i+1}}{1+\gamma_{i+1}} \left(\frac{r_{i+1}}{\beta_{i+1}} + 1 - l_{i} \right)$$

$$\frac{1-b-(1-\alpha-b)}{1-\alpha-b} \left(\frac{1}{1+\gamma_{i+1}} \right)^{\frac{5}{1-\alpha-b}} \frac{1+\gamma_{i+1}}{1-\alpha-b}$$

$$\frac{1}{1+\gamma_{i+1}} \frac{1-\alpha-b}{1-\alpha-b} \left(\frac{1}{1+\gamma_{i+1}} \right)^{\frac{5}{1-\alpha-b}}$$

$$\frac{1}{1+\gamma_{i+1}} \frac{1-\alpha-b}{1-\alpha-b} \left(\frac{1}{1+\gamma_{i+1}} \right)^{\frac{5}{1-\alpha-b}}$$

(13):
$$W_{t} = (A-a-b)bc_{t}hl_{t}^{-a-b}kcl_{t}^{a}kl_{t}^{b}$$
 $W_{t} = G_{t-1} = (A-a-b)(A+g_{t+1})bc_{t-1}G_{t-1}G_{t-1}^{a}hl_{t}^{a}kcl_{t}^{a}kl_{t}^{b}$
 $W_{t} = G_{t-1} = (A-a-b)(A+g_{t+1})bc_{t-1}G_{t-1}^{a}G_{t}^{a}kl_{t}^{a}hl_{t}^{b}$
 $W_{t} = G_{t-1} = G_{t-1}^{a}bc_{t-1}G_{t-1}^{a}bc_{t-1}G_{t-1}^{a}bl_{t-1}^{a}bc_{t-1}G_{t-1}^{a}bl_{t-1}^{a}bl_{t-1}G_{t-1}^{a}bl_{t-1}G_{t-1}^{a}bl_{t-1}^{a}$



4.) Steady state Procedure:

- 1. Drop time indexes & reunite
- 2. tollowing Oulton (p.10 & Annex A), set

 h=h1=h2, kc=kc1=kc2 and ki=ki1=ki2

 -> need to figure out market cleaning for this

 case!
 - -> need to pigure out how to deal w/ sector 2 in the st. st.
 - 1. Need to use it to get $P = \frac{1+8c}{1+8i}$ 2. But having that, most of the sector 2

 eq. conditions become redundant

 -> need to figure out how to go about

 that to still be able to get levels

 and not use any eq. twice