# $\ \, {\rm Dynare} + + \ {\rm DSGE \ solver}$

solves higher order approximation to a decision rule of a Dynamic Stochastic General Equilibrium model about deterministic and stochastic fix point 2 UTILITIES Dynare++ §1

#### 1. Utilities.

```
Exception. Start of kord_exception.h file.
  This is a simple code defining an exception and two convenience macros.
#ifndef KORD_EXCEPTION_H
#define KORD_EXCEPTION_H
#include <cstring>
#include <cstdio>
#define KORD_RAISE(mes)throw KordException(__FILE__, __LINE__, mes);
\#define KORD_RAISE_IF(expr, mes)
  if (expr) throw KordException(__FILE__, __LINE__, mes);
\#define KORD_RAISE_X(mes, c)throw KordException(__FILE__, __LINE__, mes, c);
#define KORD_RAISE_IF_X(expr, mes, c)
  \mathbf{if}\ (expr)\ \mathbf{throw}\ \mathbf{KordException}(\_\mathtt{FILE}\_\_, \_\mathtt{LINE}\_\_, mes, c);
  ⟨KordException class definition ₃⟩;
  ⟨ KordException error code definitions 4⟩;
#endif
3.
\langle KordException class definition 3 \rangle \equiv
  class KordException {
  protected:
    char fname[50];
    int lnum;
    char message[500];
    int cd;
  public:
    KordException(const char *f, int l, const char *mes, int c = 255)
      strncpy(fname, f, 50); fname[49] = '\0';
      strncpy(message, mes, 500); message[499] = '\0';
      lnum = l;
      cd = c;
    virtual ~KordException() {}
    virtual void print() const
    { printf("At_{\square}\%s:\%d:(\%d):\%s\n",fname,lnum,cd,message);}}
    virtual int code() const
    \{ \mathbf{return} \ cd; \}
    const char *get_message() const
    { return message; }
  };
This code is used in section 2.
4.
\langle KordException error code definitions 4 \rangle \equiv
#define KORD_FP_NOT_CONV 254
#define KORD_FP_NOT_FINITE 253
#define KORD_MD_NOT_STABLE 252
This code is used in section 2.
```

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5. End of kord\_exception.h file.

```
Resource usage journal. Start of journal.h file.
#ifndef JOURNAL_H
\#define JOURNAL_H
#include "int_sequence.h"
#include <sys/time.h>
#include <cstdio>
#include <iostream>
#include <fstream>
  ⟨SystemResources class declaration 7⟩;
   SystemResourcesFlash struct declaration 8);
   Journal class declaration 11);
   JournalRecord class declaration 9);
  ⟨JournalRecordPair class declaration 10⟩;
#endif
7.
\langle SystemResources class declaration 7\rangle \equiv
  class SystemResources {
    timeval start;
  public:
    SystemResources();
    static long int pageSize();
    static long int physicalPages();
    static long int onlineProcessors();
    static long int availableMemory();
    void getRUS(double &load_avg, long int &pg_avail, double &utime, double &stime, double
        & elapsed, long int & idrss, long int & majflt);
  };
This code is used in section 6.
8.
\langle SystemResourcesFlash struct declaration 8 \rangle \equiv
  struct SystemResourcesFlash {
    double load_avg;
    long int pg_avail;
    double utime;
    double stime;
    double elapsed;
    long int idrss;
    long int majflt;
    SystemResourcesFlash();
    void diff(const SystemResourcesFlash &pre);
  };
This code is used in section 6.
```

```
4
9.
```

```
#define MAXLEN 1000
\langle JournalRecord class declaration 9 \rangle \equiv
  class JournalRecord;
  JournalRecord & endrec (JournalRecord &);
  class JournalRecord {
  protected:
    char recChar;
    int ord:
  public:
    Journal & journal;
    char prefix[MAXLEN];
    char mes[MAXLEN];
    SystemResourcesFlash flash;
    typedef JournalRecord \&(*\_Tfunc)(JournalRecord \&);
    JournalRecord(Journal \& jr, char rc = 'M')
    : recChar(rc), ord(jr.getOrd()), journal(jr) { prefix[0] = `\0';
      mes[0] = '\0';
      writePrefix(flash); }
    virtual ~JournalRecord() {}
    JournalRecord & operator \ll (const IntSequence &s);
    JournalRecord & operator \ll (_Tfunc f)
    \{ (*f)(*this); \}
      return *this; }
    JournalRecord & operator \ll (const char *s)
    \{ strcat(mes, s);
      return *this; }
    JournalRecord & operator \ll (int i)
    { sprintf(mes + strlen(mes), "%d", i);
      return *this; }
    JournalRecord \& operator \ll (double d)
    { sprintf(mes + strlen(mes), "\%f", d);
      return *this; }
  protected:
    void writePrefix(const SystemResourcesFlash & f);
This code is used in section 6.
```

```
10.
\langle JournalRecordPair class declaration 10 \rangle \equiv
  class JournalRecordPair : public JournalRecord {
    char prefix_end[MAXLEN];
  public:
    \mathbf{JournalRecordPair}(\mathbf{Journal}\ \& jr)
    : JournalRecord(jr, 'S') { prefix_end[0] = '\0';
      journal.incrementDepth(); }
    ~JournalRecordPair();
  private:
    void writePrefixForEnd (const SystemResourcesFlash & f);
This code is used in section 6.
11.
\langle Journal class declaration 11 \rangle \equiv
  class Journal : public ofstream {
    int ord;
    int depth;
  public:
    Journal(const char *fname)
    : ofstream(fname), ord(0), depth(0) { printHeader(); }
    \simJournal()
    { flush(); }
    void printHeader();
    void incrementOrd()
    \{ ord ++; \}
    int getOrd() const
    { return ord; }
    void incrementDepth()
    \{ depth +++; \}
    void decrementDepth()
    \{ depth ---; \}
    int getDepth() const
      return depth;
This code is used in section 6.
```

12. End of journal.h file.

6

```
Start of journal.cpp file.
#include "journal.h"
#include "kord_exception.h"
\#if \neg defined (\_MINGW32\_)
#include <sys/resource.h>
#include <sys/utsname.h>
#endif
#include <cstdlib>
#include <unistd.h>
#include <ctime>
  SystemResources _sysres;
#if defined (__MINGW32__)
  \langle sysconf Win 32 \text{ implementation } 28 \rangle;
#endif
#if defined (__APPLE__)
#define _SC_PHYS_PAGES 2
\#define _SC_AVPHYS_PAGES 3
#endif
  ⟨SystemResources constructor code 14⟩;
   SystemResources:: pageSize code 15 >;
   SystemResources::physicalPages code 16);
   SystemResources:: onlineProcessors code 17);
   SystemResources::availableMemory code 18);
   SystemResources:: qetRUS code 19 \rangle;
   SystemResourcesFlash constructor code 20);
   SystemResourcesFlash:: diff code 21 >;
   JournalRecord::operator≪ symmetry code 22⟩;
   JournalRecord:: writePrefix code 23 \;
   JournalRecord:: writePrefixForEnd code 24);
   JournalRecordPair destructor code 25);
   endrec code 26;
  \langle \mathbf{Journal} :: printHeader \ code \ 27 \rangle;
14.
\langle SystemResources constructor code 14\rangle \equiv
  SystemResources::SystemResources()
    gettime of day(\&start, \Lambda);
This code is used in section 13.
\langle SystemResources::pageSize \text{ code } 15 \rangle \equiv
  long int SystemResources::pageSize()
    return sysconf(_SC_PAGESIZE);
```

This code is used in section 13.

```
16.

⟨SystemResources::physicalPages code 16⟩ ≡
long int SystemResources::physicalPages()
{
   return sysconf(_SC_PHYS_PAGES);
}
This code is used in section 13.

17.

⟨SystemResources::onlineProcessors code 17⟩ ≡
long int SystemResources::onlineProcessors()
{
   return sysconf(_SC_NPROCESSORS_ONLN);
}
This code is used in section 13.

18.

⟨SystemResources::availableMemory code 18⟩ ≡
long int SystemResources::availableMemory()
{
   return pageSize() * sysconf(_SC_AVPHYS_PAGES);
}
This code is used in section 13.
```

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19. Here we read the current values of resource usage. For MinGW, we implement only a number of available physical memory pages.

```
\langle SystemResources :: getRUS \text{ code } 19 \rangle \equiv
  void SystemResources::getRUS(double &load\_avg, long int &pg\_avail, double &utime, double
           &stime, double & elapsed, long int &idrss, long int &majflt)
    struct timeval now;
    gettimeofday(\&now, \Lambda);
     elapsed = now.tv\_sec - start.tv\_sec + (now.tv\_usec - start.tv\_usec) * 1.0 \cdot 10^{-6};
#if ¬defined (__MINGW32__)
    struct rusage rus;
    getrusage(RUSAGE\_SELF, \&rus);
    utime = rus.ru\_utime.tv\_sec + rus.ru\_utime.tv\_usec * 1.0 \cdot 10^{-6};
    stime = rus.ru\_stime.tv\_sec + rus.ru\_stime.tv\_usec * 1.0 \cdot 10^{-6};
    idrss = rus.ru_idrss;
    majflt = rus.ru\_majflt;
#else
    utime = -1.0;
    stime = -1.0;
    idrss = -1;
    majflt = -1;
\# endif
\#define MINGCYGTMP (\negdefined (__MINGW32__) \land \negdefined (__CYGWIN32__) \land \negdefined (__CYGWIN__))
#define MINGCYG (MINGCYGTMP \( \tau \) defined (__MINGW64__) \( \tau \) defined (__CYGWIN64__))
#if MINGCYG
    getloadavg(\&load\_avg, 1);
#else
    load\_avg = -1.0;
#endif
    pg\_avail = sysconf(\_SC\_AVPHYS\_PAGES);
This code is used in section 13.
20.
\langle SystemResourcesFlash constructor code 20 \rangle \equiv
  SystemResourcesFlash()
    _sysres.getRUS(load_avg, pg_avail, utime, stime, elapsed, idrss, majflt);
This code is used in section 13.
```

```
21.
```

```
\langle  SystemResourcesFlash :: diff  code 21 \rangle \equiv
  void SystemResourcesFlash :: diff (const SystemResourcesFlash & pre)
     utime -= pre.utime;
     stime -= pre.stime;
     elapsed -= pre.elapsed;
     idrss -= pre.idrss;
     majflt = pre.majflt;
  }
This code is used in section 13.
22.
\langle JournalRecord :: operator \ll symmetry code 22 \rangle \equiv
  JournalRecord & JournalRecord :: operator \ll (const IntSequence &s)
     operator \ll ("["];
     for (int i = 0; i < s.size(); i ++) {
       operator \ll (s[i]);
       if (i < s.size() - 1) operator \ll (",");
     operator≪("]");
     return *this;
This code is used in section 13.
23.
\langle JournalRecord :: writePrefix code 23 \rangle \equiv
  void JournalRecord::writePrefix(const SystemResourcesFlash & f)
     for (int i = 0; i < \text{MAXLEN}; i \leftrightarrow prefix[i] = '_{\sqcup}';
     double mb = 1024 * 1024;
     sprintf(prefix, "%07.6g", f.elapsed);
     sprintf(prefix + 7, ":\%c\%05d", recChar, ord);
     sprintf(prefix + 14, ":\%1.1f", f.load\_avg);
     sprintf(prefix + 18, ":\%05.4g", f.pg\_avail * \_sysres.pageSize()/mb);
     sprintf(prefix + 24, "%s", ": ":");
     \textbf{for (int } i=0; \ i<2*journal.getDepth(); \ i++) \ \textit{prefix}[i+33]=\textit{`}_{\sqcup}\textit{'};
     prefix[2*journal.getDepth() + 33] = '\0';
This code is used in section 13.
```

This code is used in section 13.

```
24.
\langle JournalRecord :: writePrefixForEnd \text{ code } 24 \rangle \equiv
  void JournalRecordPair::writePrefixForEnd(const SystemResourcesFlash & f)
     for (int i = 0; i < \text{MAXLEN}; i \leftrightarrow ) prefix_end[i] = '\sqcup';
     double mb = 1024 * 1024;
     SystemResourcesFlash difnow;
     difnow.diff(f);
     sprintf (prefix_end, "%07.6g", f.elapsed + difnow.elapsed);
     sprintf(prefix\_end + 7, ":E\%05d", ord);
     sprintf(prefix\_end + 14, ":\%1.1f", difnow.load\_avg);
     sprintf(prefix\_end + 18, ": \%05.4g", difnow.pg\_avail * \_sysres.pageSize()/mb);
     sprintf(prefix\_end + 24, ":\%06.5g", difnow.majflt * \_sysres.pageSize()/mb);
     sprintf(prefix\_end + 31, "%s", ": \sqcup");
     for (int i = 0; i < 2 * journal.getDepth(); i \leftrightarrow) prefix_end[i + 33] = ' ' ';
     prefix\_end[2*journal.getDepth() + 33] = '\0';
  }
This code is used in section 13.
25.
\langle JournalRecordPair destructor code 25 \rangle \equiv
  JournalRecordPair :: \sim JournalRecordPair()
     journal.decrementDepth();
     writePrefixForEnd(flash);
    journal \ll prefix\_end;
    journal \ll mes;
    journal \ll endl;
     journal.flush();
This code is used in section 13.
26.
\langle endrec \text{ code } 26 \rangle \equiv
  JournalRecord & endrec(JournalRecord & rec)
     rec.journal \ll rec.prefix;
     rec.journal \ll rec.mes;
     rec.journal \ll endl;
     rec.journal.flush();
     rec.journal.incrementOrd();
     return rec;
```

```
27.
\langle \mathbf{Journal} :: printHeader \ code \ 27 \rangle \equiv
  void Journal::printHeader()
     (*this) \ll "This_1 is_1 Dynare++, Copyright_1(C)_12004-2011, Ondra_1 Kamenik\n" \ll
           "Dynare++_{\sqcup}comes_{\sqcup}with_{\sqcup}ABSOLUTELY_{\sqcup}NO_{\sqcup}WARRANTY_{\sqcup}and_{\sqcup}is_{\sqcup}distributed_{\sqcup}under\setminusn" \ll
           "GPL:_{\sqcup}modules_{\sqcup}integ,_{\sqcup}tl,_{\sqcup}kord,_{\sqcup}sylv,_{\sqcup}src,_{\sqcup}extern_{\sqcup}and_{\sqcup}documentation_{\sqcup}" \ll
           "LGPL: _{\sqcup}modules _{\sqcup}parser, _{\sqcup}utils \\ "= "_{\sqcup}for_{\sqcup}GPL _{\sqcup}see_{\sqcup}http://www.gnu.org/licens \\ "
           es/gpl.html\n" \ll " for LGPL see http://www.gnu.org/licenses/lgpl.html \n" \ll " \n \n";
#if ¬defined (__MINGW32__)
     utsname\,info;
     uname(\&info);
     (*this) \ll "System_{\sqcup}info:_{\sqcup}";
     (*this) \ll info.sysname \ll " \sqcup " \ll info.release \ll " \sqcup " \ll info.version \ll " \sqcup ";
     (*this) \ll info.machine \ll ", processors on line: " \ll system.on line Processors ();
     (*this) ≪ "\n\nStart time: ";
     char ts[100];
     time_t curtime = time(\Lambda);
     tm loctime;
     local time_r(\&curtime, \&loctime);
     asctime_r(\&loctime, ts);
     (*this) \ll ts \ll "\n";
#else
     (*this) \ll "System info: (not implemented for MINGW) \n";
     (*this) \ll "Start_{\sqcup}time:_{\sqcup\sqcup}(not_{\sqcup}implemented_{\sqcup}for_{\sqcup}MINGW)\n';
#endif
     (*this) \ll "_{\text{UU}} - - - - _{\text{U}} \text{elapsed}_{\text{U}} \text{time}_{\text{U}} (\text{seconds})_{\text{UU}} \text{elapsed}_{\text{UU}} \backslash n";
     (*this) \ll "_{UU} |_{UUUUUUU}-----urecord_unique_identifier_uuuuuuuuu\n";
     (*this) \ll "_{\cup\cup} |_{\cup\cup\cup\cup\cup} |_{\cup\cup\cup\cup\cup} ----_{\cup} load_{\cup} average_{\cup\cup\cup\cup\cup\cup\cup\cup\cup\cup\cup\cup\cup\cup} \backslash n"};
     (*this) \ll \texttt{"}_{\text{UU}} \texttt{I}_{\text{UUUUU}} \texttt{I}_{\text{UUUUU}} \texttt{I}_{\text{UUUUU}} \texttt{I}_{\text{UUUUU}} \texttt{-----}_{\text{UU}} \texttt{major}_{\text{U}} \texttt{faults}_{\text{U}} (\texttt{MB}) \texttt{'n"};
     (*this) \ll "\n";
```

This code is used in section 13.

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28. Here we implement sysconf for MinGW. We implement only page size, number of physial pages, and a number of available physical pages. The pagesize is set to 1024 bytes, real pagesize can differ but it is not important. We can do this since Windows kernel32 GlobalMemoryStatus call returns number of bytes.

Number of online processors is not implemented and returns -1, since Windows kernel32 GetSystemInfo call is too complicated.

```
\langle sysconf Win 32 \text{ implementation } 28 \rangle \equiv
\#\mathbf{ifndef} NOMINMAX
\#define NOMINMAX
                       /* Do not define "min" and "max" macros */
#endif
#include <windows.h>
\#define _SC_PAGESIZE 1
#define _SC_PHYS_PAGES 2
#define _SC_AVPHYS_PAGES 3
#define _SC_NPROCESSORS_ONLN 4
  long sysconf(int name)
    \mathbf{switch} \ (name) \ \{
    case _SC_PAGESIZE:
      return 1024;
    case _SC_PHYS_PAGES:
        MEMORYSTATUS memstat;
         GlobalMemoryStatus(\&memstat);
        return memstat.dwTotalPhys/1024;
    case _SC_AVPHYS_PAGES:
        MEMORYSTATUS memstat;
         Global Memory Status (\& memstat);
        return memstat.dwAvailPhys/1024;
    case _SC_NPROCESSORS_ONLN:
      return -1;
    default:
      KORD_RAISE("Not_implemented_in_Win32_sysconf.");
      return -1;
  }
This code is used in section 13.
```

29. End of journal.cpp file.

### 30. Conjugate family for normal distribution. Start of normal\_conjugate.h file.

The main purpose here is to implement a class representing conjugate distributions for mean and variance of the normal distribution. The class has two main methods: the first one is to update itself with respect to one observation, the second one is to update itself with respect to anothe object of the class. In the both methods, the previous state of the class corresponds to the prior distribution, and the final state corresponds to the posterior distribution.

The algrebra can be found in Gelman, Carlin, Stern, Rubin (p.87). It goes as follows: Prior conjugate distribution takes the following form:

$$\sum \sim \text{InvWishart}_{\nu_0}(\Lambda_0^{-1})$$

$$\mu|\Sigma \sim N(\mu_0, \Sigma/\kappa_0)$$

If the observations are  $y_1 ldots y_n$ , then the posterior distribution has the same form with the following parameters:

$$\mu_n = \frac{\kappa_0}{\kappa_0 + n} \mu_0 + \frac{n}{\kappa_0 + n} \bar{y}$$

$$\kappa_n = \kappa_0 + n$$

$$\nu_n = \nu_0 + n$$

$$\Lambda_n = \Lambda_0 + S + \frac{\kappa_0 n}{\kappa_0 + n} (\bar{y} - \mu_0) (\bar{y} - \mu_0)^T,$$

where

$$\bar{y} = \frac{1}{n} \sum_{i=1}^{n} y_{i}$$

$$S = \sum_{i=1}^{n} (y_{i} - \bar{y})(y_{i} - \bar{y})^{T}$$

**NormalConj**:: update multiple observations code 39); **NormalConj**::update with **NormalConj** code 40);

 $\langle NormalConj :: getVariance code 41 \rangle;$ 

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The class is described by the four parameters:  $\mu$ ,  $\kappa$ ,  $\nu$  and  $\Lambda$ .  $\langle$  **NormalConj** class declaration  $31 \rangle \equiv$ class NormalConj { protected: Vector mu; int kappa; int nu; TwoDMatrix lambda; ⟨ NormalConj constructors 32⟩; virtual ~NormalConj() {} void update(const ConstVector &y); void update(const ConstTwoDMatrix &ydata); void update(const NormalConj &nc); int getDim() const { return mu.length(); } const Vector & getMean() const  $\{ \text{ return } mu; \}$ void getVariance(TwoDMatrix &v) const; }; This code is used in section 30. 32. We provide the following constructors: The first constructs diffuse (Jeffrey's) prior. It sets  $\kappa$ , and  $\Lambda$ to zeros, nu to -1 and also the mean  $\mu$  to zero (it should not be referenced). The second constructs the posterior using the diffuse prior and the observed data (columnwise). The third is a copy constructor.  $\langle$  NormalConj constructors 32 $\rangle \equiv$ NormalConj(int d); NormalConj(const ConstTwoDMatrix &ydata); NormalConj(const NormalConj &nc); This code is used in section 31. 33. End of normal\_conjugate.h file. 34. Start of normal\_conjugate.cpp file. #include "normal\_conjugate.h" #include "kord\_exception.h" ⟨ NormalConj diffuse prior constructor 35⟩; **NormalConj** data update constructor 36); **NormalConj** copy constructor 37); **NormalConj**::*update* one observation code 38);

This code is used in section 34.

```
\S 35
       Dynare++
                                                   CONJUGATE FAMILY FOR NORMAL DISTRIBUTION
35.
\langle NormalConj diffuse prior constructor 35\rangle \equiv
  NormalConj::NormalConj(int d)
  : mu(d), kappa(0), nu(-1), lambda(d,d) {
    mu.zeros();
    lambda.zeros();
This code is used in section 34.
36.
\langle NormalConj data update constructor 36 \rangle \equiv
  NormalConj::NormalConj(const ConstTwoDMatrix &ydata)
  : mu(ydata.numRows()), kappa(ydata.numCols()), nu(ydata.numCols()-1),
          lambda(ydata.numRows(), ydata.numRows())  {
    mu.zeros();
    for (int i = 0; i < ydata.numCols(); i++) mu.add(1.0/ydata.numCols(), ConstVector(ydata,i));
    lambda.zeros();
    for (int i = 0; i < ydata.numCols(); i \leftrightarrow ) {
       Vector diff(ConstVector(ydata, i));
       diff.add(-1, mu);
       lambda.addOuter(diff);
  }
This code is used in section 34.
37.
\langle NormalConj copy constructor 37\rangle \equiv
```

NormalConj::NormalConj(const NormalConj &nc)

 $: mu(nc.mu), kappa(nc.kappa), nu(nc.nu), lambda(nc.lambda) \{ \}$ 

38. The method performs the following:

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$$\mu_{1} = \frac{\kappa_{0}}{\kappa_{0} + 1} \mu_{0} + \frac{1}{\kappa_{0} + 1} y$$

$$\kappa_{1} = \kappa_{0} + 1$$

$$\nu_{1} = \nu_{0} + 1$$

$$\Lambda_{1} = \Lambda_{0} + \frac{\kappa_{0}}{\kappa_{0} + 1} (y - \mu_{0}) (y - \mu_{0})^{T},$$

```
\langle NormalConj :: update \text{ one observation code } 38 \rangle \equiv
  void NormalConj::update(const ConstVector &y)
    KORD\_RAISE\_IF(y.length() \neq mu.length(), "Wrong_length_lof_la_lvector_lin_lNormalConj::update");
    mu.mult(kappa/(1.0 + kappa));
    mu.add(1.0/(1.0 + kappa), y);
    Vector diff(y);
    diff.add(-1, mu);
    lambda.addOuter(diff, kappa/(1.0 + kappa));
    kappa ++;
    nu++;
This code is used in section 34.
    The method evaluates the formula in the header file.
\langle NormalConj :: update multiple observations code 39 \rangle \equiv
  void NormalConj::update(const ConstTwoDMatrix &ydata)
    NormalConj nc(ydata);
    update(nc);
This code is used in section 34.
40.
\langle NormalConj :: update \text{ with } NormalConj \text{ code } 40 \rangle \equiv
  void NormalConj :: update(const NormalConj &nc)
    double wold = ((\mathbf{double}) \ kappa)/(kappa + nc.kappa);
    double wnew = 1 - wold;
    mu.mult(wold);
    mu.add(wnew, nc.mu);
    Vector diff(nc.mu);
    diff.add(-1, mu);
    lambda.add(1.0, nc.lambda);
    lambda.addOuter(diff);
    kappa = kappa + nc.kappa;
    nu = nu + nc.kappa;
  }
This code is used in section 34.
```

46. End of random.h file.

**41.** This returns  $\frac{1}{\nu-d-1}\Lambda$ , which is the mean of the variance in the posterior distribution. If the number of degrees of freedom is less than d, then NaNs are returned.

```
\langle NormalConj :: getVariance \text{ code } 41 \rangle \equiv
  void NormalConj::getVariance(TwoDMatrix &v) const
    if (nu > getDim() + 1) {
      v = (\mathbf{const} \ \mathbf{TwoDMatrix} \ \&) \ lambda;
      v.mult(1.0/(nu-getDim()-1));
    else v.nans();
  }
This code is used in section 34.
     End of normal_conjugate.cpp file.
      Random number generation. Start of random.h file.
43.
\# ifndef RANDOM_H
\#\mathbf{define}\ \mathtt{RANDOM\_H}
  ⟨ RandomGenerator class declaration 44⟩;
  ⟨SystemRandomGenerator class declaration 45⟩;
  extern SystemRandomGenerator system_random_generator;
#endif
44. This is a general interface to an object able to generate random numbers. Subclass needs to implement
uniform method, other is, by default, implemented here.
\langle RandomGenerator class declaration 44 \rangle \equiv
  class RandomGenerator {
  public:
    virtual double uniform() = 0;
    int int_uniform();
    double normal();
This code is used in section 43.
45. This implements RandomGenerator interface with system drand or rand. It is not thread aware.
\langle SystemRandomGenerator class declaration 45\rangle \equiv
  {\bf class~SystemRandomGenerator~:~public~RandomGenerator~\{}
  public:
    double uniform();
    void initSeed(int seed);
  };
This code is used in section 43.
```

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```
Start of random.cpp file.
#include "random.h"
#include <cstdlib>
#include <limits>
#include <cmath>
  \langle \mathbf{RandomGenerator} :: int\_uniform \text{ code } 48 \rangle;
  \langle \mathbf{RandomGenerator} :: normal \ code \ 49 \rangle;
  SystemRandomGenerator system_random_generator;
  ⟨SystemRandomGenerator::uniform code 50⟩;
  ⟨SystemRandomGenerator::initSeed code 51⟩;
48.
\langle RandomGenerator :: int\_uniform \text{ code } 48 \rangle \equiv
  int RandomGenerator::int\_uniform(){ double s = std::numeric\_limits < int > :: max()*uniform();}
       return (int) s; }
This code is used in section 47.
49. This implements Marsaglia Polar Method.
\langle \mathbf{RandomGenerator} :: normal \ \mathrm{code} \ 49 \rangle \equiv
  double RandomGenerator::normal()
    double x1, x2;
    double w;
    do {
       x1 = 2 * uniform() - 1;
       x2 = 2 * uniform() - 1;
      w = x1 * x1 + x2 * x2;
    } while (w \ge 1.0 \lor w < 1.0 \cdot 10^{-30});
    return x1 * std :: sqrt((-2.0 * std :: log(w))/w);
  }
This code is used in section 47.
\langle SystemRandomGenerator :: uniform code 50 \rangle \equiv
  double SystemRandomGenerator::uniform()
#if ¬defined (__MINGW32__)
    return drand48();
    return ((double) rand())/RAND_MAX;
\#endif
This code is used in section 47.
```

```
51.
```

```
⟨SystemRandomGenerator::initSeed code 51⟩ ≡
  void SystemRandomGenerator::initSeed(int seed)
  {
#if ¬defined (__MINGW32__)
      srand48(seed);
#else
      srand(seed);
#endif
  }
This code is used in section 47.
```

**52.** End of random.cpp file.

## 53. Mersenne Twister PRNG. Start of mersenne\_twister.h file.

This file provides a class for generating random numbers with encapsulated state. It is based on the work of Makoto Matsumoto and Takuji Nishimura, implementation inspired by code of Richard Wagner and Geoff Kuenning.

```
54.
```

```
\langle MersenneTwister class declaration 54\rangle \equiv
  class MersenneTwister : public RandomGenerator {
  protected:
    typedef unsigned int uint32;
    enum {
      \mathtt{STATE\_SIZE} = 624
    enum {
      \mathtt{RECUR\_OFFSET} = 397
    uint32 statevec[STATE_SIZE];
    int stateptr;
  public:
    MersenneTwister(uint32 iseed);
    MersenneTwister(const MersenneTwister \& mt);
    virtual ~MersenneTwister()
    {}
    uint32 lrand();
    double drand();
    double uniform()
    { return drand(); }
  protected:
    void seed(uint32 iseed);
    void refresh();
    \langle MersenneTwister static inline methods 55\rangle;
  };
This code is used in section 53.
```

```
55.
\langle MersenneTwister static inline methods 55\rangle \equiv
  static uint32 hibit(uint32 u)
     return u \& #80000000_{UL};
  static uint32 lobit(uint32 u)
     return u \& #00000001_{UL};
  static uint32 lobits(uint32 u)
     return u \& #7ffffffffUL;
  static uint32 mixbits(uint32 u, uint32 v)
    return hibit(u) \mid lobits(v);
  static uint32 twist(uint32 m, uint32 s\theta, uint32 s1)
     return m \oplus (mixbits(s0, s1) \gg 1) \oplus (-lobit(s1) \& #9908b0df_{UL});
This code is used in section 54.
56.
\langle MersenneTwister inline method definitions 56 \rangle \equiv
  ⟨ MersenneTwister constructor code 57⟩;
   MersenneTwister copy constructor code 58);
   \langle MersenneTwister :: lrand code 59 \rangle;
   \langle MersenneTwister :: drand code 60 \rangle;
  \langle MersenneTwister :: seed code 61 \rangle;
  \langle MersenneTwister :: refresh code 62 \rangle;
This code is used in section 53.
57.
\langle MersenneTwister constructor code 57\rangle \equiv
  inline MersenneTwister::MersenneTwister(uint32 iseed)
     seed(iseed);
This code is used in section 56.
58.
\langle MersenneTwister copy constructor code 58\rangle \equiv
  inline Mersenne Twister:: Mersenne Twister (const Mersenne Twister \&mt)
  : stateptr(mt.stateptr) {
     memcpy(statevec, mt.statevec, sizeof(uint32) * STATE_SIZE);
This code is used in section 56.
```

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This code is used in section 56.

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```
59.
\langle MersenneTwister :: lrand code 59 \rangle \equiv
  inline MersenneTwister::uint32 MersenneTwister::lrand()
     if (stateptr > STATE_SIZE) refresh();
     register uint32 v = statevec[stateptr ++];
     v \oplus = v \gg 11;
     v \oplus = (v \ll 7) \& #9d2c5680;
     v \oplus = (v \ll 15) \& \#efc60000;
     return (v \oplus (v \gg 18));
This code is used in section 56.
60.
\langle MersenneTwister :: drand code 60 \rangle \equiv
  inline double MersenneTwister::drand()
     uint32 a = lrand() \gg 5;
     uint32 b = lrand() \gg 6;
     return (a * 67108864.0 + b) * (1.0/9007199254740992.0);
This code is used in section 56.
61. PRNG of D. Knuth
\langle MersenneTwister :: seed code 61 \rangle \equiv
  inline void MersenneTwister:: seed(uint32 iseed)
     statevec[0] = iseed \& #ffffffff_{UL};
     for (int i = 1; i < STATE\_SIZE; i \leftrightarrow) {
       register uint32 val = statevec[i-1] \gg 30;
       val \oplus = statevec[i-1];
       val *= 1812433253_{UL};
       val += i;
       statevec[i] = val \& #ffffffff_{UL};
     refresh();
This code is used in section 56.
62.
\langle MersenneTwister :: refresh code 62 \rangle \equiv
  inline void MersenneTwister::refresh()
     register uint32 *p = statevec;
     for (int i = \text{STATE\_SIZE} - \text{RECUR\_OFFSET}; i - \cdot \cdot \cdot + p) *p = twist(p[\text{RECUR\_OFFSET}], p[0], p[1]);
     for (int i = \text{RECUR\_OFFSET}; --i; ++p) *p = twist(p[\text{RECUR\_OFFSET} - \text{STATE\_SIZE}], p[0], p[1]);
     *p = twist(p[RECUR\_OFFSET - STATE\_SIZE], p[0], statevec[0]);
     stateptr = 0;
```

63. End of mersenne\_twister.h file.

#### 64. Faa Di Bruno evaluator. Start of faa\_di\_bruno.h file.

This defines a class which implements Faa Di Bruno Formula

$$[B_{s^k}]_{\alpha_1...\alpha_l} = [f_{z^l}]_{\beta_1...\beta_l} \sum_{c \in M_{l,k}} \prod_{m=1}^l \left[ z_{s^k(c_m)} \right]_{c_m(\alpha)}^{\beta_m}$$

```
where s^k is a general symmetry of dimension k and z is a stack of functions.
#ifndef FAA_DI_BRUNO_H
#define FAA_DI_BRUNO_H
#include "journal.h"
#include "stack_container.h"
#include "t_container.h"
#include "sparse_tensor.h"
#include "gs_tensor.h"
  ⟨ FaaDiBruno class declaration 65⟩;
#endif
65. Nothing special here. See (FaaDiBruno::calculate folded sparse code 68) for reason of having
magic\_mult.
\langle FaaDiBruno class declaration 65\rangle \equiv
  class FaaDiBruno {
    Journal & journal;
  public:
    FaaDiBruno(Journal \&jr)
    : journal(jr) \{ \}
    void calculate(const StackContainer(FGSTensor) & cont,
         const TensorContainer (FSSparseTensor) & f, FGSTensor & out);
    void calculate (const FoldedStackContainer &cont, const FGSContainer &g, FGSTensor
    void calculate (const StackContainer (UGSTensor) & cont,
         const TensorContainer (FSSparseTensor) & f, UGSTensor & out);
    \mathbf{void}\ \mathit{calculate}(\mathbf{const}\ \mathbf{UnfoldedStackContainer}\ \&\mathit{cont}, \mathbf{const}\ \mathbf{UGSContainer}\ \&\mathit{g}, \mathbf{UGSTensor}
         \&out);
  protected:
    int estimRefinment (const TensorDimens & tdims, int nr, int l, int & avmem_-mb, int & tmpmem_-mb);
    static double magic_mult;
  };
This code is used in section 64.
```

66. End of faa\_di\_bruno.h file.

This code is used in section 67.

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```
Start of faa_di_bruno.cpp file.
#include "faa_di_bruno.h"
#include "fine_container.h"
#include <cmath>
       double FaaDiBruno:: magic\_mult = 1.5;
        ⟨ FaaDiBruno :: calculate folded sparse code 68⟩;
           FaaDiBruno:: calculate folded dense code 69);
           FaaDiBruno:: calculate unfolded sparse code 70);
           FaaDiBruno:: calculate unfolded dense code 71 \rangle;
        \langle FaaDiBruno :: estimRefinment code 72 \rangle;
68. We take an opportunity to refine the stack container to avoid allocation of more memory than available.
\langle FaaDiBruno :: calculate folded sparse code 68\rangle \equiv
       \mathbf{void} \ \mathbf{FaaDiBruno} :: calculate (\mathbf{const} \ \mathbf{StackContainer} \langle \mathbf{FGSTensor} \rangle \ \& cont, \mathbf{const}
                                    TensorContainer\langle FSSparseTensor \rangle \& f, FGSTensor \& out \rangle
              out.zeros();
              for (int l = 1; l \leq out.dimen(); l \leftrightarrow ) {
                      int mem_mb, p_size_mb;
                      int max = estimRefinment(out.getDims(), out.nrows(), l, mem_mb, p_size_mb);
                      FoldedFineContainer fine_cont(cont, max);
                      fine\_cont.multAndAdd(l, f, out);
                      JournalRecord recc(journal);
                      \mathit{recc} \ll \texttt{"dim="} \ll l \ll \texttt{"} \sqcup \texttt{avmem="} \ll \mathit{mem\_mb} \ll \texttt{"} \sqcup \texttt{tmpmem="} \ll \mathit{p\_size\_mb} \ll \texttt{"} \sqcup \texttt{max="} \ll \mathit{max} \ll \mathit{max}
                                     "\_stacks=" \ll cont.numStacks() \ll "->" \ll fine\_cont.numStacks() <math>\ll endrec;
       }
This code is cited in sections 65 and 70.
This code is used in section 67.
              Here we just simply evaluate multAndAdd for the dense container. There is no opportunity for tuning.
\langle FaaDiBruno:: calculate folded dense code 69\rangle \equiv
       void FaaDiBruno::calculate(const FoldedStackContainer &cont, const FGSContainer
                                    \&g, \mathbf{FGSTensor} \&out)
              out.zeros();
              for (int l = 1; l \leq out.dimen(); l \leftrightarrow ) {
                      long int mem = SystemResources :: availableMemory();
                      cont.multAndAdd(l, g, out);
                      JournalRecord rec(journal);
                      int mem\_mb = mem/1024/1024;
                      rec \ll "dim=" \ll l \ll "_avmem=" \ll mem_mb \ll endrec;
```

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This is the same as (FaaDiBruno::calculate folded sparse code 68). The only difference is that we construct unfolded fine container.  $\langle$  FaaDiBruno:: calculate unfolded sparse code 70 $\rangle$   $\equiv$  $\mathbf{void} \ \mathbf{FaaDiBruno} :: \mathit{calculate} (\mathbf{const} \ \mathbf{StackContainer} \langle \mathbf{UGSTensor} \rangle \ \& \mathit{cont}, \mathbf{const}$ TensorContainer  $\langle FSSparseTensor \rangle \& f, UGSTensor \& out \rangle$ out.zeros(); for (int l = 1;  $l \leq out.dimen()$ ;  $l \leftrightarrow )$  { int  $mem\_mb$ ,  $p\_size\_mb$ ;  $int max = estimRefinment(out.getDims(), out.nrows(), l, mem\_mb, p\_size\_mb);$ **UnfoldedFineContainer** fine\_cont(cont, max);  $fine\_cont.multAndAdd(l, f, out);$ **JournalRecord** *recc*(*journal*);  $recc \ll "dim=" \ll l \ll "\_avmem=" \ll mem\_mb \ll "\_tmpmem=" \ll p\_size\_mb \ll "\_max=" \ll max \ll$ " $\_$ stacks="  $\ll cont.numStacks() \ll "->" \ll fine\_cont.numStacks() <math>\ll endrec;$ } This code is used in section 67. 71. Again, no tuning opportunity here.  $\langle$  FaaDiBruno :: calculate unfolded dense code 71  $\rangle \equiv$ void FaaDiBruno::calculate(const UnfoldedStackContainer &cont,const UGSContainer &g, UGSTensor &out) out.zeros(); for (int l = 1;  $l \leq out.dimen()$ ;  $l \leftrightarrow )$  { long int mem = SystemResources::availableMemory(); cont.multAndAdd(l, g, out);JournalRecord rec(journal);

This code is used in section 67.

}

int  $mem_{-}mb = mem/1024/1024;$ 

 $rec \ll "dim=" \ll l \ll " \square avmem=" \ll mem\_mb \ll endrec;$ 

**72.** This function returns a number of maximum rows used for refinement of the stacked container. We want to set the maximum so that the expected memory consumption for the number of paralel threads would be less than available memory. On the other hand we do not want to be too pesimistic since a very fine refinement can be very slow.

Besides memory needed for a dense unfolded slice of a tensor from f, each thread needs  $magic\_mult*per\_size$  bytes of memory. In the worst case,  $magic\_mult$  will be equal to 2, this means memory  $per\_size$  for target temporary (permuted symmetry) tensor plus one copy for intermediate result. However, this shows to be too pesimistic, so we set  $magic\_mult$  to 1.5. The memory for permuted symmetry temporary tensor  $per\_size$  is estimated as a weighted average of unfolded memory of the out tensor and unfolded memory of a symetric tensor with the largest coordinate size. Some experiments showed that the best combination of the two is to take 100% if the latter, so we set lambda to zero.

The max number of rows in the refined cont must be such that each slice fits to remaining memory. Number of columns of the slice are never greater  $max^{l}$ . (This is not true, since stacks corresponding to unit/zero matrices cannot be further refined). We get en equation:

```
nthreads \cdot max^{l} \cdot 8 \cdot r = mem - magic\_mult \cdot nthreads \cdot per\_size \cdot 8 \cdot r,
```

where mem is available memory in bytes, nthreads is a number of threads, r is a number of rows, and 8 is sizeof(double).

If the right hand side is less than zero, we set max to 10, just to let it do something.

```
\langle FaaDiBruno :: estimRefinment code 72 \rangle \equiv
  int FaaDiBruno::estimRefinment(const TensorDimens &tdims, int nr, int l, int &avmem_mb, int
           &tmpmem_{-}mb)
    int nthreads = THREAD_GROUP::max_parallel_threads;
    long int per\_size1 = tdims.calcUnfoldMaxOffset();
    long int per\_size2 = (long int) pow((double) tdims.getNVS().getMax(),l);
    double lambda = 0.0;
    long int per\_size = sizeof(double) * nr * (long int)(lambda * per\_size1 + (1 - lambda) * per\_size2);
    long int mem = SystemResources :: availableMemory();
    int max = 0;
    double num\_cols = ((\mathbf{double})(mem - magic\_mult * nthreads * per\_size))/nthreads/sizeof(\mathbf{double})/nr;
    if (num\_cols > 0) {
       double maxd = pow(num\_cols, ((double) 1)/l);
       max = (int) floor(maxd);
    if (max \equiv 0) {
       max = 10;
       JournalRecord rec(journal);
       rec \ll "dim=" \ll l \ll " \sqcup run \sqcup out \sqcup of \sqcup memory, \sqcup imposing \sqcup max=" \ll max;
       if (nthreads > 1) rec \ll " (decrease number of threads)";
       rec \ll endrec;
    avmem_{-}mb = mem/1024/1024;
    tmpmem\_mb = (nthreads * per\_size)/1024/1024;
    return max;
  }
This code is used in section 67.
```

73. End of faa\_di\_bruno.cpp file.

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## 74. Retrieving derivatives.

```
First order at deterministic steady. Start of first_order.h file.
\#ifndef FIRST_ORDER_H
#define FIRST_ORDER_H
#include "korder.h"
  ⟨ FirstOrder class declaration 76⟩;
  ⟨ FirstOrderDerivs class declaration 77⟩;
#endif
76.
\langle FirstOrder class declaration 76 \rangle \equiv
  template(int) class FirstOrderDerivs;
  class FirstOrder {
    template(int) friend class FirstOrderDerivs;
    PartitionY ypart;
    int nu;
    TwoDMatrix gy;
    TwoDMatrix gu;
    bool bk\_cond;
    double b_error;
    int sdim;
    Vector alphar;
    Vector alphai;
    Vector beta;
    double qz_criterium;
    Journal & journal;
  public:
    FirstOrder(int num_stat, int num_pred, int num_both, int num_forw, int num_u, const
             FSSparseTensor & f, Journal & jr, double qz_crit)
    : ypart(num\_stat, num\_pred, num\_both, num\_forw), nu(num\_u), gy(ypart.ny(), ypart.nys()),
           gu(ypart.ny(), nu), \ alphar(ypart.ny() + ypart.nboth), \ alphai(ypart.ny() + ypart.nboth),
           beta(ypart.ny() + ypart.nboth), qz\_criterium(qz\_crit), journal(jr) \{ solve(\mathbf{FFSTensor}(f)); \}
    bool isStable() const
    { return bk_cond; }
    const TwoDMatrix \&getGy() const
    \{ \mathbf{return} \ gy; \}
    const TwoDMatrix \&getGu() const
    \{ \mathbf{return} \ gu; \}
  protected:
    void solve(\mathbf{const}\ \mathbf{TwoDMatrix}\ \& f);
    void journalEigs();
  };
This code is cited in section 182.
This code is used in section 75.
```

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```
This class only converts the derivatives g_{y^*} and g_u to a folded or unfolded container.
\langle \mathbf{FirstOrderDerivs} \ \mathbf{class} \ \mathbf{declaration} \ 77 \rangle \equiv
  template \langle \text{int } t \rangle class FirstOrderDerivs : public ctraits \langle t \rangle :: Tg
  public:
     FirstOrderDerivs(const FirstOrder &fo)
     : \mathbf{ctraits}\langle t \rangle :: Tg(4) {
       IntSequence nvs(4);
       nvs[0] = fo.ypart.nys();
       nvs[1] = fo.nu;
       nvs[2] = fo.nu;
       nvs[3] = 1;
       \_Ttensor *ten = new \_Ttensor(fo.ypart.ny(), TensorDimens(Symmetry(1, 0, 0, 0), nvs));
       ten \neg zeros();
       ten \rightarrow add(1.0, fo.gy);
       \mathbf{this} \neg insert(ten):
       ten = new _Ttensor(fo.ypart.ny(), TensorDimens(Symmetry(0, 1, 0, 0), nvs));
       ten \neg zeros();
       ten \rightarrow add(1.0, fo.gu);
       \mathbf{this} \neg insert(ten);
  }
This code is used in section 75.
      End of first_order.h file.
78.
79.
      Start of first_order.cpp file.
#include "kord_exception.h"
#include "first_order.h"
#include <dynlapack.h>
  double qz_criterium = 1.000001;
  ⟨ order_eigs function code 80 ⟩;
  \langle \mathbf{FirstOrder} :: solve \ code \ 81 \rangle;
  ⟨ FirstOrder :: journalEigs code 93⟩;
80. This is a function which selects the eigenvalues pair used by dqqes. See documentation to DGGES for
details. Here we want to select (return true) the pairs for which \alpha < \beta.
\langle order\_eigs \text{ function code } 80 \rangle \equiv
  lapack_intorder_eigs(const double *alphar, const double *alphai, const double *beta)
     return (*alphar **alphar +*alphai **alphai <*beta **beta * qz_criterium);
This code is used in section 79.
```

81. Here we solve the linear approximation. The result are the matrices  $g_{y^*}$  and  $g_u$ . The method solves the first derivatives of g so that the following equation would be true:

$$E_t[F(y_{t-1}^*, u_t, u_{t+1}, \sigma)] = E_t[f(g^{**}(g^*(y_{t-1}^*, u_t, \sigma), u_{t+1}, \sigma), g(y_{t-1}^*, u_t, \sigma), y_{t-1}^*, u_t)] = 0$$

where f is a given system of equations.

This code is used in section 79.

It is known that  $g_{y^*}$  is given by  $F_{y^*} = 0$ ,  $g_u$  is given by  $F_u = 0$ , and  $g_{\sigma}$  is zero. The only input to the method are the derivatives fd of the system f, and partitioning of the vector g (from object).

```
 \begin{array}{l} \left\langle \mathbf{FirstOrder} :: solve \; \mathrm{code} \; 81 \right\rangle \equiv \\ \mathbf{void} \; \mathbf{FirstOrder} :: solve (\mathbf{const} \; \mathbf{TwoDMatrix} \; \& fd) \\ \left\{ \\ \mathbf{JournalRecordPair} \; pa(journal); \\ pa \ll \text{"Recovering}\_first\_order\_derivatives}\_\text{"} \ll endrec; \\ :: qz\_criterium = \mathbf{FirstOrder} :: qz\_criterium; \\ \left\langle \mathrm{solve} \; \mathrm{derivatives} \; gy \; 82 \right\rangle; \\ \left\langle \mathrm{solve} \; \mathrm{derivatives} \; gu \; 92 \right\rangle; \\ journalEigs(); \\ \mathbf{if} \; (\neg gy.isFinite() \lor \neg gu.isFinite()) \; \{ \\ \mathbf{throw} \; \mathbf{KordException}(\_FILE\_\_, \_LINE\_\_, \\ \\ \text{"NaN}\_or\_Inf\_asserted\_in\_first\_order\_derivatives\_in\_FirstOrder::solve"); \\ \} \\ \} \end{array}
```

The derivatives  $g_{y^*}$  are retrieved from the equation  $F_{y^*} = 0$ . The calculation proceeds as follows:

1) For each variable appearing at both t-1 and t-1 we add a dummy variable, so that the predetermined variables and forward looking would be disjoint. This is, the matrix of the first derivatives of the system written as:

$$\begin{bmatrix} f_{y_+^{**}} & f_{ys} & f_{yp} & f_{yb} & f_{yf} & f_{y_-^*} \end{bmatrix},$$

where  $f_{ys}$ ,  $f_{yp}$ ,  $f_{yb}$ , and  $f_{yf}$  are derivatives wrt static, predetermined, both, forward looking at time t, is rewritten to the matrix:

where the second line has number of rows equal to the number of both variables.

Next, provided that forward looking and predetermined are disjoint, the equation  $F_{y^*} = 0$  is written as:

$$\left[f_{+}y_{+}^{**}\right]\left[g_{y^{*}}^{**}\right]\left[g_{y^{*}}^{*}\right]+\left[f_{ys}\right]\left[g_{y^{*}}^{s}\right]+\left[f_{y^{*}}\right]\left[g_{y^{*}}^{*}\right]+\left[f_{y^{**}}\right]\left[g_{y^{*}}^{**}\right]+\left[f_{y_{-}^{*}}\right]=0$$

This is rewritten as

$$\begin{bmatrix} f_{y^*} & 0 & f_{y_{+}^{**}} \end{bmatrix} \begin{bmatrix} I \\ g_{y^*}^s \\ g_{y^*}^{**} \end{bmatrix} \begin{bmatrix} g_{y^*}^* \end{bmatrix} + \begin{bmatrix} f_{y_{-}^*} & f_{y^s} & f_{y^{**}} \end{bmatrix} \begin{bmatrix} I \\ g_{y^*}^s \\ g_{y^*}^{**} \end{bmatrix} = 0$$

Now, in the above equation, there are the auxiliary variables standing for copies of both variables at time t+1. This equation is then rewritten as:

$$\begin{bmatrix} f_{yp} & f_{yb} & 0 & f_{y_+^{**}} \\ 0 & I & 0 & 0 \end{bmatrix} \begin{bmatrix} I \\ g_{y_*^*}^* \\ g_{y_*^{**}}^{**} \end{bmatrix} \begin{bmatrix} g_{y_*^{*}}^* \end{bmatrix} + \begin{bmatrix} f_{y_-^{*}} & f_{ys} & 0 & f_{yf} \\ 0 & 0 & -I & 0 \end{bmatrix} \begin{bmatrix} I \\ g_{y_*^{*}}^* \\ g_{y_*^{*}}^{**} \end{bmatrix} = 0$$

The two matrices are denoted as D and -E, so the equation takes the form:

$$D\begin{bmatrix}I\\g^s_{y^*}\\g^{**}_{y^*}\\g^{**}_{y^*}\end{bmatrix}\left[g^*_{y^*}\right] = E\begin{bmatrix}I\\g^s_{y^*}\\g^{**}_{y^*}\end{bmatrix}$$

3) Next we solve the equation by Generalized Schur decomposition:

$$\begin{bmatrix} T_{11} & T_{12} \\ 0 & T_{22} \end{bmatrix} \begin{bmatrix} Z_{11}^T & Z_{21}^T \\ Z_{12}^T & Z_{22}^T \end{bmatrix} \begin{bmatrix} I \\ X \end{bmatrix} \begin{bmatrix} g_{y^*}^* \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ 0 & S_{22} \end{bmatrix} \begin{bmatrix} Z_{11}^T & Z_{21}^T \\ Z_{12}^T & Z_{22}^T \end{bmatrix} \begin{bmatrix} I \\ X \end{bmatrix}$$

We reorder the eigenvalue pair so that  $S_{ii}/T_{ii}$  with modulus less than one would be in the left-upper part.

4) The Blanchard-Kahn stability argument implies that the pairs with modulus less that one will be in and only in  $S_{11}/T_{11}$ . The exploding paths will be then eliminated when

$$\begin{bmatrix} Z_{11}^T & Z_{21}^T \\ Z_{12}^T & Z_{22}^T \end{bmatrix} \begin{bmatrix} I \\ X \end{bmatrix} = \begin{bmatrix} Y \\ 0 \end{bmatrix}$$

From this we have,  $Y = Z_{11}^{-1}$ , and  $X = Z_{21}Y$ , or equivalently  $X = -Z_{22}^{-T}Z_{12}^{T}$ . From the equation, we get  $\begin{bmatrix} g_{y^*}^* \end{bmatrix} = Y^{-1}T_{11}^{-1}S_{11}Y$ , which is  $Z_{11}T_{11}^{-1}S_{11}Z_{11}^{-1}$ .

5) We then copy the derivatives to storage gy. Note that the derivatives of both variables are in X and in

 $[g_{y^*}^*]$ , so we check whether the two submatrices are the same. The difference is only numerical error.

```
\langle \text{ solve derivatives } gy \mid 82 \rangle \equiv
  \langle setup submatrices of f 83\rangle;
   \langle \text{ form matrix } D \text{ 84} \rangle;
   \langle \text{ form matrix } E \text{ 85} \rangle;
   (solve generalized Schur 86);
   (make submatrices of right space 87);
   (calculate derivatives of static and forward 88);
   (calculate derivatives of predetermined 89);
   \langle \text{ copy derivatives to } qy \text{ 90} \rangle;
   (check difference for derivatives of both 91);
This code is used in section 81.
83. Here we setup submatrices of the derivatives fd.
\langle setup submatrices of f 83\rangle \equiv
  int off = 0;
  ConstTwoDMatrix fyplus(fd, off, ypart.nyss());
  off += ypart.nyss();
  ConstTwoDMatrix fyszero(fd, off, ypart.nstat);
  off += ypart.nstat;
  ConstTwoDMatrix fypzero (fd, off, ypart.npred);
  off += ypart.npred;
  ConstTwoDMatrix fybzero(fd, off, ypart.nboth);
  off += ypart.nboth;
  ConstTwoDMatrix fyfzero(fd, off, ypart.nforw);
  off += ypart.nforw;
  ConstTwoDMatrix fymins(fd, off, ypart.nys());
  off += ypart.nys();
  ConstTwoDMatrix fuzero(fd, off, nu);
  off += nu;
This code is used in section 82.
84.
\langle \text{ form matrix } D | 84 \rangle \equiv
  lapack\_intn = ypart.ny() + ypart.nboth;
  TwoDMatrix matD(n, n);
  matD.zeros();
  matD.place(fypzero, 0, 0);
  matD.place(fybzero, 0, ypart.npred);
  matD.place(fyplus, 0, ypart.nys() + ypart.nstat);
  for (int i = 0; i < ypart.nboth; i++) matD.qet(ypart.ny() + i, ypart.npred + i) = 1.0;
This code is used in section 82.
```

sfder.mult(-1);This code is used in section 82.

```
85.
\langle \text{ form matrix } E | 85 \rangle \equiv
  TwoDMatrix matE(n, n);
  matE.zeros();
  matE.place(fymins, 0, 0);
  matE.place(fyszero, 0, ypart.nys());
  matE.place(\mathit{fyfzero}\,, 0, \mathit{ypart.nys}\,(\,) + \mathit{ypart.nstat} + \mathit{ypart.nboth});
  for (int i = 0; i < ypart.nboth; i++) matE.get(ypart.ny() + i, ypart.nys() + ypart.nstat + i) = -1.0;
  matE.mult(-1.0);
This code is used in section 82.
86.
\langle solve generalized Schur 86\rangle \equiv
  TwoDMatrix vsl(n, n);
  TwoDMatrix vsr(n, n);
  lapack\_int lwork = 100 * n + 16;
  Vector work(lwork);
  lapack\_int * bwork = \mathbf{new} \ lapack\_int[n];
  lapack_intinfo;
  lapack\_intsdim2 = sdim;
  dqges("N", "V", "S", order\_eigs, &n, matE.getData().base(), &n, matD.getData().base(), &n, &sdim2,
       alphar.base(), alphai.base(), beta.base(), vsl.getData().base(), &n, vsr.getData().base(), &n,
       work.base(), &lwork, bwork, &info);
  if (info) {
     throw KordException(__FILE__, __LINE__, "DGGES_returns_an_error_in_FirstOrder::solve");
  sdim = sdim2;
  bk\_cond = (sdim \equiv ypart.nys());
  delete[] bwork;
This code is used in section 82.
87. Here we setup submatrices of the matrix Z.
\langle make submatrices of right space 87\rangle \equiv
  ConstGeneralMatrix z11(vsr, 0, 0, ypart.nys(), ypart.nys());
  ConstGeneralMatrix z12(vsr, 0, ypart.nys(), ypart.nys(), n - ypart.nys());
  \textbf{ConstGeneralMatrix} \ \textit{z21} (\textit{vsr}, \textit{ypart.nys}(), 0, n-\textit{ypart.nys}(), \textit{ypart.nys}());
  ConstGeneralMatrix z22(vsr, ypart.nys(), ypart.nys(), n - ypart.nys(), n - ypart.nys());
This code is used in section 82.
88. Here we calculate X = -Z_{22}^{-T}Z_{12}^{T}, where X is sfder in the code.
\langle calculate derivatives of static and forward 88\rangle \equiv
  GeneralMatrix sfder(z12, "transpose");
  z22.multInvLeftTrans(sfder);
```

This code is used in section 81.

```
Here we calculate g_{y^*}^* = Z_{11}T_{11}^{-1}S_{11}Z_{11}^{-1} = Z_{11}T_{11}^{-1}(Z_{11}^{-T}S_{11}^T)^T.
\langle calculate derivatives of predetermined 89\rangle \equiv
  ConstGeneralMatrix s11 (matE, 0, 0, ypart.nys(), ypart.nys());
  \textbf{ConstGeneralMatrix} \ t11 (matD, 0, 0, ypart.nys(), ypart.nys());
  GeneralMatrix dumm(s11, "transpose");
  z11.multInvLeftTrans(dumm);
  GeneralMatrix preder(dumm, "transpose");
  t11.multInvLeft(preder);
  preder.multLeft(z11);
This code is used in section 82.
\langle \text{ copy derivatives to } gy 90 \rangle \equiv
  gy.place(preder, ypart.nstat, 0);
  GeneralMatrix sder(sfder, 0, 0, ypart.nstat, ypart.nys());
  gy.place(sder, 0, 0);
  GeneralMatrix fder(sfder, ypart.nstat + ypart.nboth, 0, ypart.nforw, ypart.nys());
  gy.place(fder, ypart.nstat + ypart.nys(), 0);
This code is used in section 82.
91.
\langle check difference for derivatives of both 91\rangle \equiv
  GeneralMatrix bder((const GeneralMatrix &) sfder, ypart.nstat, 0, ypart.nboth, ypart.nys());
  GeneralMatrix bder2 (preder, ypart.npred, 0, ypart.nboth, ypart.nys());
  bder.add(-1, bder2);
  b\_error = bder.getData().getMax();
This code is used in section 82.
       The equation F_u = 0 can be written as
                                           \left[f_{y_{+}^{**}}\right]\left[g_{y_{+}^{*}}^{**}\right]\left[g_{u}^{*}\right] + \left[f_{y}\right]\left[g_{u}\right] + \left[f_{u}\right] = 0
and rewritten as
                                              \begin{bmatrix} f_y + \begin{bmatrix} 0 & f_{y_+^{**}} g_{y_-^{**}}^{**} & 0 \end{bmatrix} \end{bmatrix} g_u = f_u
This is exactly done here. The matrix \begin{bmatrix} f_y + \begin{bmatrix} 0 & f_{y_+^{**}}g_y^{**} & 0 \end{bmatrix} \end{bmatrix} is matA in the code.
\langle \text{ solve derivatives } qu \mid 92 \rangle \equiv
  GeneralMatrix matA(ypart.ny(), ypart.ny());
  matA.zeros();
  ConstGeneralMatrix gss(qy, ypart.nstat + ypart.npred, 0, ypart.nys());
  {\bf General Matrix} \ \ aux (fyplus, gss);
  matA.place(aux, 0, ypart.nstat);
  ConstGeneralMatrix fyzero(fd, 0, ypart.nys(), ypart.ny(), ypart.ny());
  matA.add(1.0, fyzero);
  gu.zeros();
  gu.add(-1.0, fuzero);
  ConstGeneralMatrix(matA).multInvLeft(gu);
```

```
93.
```

```
\langle \mathbf{FirstOrder} :: journalEigs \ \mathrm{code} \ 93 \rangle \equiv
       void FirstOrder::journalEigs()
              if (bk_cond) {
                      JournalRecord jr(journal);
                      jr \ll \texttt{"Blanchard-Kahn} \sqcup \texttt{conditition} \sqcup \texttt{satisfied,} \sqcup \texttt{model} \sqcup \texttt{stable"} \ll endrec;
              else {
                      JournalRecord jr(journal);
                     jr \ll "Blanchard-Kahn_condition_not_satisfied,_model_not_stable:_sdim=" \ll sdim delta del
                                     "_{\sqcup}" \ll "npred=" \ll ypart.nys() \ll endrec;
              if (\neg bk\_cond) {
                      for (int i = 0; i < alphar.length(); i \leftrightarrow) {
                             if (i \equiv sdim \lor i \equiv ypart.nys()) {
                                     JournalRecord jr(journal);
                                     jr \ll "-----";
                                     if (i \equiv sdim) jr \ll "sdim";
                                     else jr \ll "npred";
                                     jr \ll endrec;
                             JournalRecord jr(journal);
                             double mod = sqrt(alphar[i] * alphar[i] + alphai[i] * alphai[i]);
                             mod = mod/round(100000 * std :: abs(beta[i])) * 100000;
                             jr \ll i \ll "\t(" \ll alphar[i] \ll "," \ll alphai[i] \ll ")_{\sqcup}/_{\sqcup}" \ll beta[i] \ll "_{\sqcup\sqcup}\t" \ll mod \ll endrec;
              }
       }
This code is used in section 79.
```

94. End of first\_order.cpp file.

## 95. Higher order at deterministic steady. Start of korder.h file.

The main purpose of this file is to implement a perturbation method algorithm for an SDGE model for higher order approximations. The input of the algorithm are sparse tensors as derivatives of the dynamic system, then dimensions of vector variables, then the first order approximation to the decision rule and finally a covariance matrix of exogenous shocks. The output are higher order derivatives of decision rule  $y_t = g(y_{t-1}^*, u_t, \sigma)$ . The class provides also a method for checking a size of residuals of the solved equations.

The algorithm is implemented in **KOrder** class. The class contains both unfolded and folded containers to allow for switching (usually from unfold to fold) during the calculations. The algorithm is implemented in a few templated methods. To do this, we need some container type traits, which are in **ctraits** struct. Also, the **KOrder** class contains some information encapsulated in other classes, which are defined here. These include: **PartitionY**, **MatrixA**, **MatrixS** and **MatrixB**.

```
#ifndef KORDER_H
#define KORDER_H
#include "int_sequence.h"
#include "fs_tensor.h"
#include "gs_tensor.h"
#include "t_container.h"
#include "stack_container.h"
#include "normal_moments.h"
#include "t_polynomial.h"
#include "faa_di_bruno.h"
#include "journal.h"
#include "kord_exception.h"
#include "GeneralSylvester.h"
#include <dynlapack.h>
#include <cmath>
#define TYPENAME typename
   ctraits type traits declaration 96);
   PartitionY struct declaration 97);
   PLUMatrix class declaration 98;
   MatrixA class declaration 99);
   MatrixS class declaration 100 \;
   MatrixB class declaration 101);
  \langle \mathbf{KOrder} \ \text{class declaration } 102 \rangle;
#endif
```

Dynare++

Here we use a classical IF template, and in **ctraits** we define a number of types. We have a type for tensor *Ttensor*, and types for each pair of folded/unfolded containers used as a member in **KOrder**.

Note that we have enumeration fold and unfold. These must have the same value as the same enumeration in KOrder.

```
\langle ctraits type traits declaration 96\rangle \equiv
  class FoldedZXContainer;
  class UnfoldedZXContainer;
  class FoldedGXContainer;
  class UnfoldedGXContainer;
  template (bool condition, class Then, class Else) struct IF {
    typedef Then RET;
  template \langle class Then, class Else \rangle struct IF \langle false, Then, Else \rangle 
    typedef Else RET;
  template \langle int \ type \rangle class ctraits {
  public:
    enum { fold, unfold };
    typedef TYPENAME IF \langle type \equiv fold, FGSTensor, UGSTensor \rangle:: RET Ttensor;
    typedef TYPENAME IF\langle type \equiv fold, FFSTensor, UFSTensor \rangle :: RET Ttensym;
    typedef TYPENAME IF \langle type \equiv fold, FGSContainer, UGSContainer \rangle :: RET Tg;
    typedef TYPENAME IF \langle type \equiv fold, FGSContainer, UGSContainer \rangle:: RET Tgs;
    typedef TYPENAME IF \langle type \equiv fold, FGSContainer, UGSContainer \rangle :: RET Tgss;
    typedef TYPENAME IF \langle type \equiv fold, FGSContainer, UGSContainer \rangle :: RET TG;
    typedef TYPENAME IF \langle type \equiv fold, FoldedZContainer, UnfoldedZContainer\rangle::RET
         TZstack;
    typedef TYPENAME IF \langle type \equiv fold, FoldedGContainer, UnfoldedGContainer\rangle::RET
    typedef TYPENAME IF \langle type \equiv fold, FNormalMoments, UNormalMoments \rangle :: RET Tm;
    typedef TYPENAME IF \langle type \equiv fold, FTensorPolynomial, UTensorPolynomial \rangle :: RET Tpol;
    typedef TYPENAME IF \langle type \equiv fold, FoldedZXContainer, UnfoldedZXContainer\rangle::RET
         TZXstack:
    typedef TYPENAME IF \langle type \equiv fold, FoldedGXContainer, UnfoldedGXContainer\rangle:: RET
         TGXstack;
  };
This code is used in section 95.
```

This code is used in section 95.

**97.** The **PartitionY** class defines the partitioning of state variables y. The vector y, and subvector  $y^*$ , and  $y^{**}$  are defined.

$$y = \begin{bmatrix} \text{static} \\ \text{predeter} \\ \text{both} \\ \text{forward} \end{bmatrix}, \quad y^* = \begin{bmatrix} \text{predeter} \\ \text{both} \end{bmatrix}, \quad y^{**} = \begin{bmatrix} \text{both} \\ \text{forward} \end{bmatrix},$$

where "static" means variables appearing only at time t, "predeter" means variables appearing at time t-1, but not at t+1, "both" means variables appearing both at t-1 and t+1 (regardless appearance at t), and "forward" means variables appearing at t+1, but not at t-1.

The class maintains the four lengths, and returns the whole length, length of  $y^s$ , and length of  $y^{**}$ .

```
\langle \mathbf{PartitionY} \ \text{struct declaration } 97 \rangle \equiv
  struct PartitionY {
    const int nstat;
    const int npred;
    const int nboth;
    const int nforw;
    PartitionY (int num_stat, int num_pred, int num_both, int num_forw)
    : nstat(num_stat), npred(num_pred), nboth(num_both), nforw(num_forw) { }
    int ny() const
    { return nstat + npred + nboth + nforw; }
    int nys() const
    { return npred + nboth; }
    int nyss() const
    \{ \mathbf{return} \ nboth + nforw; \}
  };
This code is cited in section 102.
```

**PartitionY** & ypart);

This code is used in section 95.

**}**;

**98.** This is an abstraction for a square matrix with attached PLU factorization. It can calculate the PLU factorization and apply the inverse with some given matrix.

We use LAPACK PLU decomposition for the inverse. We store the L and U in the inv array and ipiv is the permutation P.

```
\langle PLUMatrix class declaration 98 \rangle \equiv
  class PLUMatrix : public TwoDMatrix {
  public:
     PLUMatrix(int n)
     : \mathbf{TwoDMatrix}(n, n), inv(nrows() * ncols()), ipiv(\mathbf{new}\ lapack\_int[nrows()]) {}
     PLUMatrix (const PLUMatrix & plu);
     virtual \sim PLUMatrix()
        delete[] ipiv;
     void multInv(TwoDMatrix &m) const;
  private:
     Vector inv;
     lapack\_int * ipiv;
  protected:
     void calcPLU();
  };
This code is used in section 95.
99. The class MatrixA is used for matrix [f_y] + \left[0\left[f_{y_+^{**}}\right] \cdot \left[g_{y_*^*}^{**}\right] 0\right], which is central for the perturbation
method step.
\langle Matrix A class declaration 99 \rangle \equiv
  class MatrixA: public PLUMatrix {
  public:
     MatrixA(const FSSparseTensor &f, const IntSequence &ss, const TwoDMatrix &gy, const
           PartitionY & ypart);
  };
This code is cited in section 102.
This code is used in section 95.
        The class MatrixS slightly differs from MatrixA. It is used for matrix
                                   [f_y] + \begin{bmatrix} 0 & \left\lceil f_{y_+^{**}} \right\rceil \cdot \left\lceil g_{y_+^{**}}^{**} \right\rceil & 0 \right\rceil + \left\lceil 0 & 0 & \left\lceil f_{y_+^{**}} \right\rceil \right\rceil
, which is needed when recovering g_{\sigma^k}.
\langle MatrixS class declaration 100 \rangle \equiv
  class MatrixS : public PLUMatrix {
  public:
     MatrixS(const\ FSSparseTensor\ \&f, const\ IntSequence\ \&ss, const\ TwoDMatrix\ \&gy, const
```

```
\S 101
         {\bf Dynare}{+}{+}
                                                                 HIGHER ORDER AT DETERMINISTIC STEADY
                                                                                                                          39
        The B matrix is equal to \left[f_{y_{+}^{**}}\right]. We have just a constructor.
\langle MatrixB class declaration 101\rangle \equiv
  class MatrixB : public TwoDMatrix \{
  public:
     MatrixB(const\ FSSparseTensor\ \&f, const\ IntSequence\ \&ss)
     : \mathbf{TwoDMatrix}(\mathbf{FGSTensor}(f, ss, \mathbf{IntSequence}(1, 0), \mathbf{TensorDimens}(ss, \mathbf{IntSequence}(1, 0)))) \ \{ \ \}
  };
This code is cited in section 102.
This code is used in section 95.
```

Here we have the class for the higher order approximations. It contains the following data:

**PartitionY** struct maintaining partitions of y, see  $\langle$  **PartitionY** variable sizes ypart struct declaration 97 tensor variable dimension variable sizes of all tensors in containers, sizes of  $y^*$ , u, u' and  $\sigma$ tensor containers folded and unfolded containers for  $g, g_{y^*}, g_{y^{**}}$  (the latter two collect appropriate subtensors of g, they do not allocate any new space), G, G stack, Z stack dynamic model derivajust a reference to the container of sparse tensors of the system derivatives, lives outside the class tives moments both folded and unfolded normal moment containers, both are calculated at initialization matrices

matrix A, matrix S, and matrix B, see  $\langle Matrix A$  class declara-

tion 99 and (MatrixB class declaration 101)

## The methods are the following:

member access we declare template methods for accessing containers depending on fold and unfold flag, we implement their specializations performStepthis performs k-order step provided that k = 2 or the k - 1-th step has been run, this is the core method

this calculates residuals of all solved equations for k-order and check

reports their sizes, it is runnable after k-order performStep has

been run

insertDerivativeinserts a g derivative to the g container and also creates subtensors

and insert them to  $g_{y^*}$  and  $g_{y^{**}}$  containers

sylvester Solvesolve the sylvester equation (templated fold, and unfold)

faaDiBrunoZcalculates derivatives of F by Faa Di Bruno for the sparse con-

tainer of system derivatives and Z stack container

faaDiBrunoGcalculates derivatives of G by Faa Di Bruno for the dense container

 $g^{**}$  and G stack

 $recover_{-}y$ recovers  $g_{y^{*i}}$ recovers  $g_{y^{*i}u^j}$  $recover\_yu$ recovers  $g_{y^{*i}\sigma^j}$  $recover\_ys$ recover\_yus recovers  $g_{u^{*i}u^{j}\sigma^{k}}$  $recover\_s$ recovers  $g_{\sigma^i}$ 

calculates specified derivatives of G and inserts them to the confillG

 $calcE_{-}ijk$ calculates  $E_{ijk}$  $calcD_{-}ijk$ calculates  $D_{ijk}$ 

Most of the code is templated, and template types are calculated in ctraits. So all templated methods get a template argument T, which can be either fold, or unfold. To shorten a reference to a type calculated by **ctraits** for a particular t, we define the following macros.

```
#define _Ttensor TYPENAME ctraits \langle t \rangle::Ttensor
#define _Ttensym TYPENAME ctraits \langle t \rangle::Ttensym
#define _{\text{T}}TYPENAME ctraits\langle t \rangle::Tg
#define \_Tgs TYPENAME ctraits\langle t \rangle::Tgs
```

```
#define \_Tgss TYPENAME ctraits\langle t \rangle::Tgss
#define _{\text{T}}TG TYPENAME ctraits\langle t \rangle::TG
#define _TZstack TYPENAME ctraits \langle t \rangle :: TZstack
#define _{\text{T}}Gstack TYPENAME ctraits\langle t \rangle::TGstack
#define \_TZXstack TYPENAME ctraits \langle t \rangle::TZXstack
#define _{\text{TGX}}stack _{\text{TYPENAME}} ctraits\langle t \rangle::_{\text{TGX}}stack
#define \_Tm TYPENAME ctraits\langle t \rangle::Tm
#define \_Tpol TYPENAME ctraits\langle t \rangle::Tpol
\langle \mathbf{KOrder} \ \mathrm{class} \ \mathrm{declaration} \ \mathbf{102} \rangle \equiv
  class KOrder {
  protected:
     const PartitionY ypart;
     const int ny:
     const int nu:
     const int maxk;
     IntSequence nvs;
     ⟨KOrder container members 124⟩;
     const MatrixA matA;
     const MatrixS matS;
     const MatrixB matB;
     ⟨KOrder member access method declarations 125⟩;
     Journal & journal;
  public:
     KOrder(int num_stat, int num_pred, int num_both,
         int num_forw, const TensorContainer(FSSparseTensor) & fcont, const TwoDMatrix
         \&gy, const TwoDMatrix \&gu, const TwoDMatrix \&v, Journal \&jr);
     enum { fold, unfold }:
     ⟨ KOrder :: performStep templated code 118⟩;
     \langle \mathbf{KOrder} :: check \text{ templated code } 119 \rangle;
     \langle \mathbf{KOrder} :: calcStochShift \text{ templated code } 123 \rangle;
     void switchToFolded();
     const PartitionY &getPartY() const
     { return ypart; }
     const FGSContainer &getFoldDers() const
     \{ \mathbf{return} \ \_fg; \}
     const UGSContainer &getUnfoldDers() const
     { return \_ug; }
     static bool is_even(int i)
     { return (i/2) * 2 \equiv i; }
  protected:
     ⟨KOrder:: insertDerivative templated code 103⟩;
     template \langle int t \rangle void sylvesterSolve(\_Ttensor \& der) const;
     \langle \mathbf{KOrder} :: faaDiBrunoZ \text{ templated code } 104 \rangle;
      KOrder:: faaDiBrunoG templated code 105\rangle;
      KOrder:: recover_y templated code 106 \;
      KOrder:: recover_yu templated code 107 \rangle;
      KOrder:: recover_ys templated code 108);
     \langle \mathbf{KOrder} :: recover\_yus \text{ templated code } 109 \rangle;
```

```
HIGHER ORDER AT DETERMINISTIC STEADY
```

```
⟨KOrder::recover_s templated code 110⟩;
⟨KOrder::fillG templated code 111⟩;
⟨KOrder::calcD_ijk templated code 112⟩;
⟨KOrder::calcD_ik templated code 114⟩;
⟨KOrder::calcD_k templated code 115⟩;
⟨KOrder::calcE_ijk templated code 113⟩;
⟨KOrder::calcE_ik templated code 116⟩;
⟨KOrder::calcE_k templated code 117⟩;
};
This code is cited in section 182.
```

103. Here we insert the result to the container. Along the insertion, we also create subtensors and insert as well.

```
 \begin{split} & \langle \mathbf{KOrder} :: insertDerivative \ \mathbf{templated} \ \operatorname{code} \ \mathbf{103} \, \rangle \equiv \\ & \mathbf{template} \langle \mathbf{int} \ t \rangle \ \mathbf{void} \ insertDerivative ( \mathbf{\_Ttensor} \ *der) \\ & \{ \\ & g < t > ().insert(der); \\ & gs < t > ().insert(\mathbf{new} \ \mathbf{\_Ttensor}(ypart.nstat, ypart.nys(), *der)); \\ & gss < t > ().insert(\mathbf{new} \ \mathbf{\_Ttensor}(ypart.nstat + ypart.npred, ypart.nyss(), *der)); \\ & \} \end{split}
```

This code is used in section 102.

This code is used in section 102.

This code is used in section 95.

104. Here we implement Faa Di Bruno formula

$$\sum_{l=1}^{k} \left[ f_{z^{l}} \right]_{\gamma_{1} \dots \gamma_{l}} \sum_{c \in M_{l,k}} \prod_{m=1}^{l} \left[ z_{s(c_{m})} \right]^{\gamma_{m}},$$

where s is a given outer symmetry and k is the dimension of the symmetry.

```
 \begin{array}{l} \langle \mathbf{KOrder} :: faaDiBrunoZ \ \ \text{templated code } 104 \rangle \equiv \\ \mathbf{template} \langle \mathbf{int} \ t \rangle \ \ _\mathbf{Ttensor} \ *faaDiBrunoZ(\mathbf{const} \ \mathbf{Symmetry} \ \&sym) \ \mathbf{const} \\ \{ \\ \mathbf{JournalRecordPair} \ pa(journal); \\ pa \ll \text{"Faa} \Box \text{Di} \Box \text{Bruno} \Box \text{Z} \Box \text{container} \Box \text{for} \Box \text{"} \ \ll sym \ \ll endrec; \\ \Box \mathbf{Ttensor} \ *res = \mathbf{new} \ \Box \mathbf{Ttensor}(ny, \mathbf{TensorDimens}(sym, nvs)); \\ \mathbf{FaaDiBruno} \ bruno(journal); \\ bruno.calculate(Zstack < t > (), f, *res); \\ \mathbf{return} \ res; \\ \} \\ \text{This code is cited in section } 105. \end{array}
```

```
105. The same as ⟨KOrder::faaDiBrunoZ templated code 104⟩, but for g** and G stack.
⟨KOrder::faaDiBrunoG templated code 105⟩ ≡
template⟨int t⟩ _Ttensor *faaDiBrunoG(const Symmetry &sym) const
{
    JournalRecordPair pa(journal);
    pa ≪ "Faa□Di□Bruno□G□container□for□" ≪ sym ≪ endrec;
    TensorDimens tdims(sym, nvs);
    _Ttensor *res = new _Ttensor(ypart.nyss(), tdims);
    FaaDiBruno bruno(journal);
    bruno.calculate(Gstack < t > (), gss < t > (), *res);
    return res;
}
This code is used in section 102.
```

106. Here we solve  $[F_{y^i}] = 0$ . First we calculate conditional  $G_{y^i}$  (it misses l = 1 and l = i since  $g_{y^i}$  does not exist yet). Then calculate conditional  $F_{y^i}$  and we have the right hand side of equation. Since we miss two orders, we solve by Sylvester, and insert the solution as the derivative  $g_{y^i}$ . Then we need to update  $G_{y^i}$  running multAndAdd for both dimensions 1 and i.

```
Requires: everything at order \leq i - 1
  Provides: g_{y^i}, and G_{y^i}
\langle \mathbf{KOrder} :: recover\_y \text{ templated code } 106 \rangle \equiv
  template \langle int t \rangle void recover_y(int i)
    Symmetry sym(i, 0, 0, 0);
    JournalRecordPair pa(journal);
    pa \ll "Recovering_{\square} symmetry_{\square}" \ll sym \ll endrec;
    _Ttensor *G_-yi = faaDiBrunoG < t > (sym);
    G < t > ().insert(G_-yi);
    Ttensor *g_yi = faaDiBrunoZ < t > (sym);
    g_-yi \rightarrow mult(-1.0);
    sylvesterSolve < t > (*g_-yi);
    insertDerivative < t > (g_-yi);
    _Ttensor *gss_y = gss < t > ().get(Symmetry(1,0,0,0));
    qs < t > ().multAndAdd(*qss_y, *G_yi);
    _Ttensor *gss\_yi = gss < t > ().get(sym);
    gs < t > (\ ).multAndAdd (*gss\_yi, *G\_yi);
```

**107.** Here we solve  $[F_{y^i u^j}] = 0$  to obtain  $g_{y^i u^j}$  for j > 0. We calculate conditional  $G_{y^i u^j}$  (this misses only l=1) and calculate conditional  $F_{y^iu^j}$  and we have the right hand side. It is solved by multiplication of inversion of A. Then we insert the result, and update  $G_{y^i u^j}$  by multAndAdd for l=1.

```
Requires: everything at order \leq i + j - 1, G_{y^{i+j}}, and g_{y^{i+j}}.
  Provides: g_{y^i u^j}, and G_{y^i u^j}
\langle \mathbf{KOrder} :: recover\_yu \text{ templated code } 107 \rangle \equiv
  template (int t) void recover\_yu(int i, int j)
     Symmetry sym(i, j, 0, 0);
     JournalRecordPair pa(journal);
     pa \ll "Recovering_{\sqcup} symmetry_{\sqcup}" \ll sym \ll endrec;
     _Ttensor *G_yiuj = faaDiBrunoG < t > (sym);
     G < t > ().insert(G_-yiuj);
     _Ttensor *g_yiuj = faaDiBrunoZ < t > (sym);
     g_-yiuj \rightarrow mult(-1.0);
     matA.multInv(*g\_yiuj);
     insertDerivative < t > (g_yiuj);
     gs < t > ().multAndAdd(*(gss < t > ().get(Symmetry(1,0,0,0))),*G_-yiuj);
```

108. Here we solve  $\left[F_{y^i\sigma^j}\right] + \left[D_{ij}\right] + \left[E_{ij}\right] = 0$  to obtain  $g_{y^i\sigma^j}$ . We calculate conditional  $G_{y^i\sigma^j}$  (missing dimensions 1 and i+j), calculate conditional  $F_{y^i\sigma^j}$ . Before we can calculate  $D_{ij}$  and  $E_{ij}$ , we have to calculate  $G_{y^iu'^m\sigma^{j-m}}$  for  $m=1,\ldots,j$ . Then we add the  $D_{ij}$  and  $E_{ij}$  to obtain the right hand side. Then we solve the sylvester to obtain  $g_{y^i\sigma^j}$ . Then we update  $G_{y^i\sigma^j}$  for l=1 and l=i+j.

**Requires:** everything at order  $\leq i + j - 1$ ,  $g_{y^{i+j}}$ ,  $G_{y^iu^{j}}$  and  $g_{y^iu^j}$  through  $D_{ij}$ ,  $g_{y^iu^m\sigma^{j-m}}$  for  $m = 1, \ldots, j-1$  through  $E_{ij}$ .

**Provides:**  $g_{y^i\sigma^j}$  and  $G_{y^i\sigma^j}$ , and finally  $G_{y^iu'^m\sigma^{j-m}}$  for  $m=1,\ldots,j$ . The latter is calculated by fill G before the actual calculation.

```
\langle \mathbf{KOrder} :: recover\_ys \text{ templated code } 108 \rangle \equiv
  template\langle int \ t \rangle void recover\_ys(int \ i, int \ j)
     Symmetry sym(i, 0, 0, j);
     JournalRecordPair pa(journal);
     pa \ll "Recovering_{\sqcup} symmetry_{\sqcup}" \ll sym \ll endrec;
     fillG < t > (i, 0, j);
     if (is\_even(j)) {
       Ttensor *G_{-}yisj = faaDiBrunoG < t > (sym);
       G < t > ().insert(G_-yisj);
       _Ttensor *g\_yisj = faaDiBrunoZ < t > (sym);
          _Ttensor *D_i = calc D_i k < t > (i, j);
          g\_yisj \neg add(1.0, *D\_ij);
          delete D_{-}ij;
       if (j \ge 3) {
          Ttensor *E_ij = calcE_ik < t > (i, j);
          g_-yisj \rightarrow add(1.0, *E_-ij);
          delete E_{-}ij;
       g_{-}yisj \rightarrow mult(-1.0);
       sylvesterSolve < t > (*g\_yisj);
       insertDerivative < t > (g_yisj);
        Gstack < t > ().multAndAdd(1, gss < t > (), *G_yisj);
        Gstack < t > ().multAndAdd(i + j, gss < t > (), *G_yisj);
  }
```

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**109.** Here we solve  $[F_{y^i u^j \sigma^k}] + [D_{ijk}] + [E_{ijk}] = 0$  to obtain  $g_{y^i u^j \sigma^k}$ . First we calculate conditional  $G_{y^i u^j \sigma^k}$ (missing only for dimension l=1), then we evaluate conditional  $F_{y^i u^j \sigma^k}$ . Before we can calculate  $D_{ijk}$ , and  $E_{ijk}$ , we need to insert  $G_{y^iu^ju'^m\sigma^{k-m}}$  for  $m=1,\ldots,k$ . This is done by fillG. Then we have right hand side and we multiply by  $A^{-1}$  to obtain  $g_{y^iu^j\sigma^k}$ . Finally we have to update  $G_{y^iu^j\sigma^k}$  by multAndAdd for dimension

**Requires:** everything at order  $\leq i + j + k$ ,  $g_{y^{i+j}\sigma^k}$  through  $G_{y^iu^j\sigma^k}$  involved in right hand side, then  $g_{y^i u^{j+k}}$  through  $D_{ijk}$ , and  $g_{y^i u^{j+m} \sigma^{k-m}}$  for  $m=1,\ldots,k-1$  through  $E_{ijk}$ .

```
Provides: g_{y^i u^j \sigma^k}, G_{y^i u^j \sigma^k}, and G_{y^i u^j u'^m \sigma^{k-m}} for m = 1, \ldots, k
\langle \mathbf{KOrder} :: recover\_yus \text{ templated code } 109 \rangle \equiv
  template \langle int \ t \rangle void recover\_yus(int \ i, int \ j, int \ k)
     Symmetry sym(i, j, 0, k);
     JournalRecordPair pa(journal);
     pa \ll "Recovering_{\sqcup} symmetry_{\sqcup}" \ll sym \ll endrec;
     fillG < t > (i, j, k);
     if (is\_even(k)) {
        Ttensor *G-yiujsk = faaDiBrunoG < t > (sym);
        G < t > ().insert(G_yiujsk);
        _Ttensor *g\_yiujsk = faaDiBrunoZ < t > (sym);
        {
          _Ttensor *D_ijk = calcD_ijk < t > (i, j, k);
          g_{-}yiujsk \rightarrow add(1.0, *D_{-}ijk);
          delete D_{-}ijk;
        if (k \ge 3) {
           _Ttensor *E_{-}ijk = calcE_{-}ijk < t > (i, j, k);
          g_-yiujsk \rightarrow add(1.0, *E_-ijk);
          delete E_{-}ijk;
        g\_yiujsk \rightarrow mult(-1.0);
        matA.multInv(*g\_yiujsk);
        insertDerivative < t > (g_yiujsk);
        Gstack < t > ().multAndAdd(1, gss < t > (), *G_yiujsk);
```

110. Here we solve  $[F_{\sigma^i}] + [D_i] + [E_i] = 0$  to recover  $g_{\sigma^i}$ . First we calculate conditional  $G_{\sigma^i}$  (missing dimension l = 1 and l = i), then we calculate conditional  $F_{\sigma^i}$ . Before we can calculate  $D_i$  and  $E_i$ , we have to obtain  $G_{u'm\sigma^{i-m}}$  for  $m = 1, \ldots, i$ . Than adding  $D_i$  and  $E_i$  we have the right hand side. We solve by  $S^{-1}$  multiplication and update  $G_{\sigma^i}$  by calling multAndAdd for dimension l = 1.

Recall that the solved equation here is:

$$\left[f_y\right]\left[g_{\sigma^k}\right] + \left\lceil f_{y_+^{**}}\right\rceil \left[g_{y_*^*}^{**}\right]\left[g_{\sigma^k}^*\right] + \left\lceil f_{y_+^{**}}\right\rceil \left[g_{\sigma^k}^{**}\right] = \mathrm{RHS}$$

This is a sort of deficient sylvester equation (sylvester equation for dimension=0), we solve it by  $S^{-1}$ . See  $\langle$  MatrixS constructor code 132 $\rangle$  to see how S looks like.

```
Requires: everything at order \leq i-1, g_{y^i} and g_{y^{i-j}\sigma^j}, then g_{u^k} through F_{u'^k}, and g_{y^m u^j \sigma^k} for j=1,\ldots,i-1 and m+j+k=i through F_{u'j\sigma^{i-j}}.

Provides: g_{\sigma^i}, G_{\sigma^i}, and G_{u'^m\sigma^{i-m}} for m=1,\ldots,i

(KOrder:: recover_s templated code 110) \equiv template (int t) void recover s(int i)
```

```
template \langle int \ t \rangle void recover\_s(int \ i)
  Symmetry sym(0,0,0,i);
  JournalRecordPair pa(journal);
  pa \ll "Recovering_{\square} symmetry_{\square}" \ll sym \ll endrec;
  fillG < t > (0,0,i);
  if (is\_even(i)) {
     _{-}Ttensor *G_{-}si = faaDiBrunoG < t > (sym);
     G < t > ().insert(G_si);
     Ttensor *g\_si = faaDiBrunoZ < t > (sym);
       Ttensor *D_i = calcD_k < t > (i);
       q_{-}si \rightarrow add(1.0, *D_{-}i);
       delete D_{-}i;
     if (i \ge 3) {
       _Ttensor *E_i = calcE_k < t > (i);
       g_si \rightarrow add(1.0, *E_i);
       delete E_{-}i;
     g\_si \rightarrow mult(-1.0);
     matS.multInv(*g\_si);
     insertDerivative < t > (g\_si);
     Gstack < t > ().multAndAdd(1, gss < t > (), *G_si);
     Gstack < t > ().multAndAdd(i, gss < t > (), *G_si);
}
```

111. Here we calculate and insert  $G_{u^iu^ju^{\prime m}\sigma^{k-m}}$  for  $m=1,\ldots,k$ . The derivatives are inserted only for k-m being even.

```
\langle \mathbf{KOrder} :: fillG \text{ templated code } 111 \rangle \equiv
  template \langle \text{int } t \rangle void fillG(\text{int } i, \text{int } j, \text{int } k)
      for (int m = 1; m \le k; m++) {
        if (is\_even(k-m)) {
           _{-}Ttensor *G_{-}yiujupms = faaDiBrunoG < t > (Symmetry(i, j, m, k - m));
           G < t > ().insert(G_yiujupms);
     }
  }
```

This code is used in section 102.

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### 112. Here we calculate

```
\left[D_{ijk}\right]_{\alpha_1...\alpha_i\beta_1...\beta_j} = \left[F_{y^iu^ju'^k}\right]_{\alpha_1...\alpha_i\beta_1...\beta_j\gamma_1...\gamma_k} \left[\Sigma\right]^{\gamma_1...\gamma_k}
```

So it is non zero only for even k.

```
\langle \mathbf{KOrder} :: calcD_{-}ijk \text{ templated code } 112 \rangle \equiv
  template \langle int t \rangle _Ttensor *calcD_ijk(int i, int j, int k) const
     \_Ttensor *res = new \_Ttensor(ny, TensorDimens(Symmetry(i, j, 0, 0), nvs));
     res \rightarrow zeros();
     if (is\_even(k)) {
       _Ttensor *tmp = faaDiBrunoZ < t > (Symmetry(i, j, k, 0));
       tmp-contractAndAdd(2, *res, *(m < t > ().get(\mathbf{Symmetry}(k))));
       delete tmp;
     return res;
```

# 113. Here we calculate

$$[E_{ijk}]_{\alpha_1...\alpha_i\beta_1...\beta_j} = \sum_{m=1}^{k-1} {k \choose m} \left[ F_{y^i u^j u'^m \sigma^{k-m}} \right]_{\alpha_1...\alpha_i\beta_1...\beta_j \gamma_1...\gamma_m} \left[ \Sigma \right]^{\gamma_1...\gamma_m}$$

```
The sum can sum only for even m.
\langle \mathbf{KOrder} :: calcE\_ijk \text{ templated code } 113 \rangle \equiv
  template \langle int \ t \rangle _Ttensor *calcE\_ijk(int \ i,int \ j,int \ k) const
     \_Ttensor *res = new \_Ttensor(ny, TensorDimens(Symmetry(i, j, 0, 0), nvs));
     res \rightarrow zeros();
     for (int n = 2; n \le k - 1; n += 2) {
        Ttensor *tmp = faaDiBrunoZ < t > (Symmetry(i, j, n, k - n));
        tmp \neg mult((\mathbf{double})(Tensor :: noverk(k, n)));
        tmp \rightarrow contractAndAdd(2, *res, *(m < t > ().get(Symmetry(n))));
        delete tmp;
     return res;
This code is used in section 102.
114.
\langle \mathbf{KOrder} :: calcD_{-}ik \text{ templated code } 114 \rangle \equiv
  template \langle int t \rangle _Ttensor *calcD_{-}ik(int i, int k) const
     return calcD_{-}ijk < t > (i, 0, k);
This code is used in section 102.
115.
\langle \mathbf{KOrder} :: calcD_k \text{ templated code } 115 \rangle \equiv
  template \langle int t \rangle _Ttensor *calcD_{-}k(int k) const
     return calcD_{-}ijk < t > (0,0,k);
This code is used in section 102.
116.
\langle \mathbf{KOrder} :: calcE_ik \text{ templated code } \mathbf{116} \rangle \equiv
  template \langle int t \rangle _Ttensor *calcE_{-i}k(int i, int k) const
     return calcE_{-}ijk < t > (i, 0, k);
```

```
117.
```

```
 \begin{split} \langle \mathbf{KOrder} &:: calcE\_k \text{ templated code } 117 \rangle \equiv \\ \mathbf{template} \langle \mathbf{int} \ t \rangle \ \_\mathbf{Ttensor} \ * calcE\_k (\mathbf{int} \ k) \ \mathbf{const} \\ \{ \\ \mathbf{return} \ \ calcE\_ijk < t > (0,0,k); \\ \} \end{split}
```

This code is used in section 102.

118. Here is the core routine. It calls methods recovering derivatives in the right order. Recall, that the code, namely Faa Di Bruno's formula, is implemented as to be run conditionally on the current contents of containers. So, if some call of Faa Di Bruno evaluates derivatives, and some derivatives are not present in the container, then it is considered to be zero. So, we have to be very careful to put everything in the right order. The order here can be derived from dependencies, or it is in the paper.

The method recovers all the derivatives of the given order.

The precondition of the method is that all tensors of order order - 1, which are not zero, exist (including G). The postcondition of of the method is derivatives of g and G of order order are calculated and stored in the containers. Responsibility of precondition lays upon the constructor (for  $order \equiv 2$ ), or upon the previous call of performStep.

From the code, it is clear, that all g are calculated. If one goes through all the recovering methods, he should find out that also all G are provided.

```
\langle \mathbf{KOrder} :: performStep \text{ templated code } 118 \rangle \equiv
  template \langle int \ t \rangle void perform Step(int \ order)
     KORD_RAISE_IF(order - 1 \neq g < t > ().getMaxDim(), "Wrong_order_for_KOrder::performStep");
     JournalRecordPair pa(journal);
     pa \ll "Performing \sqcup step \sqcup for \sqcup order \sqcup = \sqcup" \ll order \ll endrec;
     recover_y < t > (order);
     for (int i = 0; i < order; i ++) {
       recover\_yu < t > (i, order - i);
     for (int j = 1; j < order; j ++) {
       for (int i = j - 1; i \ge 1; i - -) {
          recover\_yus < t > (order - j, i, j - i);
       recover\_ys < t > (order - j, j);
     for (int i = order - 1; i \ge 1; i--) {
       recover\_yus < t > (0, i, order - i);
     recover\_s < t > (order);
This code is used in section 102.
```

119. Here we check for residuals of all the solved equations at the given order. The method returns the largest residual size. Each check simply evaluates the equation.

```
\langle \mathbf{KOrder} :: check \text{ templated code } 119 \rangle \equiv
   template(int t) double check(int dim) const
      \texttt{KORD\_RAISE\_IF}(dim > g < t > ().getMaxDim(), \texttt{"Wrong\_dimension\_for\_KOrder::check"});
      JournalRecordPair pa(journal);
      pa \ll "Checking_{\sqcup}residuals_{\sqcup}for_{\sqcup}order_{\sqcup}=_{\sqcup}" \ll dim \ll endrec;
      double maxerror = 0.0;
      \langle \operatorname{check} \text{ for } F_{y^i u^j} = 0 | 120 \rangle;
      \langle \text{check for } F_{y^i u^j u'^k} + D_{ijk} + E_{ijk} = 0 \text{ 121} \rangle;
       \langle \text{ check for } F_{\sigma^i} + D_i + E_i = 0 \text{ 122} \rangle;
      return maxerror;
This code is used in section 102.
120.
\langle \operatorname{check} \text{ for } F_{y^i u^j} = 0 | 120 \rangle \equiv
   for (int i = 0; i \le dim; i ++) {
      Symmetry sym(dim - i, i, 0, 0);
      Ttensor *r = faaDiBrunoZ < t > (sym);
      double err = r \rightarrow getData().getMax();
      \mathbf{JournalRecord}(journal) \ll "\texttt{\terror}_{\square} \mathbf{for}_{\square} \mathbf{symmetry}_{\square}" \ll sym \ll "\texttt{\tis}_{\square}" \ll err \ll endrec;
      if (err > maxerror) maxerror = err;
      delete r;
This code is used in section 119.
```

121.

```
\langle \text{check for } F_{y^i u^j u'^k} + D_{ijk} + E_{ijk} = 0 \text{ 121} \rangle \equiv
  SymmetrySet ss(dim, 3);
  for (symiterator si(ss); \neg si.isEnd(); ++si) {
     int i = (*si)[0];
     int j = (*si)[1];
     int k = (*si)[2];
     if (i+j>0 \land k>0) {
       Symmetry sym(i, j, 0, k);
       _Ttensor *r = faaDiBrunoZ < t > (sym);
       _Ttensor *D_-ijk = calcD_-ijk < t > (i, j, k);
       r \rightarrow add(1.0, *D_ijk);
       delete D_{-}ijk;
       Ttensor *E_{-ijk} = calcE_{-ijk} < t > (i, j, k);
       r \rightarrow add(1.0, *E_ijk);
       delete E_{-}ijk;
       double err = r \rightarrow getData().getMax();
       JournalRecord(journal) \ll "\terror_for_symmetry_" \ll sym \ll "\tis_" \ll err \ll endrec;
       delete r;
This code is used in section 119.
122.
\langle \text{ check for } F_{\sigma^i} + D_i + E_i = 0 \text{ 122} \rangle \equiv
  _Ttensor *r = faaDiBrunoZ < t > (Symmetry(0, 0, 0, dim));
  Ttensor *D_k = calcD_k < t > (dim);
  r \rightarrow add(1.0, *D_{-}k);
  delete D_{-}k;
  Ttensor *E_k = calcE_k < t > (dim);
  r \rightarrow add(1.0, *E_{-}k);
  delete E_{-}k;
  double err = r \neg getData().getMax();
  Symmetry sym(0,0,0,dim);
  JournalRecord(journal) \ll "\terror_for_symmetry_" \ll sym \ll "\tis_" \ll err \ll endrec;
  if (err > maxerror) maxerror = err;
  delete r;
This code is used in section 119.
```

```
123.  \langle \mathbf{KOrder} :: calcStochShift \  \, \mathbf{templated} \  \, \mathbf{code} \  \, \mathbf{123} \rangle \equiv \\ \mathbf{template} \langle \mathbf{int} \  \, t \rangle \  \, \mathbf{Vector} \  \, *calcStochShift(\mathbf{int} \  \, order, \mathbf{double} \  \, sigma) \  \, \mathbf{const} \, \, \{ \\ \mathbf{Vector} \  \, *res = \mathbf{new} \  \, \mathbf{Vector}(ny); \\ res \neg zeros(); \\ \mathbf{int} \  \, jfac = 1; \\ \mathbf{for} \  \, (\mathbf{int} \  \, j = 1; \  \, j \leq order; \  \, j + +, jfac \  \, *= j) \\ \mathbf{if} \  \, (is\_even(j)) \  \, \{ \\ \  \, \_\mathbf{Ttensor} \  \, *ten = calcD\_k < t > (j); \\ res \neg add(\mathbf{std} :: pow(sigma, j)/jfac, ten \neg getData()); \\ \mathbf{delete} \  \, ten; \\ \  \, \} \\ \mathbf{return} \  \, res; \\ \}  This code is used in section 102.
```

124. These are containers. The names are not important because they do not appear anywhere else since we access them by template functions.

```
\langle KOrder container members 124 \rangle \equiv
 UGSContainer _ug;
 \mathbf{FGSContainer} \ \_fg;
 UGSContainer _ugs;
 FGSContainer _fgs;
 UGSContainer _ugss;
 FGSContainer _fgss;
 UGSContainer \_uG;
 FGSContainer \_fG;
 UnfoldedZContainer _uZstack;
 FoldedZContainer _fZstack;
 UnfoldedGContainer \_uGstack;
 FoldedGContainer _fGstack;
 UNormalMoments _um;
 FNormalMoments _fm;
 const TensorContainer\langle FSSparseTensor \rangle \& f;
```

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These are the declarations of the template functions accessing the containers.  $\langle$  **KOrder** member access method declarations  $125\rangle \equiv$ template  $\langle \text{int } t \rangle \ \_\text{Tg } \& g();$ template(int t) const  $_{-}\mathbf{Tg} \ \&g() \ \mathbf{const};$ template  $\langle int t \rangle$  \_Tgs & gs(); template $\langle int t \rangle$  const  $\_Tgs \& gs()$  const; template(int t)  $\_$ Tgss &gss(); template(int t) const \_Tgss &gss() const; template (int t)  $_{-}\mathbf{TG} \& G()$ ; template (int t) const \_TG &G() const; template $\langle int \ t \rangle$  \_TZstack & Zstack(); template  $\langle int t \rangle$  const \_TZstack & Zstack() const; template  $\langle int t \rangle$  \_TGstack & Gstack(); template  $\langle int t \rangle$  const \_TGstack & Gstack() const; template  $\langle int t \rangle$  \_\_Tm & m(); template (int t) const \_\_Tm &m() const; This code is used in section 102. **126.** End of korder.h file. Start of korder.cpp file. 127. #include "kord\_exception.h" #include "korder.h" ⟨PLUMatrix copy constructor 128⟩;  $|\mathbf{PLUMatrix} :: calcPLU \text{ code } 129 \rangle;$  $\langle PLUMatrix :: multInv \text{ code } 130 \rangle;$ MatrixA constructor code 131); MatrixS constructor code 132); **KOrder** member access method specializations 139); **KOrder**:: sylvesterSolve unfolded specialization 136); **KOrder**:: sylvesterSolve folded specialization 137); **KOrder**:: switch To Folded code 138 \;  $\langle$  **KOrder** constructor code 133 $\rangle$ ; 128.  $\langle PLUMatrix copy constructor 128 \rangle \equiv$ PLUMatrix::PLUMatrix(const PLUMatrix & plu)

: TwoDMatrix(plu), inv(plu.inv), ipiv(new lapack\_int[nrows()]) {

memcpy(ipiv, plu.ipiv, nrows() \* sizeof (lapack\_int));

This code is used in section 127.

**129.** Here we set *ipiv* and *inv* members of the **PLUMatrix** depending on its content. It is assumed that subclasses will call this method at the end of their constructors.

```
\langle \mathbf{PLUMatrix} :: calcPLU \text{ code } 129 \rangle \equiv
  void PLUMatrix::calcPLU()
     lapack_int info;
     lapack\_introws = nrows();
     inv = (\mathbf{const} \ \mathbf{Vector} \ \&) \ getData();
     dgetrf(\&rows,\&rows,inv.base(),\&rows,ipiv,\&info);
  }
This code is used in section 127.
130. Here we just call the LAPACK machinery to multiply by the inverse.
\langle PLUMatrix :: multInv \text{ code } 130 \rangle \equiv
  void PLUMatrix::multInv(TwoDMatrix \& m) const
     KORD\_RAISE\_IF(m.nrows() \neq ncols(), "The\_matrix\_is\_not\_square\_in\_PLUMatrix::multInv");
     lapack_int info;
     lapack\_int mcols = m.ncols();
     lapack\_int mrows = m.nrows();
     double *mbase = m.getData().base();
     dgetrs("N", \&mrows, \&mcols, inv.base(), \&mrows, ipiv, mbase, \&mrows, \&info);
     KORD_RAISE_IF(info \neq 0, "Info!=0\sqcupin\sqcupPLUMatrix::multInv");
This code is used in section 127.
       Here we construct the matrix A. Its dimension is ny, and it is
                                          A = [f_y] + \left[0 \left[ f_{y_+^{**}} \right] \cdot \left[ g_{y_+^{**}}^{**} \right] 0 \right]
, where the first zero spans nstat columns, and last zero spans nforw columns.
\langle MatrixA constructor code 131 \rangle \equiv
  MatrixA::MatrixA(const\ FSSparseTensor\ \&f, const\ IntSequence\ \&ss, const\ TwoDMatrix
            &gy, const PartitionY &ypart)
  : \mathbf{PLUMatrix}(ypart.ny()) \ \{
     zeros();
     IntSequence c(1);
     c[0] = 1;
     FGSTensor f_{-}y(f, ss, c, \textbf{TensorDimens}(ss, c));
     add(1.0, f_{-}y);
     ConstTwoDMatrix\ gss\_ys(ypart.nstat + ypart.npred, ypart.nyss(), gy);
     c[0] = 0;
     FGSTensor f_{-yss}(f, ss, c, \text{TensorDimens}(ss, c));
     TwoDMatrix sub(*this, ypart.nstat, ypart.nys());
     sub.multAndAdd(\mathbf{ConstTwoDMatrix}(f\_yss), gss\_ys);
     calcPLU();
This code is cited in section 167.
```

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This code is used in section 127.

132. Here we construct the matrix S. Its dimension is ny, and it is

$$S = [f_y] + \begin{bmatrix} 0 & \left[ f_{y_+^{**}} \right] \cdot \left[ g_{y_+^{**}}^{**} \right] & 0 \end{bmatrix} + \begin{bmatrix} 0 & 0 & \left[ f_{y_+^{**}} \right] \end{bmatrix}$$

It is, in fact, the matrix A plus the third summand. The first zero in the summand spans nstat columns, the second zero spans npred columns.

```
\langle MatrixS constructor code 132 \rangle \equiv
  MatrixS::MatrixS(const\ FSSparseTensor\ \&f, const\ IntSequence\ \&ss, const\ TwoDMatrix
           &gy, const PartitionY &ypart)
  : PLUMatrix(ypart.ny()) {
    zeros();
    IntSequence c(1);
    c[0] = 1;
    FGSTensor f_{-}y(f, ss, c, \textbf{TensorDimens}(ss, c));
    add(1.0, f_{-}y);
    ConstTwoDMatrix gss_ys(ypart.nstat + ypart.npred, ypart.nyss(), gy);
    c[0] = 0;
    FGSTensor f_{-}yss(f, ss, c, \mathbf{TensorDimens}(ss, c));
    TwoDMatrix sub(*this, ypart.nstat, ypart.nys());
    sub.multAndAdd(\mathbf{ConstTwoDMatrix}(f\_yss), gss\_ys);
    TwoDMatrix sub2 (*this, ypart.nstat + ypart.npred, ypart.nyss());
    sub2.add(1.0, f_{-}yss);
    calcPLU();
This code is cited in section 110.
```

This code is used in section 127.

133. Here is the constructor of the **KOrder** class. We pass what we have to. The partitioning of the y vector, a sparse container with model derivatives, then the first order approximation, these are  $g_y$  and  $g_u$  matrices, and covariance matrix of exogenous shocks v.

We build the members, it is nothing difficult. Note that we do not make a physical copy of sparse tensors, so during running the class, the outer world must not change them.

In the body, we have to set nvs array, and initialize g and G containers to comply to preconditions of performStep.

```
\langle KOrder constructor code 133\rangle \equiv
  KOrder::KOrder(int num_stat, int num_pred, int num_both, int num_forw, const
           TensorContainer \langle FSSparseTensor \rangle & fcont, const TwoDMatrix & gy, const
           TwoDMatrix & gu, const TwoDMatrix & v, Journal & jr)
  : ypart(num\_stat, num\_pred, num\_both, num\_forw),
  ny(ypart.ny()), nu(qu.ncols()), maxk(fcont.getMaxDim()),
  nvs(4),
   \_ug(4), \ \_fg(4), \ \_ugs(4), \ \_fgs(4), \ \_ugss(4), \ \_fgss(4),
  _{-}uG(4), _{-}fG(4),
  \_uZstack(\&\_uG, ypart.nyss(), \&\_ug, ny, ypart.nys(), nu),
  _fZstack(\&_fG, ypart.nyss(), \&_fg, ny, ypart.nys(), nu),
  \_uGstack(\&\_ugs, ypart.nys(), nu),
  _fGstack(\&\_fgs, ypart.nys(), nu),
  \_um(maxk, v), \_fm(\_um), f(fcont),
  matA(*(f.get(\mathbf{Symmetry}(1))), \_uZstack.getStackSizes(), gy, ypart),
  matS(*(f.get(\mathbf{Symmetry}(1))), \_uZstack.getStackSizes(), gy, ypart),
  matB(*(f.qet(Symmetry(1))), \_uZstack.qetStackSizes()),
  journal(jr)
    KORD_RAISE_IF(gy.ncols() \neq ypart.nys(),
         "Wrong_number_of_columns_in_gy_in_KOrder_constructor");
    KORD\_RAISE\_IF(v.ncols() \neq nu, "Wrong\_number\_of\_columns\_of\_Vcov\_in\_KOrder\_constructor");
    KORD\_RAISE\_IF(nu \neq v.nrows(), "Wrong\_number\_of\_rows\_of\_Vcov\_in_KOrder\_constructor");
    KORD_RAISE_IF(maxk < 2,
         "Order_of_approximation_must_be_at_least_2_in_KOrder_constructor");
    KORD\_RAISE\_IF(gy.nrows() \neq ypart.ny(), "Wrong_lnumber_lof_lrows_lin_lgy_lin_lKOrder_lconstructor");
    KORD_RAISE_IF(gu.nrows() \neq ypart.ny(),
         "WrongunumberuofurowsuinuguuinuKOrderuconstructor");
    KORD_RAISE_IF(qu.ncols() \neq nu, "Wrong_number_of_columns_in_gu_in_KOrder_constructor");
       /* set nvs: */
    nvs[0] = ypart.nys();
    nvs[1] = nu;
    nvs[2] = nu;
    nvs[3] = 1;
     \langle \text{ put } g_y \text{ and } g_u \text{ to the container } 134 \rangle;
     \langle \text{ put } G_y, G_u \text{ and } G_{u'} \text{ to the container } 135 \rangle;
```

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134. Note that  $g_{\sigma}$  is zero by the nature and we do not insert it to the container. We insert a new physical copies.

```
\langle \text{ put } g_u \text{ and } g_u \text{ to the container } 134 \rangle \equiv
  UGSTensor *tgy = new UGSTensor(ny, TensorDimens(Symmetry(1, 0, 0, 0), nvs));
  tqy \neg getData() = gy.getData();
  insertDerivative < unfold > (tgy);
  UGSTensor *tqu = new UGSTensor(ny, TensorDimens(Symmetry(0, 1, 0, 0), nvs));
  tgu \rightarrow getData() = gu.getData();
  insertDerivative < unfold > (tgu);
This code is used in section 133.
135. Also note that since g_{\sigma} is zero, so G_{\sigma}.
\langle \text{ put } G_u, G_u \text{ and } G_{u'} \text{ to the container } 135 \rangle \equiv
  UGSTensor *tGy = faaDiBrunoG < unfold > (Symmetry(1, 0, 0, 0));
  G < unfold > ().insert(tGy);
  UGSTensor *tGu = faaDiBrunoG < unfold > (Symmetry(0, 1, 0, 0));
  G < unfold > ().insert(tGu);
  UGSTensor *tGup = faaDiBrunoG < unfold > (Symmetry(0, 0, 1, 0));
  G < unfold > ().insert(tGup);
This code is used in section 133.
```

136. Here we have an unfolded specialization of sylvester Solve. We simply create the sylvester object and solve it. Note that the  $g_y^*$  is not continuous in memory as assumed by the sylvester code, so we make a temporary copy and pass it as matrix C.

If the B matrix is empty, in other words there are now forward looking variables, then the system becomes AX = D which is solved by simple matA.multInv().

If one wants to display the diagnostic messages from the Sylvester module, then after the sylv.solve() one needs to call sylv.getParams().print("").

137. Here is the folded specialization of sylvester. We unfold the right hand side. Then we solve it by the unfolded version of *sylvesterSolve*, and fold it back and copy to output vector.

```
\langle \mathbf{KOrder} :: sylvester Solve \text{ folded specialization } 137 \rangle \equiv
  template()
  void KOrder::sylvesterSolve < KOrder::fold > (ctraits \langle fold \rangle :: Ttensor & der) const
     ctraits \langle unfold \rangle :: Ttensor tmp(der);
     sylvesterSolve < unfold > (tmp);
     ctraits \langle fold \rangle :: Ttensor ftmp(tmp);
     der.getData() = (\mathbf{const\ Vector\ } \&)(ftmp.getData());
This code is used in section 127.
138.
\langle \mathbf{KOrder} :: switch To Folded \text{ code } 138 \rangle \equiv
  void KOrder::switchToFolded()
     JournalRecordPair pa(journal);
     pa \ll "Switching from unfolded to folded" \ll endrec;
     int maxdim = g < unfold > ().getMaxDim();
     for (int dim = 1; dim \leq maxdim; dim ++) {
       SymmetrySet ss(dim, 4);
       for (symiterator si(ss); \neg si.isEnd(); ++si) {
         if ((*si)[2] \equiv 0 \land g < unfold > ().check(*si)) {
            FGSTensor *ft = \text{new FGSTensor}(*(g < unfold > ().get(*si)));
            insertDerivative < fold > (ft);
            if (dim > 1) {
              gss < unfold > ().remove(*si);
              gs < unfold > ().remove(*si);
              g < unfold > ().remove(*si);
         if (G < unfold > ().check(*si)) {
            FGSTensor *ft = new FGSTensor(*(G < unfold > ().get(*si)));
            G < fold > ().insert(ft);
            if (dim > 1) {
              G < fold > ().remove(*si);
         }
       }
This code is used in section 127.
```

These are the specializations of container access methods. Nothing interesting here.

```
\langle KOrder member access method specializations 139 \rangle \equiv
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: Tg &KOrder :: g < KOrder :: unfold > ()
  \{ \mathbf{return} \ \_ug; \}
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: Tg &KOrder :: g < KOrder :: unfold > () const
  { return \_ug; }
  template \langle \rangle ctraits \langle KOrder :: fold \rangle :: Tg & KOrder :: g < KOrder :: fold > ()
  \{ \mathbf{return} _f g; \}
  template\langle \rangle const ctraits\langle KOrder::fold \rangle ::Tg \& KOrder::g < KOrder::fold > () const
  \{ \mathbf{return} \ \_fg; \}
  template\langle \rangle ctraits\langle KOrder::unfold \rangle :: Tgs &KOrder:: qs < KOrder::unfold > ()
  { return \_ugs; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: Tgs & KOrder :: qs < KOrder :: unfold > () const
  { return \_ugs; }
  template\langle \rangle ctraits\langle KOrder :: fold \rangle :: Tgs \& KOrder :: gs < KOrder :: fold > ()
  { return \_fgs; }
  template\langle \rangle const ctraits\langle KOrder::fold \rangle :: Tgs & KOrder::gs < KOrder::fold > () const
  \{ \text{ return } \_fgs; \}
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: Tgss & KOrder :: gss < KOrder :: unfold > ()
  { return _ugss; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: Tgss & KOrder :: qss < KOrder :: unfold > () const
  { return \_uqss; }
  template\langle \rangle ctraits\langle KOrder::fold \rangle :: Tgss \& KOrder::gss < KOrder::fold > ()
  { return \_fqss; }
  template\langle \rangle const ctraits\langle KOrder :: fold \rangle :: Tgss & KOrder :: gss < KOrder :: fold > () const
  { return _fgss; }
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: TG \& KOrder :: G < KOrder :: unfold > ()
  { return \_uG; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: TG \& KOrder :: G < KOrder :: unfold > () const
  { return \_uG; }
  template\langle \rangle ctraits\langle KOrder:: fold \rangle :: TG \& KOrder:: G < KOrder:: fold > ()
  { return _fG; }
  template\langle \rangle const ctraits\langle KOrder::fold\rangle::TG \& KOrder::G < KOrder::fold > () const
  { return _{-}fG; }
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: TZstack & KOrder :: Zstack < KOrder :: unfold > ()
  { return \_uZstack; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: TZstack & KOrder :: Zstack < KOrder :: unfold > ()
       const
  { return _uZstack; }
  template\langle \rangle ctraits\langle KOrder::fold \rangle ::TZstack &KOrder::Zstack < KOrder::fold > ()
  { return _fZstack; }
  template\langle \rangle const ctraits\langle KOrder :: fold \rangle :: TZstack & KOrder :: Zstack < KOrder :: fold > () const
  { return _fZstack; }
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: TGstack & KOrder :: Gstack < KOrder :: unfold > ()
  { return \_uGstack; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: TGstack & KOrder :: Gstack < KOrder :: unfold > ()
       const
  { return _uGstack; }
  template\langle \rangle ctraits\langle KOrder::fold \rangle :: TGstack & KOrder::Gstack < KOrder::fold > ()
  { return _fGstack; }
  template\langle \rangle const ctraits\langle KOrder::fold \rangle :: TGstack & KOrder::Gstack < KOrder::fold > () const
  { return _fGstack; }
```

```
 \begin{split} & \mathbf{template} \langle \rangle \ \mathbf{ctraits} \langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{Tm} \ \& \mathbf{KOrder} :: m < \mathbf{KOrder} :: unfold > (\ ) \\ & \{ \ \mathbf{return} \ \_um; \ \} \\ & \mathbf{template} \langle \rangle \ \mathbf{const} \ \mathbf{ctraits} \langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{Tm} \ \& \mathbf{KOrder} :: m < \mathbf{KOrder} :: unfold > (\ ) \ \mathbf{const} \\ & \{ \ \mathbf{return} \ \_um; \ \} \\ & \mathbf{template} \langle \rangle \ \mathbf{ctraits} \langle \mathbf{KOrder} :: fold \rangle :: \mathbf{Tm} \ \& \mathbf{KOrder} :: m < \mathbf{KOrder} :: fold > (\ ) \\ & \{ \ \mathbf{return} \ \_fm; \ \} \\ & \mathbf{template} \langle \rangle \ \mathbf{const} \ \mathbf{ctraits} \langle \mathbf{KOrder} :: fold \rangle :: \mathbf{Tm} \ \& \mathbf{KOrder} :: m < \mathbf{KOrder} :: fold > (\ ) \ \mathbf{const} \\ & \{ \ \mathbf{return} \ \_fm; \ \} \\ & \mathbf{This} \ \mathbf{code} \ \mathbf{is} \ \mathbf{used} \ \mathbf{in} \ \mathbf{section} \ \mathbf{127}. \end{split}
```

140. End of korder.cpp file.

## 141. Higher order at stochastic steady. Start of korder\_stoch.h file.

This file defines a number of classes of which **KOrderStoch** is the main purpose. Basically, **KOrderStoch** calculates first and higher order Taylor expansion of a policy rule at  $\sigma > 0$  with explicit forward  $g^{**}$ . More formally, we have to solve a policy rule q from

$$E_t[f(g^{**}(g^*(y_t^*, u_t, \sigma), u_{t+1}, \sigma), g(y^*, u_t, \sigma), y^*, u_t)]$$

As an introduction in approximation.hweb argues,  $g^{**}$  at tine t+1 must be given from outside. Let the explicit  $E_t(g^{**}(y^*, u_{t+1}, \sigma))$  be equal to  $h(y^*, \sigma)$ . Then we have to solve

$$f(h(g^*(y^*, u, \sigma), \sigma), g(y, u, \sigma), y, u),$$

which is much easier than fully implicit system for  $\sigma = 0$ .

Besides the class **KOrderStoch**, we declare here also classes for the new containers corresponding to  $f(h(g^*(y^*, u, \sigma), \sigma), g(y, u, \sigma), y, u)$ . Further, we declare **IntegDerivs** and **StochForwardDerivs** classes which basically calculate h as an extrapolation based on an approximation to g at lower  $\sigma$ .

142. This class is a container, which has a specialized constructor integrating the policy rule at given  $\sigma$ .

```
⟨ IntegDerivs class declaration 142 ⟩ ≡
  template⟨int t⟩ class IntegDerivs : public ctraits⟨t⟩::Tgss {
   public:
    ⟨IntegDerivs constructor code 143 ⟩;
  };
This code is used in section 141.
```

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**143.** This constructor integrates a rule (namely its  $g^{**}$  part) with respect to  $u = \tilde{\sigma}\eta$ , and stores to the object the derivatives of this integral h at  $(y^*, u, \sigma) = (\tilde{y}^*, 0, \tilde{\sigma})$ . The original container of  $g^{**}$ , the moments of the stochastic shocks mom and the  $\tilde{\sigma}$  are input.

The code follows the following derivation

$$\begin{split} h(y,\sigma) &= E_t \left[ g(y,u',\sigma) \right] = \\ &= \tilde{y} + \sum_{d=1} \frac{1}{d!} \sum_{i+j+k=d} \binom{d}{i,j,k} \left[ g_{y^i u^j \sigma^k} \right] (y^* - \tilde{y}^*)^i \sigma^j \Sigma^j (\sigma - \tilde{\sigma})^k \\ &= \tilde{y} + \sum_{d=1} \frac{1}{d!} \sum_{i+m+n+k=d} \binom{d}{i,m+n,k} \left[ g_{y^i u^{m+n}\sigma^k} \right] \hat{y}^{*i} \Sigma^{m+n} \binom{m+n}{m,n} \tilde{\sigma}^m \hat{\sigma}^{k+n} \\ &= \tilde{y} + \sum_{d=1} \frac{1}{d!} \sum_{i+m+n+k=d} \binom{d}{i,m,n,k} \left[ g_{y^i u^{m+n}\sigma^k} \right] \Sigma^{m+n} \tilde{\sigma}^m \hat{y}^{*i} \hat{\sigma}^{k+n} \\ &= \tilde{y} + \sum_{d=1} \frac{1}{d!} \sum_{i+p=d} \sum_{\substack{m=0\\ n+k=p}} \binom{d}{i,m,n,k} \left[ g_{y^i u^{m+n}\sigma^k} \right] \Sigma^{m+n} \tilde{\sigma}^m \hat{y}^{*i} \hat{\sigma}^{k+n} \\ &= \tilde{y} + \sum_{d=1} \frac{1}{d!} \sum_{i+p=d} \binom{d}{i,p} \left[ \sum_{\substack{m=0\\ n+k=p}} \binom{p}{n,k} \frac{1}{m!} \left[ g_{y^i u^{m+n}\sigma^k} \right] \Sigma^{m+n} \tilde{\sigma}^m \right] \hat{y}^{*i} \hat{\sigma}^{k+n}, \end{split}$$

where  $\begin{pmatrix} a \\ b_1, \dots, b_n \end{pmatrix}$  is a generalized combination number, p = k + n,  $\hat{\sigma} = \sigma - \tilde{\sigma}$ ,  $\hat{y}^* = y^* - \tilde{y}$ , and we dropped writing the multidimensional indexes in Einstein summation.

This implies that

$$h_{y^i\sigma^p} = \sum_{\substack{m=0\\n+k=p}} \binom{p}{n,k} \frac{1}{m!} \left[ g_{y^iu^{m+n}\sigma^k} \right] \Sigma^{m+n} \tilde{\sigma}^m$$

and this is exactly what the code does.

 $\langle IntegDerivs constructor code 143 \rangle \equiv$ 

### 144. This code calculates

$$h_{y^i\sigma^p} = \sum_{\substack{m=0\\n+k=p}} \binom{p}{n,k} \frac{1}{m!} \left[ g_{y^iu^{m+n}\sigma^k} \right] \Sigma^{m+n} \tilde{\sigma}^m$$

```
and stores it in ten.
\langle \text{ calculate derivative } h_{y^i \sigma^p} | 144 \rangle \equiv
  ten \neg zeros();
  for (int n = 0; n \le p; n +++) {
     int k = p - n;
     int povern = Tensor :: noverk(p, n);
     int mfac = 1;
     for (int m = 0; i + m + n + k \le maxd; m ++ , mfac *= m) {
       double mult = (pow(at\_sigma, m) * povern)/mfac;
       Symmetry sym_{-}mn(i, m + n, 0, k);
       if (m + n \equiv 0 \land g.check(sym\_mn)) ten \neg add(mult, *(g.get(sym\_mn)));
       if (m+n > 0 \land \mathbf{KOrder} :: is\_even(m+n) \land g.check(sym\_mn)) {
         Ttensor gtmp(*(g.get(sym\_mn)));
         gtmp.mult(mult);
         gtmp.contractAndAdd(1,*ten,*(mom.get(Symmetry(m+n))));
    }
  }
```

This code is used in section 143.

145. This class calculates an extrapolation of expectation of forward derivatives. It is a container, all calculations are done in a constructor.

The class calculates derivatives of  $E[g(y*,u,\sigma)]$  at  $(\bar{y}^*,\bar{\sigma})$ . The derivatives are extrapolated based on derivatives at  $(\tilde{y}^*,\tilde{\sigma})$ .

```
\langle \textbf{StochForwardDerivs} \text{ class declaration } 145 \rangle \equiv \\ \textbf{template} \langle \textbf{int } t \rangle \textbf{ class StochForwardDerivs} : \textbf{public ctraits} \langle t \rangle :: \textbf{Tgss } \{ \\ \textbf{public:} \\ \langle \textbf{StochForwardDerivs} \text{ constructor code } 146 \rangle; \\ \}; \\ \end{cases}
```

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This is the constructor which performs the integration and the extrapolation. Its parameters are: g is the container of derivatives at  $(\tilde{y}, \tilde{\sigma})$ ; m are the moments of stochastic shocks; ydelta is a difference of the steady states  $\bar{y} - \tilde{y}$ ; sdelta is a difference between new sigma and old sigma  $\bar{\sigma} - \tilde{\sigma}$ , and at-sigma is  $\tilde{\sigma}$ . There is no need of inputing the  $\tilde{y}$ .

We do the operation in four steps:

- 1) Integrate  $g^{**}$ , the derivatives are at  $(\tilde{y}, \tilde{\sigma})$
- Form the (full symmetric) polynomial from the derivatives stacking  $\begin{bmatrix} y^* \\ \sigma \end{bmatrix}$
- Centralize this polynomial about  $(\bar{y}, \bar{\sigma})$
- Recover general symmetry tensors from the (full symmetric) polynomial

```
\langle StochForwardDerivs constructor code 146\rangle \equiv
```

```
StochForwardDerivs(const PartitionY &ypart, int nu, const _Tgss &g, const __Tm &m, const
        Vector &ydelta, double sdelta, double at_sigma)
```

```
: ctraits \langle t \rangle :: Tgss(4)  {
    int maxd = g.getMaxDim();
    int r = ypart.nyss();
    \langle \text{ make } g\_int \text{ be integral of } g^{**} \text{ at } (\tilde{y}, \tilde{\sigma}) \text{ 147} \rangle;
    \langle \text{ make } g\_int\_sym \text{ be full symmetric polynomial from } g\_int\_148 \rangle;
    \langle \text{ make } g\_int\_cent \text{ the centralized polynomial about } (\bar{y}, \bar{\sigma}) \text{ 149} \rangle;
    \langle \text{ pull out general symmetry tensors from } q_int\_cent | 150 \rangle;
}
```

This code is used in section 145.

This code is used in section 146.

This code is used in section 146.

147. This simply constructs IntegDerivs class. Note that the nvs of the tensors has zero dimensions for shocks, this is because we need to make easily stacks of the form  $\begin{vmatrix} y^* \\ \sigma \end{vmatrix}$  in the next step.

```
\langle \text{ make } g\_int \text{ be integral of } g^{**} \text{ at } (\tilde{y}, \tilde{\sigma}) \text{ 147} \rangle \equiv
   IntSequence nvs(4);
   nvs[0] = ypart.nys();
   nvs[1] = 0;
   nvs[2] = 0;
   nvs[3] = 1;
   IntegDerivs\langle t \rangle g_int(r, nvs, g, m, at\_sigma);
```

Here we just form a polynomial whose unique variable corresponds to  $\begin{bmatrix} y^* \\ \sigma \end{bmatrix}$  stack.

```
\langle \text{ make } g\_int\_sym \text{ be full symmetric polynomial from } g\_int\_148 \rangle \equiv
  _Tpol g_int_sym(r, ypart.nys() + 1);
  for (int d = 1; d \le maxd; d +++) {
    \_Ttensym *ten = new \_Ttensym(r, ypart.nys() + 1, d);
    ten \neg zeros();
    for (int i = 0; i \le d; i ++) {
       int k = d - i;
       if (g\_int.check(Symmetry(i,0,0,k))) ten\neg addSubTensor(*(g\_int.get(Symmetry(i,0,0,k))));
    g_iint_sym.insert(ten);
```

Here we centralize the polynomial to  $(\bar{y}, \bar{\sigma})$  knowing that the polynomial was centralized about  $(\tilde{y}, \tilde{\sigma})$ . This is done by derivating and evaluating the derivated polynomial at  $(\bar{y} - \tilde{y}, \bar{\sigma} - \tilde{\sigma})$ . The stack of this vector is *delta* in the code.

```
\langle \text{ make } g\_int\_cent \text{ the centralized polynomial about } (\bar{y}, \bar{\sigma}) \text{ 149} \rangle \equiv
  Vector delta(ypart.nys() + 1);
  Vector dy(delta, 0, ypart.nys());
  ConstVector dy_in(ydelta, ypart.nstat, ypart.nys());
  dy = dy_in;
  delta[ypart.nys()] = sdelta;
  _Tpol g_int_cent(r, ypart.nys() + 1);
  for (int d = 1; d \le maxd; d +++) {
     g_int_sym.derivative(d-1);
      Ttensym * der = g_int_sym.evalPartially(d, delta); 
     g_iint_cent.insert(der);
This code is used in section 146.
```

This code is used in section 146.

150. Here we only recover the general symmetry derivatives from the full symmetric polynomial. Note that the derivative get the true nvs.

```
\langle \text{ pull out general symmetry tensors from } g\_int\_cent | 150 \rangle \equiv
  IntSequence ss(4);
  ss[0] = ypart.nys();
  ss[1] = 0;
  ss[2] = 0;
  ss[3] = 1;
  IntSequence pp(4);
  pp[0] = 0;
  pp[1] = 1;
  pp[2] = 2;
  pp[3] = 3;
  IntSequence true\_nvs(nvs);
  true\_nvs[1] = nu;
  true\_nvs[2] = nu;
  for (int d = 1; d \le maxd; d ++) {
     if (g_int_cent.check(Symmetry(d))) {
       for (int i = 0; i \le d; i ++) {
          Symmetry sym(i, 0, 0, d - i);
          IntSequence coor(sym, pp);
          -\mathbf{Ttensor} * ten = \mathbf{new} \ -\mathbf{Ttensor} (*(g\_int\_cent.get(\mathbf{Symmetry}(d))), ss, coor,
               TensorDimens(sym, true_nvs));
          \mathbf{this} \neg insert(ten);
       }
  }
```

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**151.** This container corresponds to  $h(g^*(y,u,\sigma),\sigma)$ . Note that in our application, the  $\sigma$  as a second argument to h will be its fourth variable in symmetry, so we have to do four member stack having the second and third stack dummy.

```
\langle GXContainer class declaration 151\rangle \equiv
          template \langle class \_Ttype \rangle \ class \ GXContainer : public \ GContainer \langle \_Ttype \rangle \ 
public: typedef StackContainerInterface < _Ttype > _Stype;
          typedef typename StackContainer \( \_\text{Ttype} \) :: \( \_\text{Ctype} \) :
          typedef typename StackContainer \( \_\text{Ttype} \) :: itype itype;
          GXContainer(const \_Ctype *gs, int ngs, int nu)
          : GContainer \langle \text{-Ttype} \rangle (gs, ngs, nu) \}
            \langle \mathbf{GXContainer} :: getType \text{ code } 152 \rangle;
          };
This code is used in section 141.
                                  This routine corresponds to this stack:
```

This code is used in section 141.

```
dummy
dummy
```

```
\langle \mathbf{GXContainer} :: qetType \text{ code } 152 \rangle \equiv
  itype getType (int i, const Symmetry &s) const
     if (i \equiv 0)
        if (s[2] > 0) return \_Stype :: zero;
        else return _Stype :: matrix;
     if (i \equiv 1) return \_Stype :: zero;
     if (i \equiv 2) return \_Stype :: zero;
     if (i \equiv 3)
        if (s \equiv \mathbf{Symmetry}(0,0,0,1)) return \_Stype :: unit;
        else return \_Stype :: zero;
     KORD_RAISE("Wrong_stack_index_in_GXContainer::getType");
This code is used in section 151.
```

**153.** This container corresponds to  $f(H(y, u, \sigma), g(y, u, sigma), y, u)$ , where the H has the size (number of rows) as  $g^{**}$ . Since it is very simmilar to **ZContainer**, we inherit form it and override only qetType method.

```
\langle ZXContainer class declaration 153 \rangle \equiv
  template\langle class \_Ttype \rangle \ class \ ZXContainer : public \ ZContainer \langle \_Ttype \rangle \ \{
  public:
     typedef StackContainerInterface(_Ttype) _Stype;
     typedef typename StackContainer \( \_\text{Ttype} \) :: \( \_\text{Ctype} \) \( \_\text{Ctype} \);
     typedef typename StackContainer \( -Ttype \) :: itype itype;
     ZXContainer(const _Ctype *gss, int ngss, const _Ctype *g, int ng, int ny, int nu)
     : ZContainer\langle \text{-Ttype} \rangle (gss, ngss, g, ng, ny, nu)  { }
     \langle \mathbf{ZXContainer} :: qetType \text{ code } 154 \rangle;
  };
```

**154.** This *getType* method corresponds to this stack:

$$\begin{bmatrix} H(y,u,\sigma) \\ g(y,u,\sigma) \\ y \\ u \end{bmatrix}$$

```
\langle \mathbf{ZXContainer} :: getType \text{ code } 154 \rangle \equiv
  itype getType(int i, const Symmetry \&s) const
    if (i \equiv 0)
       if (s[2] > 0) return _Stype::zero;
       else return _Stype::matrix;
    if (i \equiv 1)
       if (s[2] > 0) return _Stype::zero;
       else return _Stype:: matrix;
    if (i \equiv 2)
       if (s \equiv \text{Symmetry}(1,0,0,0)) return \_\text{Stype}::unit;
       else return _Stype::zero;
    if (i \equiv 3)
       if (s \equiv \text{Symmetry}(0, 1, 0, 0)) return _Stype::unit;
       else return _Stype::zero;
    KORD_RAISE("Wrong_stack_index_in_ZXContainer::getType");
This code is used in section 153.
155.
\langle UnfoldedGXContainer class declaration 155 \rangle \equiv
  class UnfoldedGXContainer : public <math>GXContainer \langle UGSTensor \rangle, public
         UnfoldedStackContainer {
  public:
    typedef TensorContainer(UGSTensor) _Ctype;
    UnfoldedGXContainer(const \_Ctype *gs, int ngs, int nu)
    : GXContainer \langle UGSTensor \rangle (gs, ngs, nu) \{ \}
  };
This code is used in section 141.
156.
\langle FoldedGXContainer class declaration 156\rangle \equiv
  class FoldedGXContainer : public GXContainer \langle FGSTensor \rangle, public FoldedStackContainer
  public:
    typedef TensorContainer(FGSTensor) _Ctype;
    FoldedGXContainer(const \_Ctype *gs, int ngs, int nu)
    : GXContainer \langle FGSTensor\rangle (gs, ngs, nu) \{\}
  };
This code is used in section 141.
```

```
157.
\langle UnfoldedZXContainer class declaration 157 \rangle \equiv
  class UnfoldedZXContainer : public ZXContainer (UGSTensor),
          public UnfoldedStackContainer {
  public:
    typedef TensorContainer(UGSTensor) _Ctype;
    UnfoldedZXContainer(const _Ctype *gss, int ngss, const _Ctype *g, int ng, int ny, int nu)
    : ZXContainer \langle \mathbf{UGSTensor} \rangle (gss, ngss, g, ng, ny, nu)  { }
  };
This code is used in section 141.
158.
\langle FoldedZXContainer class declaration 158\rangle \equiv
  class FoldedZXContainer: public ZXContainer(FGSTensor), public FoldedStackContainer {
  public:
    typedef TensorContainer(FGSTensor) _Ctype;
    FoldedZXContainer(const _Ctype *gs, int ngss, const _Ctype *g, int ng, int ny, int nu)
    : ZXContainer\langleFGSTensor\rangle(gss, ngss, g, ng, ny, nu) { } { }
  };
This code is used in section 141.
159. This matrix corresponds to
                                          [f_y] + \left[0 \left[f_{y_+^{**}}\right] \cdot \left[h_{y^*}^{**}\right] 0\right]
This is very the same as MatrixA, the only difference that the MatrixA is constructed from whole h_{y^*},
not only from h_{y^*}^{**}, hence the new abstraction.
```

```
\langle MatrixAA \text{ class declaration } 159 \rangle \equiv
  class MatrixAA : public PLUMatrix {
  public:
    MatrixAA (const FSSparseTensor &f, const IntSequence &ss, const TwoDMatrix
         \&gyss, const PartitionY \&ypart);
  };
This code is used in section 141.
```

**160.** This class calculates derivatives of g given implicitly by  $f(h(g^*(y, u, \sigma), \sigma), g(y, u, \sigma), y, u)$ , where  $h(y, \sigma)$  is given from outside.

Structurally, the class is very similar to **KOrder**, but calculations are much easier. The two constructors construct an object from sparse derivatives of f, and derivatives of h. The caller must ensure that the both derivatives are done at the same point.

The calculation for order k (including k = 1) is done by a call performStep(k). The derivatives can be retrived by getFoldDers() or getUnfoldDers().

```
\langle KOrderStoch class declaration 160 \rangle \equiv
  class KOrderStoch {
  protected:
    IntSequence nvs;
    PartitionY ypart;
    Journal & journal:
    UGSContainer _ug;
    FGSContainer _fg;
    UGSContainer _ugs;
    FGSContainer \_fgs;
    UGSContainer \_uG;
    FGSContainer _{-}fG;
    const UGSContainer *_uh;
    const FGSContainer *_fh;
    UnfoldedZXContainer _uZstack;
    FoldedZXContainer _fZstack;
    UnfoldedGXContainer _uGstack;
    FoldedGXContainer _fGstack;
    const TensorContainer \langle FSSparseTensor \rangle \& f;
    MatrixAA matA;
  public:
    KOrderStoch(const\ PartitionY\ \&ypart, int\ nu, const\ TensorContainer\langle FSSparseTensor\rangle
         &fcont, const FGSContainer &hh, Journal &jr);
    KOrderStoch(const\ PartitionY\ \&ypart, int\ nu, const\ TensorContainer\langle FSSparseTensor\rangle
         &fcont, const UGSContainer &hh, Journal &jr);
    \langle \mathbf{KOrderStoch} :: performStep \text{ templated code } 163 \rangle;
    const FGSContainer &getFoldDers() const
    \{ \text{ return } \_fg; \}
    const UGSContainer & getUnfoldDers() const
    \{ \mathbf{return} \ \_ug; \}
  protected:
     \langle KOrderStoch :: faaDiBrunoZ \text{ templated code } 161 \rangle;
     \langle \mathbf{KOrderStoch} :: faaDiBrunoG \text{ templated code } 162 \rangle;
     ⟨KOrderStoch convenience access methods 164⟩;
  };
This code is cited in section 182.
This code is used in section 141.
```

```
70
       HIGHER ORDER AT STOCHASTIC STEADY
161. This calculates a derivative of f(G(y, u, \sigma), g(y, u, \sigma), y, u) of a given symmetry.
\langle \mathbf{KOrderStoch} :: faaDiBrunoZ \text{ templated code } 161 \rangle \equiv
  template\langle int t \rangle _Ttensor *faaDiBrunoZ(const Symmetry &sym) const
     JournalRecordPair pa(journal);
     pa \ll \texttt{"Faa} \_ \texttt{Di} \_ \texttt{Bruno} \_ \texttt{ZX} \_ \texttt{container} \_ \texttt{for} \_ \texttt{"} \ll sym \ll endrec;
     \_Ttensor *res = new \_Ttensor(ypart.ny(),TensorDimens(sym, nvs));
     FaaDiBruno bruno(journal);
     bruno.calculate(Zstack < t > (), f, *res);
```

This code is used in section 160.

This code is used in section 160.

return res;

```
162. This calculates a derivative of G(y, u, \sigma) = h(g^*(y, u, \sigma), \sigma) of a given symmetry.
\langle \mathbf{KOrderStoch} :: faaDiBrunoG \text{ templated code } 162 \rangle \equiv
  template \langle int t \rangle _Ttensor *faaDiBrunoG(const Symmetry &sym) const
     JournalRecordPair pa(journal);
     pa \ll "Faa_{\sqcup}Di_{\sqcup}Bruno_{\sqcup}GX_{\sqcup}container_{\sqcup}for_{\sqcup}" \ll sym \ll endrec;
     TensorDimens tdims(sym, nvs);
     \_Ttensor *res = new \_Ttensor(ypart.nyss(), tdims);
     FaaDiBruno bruno(journal);
     bruno.calculate(Gstack < t > (), h < t > (), *res);
     return res;
```

**163.** This retrives all g derivatives of a given dimension from implicit  $f(h(g^*(y, u, \sigma), \sigma), g(y, u, \sigma), y, u)$ . It suppose that all derivatives of smaller dimensions have been retrieved.

So, we go through all symmetries s, calculate  $G_s$  conditional on  $g_s = 0$ , insert the derivative to the G container, then calculate  $F_s$  conditional on  $g_s = 0$ . This is a righthand side. The left hand side is  $matA \cdot g_s$ . The  $g_s$  is retrieved as

```
q_s = -matA^{-1} \cdot RHS.
```

```
Finally we have to update G_s by calling Gstack < t > ().multAndAdd(1, h < t > (), *<math>G_sym).
\langle \mathbf{KOrderStoch} :: performStep \text{ templated code } 163 \rangle \equiv
  template (int \ t) \ void \ performStep (int \ order)
     int maxd = g < t > ().getMaxDim();
     KORD_RAISE_IF(order - 1 \neq maxd \land (order \neq 1 \lor maxd \neq -1),
          "Wrong⊔order⊔for⊔KOrderStoch::performStep");
     SymmetrySet ss(order, 4);
     for (symiterator si(ss); \neg si.isEnd(); ++si) {
       if ((*si)[2] \equiv 0) {
          JournalRecordPair pa(journal);
          pa \ll "Recovering_{\square} symmetry_{\square}" \ll *si \ll endrec;
          \_Ttensor *G\_sym = faaDiBrunoG < t > (*si);
          G < t > ().insert(G_sym);
          Ttensor *g\_sym = faaDiBrunoZ < t > (*si);
          g\_sym \rightarrow mult(-1.0);
          matA.multInv(*g\_sym);
          g < t > ().insert(g\_sym);
          gs < t > ().insert(\mathbf{new\_Ttensor}(ypart.nstat, ypart.nys(), *g\_sym));
          Gstack < t > ().multAndAdd(1, h < t > (), *G_sym);
  }
This code is used in section 160.
164.
\langle KOrderStoch convenience access methods 164\rangle \equiv
  template (int t) _{-}Tg &g();
  template \langle \text{int } t \rangle \text{ const } _{\mathbf{T}} \mathbf{g} \& g() \text{ const};
  template (int t) _{-}Tgs & gs();
  template (int t) const _Tgs &gs() const;
  template (int t) const _Tgss &h() const;
  template (int t) _{-}\mathbf{TG} \& G();
  template (int t) const _{-}\mathbf{TG} \& G() const;
  template \langle int t \rangle _TZXstack & Zstack();
  template \langle int t \rangle const _TZXstack & Zstack() const;
  template \langle int t \rangle _TGXstack & Gstack();
  template \langle int \ t \rangle const _TGXstack & Gstack() const;
This code is used in section 160.
```

165. End of korder\_stoch.h file.

```
166.
      Start of korder_stoch.cpp file.
#include "korder_stoch.h"
  ⟨ MatrixAA constructor code 167⟩;
   KOrderStoch folded constructor code 168);
   KOrderStoch unfolded constructor code 169);
  ⟨ KOrderStoch convenience method specializations 170⟩;
167.
       Same as \langle Matrix A  constructor code 131\rangle, but the submatrix gss\_ys is passed directly.
\langle MatrixAA \text{ constructor code } 167 \rangle \equiv
  MatrixAA :: MatrixAA (const FSSparseTensor & f, const IntSequence & ss, const TwoDMatrix
           &gss_ys, const PartitionY &ypart)
  : PLUMatrix(ypart.ny()) {
    zeros();
    IntSequence c(1);
    c[0] = 1;
    FGSTensor f_{-y}(f, ss, c, \text{TensorDimens}(ss, c));
    add(1.0, f_{-}y);
    c[0] = 0;
    FGSTensor f_{-}yss(f, ss, c, \textbf{TensorDimens}(ss, c));
    TwoDMatrix sub(*this, ypart.nstat, ypart.nys());
    sub.multAndAdd(f_{-}yss, gss_{-}ys);
    calcPLU();
This code is used in section 166.
168.
\langle KOrderStoch \text{ folded constructor code } 168 \rangle \equiv
  KOrderStoch :: KOrderStoch (const PartitionY & yp, int nu,
           const TensorContainer \langle FSSparseTensor \rangle \& fcont, const FGSContainer \& hh, Journal
            \&jr)
  : nvs(4), ypart(yp), journal(jr),
  _{ug}(4), _{fg}(4), _{ugs}(4), _{fgs}(4), _{ug}(4), _{f}(4),
  \_uh(\Lambda), \_fh(\&hh),
  \_uZstack(\&\_uG, ypart.nyss(), \&\_ug, ypart.ny(), ypart.nys(), nu),
  _fZstack(\&_fG, ypart.nys(), \&_fg, ypart.ny(), ypart.nys(), nu),
  \_uGstack(\&\_ugs, ypart.nys(), nu),
  _fGstack(\&\_fgs, ypart.nys(), nu),
  f(fcont),
  matA(*(fcont.get(\mathbf{Symmetry}(1))), uZstack.getStackSizes(), *(hh.get(\mathbf{Symmetry}(1, 0, 0, 0))), ypart)
    nvs[0] = ypart.nys();
    nvs[1] = nu;
    nvs[2] = nu;
    nvs[3] = 1;
```

```
169.
\langle KOrderStoch unfolded constructor code 169 \rangle \equiv
  KOrderStoch::KOrderStoch(const PartitionY & yp, int nu,
            const TensorContainer \langle FSSparseTensor \rangle & fcont, const UGSContainer & hh, Journal
  : \ nvs(4), \ ypart(yp), \ journal(jr),
  _{-}ug(4), _{-}fg(4), _{-}ugs(4), _{-}fgs(4), _{-}uG(4), _{-}fG(4),
  \_uh(\&hh), \_fh(\Lambda),
  \_uZstack(\&\_uG, ypart.nyss(), \&\_ug, ypart.ny(), ypart.nys(), nu),
   \_fZstack(\&\_fG, ypart.nys(), \&\_fg, ypart.ny(), ypart.nys(), nu), \\
  \_uGstack(\&\_ugs, ypart.nys(), nu),
  \_fGstack(\&\_fgs, ypart.nys(), nu),
  f(fcont),
  matA(*(fcont.get(\mathbf{Symmetry}(1))), uZstack.getStackSizes(), *(hh.get(\mathbf{Symmetry}(1, 0, 0, 0))), ypart)  {
     nvs[0] = ypart.nys();
     nvs[1] = nu;
     nvs[2] = nu;
     nvs[3] = 1;
```

This code is used in section 166.

 $\mathbf{const}$ 

```
170.
\langle KOrderStoch convenience method specializations 170 \rangle \equiv
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: Tg &KOrderStoch :: q < KOrder :: unfold > ()
  { return \_uq; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: Tg & KOrder Stoch :: g < KOrder :: unfold > () const
  { return \_ug; }
  template\langle \rangle ctraits\langle KOrder::fold \rangle :: Tg &KOrderStoch:: g < KOrder::fold > ()
  \{ \mathbf{return} _f g; \}
  template\langle \rangle const ctraits\langle KOrder::fold \rangle :: Tg &KOrderStoch:: g < KOrder::fold > () const
  \{ \text{ return } \_fg; \}
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: Tgs &KOrderStoch :: gs < KOrder :: unfold > ()
   { return \_ugs; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: Tgs &KOrderStoch :: gs < KOrder :: unfold > ()
        const
   \{ \mathbf{return} \ \_ugs; \}
  template\langle \rangle ctraits\langle KOrder::fold\rangle::Tgs \&KOrderStoch::qs < KOrder::fold > ()
  \{ \text{ return } \_fgs; \}
  template\langle \rangle const ctraits\langle KOrder::fold \rangle :: Tgs &KOrderStoch::gs < KOrder::fold > () const
  \{ \mathbf{return} \_fgs; \}
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: Tgss & KOrder Stoch :: h < KOrder :: unfold > ()
        const
  { return *_uh; }
  template\langle \rangle const ctraits\langle KOrder::fold \rangle :: Tgss & KOrderStoch::h < KOrder::fold > () const
   { return *_fh; }
  \mathbf{template} \langle \ \rangle \ \mathbf{ctraits} \langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{TG} \ \& \mathbf{KOrderStoch} :: G < \mathbf{KOrder} :: unfold > (\ )
   { return \_uG; }
  template\langle \rangle const ctraits\langle KOrder :: unfold \rangle :: TG &KOrder Stoch :: G < KOrder :: unfold > ()
        const
   { return \_uG; }
  template\langle \rangle ctraits\langle KOrder :: fold \rangle :: TG \& KOrder Stoch :: G < KOrder :: fold > ()
  \{ \text{ return } _fG; \}
  template\langle \rangle const ctraits\langle KOrder::fold \rangle :: TG &KOrderStoch::G < KOrder::fold > () const
  \{ \mathbf{return} \ \_fG; \}
  template\langle \rangle ctraits\langle KOrder::unfold \rangle ::TZXstack &KOrderStoch::Zstack < KOrder::unfold > ()
  { return _uZstack; }
  template\langle \rangle const ctraits\langle KOrder::unfold \rangle :: TZXstack &KOrderStoch:: Zstack <
             KOrder :: unfold > () const
  { return _uZstack; }
  template\langle \rangle ctraits\langle KOrder::fold \rangle :: TZXstack &KOrderStoch:: Zstack < KOrder::fold > ()
  { return _fZstack; }
  template\langle \rangle const ctraits\langle KOrder :: fold \rangle :: TZXstack &KOrderStoch :: Zstack < KOrder :: fold > ()
        const
  { return _fZstack; }
  template\langle \rangle ctraits\langle KOrder :: unfold \rangle :: TGXstack &KOrderStoch :: Gstack < KOrder :: unfold > ()
  { return \_uGstack; }
  \mathsf{template}\langle \rangle \ \mathsf{const} \ \mathsf{ctraits}\langle \mathsf{KOrder} :: unfold \rangle :: \mathsf{TGXstack} \ \& \mathsf{KOrderStoch} :: \mathit{Gstack} \ <
              KOrder :: unfold > () const
  { return _uGstack; }
  template\langle \rangle ctraits\langle KOrder::fold \rangle :: TGXstack & KOrderStoch:: Gstack < KOrder::fold > ()
  { return _fGstack; }
  template\langle \rangle const ctraits\langle KOrder :: fold \rangle :: TGXstack \& KOrderStoch :: Gstack < KOrder :: fold > ()
```

{ return \_fGstack; }
This code is used in section 166.

171. End of korder\_stoch.cpp file.

76 PUTTING ALL TOGETHER Dynare++  $\S172$ 

## 172. Putting all together.

173. Dynamic model abstraction. Start of dynamic\_model.h file.

This file only defines a generic interface to an SDGE model. The model takes the form:

$$E_t \left[ f(g^{**}(g^*(y, u_t), u_{t+1}), g(y, u), y, u_t) \right] = 0$$

```
The interface is defined via pure virtual class DynamicModel.
```

174. The class is a virtual pure class which provides an access to names of the variables.

```
 \begin{split} &\langle \, \mathbf{NameList} \,\, \mathsf{class} \,\, \mathsf{declaration} \,\, 174 \, \rangle \equiv \\ & \mathbf{class} \,\, \mathbf{NameList} \,\, \{ \\ & \mathbf{public:} \\ & \mathbf{virtual} \,\, \sim \! \mathbf{NameList}(\,) \\ & \{ \, \} \\ & \mathbf{virtual} \,\, \mathsf{int} \,\, \mathit{getNum}(\,) \,\, \mathbf{const} = 0; \\ & \mathbf{virtual} \,\, \mathsf{const} \,\, \mathsf{char} \,\, *\mathit{getName}(\mathsf{int} \,\, i) \,\, \mathsf{const} = 0; \\ & \mathbf{void} \,\, \mathit{print}(\,) \,\, \mathbf{const}; \\ & \mathbf{void} \,\, \mathit{writeMat}(\mathit{mat\_t} \, *\mathit{fd}, \mathsf{const} \,\, \mathsf{char} \,\, *\mathit{vname}) \,\, \mathsf{const}; \\ & \mathbf{void} \,\, \mathit{writeMatIndices}(\mathit{mat\_t} \, *\mathit{fd}, \mathsf{const} \,\, \mathsf{char} \,\, *\mathit{prefix}) \,\, \mathsf{const}; \\ & \}; \end{split}
```

This code is used in section 173.

175. This is the interface to an information on a generic SDGE model. It is sufficient for calculations of policy rule Taylor approximations at some (not necessarily deterministic) steady state.

We need to know a partitioning of endogenous variables y. We suppose that y is partitioned as

$$y = \begin{bmatrix} \text{static} \\ \text{pred} \\ \text{both} \\ \text{forward} \end{bmatrix}$$

of which we define

$$y^* = \begin{bmatrix} \text{pred} \\ \text{both} \end{bmatrix}$$
  $y^{**} = \begin{bmatrix} \text{both} \\ \text{forward} \end{bmatrix}$ 

where "static" are meant those variables, which appear only at time t; "pred" are meant those variables, which appear at least at t-1 and t+1; and "forward" are meant those variables, which appear at least at t-1 and t+1; and "forward" are meant those variables, which appear only at t and t+1. This partitioning is given by methods nstat(), npred(), nboth(), and nforw(). The number of equations numeq() must be the same as a number of endogenous variables.

In order to complete description, we need to know a number of exogenous variables, which is a size of u, hence nexog() method.

The model contains an information about names of variables, the variance-covariance matrix of the shocks, the derivatives of equations of f at some steady state, and the steady state. These can be retrieved by the corresponding methods.

The derivatives of the system are calculated with respect to stacked variables, the stack looks as:

$$\begin{bmatrix} y_{t+1}^{**} \\ y_t \\ y_{t-1}^* \\ u_t \end{bmatrix}.$$

There are only three operations. The first solveDeterministicSteady() solves the deterministic steady steate which can be retrieved by getSteady() later. The method evaluateSystem calculates  $f(y^{**}, y, y^{*}, u)$ , where y and u are passed, or  $f(y^{**}_{t+1}, y_t, y^{*}_{t-1}, u)$ , where  $y^{**}_{t+1}, y_t, y^{*}_{t-1}, u$  are passed. Finally, the method calcDerivativesAtSteady() calculates derivatives of f at the current steady state, and zero shocks. The derivatives can be retrieved with getModelDerivatives(). All the derivatives are done up to a given order in the model, which can be retrieved by order().

The model initialization is done in a constructor of the implementing class. The constructor usually calls a parser, which parses a given file (usually a text file), and retrieves all necessary information about the model, inluding variables, partitioning, variance-covariance matrix, information helpful for calculation of the deterministic steady state, and so on.

```
⟨ DynamicModel class declaration 175⟩ ≡
  class DynamicModel {
  public:
    virtual DynamicModel *clone() const = 0;
    virtual ~DynamicModel()
    {}
    virtual int nstat() const = 0;
    virtual int nboth() const = 0;
    virtual int npred() const = 0;
    virtual int nerog() const = 0;
    virtual int nerog() const = 0;
    virtual int order() const = 0;
    int numeq() const
```

```
{ return nstat() + nboth() + npred() + nforw(); }
                virtual const NameList \&getAllEndoNames() const = 0;
                virtual const NameList \&getStateNames() const = 0;
                virtual const NameList \&getExogNames() const = 0;
                virtual const TwoDMatrix & qetVcov() const = 0;
                virtual const TensorContainer (FSSparseTensor) & getModelDerivatives() const = 0;
                virtual const Vector \&getSteady() const = 0;
                virtual Vector \&getSteady() = 0;
                virtual void solveDeterministicSteady() = 0;
                virtual void evaluateSystem(Vector \& out, const Vector \& yy, const Vector \& xx) = 0;
                \mathbf{virtual} \ \mathbf{void} \ \mathit{evaluateSystem} (\mathbf{Vector} \ \&\mathit{out}, \mathbf{const} \ \mathbf{Vector} \ \&\mathit{yym}, \mathbf{const} \ \mathbf{Vector} \ \&\mathit{yy}, \mathbf{const} \ \mathbf{Vector} \ \&\mathit{yy}, \mathbf{const} \ \mathbf{Vector} \ \&\mathit{yym}, \mathbf{const} \ \mathbf{vector} \ \ \mathsf{vector} 
                                &yyp, const Vector &xx) = 0;
                virtual void calcDerivativesAtSteady() = 0;
        };
This code is used in section 173.
176.
                         End of dynamic_model.h file.
                         Start of dynamic_model.cpp file.
#include "dynamic_model.h"
        \langle NameList :: print code 178 \rangle;
         \langle NameList :: writeMat code 179 \rangle;
         ⟨ NameList :: writeMatIndices code 180 ⟩;
178.
\langle NameList :: print code 178 \rangle \equiv
        void NameList::print() const
                for (int i = 0; i < getNum(); i++) printf("%s\n", getName(i));
This code is used in section 177.
```

```
179.
\langle NameList :: writeMat \text{ code } 179 \rangle \equiv
  void NameList::writeMat(mat\_t * fd, const char * vname) const
     int maxlen = 0;
     for (int i = 0; i < getNum(); i \leftrightarrow)
       if (maxlen < (int) strlen(getName(i))) maxlen = (int) strlen(getName(i));
     if (maxlen \equiv 0) return;
     char *m = new char[getNum() * maxlen];
     for (int i = 0; i < getNum(); i \leftrightarrow)
       for (int j = 0; j < maxlen; j \leftrightarrow)
         if (j < (int) strlen(getName(i))) m[j * getNum() + i] = getName(i)[j];
          else m[j*getNum()+i] = '_{\sqcup}';
\#\mathbf{if} \ \mathtt{MATIO\_MAJOR\_VERSION} > 1 \lor (\mathtt{MATIO\_MAJOR\_VERSION} \equiv 1 \land \mathtt{MATIO\_MINOR\_VERSION} \ge 5)
     size_t dims[2];
     const matio_compression compression = MAT_COMPRESSION_NONE;
#else
     int dims[2];
     const int compression = COMPRESSION_NONE;
#endif
     dims[0] = getNum();
     dims[1] = maxlen;
     matvar_{-}t * v = Mat_{-}VarCreate(vname, MAT_{-}C_{-}CHAR, MAT_{-}T_{-}UINT8, 2, dims, m, 0);
     Mat_{-}VarWrite(fd, v, compression);
     Mat\_VarFree(v);
     \mathbf{delete}[] m;
This code is used in section 177.
\langle NameList :: writeMatIndices code 180 \rangle \equiv
  void NameList::writeMatIndices(mat_t * fd, const char * prefix) const
     char tmp[100];
     TwoDMatrix aux(1,1);
     for (int i = 0; i < getNum(); i ++ ) {
       sprintf(tmp, "%s_i_%s", prefix, getName(i));
       aux.get(0,0) = i + 1;
       aux.writeMat(fd, tmp);
  }
This code is used in section 177.
```

181. End of dynamic\_model.cpp file.

## 182. Approximating model solution. Start of approximation.h file.

The class **Approximation** in this file is a main interface to the algorithms calculating approximations to the decision rule about deterministic and stochastic steady states.

The approximation about a deterministic steady state is solved by classes  $\langle \mathbf{FirstOrder} \ \text{class} \ \text{declaration} \ 76 \rangle$  and  $\langle \mathbf{KOrder} \ \text{class} \ \text{declaration} \ 102 \rangle$ . The approximation about the stochastic steady state is solved by class  $\langle \mathbf{KOrderStoch} \ \text{class} \ \text{declaration} \ 160 \rangle$  together with a method of **Approximation** class  $\langle \mathbf{Approximation} :: walkStochSteady \ \text{code} \ 194 \rangle$ .

The approximation about the stochastic steady state is done with explicit expression of forward derivatives of  $g^{**}$ . More formally, we have to solve the decision rule g from the implicit system:

$$E_t(f(g^{**}(g^*(y^*, u_t, \sigma), u_{t+1}, \sigma), g(y^*, u_t, \sigma), y_t, u_t)) = 0$$

The term within the expectations can be Taylor expanded, and the expectation can be driven into the formula. However, when doing this at  $\sigma \neq 0$ , the term  $g^{**}$  at  $\sigma \neq 0$  is dependent on  $u_{t+1}$  and thus the integral of its approximation includes all derivatives wrt. u of  $g^{**}$ . Note that for  $\sigma = 0$ , the derivatives of  $g^{**}$  in this context are constant. This is the main difference between the approximation at deterministic steady  $(\sigma = 0)$ , and stochastic steady  $(\sigma \neq 0)$ . This means that k-order derivative of the above equation at  $\sigma \neq 0$  depends of all derivatives of  $g^{**}$  (including those with order greater than k).

The explicit expression of the forward  $g^{**}$  means that the derivatives of g are not solved simultaneously, but that the forward derivatives of  $g^{**}$  are calculated as an extrapolation based on the approximation at lower  $\sigma$ . This is exactly what does the  $\langle$  **Approximation**::walkStochSteady code 194 $\rangle$ . It starts at the deterministic steady state, and in a few steps it adds to  $\sigma$  explicitly expressing forward  $g^{**}$  from a previous step.

Further details on the both solution methods are given in (todo: put references here when they exist).

Very important note: all classes here used for calculation of decision rule approximation are folded. For the time being, it seems that faa Di Bruno formula is quicker for folded tensors, and that is why we stick to folded tensors here. However, when the calcs are done, we calculate also its unfolded versions, to be available for simulations and so on.

183. This class is used to calculate derivatives by faa Di Bruno of the

$$f(g^{**}(g^*(y^*, u, \sigma), u', \sigma), g(y^*, u, \sigma), y^*, u)$$

with respect u'. In order to keep it as simple as possible, the class represents an equivalent (with respect to u') container for  $f(g^{**}(y^*, u', \sigma), 0, 0, 0)$ . The class is used only for evaluation of approximation error in **Approximation** class, which is calculated in **Approximation** :: calcStochShift method.

Since it is a folded version, we inherit from **StackContainer**  $\langle \mathbf{FGSTensor} \rangle$  and **FoldedStackContainer**. To construct it, we need only the  $g^{**}$  container and size of stacks.

```
⟨ZAuxContainer class declaration 183⟩ ≡
  class ZAuxContainer : public StackContainer⟨FGSTensor⟩, public FoldedStackContainer {
    public:
        typedef StackContainer⟨FGSTensor⟩::_Ctype _Ctype;
        typedef StackContainer⟨FGSTensor⟩::itype itype;
        ZAuxContainer(const _Ctype *gss,int ngss,int ng,int ny,int nu);
        itype getType(int i, const Symmetry &s) const;
    };
This code is cited in section 202.
This code is used in section 182.
```

184. This class provides an interface to approximation algorithms. The core method is walkStochSteady which calculates the approximation about stochastic steady state in a given number of steps. The number is given as a parameter ns of the constructor. If the number is equal to zero, the resulted approximation is about the deterministic steady state.

An object is constructed from the **DynamicModel**, and the number of steps ns. Also, we pass a reference to journal. That's all. The result of the core method walkStochSteady is a decision rule dr and a matrix ss whose columns are steady states for increasing  $\sigma$  during the walk. Both can be retrived by public methods. The first column of the matrix is the deterministic steady state, the last is the stochastic steady state for the full size shocks.

The method walkStochSteady calls the following methods: approxAtSteady calculates an initial approximation about the deterministic steady, saveRuleDerivs saves derivatives of a rule for the following step in  $rule\_ders$  and  $rule\_ders\_ss$  (see  $\langle$  **Approximation**:: saveRuleDerivs code 201 $\rangle$  for their description), check reports an error of the current approximation and calcStochShift (called from check) calculates a shift of the system equations due to uncertainity.

dr\_centralize is a new option. dynare++ was automatically expressing results around the fixed point instead of the deterministic steady state. dr\_centralize controls this behavior.

```
\langle Approximation class declaration 184 \rangle \equiv
 class Approximation {
    DynamicModel & model;
    Journal & journal;
    FGSContainer *rule_ders;
    FGSContainer *rule_ders_ss;
    FoldDecisionRule *fdr;
    UnfoldDecisionRule *udr;
    const PartitionY ypart;
    const FNormalMoments mom;
    IntSequence nvs;
    int steps;
    bool dr_centralize;
    double qz_criterium;
    TwoDMatrix ss;
 public:
    Approximation(DynamicModel &m, Journal &j, int ns, bool dr_centr, double qz_crit);
    virtual \simApproximation();
    const FoldDecisionRule & getFoldDecisionRule() const;
    const UnfoldDecisionRule & getUnfoldDecisionRule() const;
    const TwoDMatrix & getSS() const
    \{ \text{ return } ss; \}
    const DynamicModel & getModel() const
    { return model; }
    void walkStochSteady();
    TwoDMatrix *calcYCov() const;
    const FGSContainer *get_rule_ders() const
    { return rule_ders; }
    const FGSContainer *get_rule_ders_ss() const
    { return rule_ders; }
 protected:
    void approxAtSteady();
    void calcStochShift(Vector & out, double at_sigma) const;
    void saveRuleDerivs (const FGSContainer &g);
```

```
void check(double at_sigma) const;
  };
This code is used in section 182.
185.
       End of approximation.h file.
186.
       Start of approximation.cpp file.
#include "kord_exception.h"
\#include "approximation.h"
#include "first_order.h"
#include "korder_stoch.h"
   ZAuxContainer constructor code 187);
   ZAuxContainer :: getType \text{ code } 188 >;
   Approximation constructor code 189 \;
   Approximation destructor code 190 \;
   Approximation:: getFoldDecisionRule code 191 \rangle;
   Approximation:: getUnfoldDecisionRule \text{ code } 192;
   Approximation :: approxAtSteady \text{ code } 193;
   Approximation:: walkStochSteady code 194\rangle;
   Approximation:: saveRuleDerivs \text{ code } 201 \rangle;
   \langle Approximation :: calcStochShift code 202 \rangle;
   \langle Approximation :: check \text{ code } 205 \rangle;
  \langle Approximation :: calc YCov \text{ code } 206 \rangle;
187.
\langle \mathbf{ZAuxContainer} \ \text{constructor code } 187 \rangle \equiv
  ZAuxContainer::ZAuxContainer(const _Ctype *gss, int ngss, int ng, int ny, int nu)
  : StackContainer\langle FGSTensor \rangle (4,1) {
     stack\_sizes[0] = ngss;
     stack\_sizes[1] = ng;
     stack\_sizes[2] = ny;
     stack\_sizes[3] = nu;
     conts[0] = gss;
     calculateOffsets();
  }
This code is used in section 186.
188. The getType method corresponds to f(g^{**}(y^*, u', \sigma), 0, 0, 0). For the first argument we return matrix,
for other three we return zero.
\langle \mathbf{ZAuxContainer} :: getType \text{ code } 188 \rangle \equiv
  ZAuxContainer::itype ZAuxContainer::qetType(int i, const Symmetry \& s) const
     if (i \equiv 0)
       if (s[2] > 0) return zero;
       else return matrix;
     return zero;
This code is used in section 186.
```

189.

```
APPROXIMATING MODEL SOLUTION
```

```
\langle Approximation constructor code 189\rangle \equiv
  Approximation::Approximation(DynamicModel &m, Journal &j, int ns, bool dr_centr, double
            qz_{-}crit)
  : model(m), journal(j), rule\_ders(\Lambda), rule\_ders\_ss(\Lambda),
          fdr(\Lambda), udr(\Lambda), ypart(model.nstat(), model.npred(), model.nboth(), model.nforw()),
         mom(\mathbf{UNormalMoments}(model.order(), model.getVcov())), \ nvs(4), \ steps(ns),
         dr\_centralize(dr\_centr), qz\_criterium(qz\_crit), ss(ypart.ny(), steps + 1) {
    nvs[0] = ypart.nys();
    nvs[1] = model.nexog();
    nvs[2] = model.nexog();
    nvs[3] = 1;
    ss.nans();
This code is used in section 186.
190.
\langle Approximation destructor code 190\rangle \equiv
  Approximation :: \sim Approximation()
    if (rule_ders_ss) delete rule_ders_ss;
    if (rule_ders) delete rule_ders;
    if (fdr) delete fdr;
    if (udr) delete udr;
This code is used in section 186.
191. This just returns fdr with a check that it is created.
\langle Approximation :: qetFoldDecisionRule code 191 \rangle \equiv
  const FoldDecisionRule &Approximation:: getFoldDecisionRule() const
    KORD_RAISE_IF(fdr \equiv \Lambda,
         "Folded_decision_rule_has_not_been_created_in_Approximation::getFoldDecisionRule");
    return *fdr;
This code is used in section 186.
192. This just returns udr with a check that it is created.
\langle Approximation :: qetUnfoldDecisionRule code 192 \rangle \equiv
  const\ UnfoldDecisionRule\ \& Approximation :: getUnfoldDecisionRule()\ const
    KORD\_RAISE\_IF(udr \equiv \Lambda, "Unfolded\_decision\_rule\_has\_not\_been\_created\_in\_Approximatio
         n::getUnfoldDecisionRule");
    return *udr;
This code is used in section 186.
```

193. This methods assumes that the deterministic steady state is model.getSteady(). It makes an approximation about it and stores the derivatives to  $rule\_ders$  and  $rule\_ders\_ss$ . Also it runs a check for  $\sigma = 0$ .

```
\langle Approximation :: approxAtSteady \text{ code } 193 \rangle \equiv
  void Approximation :: approxAtSteady()
    model.calcDerivativesAtSteady();
    FirstOrder fo(model.nstat(), model.npred(), model.nboth(), model.nforw(), model.nexog(),
         *(model.getModelDerivatives().get(Symmetry(1))), journal, qz\_criterium);
    KORD\_RAISE\_IF\_X(\neg fo.isStable(), "The\_model\_is\_not\_Blanchard-Kahn\_stable",
         KORD_MD_NOT_STABLE);
    if (model.order() \ge 2) {
       KOrder korder(model.nstat(), model.npred(), model.nboth(), model.nforw(),
           model.getModelDerivatives(), fo.getGy(), fo.getGu(), model.getVcov(), journal);
       korder.switchToFolded();
       for (int k = 2; k \le model.order(); k++) korder.performStep < KOrder::<math>fold > (k);
       saveRuleDerivs(korder.getFoldDers());
    else {
       FirstOrderDerivs \langle KOrder :: fold \rangle fo_ders(fo);
       saveRuleDerivs(fo\_ders);
    check(0.0);
  }
This code is used in section 186.
```

## **194.** This is the core routine of **Approximation** class.

First we solve for the approximation about the deterministic steady state. Then we perform steps cycles toward the stochastic steady state. Each cycle moves the size of shocks by dsigma = 1.0/steps. At the end of a cycle, we have  $rule\_ders$  being the derivatives at stochastic steady state for  $\sigma = sigma\_so\_far + dsigma$  and model.getSteady() being the steady state.

If the number of *steps* is zero, the decision rule dr at the bottom is created from derivatives about deterministic steady state, with size of  $\sigma = 1$ . Otherwise, the dr is created from the approximation about stochastic steady state with  $\sigma = 0$ .

Within each cycle, we first make a backup of the last steady (from initialization or from a previous cycle), then we calculate the fix point of the last rule with  $\sigma = dsigma$ . This becomes a new steady state at the  $\sigma = sigma\_so\_far + dsigma$ . We calculate expectations of  $g^{**}(y, \sigma \eta_{t+1}, \sigma)$  expressed as a Taylor expansion around the new  $\sigma$  and the new steady state. Then we solve for the decision rule with explicit  $g^{**}$  at t+1 and save the rule.

After we reached  $\sigma = 1$ , the decision rule is formed.

The biproduct of this method is the matrix ss, whose columns are steady states for subsequent  $\sigma s$ . The first column is the deterministic steady state, the last column is the stochastic steady state for a full size of shocks ( $\sigma = 1$ ). There are steps + 1 columns.

```
\langle Approximation :: walkStochSteady code 194 \rangle \equiv
  void Approximation :: walkStochSteady()
     (initial approximation at deterministic steady 195);
     double sigma\_so\_far = 0.0;
     double dsigma = (steps \equiv 0) ? 0.0 : 1.0/steps;
     for (int i = 1; i < steps; i \leftrightarrow) {
       JournalRecordPair pa(journal);
       pa \ll "Approximation\_about\_stochastic\_steady\_for\_sigma=" \ll sigma\_so\_far + dsigma \ll endrec;
       Vector last_steady((const Vector &) model.getSteady());
       \langle calculate fix-point of the last rule for dsigma \ 196 \rangle;
        \langle calculate hh as expectations of the last g^{**} 197\rangle;
        \langle \text{ form KOrderStoch}, \text{ solve and save } 198 \rangle;
       check(sigma\_so\_far + dsigma);
       sigma\_so\_far += dsigma;
     (construct the resulting decision rules 199);
  }
This code is cited in section 182.
This code is used in section 186.
195. Here we solve for the deterministic steady state, calculate approximation at the deterministic steady
and save the steady state to ss.
\langle \text{ initial approximation at deterministic steady } 195 \rangle \equiv
  model.solveDeterministicSteady();
  approxAtSteady();
  Vector steady\theta(ss,0);
  steady0 = (\mathbf{const\ Vector\ }\&)\ model.getSteady();
This code is used in section 194.
```

```
We form the DRFixPoint object from the last rule with \sigma = dsigma. Then we save the steady
state to ss. The new steady is also put to model.getSteady().
\langle calculate fix-point of the last rule for dsigma 196 \rangle \equiv
    \mathbf{DRFixPoint}\langle \mathbf{KOrder}:: fold \rangle \ fp(*rule\_ders, ypart, model.getSteady(), dsigma);
    bool converged = fp.calcFixPoint(DecisionRule::horner, model.getSteady());
    JournalRecord rec(journal);
    fp.getNewtonTotalIter() \ll ", last_newton_iter=" \ll fp.getNewtonLastIter() \ll ".";
    if (converged) rec \ll " \Box Converged." \ll endrec;
    else {
         rec \ll " \ Not \ converged!!" \ll endrec;
         KORD_RAISE_X("Fix_point_calculation_not_converged", KORD_FP_NOT_CONV);
    Vector steadyi(ss, i);
    steadyi = (\mathbf{const} \ \mathbf{Vector} \ \&) \ model.getSteady();
This code is used in section 194.
197. We form the steady state shift dy, which is the new steady state minus the old steady state. Then
we create StochForwardDerivs object, which calculates the derivatives of g^{**} expectations at new sigma
and new steady.
\langle calculate hh as expectations of the last g^{**} 197\rangle \equiv
    Vector dy((\mathbf{const}\ \mathbf{Vector}\ \&)\ model.getSteady());
    dy.add(-1.0, last\_steady);
    \textbf{StochForwardDerivs} \\ \langle \textbf{KOrder} :: fold \rangle \ hh(ypart, model.nexog(), *rule\_ders\_ss, mom, dy, dsigma, dsi
              sigma\_so\_far);
    JournalRecord rec1 (journal);
    rec1 \ll "Calculation_{\square} of_{\square} g **_{\square} expectations_{\square} done" \ll endrec;
This code is used in section 194.
198. We calculate derivatives of the model at the new steady, form KOrderStoch object and solve, and
\langle form KOrderStoch, solve and save 198\rangle \equiv
    model.calcDerivativesAtSteady();
    KOrderStoch \ korder\_stoch(ypart, model.nexog(), model.getModelDerivatives(), hh, journal);
    for (int d = 1; d \leq model.order(); d \leftrightarrow ) {
         korder\_stoch.performStep < KOrder::fold > (d);
    saveRuleDerivs(korder_stoch.getFoldDers());
This code is used in section 194.
```

This code is used in section 199.

```
199.
\langle construct the resulting decision rules 199 \rangle \equiv
      if (fdr) {
            delete fdr;
            fdr = \Lambda;
      if (udr) {
            delete udr;
             udr = \Lambda;
      fdr = \mathbf{new} \ \mathbf{FoldDecisionRule}(*rule\_ders, ypart, model.nexog(), model.getSteady(), 1.0 - sigma\_so\_far);
      if (steps \equiv 0 \land dr\_centralize) {
             ⟨ centralize decision rule for zero steps 200 ⟩;
This code is used in section 194.
200.
\langle centralize decision rule for zero steps 200\rangle \equiv
      DRFixPoint \langleKOrder :: fold\rangle fp (*rule_ders, ypart, model.getSteady(), 1.0);
      \mathbf{bool}\ \ converged = \mathit{fp.calcFixPoint}(\mathbf{DecisionRule} :: horner, model.getSteady());
      JournalRecord rec(journal);
      rec \ll "Fix_point_calcs:_iiter=" \ll fp.qetNumIter() \ll ",_inewton_iiter=" \ll fp.qetNumIter() \times ",_inewton_iiter=" \times fp.qetNumIter() \times f
                   fp.getNewtonTotalIter() \ll ", last_newton_iter=" \ll fp.getNewtonLastIter() \ll ".";
      if (converged) rec \ll " \Box Converged." \ll endrec;
             rec \ll " \sqcup Not \sqcup converged!!" \ll endrec;
            KORD_RAISE_X("Fix_point_calculation_not_converged", KORD_FP_NOT_CONV);
             JournalRecordPair recp(journal);
             recp \ll "Centralizing_{\square}about_{\square}fix-point." \ll endrec;
             FoldDecisionRule *dr\_backup = fdr;
            fdr = new FoldDecisionRule(*dr_backup, model.getSteady());
            delete dr\_backup;
```

**201.** Here we simply make a new hardcopy of the given rule *rule\_ders*, and make a new container of inplace subtensors of the derivatives corresponding to forward looking variables. The given container comes from a temporary object and will be destroyed.

```
⟨ Approximation::saveRuleDerivs code 201⟩ ≡

void Approximation::saveRuleDerivs(const FGSContainer &g)
{
    if (rule_ders) {
        delete rule_ders;
        delete rule_ders_ss;
    }

    rule_ders = new FGSContainer(g);
    rule_ders_ss = new FGSContainer(4);
    for (FGSContainer::iteratorrun = (*rule_ders).begin(); run ≠ (*rule_ders).end(); ++run) {
        FGSTensor *ten = new FGSTensor(ypart.nstat + ypart.npred, ypart.nyss(), *((*run).second));
        rule_ders_ss→insert(ten);
    }
}

This code is cited in section 184.

This code is used in section 186.
```

**202.** This method calculates a shift of the system equations due to integrating shocks at a given  $\sigma$  and current steady state. More precisely, if

$$F(y, u, u', \sigma) = f(g^{**}(g^{*}(y, u, \sigma), u', \sigma), g(y, u, \sigma), y, u)$$

then the method returns a vector

This code is used in section 186.

$$\sum_{d=1} \frac{1}{d!} \sigma^d \left[ F_{u'^d} \right]_{\alpha_1 \dots \alpha_d} \Sigma^{\alpha_1 \dots \alpha_d}$$

For a calculation of  $[F_{u'^d}]$  we use  $\langle \mathbf{ZAuxContainer} \text{ class declaration 183} \rangle$ , so we create its object. In each cycle we calculate  $[F_{u'^d}]$ , and then multiply with the shocks, and add the  $\frac{\sigma^d}{d!}$  multiple to the result.

```
203.
```

90

```
\langle \text{ calculate } F_{n'^d} \text{ via } \mathbf{ZAuxContainer } 203 \rangle \equiv
  FGSTensor *ten = new FGSTensor(ypart.ny(), TensorDimens(sym, nvs));
  ten \neg zeros();
  for (int l = 1; l < d; l ++) {
     const\ FSSparseTensor\ *f = model.getModelDerivatives().get(Symmetry(l));
     zaux.multAndAdd(*f,*ten);
  }
This code is used in section 202.
204.
\langle multiply with shocks and add to result 204\rangle \equiv
  \mathbf{FGSTensor} *tmp = \mathbf{new} \ \mathbf{FGSTensor}(ypart.ny(), \mathbf{TensorDimens}(\mathbf{Symmetry}(0, 0, 0, 0), nvs));
  tmp \neg zeros();
  ten \neg contractAndAdd(1, *tmp, *(mom.get(Symmetry(d))));
  out.add(pow(at\_sigma, d)/dfac, tmp \neg getData());
  delete ten;
  delete tmp:
This code is used in section 202.
```

205. This method calculates and reports

$$f(\bar{y}) + \sum_{d=1}^{\infty} \frac{1}{d!} \sigma^d \left[ F_{u'^d} \right]_{\alpha_1 \dots \alpha_d} \Sigma^{\alpha_1 \dots \alpha_d}$$

```
at \bar{y}, zero shocks and \sigma. This number should be zero.
        We evaluate the error both at a given \sigma and \sigma = 1.0.
\langle Approximation :: check code 205 \rangle \equiv
        void Approximation:: check(double at_sigma) const
                  Vector stoch_shift(ypart.ny());
                 Vector system_resid(ypart.ny());
                 Vector xx(model.nexog());
                 xx.zeros();
                 model.evaluateSystem(system\_resid, model.getSteady(), xx);
                 calcStochShift(stoch_shift, at_sigma);
                 stoch\_shift.add(1.0, system\_resid);
                 JournalRecord rec1 (journal);
                 rec1 \ll "Error_{\sqcup} of_{\sqcup} current_{\sqcup} approximation_{\sqcup} for_{\sqcup} shocks_{\sqcup} at_{\sqcup} sigma_{\sqcup}" \ll at\_sigma \ll "_{\sqcup} is_{\sqcup}" \ll at\_sigma
                                  stoch\_shift.getMax() \ll endrec;
                 calcStochShift(stoch_shift, 1.0);
                 stoch\_shift.add(1.0, system\_resid);
                 JournalRecord rec2(journal);
                 rec2 \ll "Error_{\cup}of_{\cup}current_{\cup}approximation_{\cup}for_{\cup}full_{\cup}shocks_{\cup}is_{\cup}" \ll stoch\_shift.getMax() \ll sto
This code is used in section 186.
```

**206.** The method returns unconditional variance of endogenous variables based on the first order. The first order approximation looks like

$$\hat{y}_t = g_{y^*} \hat{y}_{t-1}^* + g_u u_t$$

where  $\hat{y}$  denotes a deviation from the steady state. It can be written as

$$\hat{y}_t = [0 \, g_{y^*} \, 0] \, \hat{y}_{t-1} + g_u u_t$$

which yields unconditional covariance V for which

$$V = GVG^T + g_u \Sigma g_u^T,$$

where  $G = [0 g_{y^*} 0]$  and  $\Sigma$  is the covariance of the shocks.

For solving this Lyapunov equation we use the Sylvester module, which solves equation of the type

$$AX + BX(C \otimes \cdots \otimes C) = D$$

```
So we invoke the Sylvester solver for the first dimension with A = I, B = -G, C = G^T and D = g_u \Sigma g_u^T.
\langle Approximation :: calc YCov \text{ code } 206 \rangle \equiv
  TwoDMatrix *Approximation:: calcYCov() const
    const TwoDMatrix &gy = *(rule\_ders \neg get(Symmetry(1, 0, 0, 0)));
    const TwoDMatrix & gu = *(rule\_ders \neg get(Symmetry(0, 1, 0, 0)));
    TwoDMatrix G(model.numeq(), model.numeq());
    G.zeros();
    G.place(gy, 0, model.nstat());
    TwoDMatrix B((const\ TwoDMatrix\ \&)\ G);
    B.mult(-1.0);
    TwoDMatrix C(G, "transpose");
    TwoDMatrix A(model.numeq(), model.numeq());
    A.zeros();
    for (int i = 0; i < model.numeq(); i +++) A.get(i, i) = 1.0;
    TwoDMatrix guSigma(gu, model.getVcov());
    TwoDMatrix guTrans(gu, "transpose");
    TwoDMatrix *X = new TwoDMatrix(guSigma, guTrans);
    GeneralSylvester gs(1, model.numeq(), model.numeq(), 0, A.base(), B.base(), C.base(), X \neg base());
    gs.solve();
    return X;
```

207. End of approximation.cpp file.

This code is used in section 186.

## 208. Decision rule and simulation. Start of decision\_rule.h file.

The main purpose of this file is a decision rule representation which can run a simulation. So we define an interface for classes providing realizations of random shocks, and define the class **DecisionRule**. The latter basically takes tensor container of derivatives of policy rules, and adds them up with respect to  $\sigma$ . The class allows to specify the  $\sigma$  different from 1.

In addition, we provide classes for running simulations and storing the results, calculating some statistics and generating IRF. The class **DRFixPoint** allows for calculation of the fix point of a given decision rule.

```
#ifndef DECISION_RULE_H
#define DECISION_RULE_H
#include <matio.h>
#include "kord_exception.h"
#include "korder.h"
#include "normal_conjugate.h"
#include "mersenne_twister.h"
  (ShockRealization class declaration 209);
   DecisionRule class declaration 210);
   DecisionRuleImpl class declaration 211 >:
   FoldDecisionRule class declaration 224);
   UnfoldDecisionRule class declaration 225);
   DRFixPoint class declaration 226);
   SimResults class declaration 233);
   SimResultsStats class declaration 234);
   SimResultsDynamicStats class declaration 235);
   SimResultsIRF class declaration 236);
   RTSimResultsStats class declaration 237 :
   IRFResults class declaration 238);
   SimulationWorker class declaration 239);
   SimulationIRFWorker class declaration 240);
   RTSimulationWorker class declaration 241);
   RandomShockRealization class declaration 242);
   ExplicitShockRealization class declaration 243);
   GenShockRealization class declaration 244);
#endif
```

**209.** This is a general interface to a shock realizations. The interface has only one method returning the shock realizations at the given time. This method is not constant, since it may change a state of the object.

```
⟨ ShockRealization class declaration 209⟩ ≡
  class ShockRealization {
  public:
    virtual ~ShockRealization() {}
    virtual void get(int n, Vector &out) = 0;
    virtual int numShocks() const = 0;
  };
This code is used in section 208.
```

210. This class is an abstract interface to decision rule. Its main purpose is to define a common interface for simulation of a decision rule. We need only a simulate, evaluate, cetralized clone and output method. The *simulate* method simulates the rule for a given realization of the shocks. *eval* is a primitive evaluation (it takes a vector of state variables (predetermined, both and shocks) and returns the next period variables. Both input and output are in deviations from the rule's steady. *evaluate* method makes only one step of simulation (in terms of absolute values, not deviations). *centralizedClone* returns a new copy of the decision rule, which is centralized about provided fix-point. And finally *writeMat* writes the decision rule to the MAT file.

```
\langle \mathbf{DecisionRule} \ \mathrm{class} \ \mathrm{declaration} \ 210 \rangle \equiv
  class DecisionRule {
  public:
    enum emethod { horner, trad };
    virtual ~DecisionRule() {}
    virtual TwoDMatrix *simulate(emethod em, int np, const Vector &ystart, ShockRealization
         & sr) const = 0;
    virtual void eval (emethod em, Vector & out, const Const Vector & v) const = 0:
    virtual void evaluate (emethod em, Vector & out, const ConstVector & ys, const ConstVector
         &u) \mathbf{const} = 0;
    virtual void writeMat(mat_{-}t * fd, \mathbf{const} \ \mathbf{char} * prefix) \ \mathbf{const} = 0;
    virtual DecisionRule *centralizedClone (const Vector & fixpoint) const = 0;
    virtual const Vector \&getSteady() const = 0;
    virtual int nexog() const = 0;
    virtual const PartitionY & getYPart() const = 0;
  };
This code is used in section 208.
```

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protected:

The main purpose of this class is to implement **DecisionRule** interface, which is a simulation. To be able to do this we have to know the partitioning of state vector y since we will need to pick only predetermined part  $y^*$ . Also, we need to know the steady state.

The decision rule will take the form:

$$y_t - \bar{y} = \sum_{i=0}^n \left[ g_{(yu)^i} \right]_{\alpha_1 \dots \alpha_i} \prod_{m=1}^i \left[ \begin{array}{c} y_{t-1}^* - \bar{y}^* \\ u_t \end{array} \right]^{\alpha_m},$$

where the tensors  $[g_{(yu)^i}]$  are tensors of the constructed container, and  $\bar{y}$  is the steady state.

If we know the fix point of the rule (conditional zero shocks)  $\tilde{y}$ , the rule can be transformed to so called "centralized" form. This is very similar to the form above but the zero dimensional tensor is zero:

$$y_t - \tilde{y} = \sum_{i=1}^n \left[ \tilde{g}_{(yu)^i} \right]_{\alpha_1 \dots \alpha_i} \prod_{m=1}^i \left[ \begin{array}{c} y_{t-1}^* - \tilde{y}^* \\ u_t \end{array} \right]^{\alpha_m}.$$

We provide a method and a constructor to transform a rule to the centralized form.

The class is templated, the template argument is either **KOrder**:: fold or **KOrder**:: unfold. So, there are two implementations of **DecisionRule** interface.

```
\langle DecisionRuleImpl class declaration 211 \rangle \equiv
  template (int t) class DecisionRuleImpl : public ctraits (t)::Tpol, public DecisionRule {
     typedef typename ctraits \langle t \rangle::Tpol_Tparent;
     const Vector ysteady;
     const PartitionY ypart;
     const int nu;
  public:
     DecisionRuleImpl(const_Tparent &pol, const PartitionY &yp, int nuu, const Vector &ys)
     : \mathbf{ctraits}\langle t \rangle :: \mathbf{Tpol}(pol), \ ysteady(ys), \ ypart(yp), \ nu(nuu) \ \{ \}
     DecisionRuleImpl(_Tparent &pol, const PartitionY &yp, int nuu, const Vector &ys)
     : \operatorname{ctraits}\langle t \rangle :: \operatorname{Tpol}(0, yp.ny(), pol), \ ysteady(ys), \ ypart(yp), \ nu(nuu) \ \{ \}
     DecisionRuleImpl(const \_Tg &g, const PartitionY &yp, int nuu, const Vector &ys, double
     : \operatorname{\mathbf{ctraits}}\langle t \rangle :: \operatorname{\mathbf{Tpol}}(yp.ny(), yp.nys() + nuu), \ ysteady(ys), \ ypart(yp), \ nu(nuu) \ \{
       fillTensors(g, sigma);  }
     DecisionRuleImpl(const DecisionRuleImpl\langle t \rangle \& dr, const ConstVector & fixpoint)
     : \operatorname{\mathbf{ctraits}}\langle t \rangle:: \operatorname{\mathbf{Tpol}}(dr.ypart.ny(), dr.ypart.nys() + dr.nu), ysteady(fixpoint), ypart(dr.ypart),
             nu(dr.nu) { centralize(dr); }
     const Vector &getSteady() const
     { return ysteady; }
     ⟨ DecisionRuleImpl :: simulate code 215 ⟩;
      DecisionRuleImpl:: evaluate code 220 \;
      DecisionRuleImpl:: centralizedClone code 221);
     \langle \mathbf{DecisionRuleImpl} :: writeMat \text{ code } 223 \rangle;
     int nexog() const
     \{ \mathbf{return} \ nu; \}
     const PartitionY &getYPart() const
       return ypart;
```

```
⟨ DecisionRuleImpl::fillTensors code 212⟩;
  ⟨ DecisionRuleImpl::centralize code 214⟩;
  ⟨ DecisionRuleImpl::eval code 222⟩;
  };
This code is used in section 208.
```

**212.** Here we have to fill the tensor polynomial. This involves two separated actions. First is to evaluate the approximation at a given  $\sigma$ , the second is to compile the tensors  $[g_{(yu)^{i+j}}]$  from  $[g_{y^iu^j}]$ . The first action is done here, the second is done by method addSubTensor of a full symmetry tensor.

The way how the evaluation is done is described here:

The q-order approximation to the solution can be written as:

$$y_{t} - \bar{y} = \sum_{l=1}^{q} \frac{1}{l!} \left[ \sum_{i+j+k=l} {l \choose i,j,k} \left[ g_{y^{i}u^{j}\sigma^{k}} \right]_{\alpha_{1}...\alpha_{j}\beta_{1}...\beta_{j}} \prod_{m=1}^{i} [y_{t-1}^{*} - \bar{y}^{*}]^{\alpha_{m}} \prod_{n=1}^{j} [u_{t}]^{\beta_{m}} \sigma^{k} \right]$$

$$= \sum_{l=1}^{q} \left[ \sum_{i+j \leq l} {i+j \choose i} \left[ \sum_{k=0}^{l-i-j} \frac{1}{l!} {l \choose k} \left[ g_{y^{i}u^{j}\sigma^{k}} \right] \sigma^{k} \right] \prod_{m=1}^{i} [y_{t-1}^{*} - \bar{y}^{*}]^{\alpha_{m}} \prod_{n=1}^{j} [u_{t}]^{\beta_{m}} \sigma^{k} \right]$$

This means that for each i + j + k = l we have to add

This code is used in section 211.

$$\frac{1}{l!} \begin{pmatrix} l \\ k \end{pmatrix} \left[ g_{y^i u^j \sigma^k} \right] \cdot \sigma^k = \frac{1}{(i+j)!k!} \left[ g_{y^i u^j \sigma^k} \right] \cdot \sigma^k$$

to  $g_{(yu)^{i+j}}$ . In addition, note that the multiplier  $\binom{i+j}{i}$  is applied when the fully symmetric tensor  $[g_{(yu)^{i+j}}]$  is evaluated.

So we go through  $i+j=d=0\dots q$  and in each loop we form the fully symmetric tensor  $[g_{(yu)^l}]$  and insert it to the container.

```
 \begin{tabular}{l} \textbf{OecisionRuleImpl} :: fill Tensors \ code \ 212 \end{tabular} \equiv \\ \textbf{void} \ fill Tensors (\textbf{const } \_\textbf{Tg} \& g, \textbf{double} \ sigma) \\ \{ & \textbf{IntSequence} \ tns(2); \\ tns[0] = ypart.nys(); \\ tns[1] = nu; \\ \textbf{int} \ dfact = 1; \\ \textbf{for} \ (\textbf{int} \ d = 0; \ d \leq g.getMaxDim(); \ d++, dfact *= d) \ \{ \\ & \_\textbf{Ttensym} \ *g\_yud = \textbf{new} \ \_\textbf{Ttensym}(ypart.ny(), ypart.nys() + nu, d); \\ g\_yud \neg zeros(); \\ & \langle \text{fill tensor of} \ g\_yud \ of \ dimension} \ d \ 213 \end{tabular} ; \\ & \textbf{this} \neg insert(g\_yud); \\ \} \\ \} \\ \end{tabular}  This code is cited in section 213. }
```

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**213.** Here we have to fill the tensor  $[g_{(yu)^d}]$ . So we go through all pairs (i,j) giving i+j=d, and through all k from zero up to maximal dimension minus d. In this way we go through all symmetries of  $g_{y^iu^j\sigma^k}$  which will be added to  $g_{(uu)^d}$ .

Note that at the beginning, dfact is a factorial of d. We calculate kfact is equal to k!. As indicated in  $\langle \mathbf{DecisionRuleImpl} :: fillTensors \text{ code } 212 \rangle$ , the added tensor is thus multiplied with  $\frac{1}{dlk!} \sigma^k$ .

```
 \begin{split} & \langle \text{ fill tensor of } g\text{-}yud \text{ of dimension } d \text{ } 213 \rangle \equiv \\ & \text{ for (int } i=0; \text{ } i \leq d; \text{ } i\text{++}) \text{ } \{ \\ & \text{ int } j=d-i; \\ & \text{ int } kfact=1; \\ & \text{-}\textbf{Ttensor } tmp(ypart.ny(), \textbf{TensorDimens}(\textbf{Symmetry}(i,j),tns)); \\ & tmp.zeros(); \\ & \text{ for (int } k=0; \text{ } k+d \leq g.getMaxDim(); \text{ } k\text{++}, kfact *=k) \text{ } \{ \\ & \text{ Symmetry } sym(i,j,0,k); \\ & \text{ if } (g.check(sym)) \text{ } \{ \\ & \text{ double } mult = pow(sigma,k)/dfact/kfact; \\ & tmp.add(mult,*(g.get(sym))); \\ & \text{ } \} \\ & g\text{-}yud\text{--}addSubTensor(tmp); \\ & \} \end{split}  This code is used in section 212.
```

**214.** The centralization is straightforward. We suppose here that the object's steady state is the fix point  $\tilde{y}$ . It is clear that the new derivatives  $\left[\tilde{g}_{(yu)^i}\right]$  will be equal to the derivatives of the original decision rule dr at the new steady state  $\tilde{y}$ . So, the new derivatives are obtained by derivating the given decision rule dr and evaluating its polynomial at

 $dstate = \begin{bmatrix} \tilde{y}^* - \bar{y}^* \\ 0 \end{bmatrix},$ 

where  $\bar{y}$  is the steady state of the original rule dr.

```
\langle \text{ DecisionRuleImpl} :: centralize \text{ code } 214 \rangle \equiv
  void centralize(\mathbf{const}\ \mathbf{DecisionRuleImpl}\ \&dr)
     Vector dstate(ypart.nys() + nu);
     dstate.zeros();
     Vector dstate\_star(dstate, 0, ypart.nys());
     ConstVector newsteady_star(ysteady, ypart.nstat, ypart.nys());
     ConstVector oldsteady\_star(dr.ysteady, ypart.nstat, ypart.nys());
     dstate\_star.add(1.0, newsteady\_star);
     dstate\_star.add(-1.0, oldsteady\_star);
     Tpol pol(dr);
     int dfac = 1;
     for (int d = 1; d \leq dr.getMaxDim(); d \leftrightarrow dfac *= d) {
        pol.derivative(d-1);
        \_Ttensym *der = pol.evalPartially(d, dstate);
        der \rightarrow mult(1.0/dfac);
        \mathbf{this} \rightarrow insert(der);
  }
This code is used in section 211.
```

**215.** Here we evaluate repeatedly the polynomial storing results in the created matrix. For exogenous shocks, we use **ShockRealization** class, for predetermined variables, we use ystart as the first state. The ystart vector is required to be all state variables ypart.ny(), although only the predetermined part of ystart is used.

We simulate in terms of  $\Delta y$ , this is, at the beginning the *ysteady* is canceled from *ystart*, we simulate, and at the end *ysteady* is added to all columns of the result.

```
\langle \text{ DecisionRuleImpl} :: simulate \text{ code } 215 \rangle \equiv
  TwoDMatrix *simulate (emethod em, int np, const Vector \&ystart, ShockRealization \&sr) const
     {\tt KORD\_RAISE\_IF}(ysteady.length() \neq ystart.length(),
          "Start_{\square}and_{\square}steady_{\square}lengths_{\square}differ_{\square}in_{\square}DecisionRuleImpl::simulate");
     TwoDMatrix *res = new TwoDMatrix(ypart.ny(), np);
     (initialize vectors and subvectors for simulation 216);
     \langle \text{ perform the first step of simulation } 217 \rangle;
     \langle \text{ perform all other steps of simulations } 218 \rangle;
     \langle add the steady state to columns of res 219\rangle;
     return res;
  }
This code is used in section 211.
216. Here allocate the stack vector (\Delta y^*, u), define the subvectors dy, and u, then we pickup predetermined
parts of ystart and ysteady.
\langle initialize vectors and subvectors for simulation 216\rangle \equiv
  Vector dyu(ypart.nys() + nu);
  ConstVector ystart_pred(ystart, ypart.nstat, ypart.nys());
  ConstVector ysteady_pred(ysteady, ypart.nstat, ypart.nys());
  Vector dy(dyu, 0, ypart.nys());
  Vector u(dyu, ypart.nys(), nu);
See also section 277.
This code is used in sections 215 and 276.
217. We cancel ysteady from ystart, get realization to u, and evaluate the polynomial.
\langle perform the first step of simulation 217 \rangle \equiv
  dy = ystart\_pred;
  dy.add(-1.0, ysteady\_pred);
  sr.get(0,u);
  Vector out(*res, 0);
  eval(em, out, dyu);
This code is used in section 215.
```

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Also clear. If the result at some period is not finite, we pad the rest of the matrix with zeros.

```
\langle perform all other steps of simulations 218\rangle \equiv
  int i = 1;
  while (i < np) {
    ConstVector ym(*res, i-1);
    ConstVector dym(ym, ypart.nstat, ypart.nys());
    dy = dym;
    sr.get(i, u);
    Vector out(*res, i);
    eval(em, out, dyu);
    if (\neg out.isFinite())  {
      if (i + 1 < np) {
         TwoDMatrix rest(*res, i + 1, np - i - 1);
         rest.zeros();
      break;
    i++;
  }
```

This code is used in section 215.

219. Even clearer. We add the steady state to the numbers computed above and leave the padded columns to zero.

```
\langle add the steady state to columns of res 219\rangle \equiv
  for (int j = 0; j < i; j ++) {
     Vector col(*res, j);
     col.add(1.0, ysteady);
```

This code is used in section 215.

**220.** This is one period evaluation of the decision rule. The simulation is a sequence of repeated one period evaluations with a difference, that the steady state (fix point) is cancelled and added once. Hence we have two special methods.

```
\langle \mathbf{DecisionRuleImpl} :: evaluate \ \mathrm{code} \ 220 \rangle \equiv
  void evaluate (emethod em, Vector & out, const ConstVector & ys, const ConstVector & u) const
    KORD_RAISE_IF(ys.length() \neq ypart.nys() \lor u.length() \neq nu,
         "Wrong_dimensions_of_input_vectors_in_DecisionRuleImpl::evaluate");
    KORD_RAISE_IF(out.length() \neq ypart.ny(),
         "Wrong_dimension_of_output_vector_in_DecisionRuleImpl::evaluate");
    ConstVector ysteady_pred(ysteady, ypart.nstat, ypart.nys());
    Vector ys_u(ypart.nys() + nu);
    Vector ys\_u1(ys\_u, 0, ypart.nys());
    ys_{-}u1 = ys;
    ys\_u1.add(-1.0, ysteady\_pred);
    Vector ys_{-}u2(ys_{-}u, ypart.nys(), nu);
    ys_{-}u2 = u;
    eval(em, out, ys_u);
    out.add(1.0, ysteady);
This code is used in section 211.
221. This is easy. We just return the newly created copy using the centralized constructor.
\langle DecisionRuleImpl :: centralizedClone code 221 \rangle \equiv
  DecisionRule *centralizedClone(const Vector &fixpoint) const
    return new DecisionRuleImpl\langle t \rangle(*this, fixpoint);
This code is used in section 211.
222. Here we only encapsulate two implementations to one, deciding according to the parameter.
\langle \mathbf{DecisionRuleImpl} :: eval \ \mathbf{code} \ \mathbf{222} \rangle \equiv
  void eval(emethod em, Vector &out, const ConstVector &v) const
    if (em \equiv \mathbf{DecisionRule} :: horner) _Tparent :: evalHorner(out, v);
    else \_Tparent :: evalTrad(out, v);
This code is used in section 211.
```

Dynare++ 223. Write the decision rule and steady state to the MAT file.  $\langle \mathbf{DecisionRuleImpl} :: writeMat \text{ code } 223 \rangle \equiv$ void  $writeMat(mat_t * fd, const char * prefix) const$  $\mathbf{ctraits}\langle t \rangle :: \mathbf{Tpol} :: writeMat(fd, prefix);$ **TwoDMatrix** dum(ysteady.length(),1); dum.getData() = ysteady;char tmp[100];  $sprintf(tmp, "%s_ss", prefix);$ ConstTwoDMatrix(dum).writeMat(fd, tmp);This code is used in section 211. This is exactly the same as **DecisionRuleImpl**(**KOrder**:: fold). The only difference is that we have a conversion from UnfoldDecisionRule, which is exactly DecisionRuleImpl(KOrder::unfold).  $\langle$  FoldDecisionRule class declaration 224 $\rangle$   $\equiv$ class UnfoldDecisionRule; class  $FoldDecisionRule : public DecisionRuleImpl\langle KOrder :: fold \rangle$  { friend class UnfoldDecisionRule: public: FoldDecisionRule(const ctraits KOrder:: fold)::Tpol &pol, const PartitionY &yp, int nuu, const Vector &ys) :  $\mathbf{DecisionRuleImpl}\langle \mathbf{KOrder} :: fold \rangle (pol, yp, nuu, ys) \ \{ \ \}$ FoldDecisionRule(ctraits  $\langle KOrder :: fold \rangle :: Tpol \& pol, const PartitionY \& yp, int nuu, const$ Vector &ys) :  $\mathbf{DecisionRuleImpl}\langle \mathbf{KOrder} :: fold \rangle (pol, yp, nuu, ys) \ \{ \ \}$ FoldDecisionRule(const ctraits  $\langle KOrder :: fold \rangle :: Tg \& g$ , const PartitionY & yp, int nuu, const Vector &ys, double sigma) : DecisionRuleImpl $\langle$ KOrder:: $fold \rangle (g, yp, nuu, ys, sigma) \{ \}$ FoldDecisionRule(const DecisionRuleImpl $\langle KOrder::fold \rangle \&dr$ , const ConstVector &fixpoint)

This code is used in section 208.

};

: **DecisionRuleImpl** $\langle$ **KOrder**:: $fold \rangle (dr, fixpoint) \{ \}$ FoldDecisionRule (const UnfoldDecisionRule &udr); This code is used in section 208.

```
This is exactly the same as DecisionRuleImpl\langle KOrder :: unfold \rangle, but with a conversion from
FoldDecisionRule, which is exactly DecisionRuleImpl(KOrder:: fold).
\langle \, \text{UnfoldDecisionRule class declaration} \, \, 225 \, \rangle \equiv
  {\bf class} \ {\bf UnfoldDecisionRule}: {\bf public} \ {\bf DecisionRuleImpl} \langle {\bf KOrder} :: {\it unfold} \rangle \ \{
     friend class FoldDecisionRule;
  public:
     \mathbf{UnfoldDecisionRule}(\mathbf{const}\ \mathbf{ctraits} \\ \\ \langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{Tpol}\ \&pol, \mathbf{const}\ \mathbf{PartitionY}\ \&yp, \mathbf{int}
                 nuu, const Vector & ys)
     : DecisionRuleImpl\langle KOrder :: unfold \rangle (pol, yp, nuu, ys) \}
     \mathbf{UnfoldDecisionRule}(\mathbf{ctraits} \langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{Tpol} \ \&pol, \mathbf{const} \ \mathbf{PartitionY} \ \&yp, \mathbf{int}
                 nuu, const Vector &ys)
     : \mathbf{DecisionRuleImpl}\langle \mathbf{KOrder} :: unfold \rangle (pol, yp, nuu, ys) \ \{ \ \}
     UnfoldDecisionRule(const ctraits \( \) KOrder::unfold \( \)::Tg \( &q, \) const PartitionY \( &yp, \) int
                 nuu, const Vector & ys, double sigma)
     : DecisionRuleImpl\langleKOrder :: unfold\rangle(g, yp, nuu, ys, sigma) { }
     UnfoldDecisionRule(const\ DecisionRuleImpl\langle KOrder::unfold\rangle\ \&dr, const\ ConstVector
                 & fixpoint)
     : \mathbf{DecisionRuleImpl}\langle \mathbf{KOrder} :: unfold \rangle (dr, fixpoint) \{ \}
     UnfoldDecisionRule(const FoldDecisionRule &udr);
  };
```

**226.** This class serves for calculation of the fix point of the decision rule given that the shocks are zero. The class is very similar to the **DecisionRuleImpl**. Besides the calculation of the fix point, the only difference between **DRFixPoint** and **DecisionRuleImpl** is that the derivatives wrt. shocks are ignored (since shocks are zero during the calculations). That is why have a different *fillTensor* method.

The solution algorithm is Newton and is described in  $\langle \mathbf{DRFixPoint} :: solveNewton \text{ code } 230 \rangle$ . It solves F(y) = 0, where F = g(y,0) - y. The function F is given by its derivatives bigf. The Jacobian of the solved system is given by derivatives stored in bigfder.

```
\langle DRFixPoint class declaration 226 \rangle \equiv
  template (int t) class DRFixPoint : public ctraits (t) :: Tpol {
    typedef typename ctraits \langle t \rangle::Tpol _Tparent;
    static int max_iter;
    static int max_newton_iter;
    static int newton_pause;
    static double tol;
    const Vector ysteady;
    const PartitionY ypart;
    -Tparent *bigf:
    _Tparent *bigfder;
  public:
    typedef typename DecisionRule::emethod emethod;
     ⟨ DRFixPoint constructor code 227⟩;
     ⟨DRFixPoint destructor code 228⟩;
     \langle \mathbf{DRFixPoint} :: calcFixPoint \text{ code } 232 \rangle;
    int getNumIter() const
    { return iter; }
    int getNewtonLastIter() const
    { return newton_iter_last; }
    int getNewtonTotalIter() const
    { return newton_iter_total; }
  protected:
     ⟨ DRFixPoint :: fillTensors code 229 ⟩;
     \langle \mathbf{DRFixPoint} :: solveNewton \text{ code } 230 \rangle;
  private:
    int iter;
    int newton_iter_last;
    int newton_iter_total;
  };
```

This code is used in section 208.

This code is used in section 226.

**227.** Here we have to setup the function F = g(y,0) - y and  $\frac{\partial F}{\partial y}$ . The former is taken from the given derivatives of g where a unit matrix is subtracted from the first derivative (**Symmetry**(1)). Then the derivative of the F polynomial is calculated.

```
\langle \mathbf{DRFixPoint} \ \text{constructor code} \ 227 \rangle \equiv
  DRFixPoint(const _{-}Tg &g, const PartitionY &yp, const Vector &ys, double sigma)
  : \operatorname{ctraits}\langle t \rangle::\operatorname{Tpol}(yp.ny(),yp.nys()), ysteady(ys), ypart(yp), bigf(\Lambda), bigfder(\Lambda) {
     fillTensors(q, sigma);
     _Tparent yspol(ypart.nstat, ypart.nys(), *this);
     bigf = new _Tparent((const _Tparent &) yspol);
     \_Ttensym *frst = bigf \neg get(\mathbf{Symmetry}(1));
     for (int i = 0; i < ypart.nys(); i \leftrightarrow frst \neg get(i, i) = frst \neg get(i, i) - 1;
     bigfder = \mathbf{new} \ \_\mathbf{Tparent}(*bigf, 0);
  }
This code is used in section 226.
228.
\langle \mathbf{DRFixPoint} \ destructor \ code \ 228 \rangle \equiv
  virtual \sim DRFixPoint()
     if (biqf) delete biqf;
     if (bigfder) delete bigfder;
This code is used in section 226.
229. Here we fill the tensors for the DRFixPoint class. We ignore the derivatives g_{y^i u^j \sigma^k} for which j > 0.
So we go through all dimensions d, and all k such that d + k is between the maximum dimension and d, and
add \frac{\sigma^k}{d!k!}g_{y^d\sigma^k} to the tensor g_{(y)^d}.
\langle \mathbf{DRFixPoint} :: fillTensors \ \text{code} \ 229 \rangle \equiv
  void fillTensors(const _Tg &g, double sigma)
     int dfact = 1;
     for (int d = 0; d \le g.getMaxDim(); d++, dfact *= d) {
        \_Ttensym *g\_yd = new \_Ttensym(ypart.ny(), ypart.nys(), d);
        g_yd \rightarrow zeros();
        int kfact = 1;
        for (int k = 0; d + k \le g.getMaxDim(); k \leftrightarrow kfact *= k) {
          if (g.check(Symmetry(d, 0, 0, k))) {
             const _Ttensor *ten = g.get(\mathbf{Symmetry}(d, 0, 0, k));
             double mult = pow(sigma, k)/dfact/kfact;
             g_-yd \rightarrow add(mult, *ten);
        this\neg insert(g\_yd);
```

**230.** This tries to solve polynomial equation F(y) = 0, where F polynomial is bigf and its derivative is in bigfder. It returns true if the Newton converged. The method takes the given vector as initial guess, and rewrites it with a solution. The method guarantees to return the vector, which has smaller norm of the residual. That is why the input/output vector y is always changed.

The method proceeds with a Newton step, if the Newton step improves the residual error. So we track residual errors in *flastnorm* and *fnorm* (former and current). In addition, at each step we search for an underrelaxation parameter *urelax*, which improves the residual. If *urelax* is less that *urelax\_threshold*, we stop searching and stop the Newton.

```
\langle \mathbf{DRFixPoint} :: solveNewton \text{ code } 230 \rangle \equiv
  bool solveNewton(Vector &y)
     const double urelax\_threshold = 1. \cdot 10^{-5};
     Vector sol((const\ Vector\ \&)\ y);
     Vector delta(y.length());
     newton\_iter\_last = 0;
     bool delta\_finite = true;
     double flastnorm = 0.0;
     double fnorm = 0.0;
     bool converged = false;
     double urelax = 1.0;
       \_Ttensym *jacob = bigfder \neg evalPartially(1, sol);
       bigf \rightarrow evalHorner(delta, sol);
       if (newton\_iter\_last \equiv 0) flastnorm = delta.getNorm();
       delta\_finite = delta.isFinite();
       if (delta_finite) {
          ConstTwoDMatrix(*jacob).multInvLeft(delta);
          \langle \text{ find } urelax \text{ improving residual } 231 \rangle;
          sol.add(-urelax, delta);
          delta\_finite = delta.isFinite();
       delete jacob;
       newton\_iter\_last ++;
       converged = delta\_finite \land fnorm < tol;
       flastnorm = fnorm;
     \} while (\neg converged \land newton\_iter\_last < max\_newton\_iter \land urelax > urelax\_threshold);
     newton\_iter\_total += newton\_iter\_last;
     if (\neg converged) newton\_iter\_last = 0;
     y = (\mathbf{const\ Vector\ } \&)\ sol;
     return converged;
This code is cited in section 226.
This code is used in section 226.
```

**231.** Here we find the *urelax*. We cycle as long as the new residual size *fnorm* is greater than last residual size *flastnorm*. If the urelax is less than *urelax\_threshold* we give up. The *urelax* is damped by the ratio of *flastnorm* and *fnorm*. It the ratio is close to one, we damp by one half.

```
⟨ find urelax improving residual 231⟩ ≡
bool urelax_found = false;
urelax = 1.0;
while (¬urelax_found ∧ urelax > urelax_threshold) {
    Vector soltmp((const Vector &) sol);
    soltmp.add(¬urelax, delta);
    Vector f(sol.length());
    bigf¬evalHorner(f, soltmp);
    fnorm = f.getNorm();
    if (fnorm ≤ flastnorm) urelax_found = true;
    else urelax *= std::min(0.5, flastnorm/fnorm);
}
This code is used in section 230.
```

This code is used in section 226.

**232.** This method solves the fix point of the no-shocks rule  $y_{t+1} = f(y_t)$ . It combines dull steps with Newton attempts. The dull steps correspond to evaluations setting  $y_{t+1} = f(y_t)$ . For reasonable models the dull steps converge to the fix-point but very slowly. That is why we make Newton attempt from time to time. The frequency of the Newton attempts is given by *newton\_pause*. We perform the calculations in deviations from the steady state. So, at the end, we have to add the steady state.

The method also sets the members iter,  $newton\_iter\_last$  and  $newton\_iter\_total$ . These numbers can be examined later.

The *out* vector is not touched if the algorithm has not convered.

```
\langle \mathbf{DRFixPoint} :: calcFixPoint \text{ code } 232 \rangle \equiv
  bool calcFixPoint(emethod em, Vector &out)
    KORD\_RAISE\_IF(out.length() \neq ypart.ny(), "Wrong\_length\_of\_out\_in\_DRFixPoint::calcFixPoint");
    Vector delta(ypart.nys());
    Vector ystar(ypart.nys());
    ystar.zeros();
    iter = 0;
    newton\_iter\_last = 0;
    newton\_iter\_total = 0;
    bool converged = false;
    do {
       if ((iter/newton\_pause) * newton\_pause \equiv iter) converged = solveNewton(ystar);
       if (\neg converged) {
          biqf \rightarrow evalHorner(delta, ystar);
         KORD\_RAISE\_IF\_X(\neg delta.isFinite(), "NaN_{\square}or_{\square}Inf_{\square}asserted_{\square}in_{\square}DRFixPoint::calcFixPoint",
               KORD_FP_NOT_FINITE);
          ystar.add(1.0, delta);
          converged = delta.getNorm() < tol;
       iter ++;
     } while (iter < max\_iter \land \neg converged);
    if (converged) {
       _Tparent :: evalHorner(out, ystar);
       out.add(1.0, ysteady);
    return converged;
```

This is a basically a number of matrices of the same dimensions, which can be obtained as simulation results from a given decision rule and shock realizations. We also store the realizations of shocks.

```
\langle SimResults class declaration 233\rangle \equiv
  class ExplicitShockRealization;
  class SimResults {
  protected:
    int num_{-}y;
    int num_per;
    int num_burn;
    \mathbf{vector}\langle \mathbf{TwoDMatrix} * \rangle \ data;
    vector \( \) ExplicitShockRealization *\\ \) shocks;
  public:
    SimResults(int ny, int nper, int nburn = 0)
    : num_y(ny), num_per(nper), num_burn(nburn) \{ \}
    virtual ~SimResults();
    void simulate(int num_sim, const DecisionRule &dr, const Vector &start, const TwoDMatrix
         &vcov, Journal &journal);
    void simulate(int num\_sim, const DecisionRule \&dr, const Vector \&start, const TwoDMatrix
         \&vcov);
    int getNumPer() const
    { return num_per; }
    int getNumBurn() const
    { return num_burn; }
    int getNumSets() const
    { return (int) data.size(); }
    const TwoDMatrix & getData(int i) const
    { return *(data[i]); }
    const\ ExplicitShockRealization\ \&getShocks(int\ i)\ const
    { return *(shocks[i]); }
    bool addDataSet(TwoDMatrix *d, ExplicitShockRealization *sr);
    void writeMat(const char *base, const char *lname) const;
    void writeMat(mat_{-}t * fd, \mathbf{const} \ \mathbf{char} * lname) \ \mathbf{const};
  };
This code is used in section 208.
```

This code is used in section 208.

This does the same as **SimResults** plus it calculates means and covariances of the simulated data.  $\langle$  SimResultsStats class declaration 234 $\rangle$   $\equiv$ class SimResultsStats : public SimResults { protected: Vector mean; TwoDMatrix vcov; public: SimResultsStats(int ny, int nper, int nburn = 0):  $SimResults(ny, nper, nburn), mean(ny), vcov(ny, ny) \{ \}$ void  $simulate(int num\_sim, const DecisionRule \& dr, const Vector \& start, const TwoDMatrix$ &vcov, **Journal** &journal); **void**  $writeMat(mat_{-}t * fd, \mathbf{const} \ \mathbf{char} \ * lname) \ \mathbf{const};$ protected: void calcMean(); void calcVcov(); }; This code is used in section 208. 235. This does the similar thing as SimResultsStats but the statistics are not calculated over all periods but only within each period. Then we do not calculate covariances with periods but only variances.  $\langle SimResultsDynamicStats class declaration 235 \rangle \equiv$ class SimResultsDynamicStats : public SimResults { protected: TwoDMatrix mean; TwoDMatrix variance; public: SimResultsDynamicStats(int ny, int nper, int nburn = 0):  $SimResults(ny, nper, nburn), mean(ny, nper), variance(ny, nper) \{ \}$ void simulate (int num\_sim, const DecisionRule & dr, const Vector & start, const TwoDMatrix &vcov, **Journal** &journal); **void**  $writeMat(mat_{-}t * fd, \mathbf{const} \ \mathbf{char} * lname) \ \mathbf{const};$ protected: void calcMean(); void calcVariance();

236. This goes through control simulation results, and for each control it adds a given impulse to a given shock and runs a simulation. The control simulation is then cancelled and the result is stored. After that these results are averaged with variances calculated.

The means and the variances are then written to the MAT-4 file.

```
\langle SimResultsIRF class declaration 236 \rangle \equiv
  class SimulationIRFWorker;
  class SimResultsIRF : public SimResults {
    friend class SimulationIRFWorker;
  protected:
    const SimResults &control;
    int ishock;
    double imp;
    TwoDMatrix means;
    TwoDMatrix variances;
  public:
    SimResultsIRF(const SimResults & cntl, int ny, int nper, int i, double impulse)
    : SimResults(ny, nper, 0), control(cntl), ishock(i), imp(impulse), means(ny, nper),
         variances(ny, nper) \{ \}
    void simulate(const DecisionRule & dr, Journal & journal);
    void simulate(\mathbf{const}\ \mathbf{DecisionRule}\ \&dr);
    void writeMat(mat_t * fd, const char *lname) const;
  protected:
    void calcMeans();
    void calcVariances();
This code is used in section 208.
```

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This simulates and gathers all statistics from the real time simulations. In the *simulate* method, it runs RTSimulationWorkers which accumulate information from their own estimates. The estimation is done by means of **NormalConj** class, which is a conjugate family of densities for normal distibutions.

```
\langle RTSimResultsStats class declaration 237 \rangle \equiv
  class RTSimulationWorker;
  class RTSimResultsStats {
    friend class RTSimulationWorker;
  protected:
    Vector mean:
    TwoDMatrix vcov;
    int num_per;
    int num_burn;
    NormalConj nc;
    int incomplete_simulations;
    int thrown_periods;
  public:
    RTSimResultsStats(int ny, int nper, int nburn = 0)
    : mean(ny), vcov(ny, ny), num\_per(nper), num\_burn(nburn), nc(ny), incomplete\_simulations(0),
         thrown\_periods(0) \{ \}
    void simulate(int num_sim, const DecisionRule &dr, const Vector &start, const TwoDMatrix
        &vcov, Journal & journal);
    void simulate(int num_sim, const DecisionRule & dr, const Vector & start, const TwoDMatrix
    void writeMat(mat_t * fd, \mathbf{const} \ \mathbf{char} \ * lname);
  };
This code is used in section 208.
```

238. For each shock, this simulates plus and minus impulse. The class maintains a vector of simulation results, each gets a particular shock and sign (positive/negative). The results of type SimResultsIRF are stored in a vector so that even ones are positive, odd ones are negative.

The constructor takes a reference to the control simulations, which must be finished before the constructor is called. The control simulations are passed to all SimResultsIRFs.

The constructor also takes the vector of indices of exogenous variables (ili) for which the IRFs are generated. The list is kept (as *irf\_list\_ind*) for other methods.

```
\langle IRFResults class declaration 238 \rangle \equiv
  {\bf class\ Dynamic Model};
  class IRFResults {
     vector (SimResultsIRF *) irf_res;
     const DynamicModel & model;
     vector\langle int \rangle irf_list_ind;
     IRFResults(const DynamicModel & mod, const DecisionRule & dr, const SimResults
          & control, const vector \langle int \rangle & ili, Journal & journal);
     \simIRFResults();
     void writeMat(mat_t * fd, \mathbf{const} \ \mathbf{char} \ *prefix) \ \mathbf{const};
This code is used in section 208.
```

```
239.
       This worker simulates the given decision rule and inserts the result to SimResults.
\langle SimulationWorker class declaration 239\rangle \equiv
  class SimulationWorker: public THREAD
  protected:
    SimResults & res;
    const DecisionRule \&dr;
    DecisionRule::emethod em;
    int np;
    const Vector &st;
    ShockRealization \&sr;
  public:
    SimulationWorker(SimResults & sim_res, const DecisionRule & dec_rule,
              DecisionRule::emethod emet, int num_per, const Vector & start, ShockRealization
    : res(sim\_res), dr(dec\_rule), em(emet), np(num\_per), st(start), sr(shock\_r) {}
    void operator()();
This code is used in section 208.
240. This worker simulates a given impulse imp to a given shock ishock based on a given control simulation
with index idata. The control simulations are contained in SimResultsIRF which is passed to the
constructor.
\langle SimulationIRFWorker class declaration 240\rangle \equiv
  class SimulationIRFWorker: public THREAD
    SimResultsIRF &res;
    const DecisionRule \&dr;
    DecisionRule::emethod em;
    int np;
    int idata;
    int ishock;
    \mathbf{double}\ imp;
  public:
    SimulationIRFWorker(SimResultsIRF & sim_res, const DecisionRule & dec_rule,
              \textbf{DecisionRule} :: \textbf{emethod} \ \textit{emet}, \textbf{int} \ \textit{num\_per}, \textbf{int} \ \textit{id}, \textbf{int} \ \textit{ishck}, \textbf{double} \ \textit{impulse})
    : res(sim\_res), dr(dec\_rule), em(emet), np(num\_per), idata(id), ishock(ishck), imp(impulse) {}
    void operator()();
  }
This code is used in section 208.
```

**241.** This class does the real time simulation job for **RTSimResultsStats**. It simulates the model period by period. It accumulates the information in the **RTSimResultsStats**:: nc. If NaN or Inf is observed, it ends the simulation and adds to the thrown\_periods of **RTSimResultsStats**.

```
\langle RTSimulationWorker class declaration 241 \rangle \equiv
  class RTSimulationWorker: public THREAD
  {
  protected:
    RTSimResultsStats & res;
    const DecisionRule \&dr;
    DecisionRule::emethod em;
    int np:
    const Vector & ystart;
    ShockRealization \&sr;
  public:
    RTSimulationWorker(RTSimResultsStats & sim_res, const DecisionRule & dec_rule,
             DecisionRule::emethod emet, int num_per, const Vector & start, ShockRealization
    : res(sim\_res), dr(dec\_rule), em(emet), np(num\_per), ystart(start), sr(shock\_r) {}
    void operator()();
This code is used in section 208.
242. This class generates draws from Gaussian distribution with zero mean and the given variance-
covariance matrix. It stores the factor of vcov V matrix, yielding FF^T = V.
\langle RandomShockRealization class declaration 242 \rangle \equiv
  class RandomShockRealization : virtual public ShockRealization {
  protected:
    MersenneTwister mtwister;
    TwoDMatrix factor;
  public:
    RandomShockRealization(const TwoDMatrix &v, unsigned int iseed)
    : mtwister(iseed), factor(v.nrows(), v.nrows()) { schurFactor(v); }
    RandomShockRealization(const RandomShockRealization \&sr)
    : mtwister(sr.mtwister), factor(sr.factor) \{ \}
    virtual ~RandomShockRealization() {}
    void get(int \ n, Vector \& out);
    int numShocks() const
    { return factor.nrows(); }
  protected:
    void choleskyFactor(const TwoDMatrix &v);
    void schurFactor(\mathbf{const}\ \mathbf{TwoDMatrix}\ \&v);
  };
This code is used in section 208.
```

**243.** This is just a matrix of finite numbers. It can be constructed from any **ShockRealization** with a given number of periods.

```
\langle ExplicitShockRealization class declaration 243 \rangle \equiv
  class ExplicitShockRealization: virtual public ShockRealization {
    TwoDMatrix shocks;
  public:
    ExplicitShockRealization(const TwoDMatrix &sh)
    ExplicitShockRealization(const ConstTwoDMatrix &sh)
    : shocks(sh) \{ \}
    ExplicitShockRealization (const ExplicitShockRealization \&sr)
    : shocks(sr.shocks) \{ \}
    ExplicitShockRealization(ShockRealization &sr, int num_per);
    void get(int \ n, Vector \& out);
    int numShocks() const
    { return shocks.nrows(); }
    const TwoDMatrix &getShocks()
    { return shocks; }
    void addToShock(int ishock, int iper, double val);
    void print() const
    \{ shocks.print(); \}
  };
This code is used in section 208.
```

244. This represents a user given shock realization. The first matrix of the constructor is a covariance matrix of shocks, the second matrix is a rectangular matrix, where columns correspond to periods, rows to shocks. If an element of the matrix is NaN, or Inf, or -Inf, then the random shock is taken instead of that element.

In this way it is a generalization of both RandomShockRealization and ExplicitShockRealization.

245. End of decision\_rule.h file.

```
246.
      Start of decision_rule.cpp file.
#include "kord_exception.h"
#include "decision_rule.h"
#include "dynamic_model.h"
#include "SymSchurDecomp.h"
#include <dynlapack.h>
#include <limits>
  template\langle \rangle int DRFixPoint\langle KOrder:: fold \rangle :: max\_iter = 10000;
  template\langle \rangle int DRFixPoint\langle KOrder::unfold \rangle :: max\_iter = 10000;
  template\langle \rangle double DRFixPoint\langle KOrder:: fold \rangle :: tol = 1. \cdot 10^{-10};
  \mathbf{template}\langle\,\rangle\,\,\mathbf{double}\,\,\mathbf{DRFixPoint}\,\langle\mathbf{KOrder}::\mathit{unfold}\,\rangle::\mathit{tol}\,=1.\cdot\,10^{-10};
  template() int DRFixPoint(KOrder::fold)::max\_newton\_iter = 50;
  template\langle \rangle int DRFixPoint\langle KOrder::unfold \rangle :: max\_newton\_iter = 50;
  template\langle \rangle int DRFixPoint\langle KOrder:: fold \rangle :: newton\_pause = 100;
  template\langle \rangle int DRFixPoint\langle KOrder :: unfold \rangle :: newton\_pause = 100;
  ⟨ FoldDecisionRule conversion from UnfoldDecisionRule 247⟩;
   UnfoldDecisionRule conversion from FoldDecisionRule 248);
   SimResults destructor 249);
   SimResults:: simulate code1 250 \;
   SimResults:: simulate \text{ code } 251;
   SimResults :: addDataSet code 252;
   SimResults:: writeMat code1 253 \;
   SimResults:: writeMat \text{ code } 254 >:
   SimResultsStats:: simulate code 255 >:
   SimResultsStats:: writeMat code 256);
   SimResultsStats:: calcMean code 257 >;
   SimResultsStats:: calc Vcov code 258 \:
   SimResultsDynamicStats::simulate code 259);
   SimResultsDynamicStats:: writeMat code 260 \;
   SimResultsDynamicStats:: calcMean code 261 >;
   SimResultsDynamicStats:: calc Variance code 262 \;
   SimResultsIRF:: simulate code1 263 >;
   SimResultsIRF:: simulate code2 264 >;
   SimResultsIRF :: calcMeans code 265 >;
   SimResultsIRF :: calc Variances code 266 >;
   SimResultsIRF:: writeMat code 267);
   RTSimResultsStats:: simulate code1 268 \;
   RTSimResultsStats:: simulate code2 269 \;
   RTSimResultsStats::writeMat code 270);
   IRFResults constructor 271);
   IRFResults destructor 272);
   IRFResults:: writeMat code 273 \;
   SimulationWorker::operator()() code 274);
   SimulationIRFWorker::operator()() code 275);
   RTSimulationWorker::operator()() code 276);
   RandomShockRealization::choleskyFactor code 280):
   RandomShockRealization::schurFactor code 281);
   RandomShockRealization:: get \text{ code } 282;
   ExplicitShockRealization constructor code 283);
   ExplicitShockRealization:: qet code 284 \;
   ExplicitShockRealization:: addToShock code 285);
   GenShockRealization:: get code 286);
```

```
§247
                   Dynare++
                                                                                                                                                              DECISION RULE AND SIMULATION
247.
⟨ FoldDecisionRule conversion from UnfoldDecisionRule 247⟩ ≡
     FoldDecisionRule :: FoldDecisionRule (const UnfoldDecisionRule \&udr)
     : DecisionRuleImpl\langle KOrder :: fold \rangle (ctraits \langle KOrder :: fold \rangle :: Tpol(udr.nrows(), udr.nvars()),
                      udr.ypart, udr.nu, udr.ysteady) {
           \textbf{for (ctraits} \langle \textbf{KOrder} :: unfold \rangle :: \textbf{Tpol} :: const\_iterator it = udr.begin(); \ it \neq udr.end(); \ ++it) \ \{ const\_iterator it = udr.begin(); \ it \neq udr.end(); \ ++it \} \}
                insert(\mathbf{new\ ctraits}\langle\mathbf{KOrder}::fold\rangle::\mathbf{Ttensym}(*((*it).second)));
This code is used in section 246.
248.
⟨UnfoldDecisionRule conversion from FoldDecisionRule 248⟩ ≡
     UnfoldDecisionRule :: UnfoldDecisionRule (const FoldDecisionRule \&fdr)
     : \mathbf{DecisionRuleImpl}\langle \mathbf{KOrder} :: unfold \rangle (\mathbf{ctraits}\langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{Tpol}(fdr.nrows(), fdr.nvars()),
                     fdr.ypart, fdr.nu, fdr.ysteady) {
           for (ctraits \langle KOrder::fold \rangle :: Tpol::const\_iteratorit = fdr.begin(); it \neq fdr.end(); ++it) {
                insert(\mathbf{new\ ctraits} \langle \mathbf{KOrder} :: unfold \rangle :: \mathbf{Ttensym}(*((*it).second)));
This code is used in section 246.
249.
\langle SimResults destructor 249\rangle \equiv
     SimResults:: \sim SimResults()
           for (int i = 0; i < getNumSets(); i \leftrightarrow ) {
                delete data[i];
                delete shocks[i];
This code is used in section 246.
250. This runs simulations with an output to journal file. Note that we report how many simulations had
to be thrown out due to Nan or Inf.
\langle \mathbf{SimResults} :: simulate \ \text{code1} \ 250 \rangle \equiv
     void SimResults::simulate(int num_sim, const DecisionRule & dr, const Vector & start, const
                           TwoDMatrix &vcov, Journal &journal)
           JournalRecordPair paa(journal);
           paa \ll "Performing_{\sqcup}" \ll num\_sim \ll "_{\sqcup} stochastic_{\sqcup} simulations_{\sqcup} for_{\sqcup}" \ll num\_per \ll num\_per \ll num\_sim = n
                      "uperiods burning " \ll num_burn \ll "uinitial periods" \ll endrec;
           simulate(num\_sim, dr, start, vcov);
           int thrown = num\_sim - data.size();
```

 $rec \ll "I_{\square}had_{\square}to_{\square}throw_{\square}" \ll throw_{n} \ll "_{\square}simulations_{\square}away_{\square}due_{\square}to_{\square}Nan_{\square}or_{\square}Inf" \ll endrec;$ 

This code is used in section 246.

if (thrown > 0) {

**JournalRecord** rec(journal);

This code is used in section 246.

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251. This runs a given number of simulations by creating SimulationWorker for each simulation and inserting them to the thread group.

```
\langle \mathbf{SimResults} :: simulate \ \mathrm{code2} \ 251 \rangle \equiv
  void SimResults::simulate(int num_sim, const DecisionRule & dr, const Vector & start, const
           TwoDMatrix &vcov)
    std::vector\langle RandomShockRealization\rangle \ rsrs;
    rsrs.reserve(num\_sim);
    THREAD_GROUP gr;
    for (int i = 0; i < num\_sim; i ++) {
       RandomShockRealization sr(vcov, system\_random\_qenerator.int\_uniform());
       rsrs.push\_back(sr);
       THREAD * worker = new SimulationWorker(*this, dr, DecisionRule::horner,
           num\_per + num\_burn, start, rsrs.back());
       gr.insert(worker);
    gr.run();
This code is used in section 246.
252. This adds the data with the realized shocks. It takes only periods which are not to be burnt. If the
data is not finite, the both data and shocks are thrown away.
\langle \mathbf{SimResults} :: addDataSet \ \mathrm{code} \ 252 \rangle \equiv
  \textbf{bool SimResults} :: addDataSet(\textbf{TwoDMatrix} *d, \textbf{ExplicitShockRealization} *sr)
    KORD_RAISE_IF(d\rightarrow nrows() \neq num_y,
         "Incompatible_number_of_rows_for_SimResults::addDataSets");
    KORD_RAISE_IF(d\rightarrow ncols() \neq num\_per + num\_burn,
         "Incompatible_number_of_cols_for_SimResults::addDataSets");
    bool ret = false;
    if (d→isFinite()) {
       data.push_back(new TwoDMatrix((const TwoDMatrix &)(*d), num_burn, num_per));
       shocks.push\_back (new ExplicitShockRealization (ConstTwoDMatrix (sr \neg qetShocks()),
           num\_burn, num\_per)));
       ret = true;
    delete d;
    delete sr;
    return ret;
```

```
253.
\langle \mathbf{SimResults} :: writeMat \text{ code1 } 253 \rangle \equiv
  void SimResults::writeMat(const char *base, const char *lname) const
     char matfile\_name[100];
     sprintf(matfile_name, "%s.mat", base);
     mat_{-}t * matfd = Mat_{-}Create(matfile_name, \Lambda);
     if (matfd \neq \Lambda) {
       writeMat(matfd, lname);
       Mat\_Close(matfd);
  }
This code is used in section 246.
254. This save the results as matrices with given prefix and with index appended. If there is only one
matrix, the index is not appended.
\langle \mathbf{SimResults} :: writeMat \text{ code } 254 \rangle \equiv
  void SimResults::writeMat(mat_{-}t * fd, const char * lname) const
     char tmp[100];
     for (int i = 0; i < getNumSets(); i \leftrightarrow ) {
       if (getNumSets() > 1) sprintf(tmp, "%s_data%d", lname, i + 1);
       \mathbf{else} \ \mathit{sprintf}(\mathit{tmp}, \texttt{"\%s\_data"}, \mathit{lname});
       ConstTwoDMatrix m(*(data[i]));
       m.writeMat(fd, tmp);
  }
This code is used in section 246.
255.
\langle SimResultsStats :: simulate code 255 \rangle \equiv
  void SimResultsStats::simulate(int num_sim, const DecisionRule & dr, const Vector
            &start, const TwoDMatrix &vcov, Journal &journal)
     SimResults :: simulate(num\_sim, dr, start, vcov, journal);
       JournalRecordPair paa(journal);
       paa \ll "Calculating means from the simulations." \ll endrec;
       calcMean();
       JournalRecordPair paa(journal);
       paa \ll "Calculating covariances from the simulations." \ll endrec;
       calc Vcov();
```

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**256.** Here we do not save the data itself, we save only mean and vcov.  $\langle SimResultsStats :: writeMat code 256 \rangle \equiv$ void  $SimResultsStats::writeMat(mat_t * fd, const char * lname)$  const char tmp[100];  $sprintf(tmp, "%s_mean", lname);$ ConstTwoDMatrix  $m(num_-y, 1, mean.base())$ ; m.writeMat(fd, tmp);sprintf(tmp, "%s\_vcov", lname);  ${\bf ConstTwoDMatrix}(\textit{vcov}).\textit{writeMat}(\textit{fd},\textit{tmp});$ This code is used in section 246. 257.  $\langle SimResultsStats :: calcMean code 257 \rangle \equiv$ void SimResultsStats::calcMean() mean.zeros(); if  $(data.size()*num\_per > 0)$  { **double**  $mult = 1.0/data.size()/num\_per;$ for (unsigned int i = 0; i < data.size(); i++) { for (int j = 0;  $j < num\_per$ ; j ++) { ConstVector col(\*data[i], j); mean.add(mult, col);

```
258.
\langle \mathbf{SimResultsStats} :: calc V cov \ \text{code} \ 258 \rangle \equiv
  void SimResultsStats::calcVcov()
    if (data.size()*num\_per > 1) {
      vcov.zeros();
      double mult = 1.0/(data.size() * num\_per - 1);
      for (unsigned int i = 0; i < data.size(); i++) {
         const TwoDMatrix &d = *(data[i]);
         for (int j = 0; j < num\_per; j ++) {
           for (int m = 0; m < num_y; m++) {
             for (int n = m; n < num_y; n \leftrightarrow) {
                double s = (d.get(m, j) - mean[m]) * (d.get(n, j) - mean[n]);
                vcov.get(m, n) += mult * s;
                if (m \neq n) vcov.get(n,m) += mult * s;
           }
    else {
      vcov.infs();
This code is used in section 246.
259.
\langle SimResultsDynamicStats::simulate code 259 \rangle \equiv
  void SimResultsDynamicStats::simulate(int num\_sim, const DecisionRule \& dr, const Vector
           &start, const TwoDMatrix &vcov, Journal &journal)
  {
    SimResults :: simulate(num\_sim, dr, start, vcov, journal);
      JournalRecordPair paa(journal);
      paa \ll "Calculating \_means \_of \_the \_conditional \_simulations." \ll endrec;
      calcMean();
      JournalRecordPair paa(journal);
      paa \ll "Calculating variances of the conditional simulations." \ll endrec;
      calc Variance();
  }
```

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```
\langle SimResultsDynamicStats :: writeMat code 260 \rangle \equiv
  void SimResultsDynamicStats::writeMat(mat\_t * fd, const char * lname) const
    char tmp[100];
     sprintf(tmp, "%s\_cond\_mean", lname);
    ConstTwoDMatrix(mean).writeMat(fd, tmp);
     sprintf(tmp, "%s_cond_variance", lname);
     ConstTwoDMatrix(variance).writeMat(fd, tmp);
This code is used in section 246.
261.
\langle SimResultsDynamicStats :: calcMean code 261 \rangle \equiv
  void SimResultsDynamicStats::calcMean()
    mean.zeros();
    if (data.size() > 0) {
       double mult = 1.0/data.size();
       {\bf for} \ ({\bf int} \ j=0; \ j < num\_per; \ j+\!\!\!+) \ \{
         Vector meanj(mean, j);
         for (unsigned int i = 0; i < data.size(); i \leftrightarrow) {
            ConstVector col(*data[i], j);
            mean j. add \, (mult, \, col);
       }
This code is used in section 246.
```

```
262.
\langle SimResultsDynamicStats:: calc Variance code 262 \rangle \equiv
       void SimResultsDynamicStats::calcVariance()
               if (data.size() > 1) {
                       variance.zeros();
                       double mult = 1.0/(data.size() - 1);
                       for (int j = 0; j < num\_per; j ++) {
                              ConstVector meanj(mean, j);
                               Vector varj(variance, j);
                              for (int i = 0; i < (int) data.size(); i \leftrightarrow ) {
                                      Vector col(ConstVector((*data[i]), j));
                                      col.add(-1.0, meanj);
                                      for (int k = 0; k < col.length(); k++) col[k] = col[k] * col[k];
                                      varj.add(mult, col);
                       }
               else {
                      variance.infs();
This code is used in section 246.
263.
\langle \mathbf{SimResultsIRF} :: simulate \text{ code1 } 263 \rangle \equiv
       void SimResultsIRF::simulate(const DecisionRule \&dr, Journal \&journal)
               JournalRecordPair paa(journal);
               paa \ll "Performing_{\sqcup}" \ll control.getNumSets() \ll "_{\sqcup}IRF_{\sqcup}simulations_{\sqcup}for_{\sqcup}" \ll num\_per 
                               "uperiods; ushock=" \ll ishock \ll ", uimpulse=" \ll imp \ll endrec;
               simulate(dr);
               int thrown = control.getNumSets() - data.size();
               if (thrown > 0) {
                       JournalRecord rec(journal);
                       rec \ll "I_{\square}had_{\square}to_{\square}throw_{\square}" \ll throw_{n} \ll "_{\square}simulations_{\square}away_{\square}due_{\square}to_{\square}Nan_{\square}or_{\square}Inf" \ll endrec;
               calcMeans();
               calc Variances();
This code is used in section 246.
```

**264.** 

#### DECISION RULE AND SIMULATION

```
\langle \mathbf{SimResultsIRF} :: simulate \ \mathrm{code2} \ 264 \rangle \equiv
  void SimResultsIRF::simulate(const DecisionRule & dr)
     THREAD_GROUP qr;
     for (int idata = 0; idata < control.getNumSets(); idata++) {
       THREAD * worker = new SimulationIRFWorker (*this, dr, DecisionRule :: horner, num_per,
            idata, ishock, imp);
       gr.insert(worker);
    gr.run();
This code is used in section 246.
265.
\langle \mathbf{SimResultsIRF} :: calcMeans \ \mathbf{code} \ 265 \rangle \equiv
  void SimResultsIRF :: calcMeans()
     means.zeros();
    if (data.size() > 0) {
       \textbf{for (unsigned int } i = 0; \ i < data.size(); \ i++) \ means.add(1.0,*(data[i]));
       means.mult(1.0/data.size());
This code is used in section 246.
266.
\langle SimResultsIRF :: calc Variances code 266 \rangle \equiv
  void SimResultsIRF :: calc Variances()
    if (data.size() > 1) {
       variances.zeros();
       for (unsigned int i = 0; i < data.size(); i \leftrightarrow) {
         TwoDMatrix d((const\ TwoDMatrix\ \&)(*(data[i])));
         d.add(-1.0, means);
         for (int j = 0; j < d.nrows(); j ++ )
            for (int k = 0; k < d.ncols(); k +++) variances.get(j, k) += d.get(j, k) * d.get(j, k);
         d.mult(1.0/(data.size()-1));
    else {
       variances.infs();
This code is used in section 246.
```

```
§267
                                  Dynare++
                                                                                                                                                                                                                                                                                       DECISION RULE AND SIMULATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                        123
267.
\langle \mathbf{SimResultsIRF} :: writeMat \text{ code } 267 \rangle \equiv
         void SimResultsIRF :: writeMat(mat_t * fd, const char * lname) const
                   char tmp[100];
                   sprintf(tmp, "%s_mean", lname);
                   means.writeMat(fd, tmp);
                   sprintf(tmp, "%s_var", lname);
                   variances.writeMat(fd, tmp);
This code is used in section 246.
268.
\langle RTSimResultsStats :: simulate code1 268 \rangle \equiv
         void RTSimResultsStats::simulate(int num_sim,const DecisionRule & dr,const Vector
                                                &start, const TwoDMatrix &v, Journal &journal)
                   JournalRecordPair paa(journal);
                   paa \ll "Performing \sqcup" \ll num\_sim \ll " \sqcup real-time \sqcup stochastic \sqcup simulations \sqcup for \sqcup" \ll num\_per \ll num\_per \ll num\_per \ll num\_simulations \sqcup for \sqcup for
                                       "\_periods" \ll endrec;
                   simulate(num\_sim, dr, start, v);
                   mean = nc.getMean();
                   mean.add(1.0, dr.getSteady());
                   nc.getVariance(vcov);
                   if (thrown\_periods > 0) {
                             JournalRecord rec(journal);
                             \mathit{rec} \ll \texttt{"I\_had\_to\_throw\_"} \ll \mathit{thrown\_periods} \ll \texttt{"\_periods\_away\_due\_to\_Nan\_or\_Inf"} \ll \mathit{endrec};
                             JournalRecord rec1 (journal);
                             rec1 \ll "This_{||} affected_{||}" \ll incomplete\_simulations \ll "_{||} out_{||} of_{||}" \ll num\_sim \ll "
                                                 "usimulations" \ll endrec;
```

This code is used in section 246.

}

### DECISION RULE AND SIMULATION

```
269.
\langle \mathbf{RTSimResultsStats} :: simulate \ \text{code2} \ 269 \rangle \equiv
  void RTSimResultsStats::simulate(int num_sim,const DecisionRule & dr,const Vector
           &start, const TwoDMatrix &vcov)
    std::vector\langle RandomShockRealization\rangle \ rsrs;
    rsrs.reserve(num\_sim);
    THREAD_GROUP gr;
    for (int i = 0; i < num\_sim; i ++) {
      RandomShockRealization \ sr(vcov, system\_random\_generator.int\_uniform());
      rsrs.push\_back(sr);
      THREAD * worker = new RTSimulationWorker(*this, dr, DecisionRule::horner, num_per, start,
           rsrs.back());
      gr.insert(worker);
    gr.run();
  }
This code is used in section 246.
270.
\langle RTSimResultsStats::writeMat code 270 \rangle \equiv
  void RTSimResultsStats::writeMat(mat_{-}t * fd, const char * lname)
    char tmp[100];
    sprintf(tmp, "%s_rt_mean", lname);
    ConstTwoDMatrix m(nc.getDim(), 1, mean.base());
    m.writeMat(fd, tmp);
    sprintf(tmp, "%s_rt_vcov", lname);
    ConstTwoDMatrix(vcov).writeMat(fd, tmp);
  }
This code is used in section 246.
```

```
271.
\langle IRFResults constructor 271 \rangle \equiv
  IRFResults::IRFResults(const DynamicModel \& mod, const DecisionRule \& dr, const
            SimResults & control, const vector (int) & ili, Journal & journal)
  : model(mod), irf_list_ind(ili) {
     int num\_per = control.getNumPer();
     JournalRecordPair pa(journal);
     pa \ll \text{"Calculating} \sqcup \text{IRFs} \sqcup \text{against} \sqcup \text{control} \sqcup \text{for} \sqcup \text{"} \ll (\text{int})
          irf\_list\_ind.size() \ll " \sqcup shocks \sqcup and \sqcup for \sqcup " \ll num\_per \ll " \sqcup periods" \ll endrec;
     const TwoDMatrix &vcov = mod.getVcov();
     for (unsigned int ii = 0; ii < irf_list_ind.size(); ii \leftrightarrow ) {
       int ishock = irf\_list\_ind[ii];
       double stderror = sqrt(vcov.get(ishock, ishock));
       irf_res.push_back(new SimResultsIRF(control, model.numeq(), num_per, ishock, stderror));
       irf_res.push_back(new SimResultsIRF(control, model.numeq(), num_per, ishock, -stderror));
     for (unsigned int ii = 0; ii < irf_list_ind.size(); ii \leftrightarrow ) {
       irf_res[2*ii] \rightarrow simulate(dr, journal);
       irf_res[2*ii+1] \rightarrow simulate(dr, journal);
This code is used in section 246.
272.
\langle IRFResults destructor 272 \rangle \equiv
  IRFResults::~IRFResults()
     for (unsigned int i = 0; i < irf_res.size(); i++) delete irf_res[i];
This code is used in section 246.
273.
\langle IRFResults :: writeMat \text{ code } 273 \rangle \equiv
  void IRFResults::writeMat(mat_t * fd, const char * prefix) const
     for (unsigned int i = 0; i < irf_list_ind.size(); i++) {
       char tmp[100];
       int ishock = irf_list_ind[i];
       const\ char *shockname = model.getExogNames().getName(ishock);
       sprintf(tmp, "%s_irfp_%s", prefix, shockname);
       irf\_res[2*i] \rightarrow writeMat(fd, tmp);
       sprintf(tmp, "%s_irfm_%s", prefix, shockname);
       irf\_res[2*i+1] \neg writeMat(fd, tmp);
  }
```

```
274.
\langle SimulationWorker::operator()() code 274 \rangle \equiv
  void SimulationWorker::operator()()
    ExplicitShockRealization *esr = new ExplicitShockRealization(sr, np);
    TwoDMatrix *m = dr.simulate(em, np, st, *esr);
      SYNCHROsyn(\&res, "simulation");
      res.addDataSet(m, esr);
This code is used in section 246.
275. Here we create a new instance of ExplicitShockRealization of the corresponding control, add the
impulse, and simulate.
\langle SimulationIRFWorker::operator()() code 275 \rangle \equiv
  void SimulationIRFWorker::operator()()
    ExplicitShockRealization *esr = new ExplicitShockRealization(res.control.getShocks(idata));
    esr \neg add To Shock (ishock, 0, imp);
    const TwoDMatrix & data = res.control.getData(idata);
    ConstVector st(data, res.control.getNumBurn());
    TwoDMatrix *m = dr.simulate(em, np, st, *esr);
    m \rightarrow add(-1.0, res.control.getData(idata));
      SYNCHROsyn(\&res, "simulation");
      res.addDataSet(m, esr);
```

```
276.
\langle \mathbf{RTSimulationWorker} :: \mathbf{operator}()() \text{ code } 276 \rangle \equiv
  void RTSimulationWorker::operator()()
     NormalConj nc(res.nc.getDim());
     const PartitionY &ypart = dr.getYPart();
     int nu = dr.nexog();
     const Vector \&ysteady = dr.getSteady();
     (initialize vectors and subvectors for simulation 216);
     (simulate the first real-time period 278);
     \langle \text{ simulate other real-time periods } 279 \rangle;
       SYNCHRO syn(&res, "rtsimulation");
       res.nc.update(nc);
       if (res.num\_per - ip > 0) {
          res.incomplete\_simulations ++;
          res.thrown\_periods += res.num\_per - ip;
  }
This code is used in section 246.
277.
\langle \text{ initialize vectors and subvectors for simulation } 216 \rangle + \equiv
  Vector dyu(ypart.nys() + nu);
  ConstVector ystart_pred(ystart, ypart.nstat, ypart.nys());
  ConstVector ysteady_pred(ysteady,ypart.nstat,ypart.nys());
  Vector dy(dyu, 0, ypart.nys());
  Vector u(dyu, ypart.nys(), nu);
  Vector y(nc.qetDim());
  {\bf ConstVector}\ \ ypred(y,ypart.nstat,ypart.nys(\ ));
278.
\langle\,{\rm simulate} the first real-time period \,{}^{278}\,\rangle \equiv
  int ip = 0;
  dy = ystart\_pred;
  dy.add(-1.0, ysteady\_pred);
  sr.get(ip, u);
  dr.eval(em, y, dyu);
```

**if**  $(ip \ge res.num\_burn)$  nc.update(y);

279.

```
O DECIDION ROLL AND DIMICEATION
```

```
\langle \text{ simulate other real-time periods } 279 \rangle \equiv
  while (y.isFinite() \land ip < res.num\_burn + res.num\_per) {
    ip ++;
    dy = ypred;
    sr.get(ip, u);
    dr.eval(em, y, dyu);
    if (ip \geq res.num\_burn) nc.update(y);
This code is used in section 276.
280. This calculates factorization FF^T = V in the Cholesky way. It does not work for semidefinite
matrices.
\langle RandomShockRealization :: choleskyFactor code 280 \rangle \equiv
  void RandomShockRealization::choleskyFactor(const TwoDMatrix &v)
    factor = v;
    lapack\_introws = factor.nrows();
    for (int i = 0; i < rows; i \leftrightarrow)
       {\bf for} \ ({\bf int} \ j = i+1; \ j < rows; \ j+\!\!\!\!+) \ factor.get(i,j) = 0.0;
    lapack_intinfo;
    dpotrf("L", &rows, factor.base(), &rows, &info);
    KORD_RAISE_IF(info \neq 0, "Info!=0\_in\_RandomShockRealization::choleskyFactor");
This code is used in section 246.
281. This calculates FF^T = V factorization by symmetric Schur decomposition. It works for semidifinite
matrices.
\langle RandomShockRealization :: schurFactor code 281 \rangle \equiv
  void RandomShockRealization::schurFactor(const TwoDMatrix &v)
    SymSchurDecompssd(v);
    ssd.qetFactor(factor);
This code is used in section 246.
282.
\langle RandomShockRealization :: get code 282 \rangle \equiv
  void RandomShockRealization:: qet(int n, Vector \& out)
    KORD_RAISE_IF(out.length() \neq numShocks(),
         "Wrong_length_of_out_vector_in_RandomShockRealization::get");
    Vector d(out.length());
    for (int i = 0; i < d.length(); i ++) {
       d[i] = mtwister.normal();
    out.zeros();
    factor.multa Vec(out, ConstVector(d));
This code is used in section 246.
```

```
283.
\langle ExplicitShockRealization constructor code 283 \rangle \equiv
  \textbf{ExplicitShockRealization} : \textbf{ExplicitShockRealization} (\textbf{ShockRealization} \& sr, \textbf{int} \ num\_per)
  : shocks(sr.numShocks(), num\_per)  {
     for (int j = 0; j < num\_per; j +++) {
       Vector jcol(shocks, j);
       sr.get(j, jcol);
This code is used in section 246.
284.
\langle ExplicitShockRealization :: get code 284 \rangle \equiv
  void ExplicitShockRealization:: get(int \ n, Vector \ \& out)
     KORD_RAISE_IF(out.length() \neq numShocks(),
          \verb|"Wrong| length| of | out| vector| in| Explicit Shock Realization::get");
     int i = n \% shocks.ncols();
     ConstVector icol(shocks, i);
     out = icol;
This code is used in section 246.
285.
\langle \text{ExplicitShockRealization} :: addToShock \text{ code } 285 \rangle \equiv
  void ExplicitShockRealization:: addToShock(int ishock, int iper, double val)
     KORD_RAISE_IF(ishock < 0 \lor ishock > numShocks(),
          "Wrong_index_of_shock_in_ExplicitShockRealization::addToShock");
     int j = iper \% shocks.ncols();
     shocks.get(ishock, j) += val;
  }
This code is used in section 246.
\langle \text{ GenShockRealization} :: get \text{ code } 286 \rangle \equiv
  void GenShockRealization:: get(int \ n, Vector \ \& out)
     KORD_RAISE_IF(out.length() \neq numShocks(),
          \verb|"Wrong| length| of || out| || vector| || in| || GenShockRealization::get");
     ExplicitShockRealization :: get(n, out);
     Vector r(numShocks());
     RandomShockRealization :: get(n, r);
     for (int j = 0; j < numShocks(); j +++)
       if (\neg isfinite(out[j])) out[j] = r[j];
```

287. End of decision\_rule.cpp file.

130 GLOBAL CHECK Dynare++ §288

# 288. Global check. Start of global\_check.h file.

The purpose of this file is to provide classes for checking error of approximation. If  $y_t = g(y_{t-1}^*, u)$  is an approximate solution, then we check for the error of residuals of the system equations. Let  $F(y^*, u, u') = f(g^{**}(g^*(y^*, u'), u), g(y^*, u), y^*, u)$ , then we calculate integral

$$E[F(y^*, u, u')]$$

which we want to be zero for all  $y^*$ , and u.

There are a few possibilities how and where the integral is evaluated. Currently we offer the following:

- 1) Along shocks. The  $y^*$  is set to steady state, and u is set to zero but one element is going from minus through plus shocks in few steps. The user gives the scaling factor, for instance interval  $\langle < -3\sigma, 3\sigma \rangle$  (where sigma is a standard error of the shock), and a number of steps. This is repeated for each shock (element of the u vector).
- 2) Along simulation. Some random simulation is run, and for each realization of  $y^*$  and u along the path we evaluate the residual.
- 3) On ellipse. Let  $V = AA^T$  be a covariance matrix of the predetermined variables  $y^*$  based on linear approximation, then we calculate integral for points on the ellipse  $\{Ax | ||x||_2 = 1\}$ . The points are selected by means of low discrepancy method and polar transformation. The shock u are zeros.
- 4) Unconditional distribution.

**289.** This is a class for implementing **VectorFunction** interface evaluating the residual of equations, this is

$$F(y^*, u, u') = f(g^{**}(g^*(y^*, u), u'), y^*, u)$$

is written as a function of u'.

When the object is constructed, one has to specify  $(y^*, u)$ , this is done by set YU method. The object has basically two states. One is after construction and before call to set YU. The second is after call set YU. We distinguish between the two states, an object in the second state contains yplus, ystar, u, and hss.

The vector yplus is  $g^*(y^*, u)$ . ystar is  $y^*$ , and polynomial hss is partially evaluated  $g^* * (yplus, u)$ .

The pointer to **DynamicModel** is important, since the **DynamicModel** evaluates the function f. When copying the object, we have to make also a copy of **DynamicModel**.

```
\langle \mathbf{ResidFunction} \ \mathbf{class} \ \mathbf{declaration} \ \mathbf{289} \rangle \equiv
  class ResidFunction : public VectorFunction {
  protected:
    const Approximation & approx;
    DynamicModel *model:
    Vector *yplus;
    Vector *ystar;
    Vector *u;
    FTensorPolynomial *hss;
  public:
    ResidFunction(const Approximation \&app);
    ResidFunction(const ResidFunction \&rf);
    virtual \simResidFunction();
    virtual VectorFunction *clone() const
    { return new ResidFunction(*this); }
    virtual void eval(const Vector &point, const ParameterSignal &sig, Vector &out);
    void set YU(const Vector &ys, const Vector &xx);
  };
This code is used in section 288.
     This is a ResidFunction wrapped with GaussConverterFunction.
\langle GResidFunction class declaration 290\rangle \equiv
  {\bf class} \ {\bf GResidFunction} : {\bf public} \ {\it GaussConverterFunction}
  public:
    GResidFunction(const Approximation & app)
    : GaussConverterFunction(new ResidFunction(app), app.getModel().getVcov()) {}
    GResidFunction(const\ GResidFunction\ \&rf)
    : GaussConverterFunction(rf) {}
    \mathbf{virtual} \sim \mathbf{GResidFunction}() \{ \}
    virtual VectorFunction *clone() const
    { return new GResidFunction(*this); }
    void set YU(const Vector &ys, const Vector &xx)
      ((\mathbf{ResidFunction} *) func) \rightarrow set YU(ys, xx);
  }
This code is used in section 288.
```

132 GLOBAL CHECK Dynare++ §291

**291.** This is a class encapsulating checking algorithms. Its core routine is check, which calculates integral  $E[F(y^*, u, u')|y^*, u]$  for given realizations of  $y^*$  and u. The both are given in matrices. The methods checking along shocks, on ellipse and anlong a simulation path, just fill the matrices and call the core check.

The method *checkUnconditionalAndSave* evaluates unconditional E[F(y, u, u')].

The object also maintains a set of **GResidFunction** functions *vfs* in order to save (possibly expensive) copying of **DynamicModels**.

```
\langle GlobalChecker class declaration 291\rangle \equiv
  class GlobalChecker {
    const Approximation & approx;
    const DynamicModel & model;
    Journal & journal;
    GResidFunction rf;
    VectorFunctionSet vfs;
  public:
    GlobalChecker(const Approximation & app, int n, Journal & jr)
    : approx(app), \ model(approx.getModel()), \ journal(jr), \ rf(approx), \ vfs(rf,n) \ \{ \}
    void check(int max_evals, const ConstTwoDMatrix &y, const ConstTwoDMatrix
        \&x, TwoDMatrix \&out);
    void checkAlongShocksAndSave(mat\_t * fd, const char *prefix, int m, double mult, int max\_evals);
    void checkOnEllipseAndSave(mat_t * fd, const char *prefix, int m, double mult, int max_evals);
    void checkAlongSimulationAndSave(mat_t * fd, const char * prefix, int m, int max_evals);
    void checkUnconditionalAndSave(mat_t * fd, const char *prefix, int m, int max_evals);
  protected:
    void check(const Quadrature & quad, int level, const ConstVector & y, const ConstVector
        &x, Vector &out);
  };
This code is used in section 288.
      Signalled resid function. Not implemented yet. todo:
\langle ResidFunctionSig class declaration 292 \rangle \equiv
  class ResidFunctionSig : public ResidFunction {
  public:
    ResidFunctionSig(const Approximation & app, const Vector & ys, const Vector & xx);
  };
This code is used in section 288.
```

293. End of global\_check.h file.

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```
294.
       Start of global_check.cpp file.
#include "SymSchurDecomp.h"
#include "global_check.h"
#include "smolyak.h"
#include "product.h"
#include "quasi_mcarlo.h"
#ifdef __MINGW32__
#define __CROSS_COMPILATION__
#endif
#ifdef __MINGW64__
#define __CROSS_COMPILATION__
#endif
#ifdef __CROSS_COMPILATION__
#define M_PI 3.14159265358979323846
#endif
  ⟨ ResidFunction constructor code 295 ⟩;
   ResidFunction copy constructor code 296 :
   ResidFunction destructor code 297);
   ResidFunction:: set YU \text{ code } 299 \rangle;
   ResidFunction:: eval \text{ code } 303 \rangle;
   GlobalChecker:: check vector code 304);
   GlobalChecker:: check matrix code 305);
   GlobalChecker:: checkAlongShocksAndSave code 309);
   GlobalChecker:: checkOnEllipseAndSave code 313 \;
   GlobalChecker:: checkAlongSimulationAndSave code 318);
     Here we just set a reference to the approximation, and create a new DynamicModel.
\langle  ResidFunction constructor code 295\rangle \equiv
  ResidFunction::ResidFunction(const Approximation \&app)
  : VectorFunction(app.getModel().nexog(), app.getModel().numeq()), approx(app),
      model(app.getModel().clone()), \ yplus(\Lambda), \ ystar(\Lambda), \ u(\Lambda), \ hss(\Lambda) \ \{ \}
This code is used in section 294.
296.
\langle ResidFunction copy constructor code 296\rangle \equiv
  ResidFunction::ResidFunction(const ResidFunction \&rf)
  : VectorFunction(rf), approx(rf.approx), model(rf.model \neg clone()), yplus(\Lambda), ystar(\Lambda), u(\Lambda),
    if (rf.yplus) yplus = \mathbf{new} \ \mathbf{Vector}(*(rf.yplus));
    if (rf.ystar) ystar = new Vector(*(rf.ystar));
    if (rf.u) u = \text{new Vector}(*(rf.u));
    if (rf.hss) hss = new FTensorPolynomial(*(rf.hss));
This code is used in section 294.
```

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```
297.
\langle \mathbf{ResidFunction} \ destructor \ code \ 297 \rangle \equiv
  ResidFunction: \sim ResidFunction()
     delete model;
     \langle \text{ delete } y \text{ and } u \text{ dependent data } 298 \rangle;
This code is used in section 294.
298.
\langle \text{ delete } y \text{ and } u \text{ dependent data } 298 \rangle \equiv
  if (yplus) delete yplus;
  if (ystar) delete ystar;
  if (u) delete u;
  if (hss) delete hss;
This code is used in sections 297 and 299.
       This sets y^* and u. We have to create ystar, u, yplus and hss.
\langle \mathbf{ResidFunction} :: set YU \ \mathrm{code} \ 299 \rangle \equiv
  void ResidFunction::setYU(const Vector &ys, const Vector &xx)
     \langle \text{ delete } y \text{ and } u \text{ dependent data } 298 \rangle;
     ystar = \mathbf{new} \ \mathbf{Vector}(ys);
     u = \mathbf{new} \ \mathbf{Vector}(xx);
     yplus = new Vector(model \neg numeq());
     approx.getFoldDecisionRule().evaluate(\mathbf{DecisionRule}::horner,*yplus,*ystar,*u);
     (make a tensor polynomial of in-place subtensors from decision rule 300);
     \langle \text{ make } ytmp\_star \text{ be a difference of } yplus \text{ from steady } 301 \rangle;
     \langle \text{ make } hss \text{ and add steady to it } 302 \rangle;
  }
This code is used in section 294.
300. Here we use a dirty tricky of converting const to non-const to obtain a polynomial of subtensor
corresponding to non-predetermined variables. However, this new non-const polynomial will be used for a
construction of hss and will be used in const context. So this dirty thing is safe.
  Note, that there is always a folded decision rule in Approximation.
\langle make a tensor polynomial of in-place subtensors from decision rule 300\rangle \equiv
  union {
     const FoldDecisionRule *c;
     FoldDecisionRule *n;
  dr.c = \&(approx.qetFoldDecisionRule());
  FTensorPolynomial dr_ss(model \neg nstat() + model \neg npred(), model \neg nboth() + model \neg nforw(), *(dr.n));
This code is used in section 299.
```

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```
301.
\langle \text{ make } ytmp\_star \text{ be a difference of } yplus \text{ from steady } 301 \rangle \equiv
  \textbf{Vector} \ ytmp\_star(\textbf{ConstVector}(*yplus, model \neg nstat(), model \neg npred() + model \neg nboth()));
  \textbf{ConstVector} \ ysteady\_star(dr.c\neg getSteady(), model\neg nstat(), model\neg npred() + model\neg nboth());
  ytmp\_star.add(-1.0, ysteady\_star);
This code is used in section 299.
       Here is the const context of dr_{-}ss.
\langle make hss and add steady to it 302 \rangle \equiv
  hss = new FTensorPolynomial(dr_ss, ytmp_star);
  Const Vector ysteady\_ss(dr.c \neg getSteady(), model \neg nstat() + model \neg npred(),
       model \neg nboth() + model \neg nforw());
  if (hss \neg check(\mathbf{Symmetry}(0))) {
     hss \neg get(\mathbf{Symmetry}(0)) \neg getData().add(1.0, ysteady\_ss);
  else {
     FFSTensor *ten = new FFSTensor(hss \neg nrows(), hss \neg nvars(), 0);
     ten \neg getData() = ysteady\_ss;
     hss \neg insert(ten);
This code is used in section 299.
303. Here we evaluate the residual F(y^*, u, u'). We have to evaluate hss for u' = point and then we evaluate
the system f.
\langle \mathbf{ResidFunction} :: eval \ \mathrm{code} \ 303 \rangle \equiv
  void ResidFunction::eval(const Vector &point, const ParameterSignal &siq, Vector &out)
     KORD_RAISE_IF(point.length() \neq hss \neg nvars(),
          "Wrong dimension of input vector in ResidFunction::eval");
     \texttt{KORD\_RAISE\_IF}(out.length() \neq model \neg numeq(),
          "Wrong_dimension_of_output_vector_in_ResidFunction::eval");
     Vector yss(hss \neg nrows());
     hss \rightarrow evalHorner(yss, point);
     model \rightarrow evaluateSystem(out, *ystar, *yplus, yss, *u);
  }
This code is used in section 294.
304. This checks the E[F(y^*, u, u')] for a given y^* and u by integrating with a given quadrature. Note
that the input ys is y^* not whole y.
\langle GlobalChecker:: check vector code 304\rangle \equiv
  void GlobalChecker::check(const Quadrature &quad,int level,const ConstVector &ys,const
            ConstVector &x, Vector &out)
  {
     for (int ifunc = 0; ifunc < vfs.getNum(); ifunc +++)
       ((GResidFunction \&)(vfs.getFunc(ifunc))).setYU(ys,x);
     quad.integrate(vfs, level, out);
  }
This code is cited in section 305.
This code is used in section 294.
```

136 GLOBAL CHECK Dynare++ §305

**305.** This method is a bulk version of  $\langle$  **GlobalChecker**:: check vector code 304 $\rangle$ . It decides between Smolyak and product quadrature according to max\_evals constraint.

Note that y can be either full (all endogenous variables including static and forward looking), or just  $y^*$  (state variables). The method is able to recognize it.

```
\langle GlobalChecker :: check matrix code 305\rangle \equiv
  void GlobalChecker::check(int max_evals,const ConstTwoDMatrix &y,const
            ConstTwoDMatrix &x, TwoDMatrix &out)
     JournalRecordPair pa(journal);
     pa \ll "Checking_{\square}approximation_{\square}error_{\square}for_{\square}" \ll y.ncols() \ll "_{\square}states_{\square}with_{\square}at_{\square}most_{\square}" \ll y.ncols()
          max\_evals \ll "\_evaluations" \ll endrec;
     \langle decide about type of quadrature 306\rangle;
     Quadrature *quad;
     int lev;
     (create the quadrature and report the decision 307);
     \langle \text{ check all column of } y \text{ and } x \text{ 308} \rangle;
     delete quad;
This code is used in section 294.
306.
\langle decide about type of quadrature 306\rangle \equiv
  GaussHermite qh;
  SmolyakQuadrature dummy_sq(model.nexog(),1,gh);
  int smol_evals;
  int smol_level;
  dummy_sq.designLevelForEvals(max_evals, smol_level, smol_evals);
  ProductQuadrature dummy_pq(model.nexog(), gh);
  int prod_evals;
  int prod_level;
  dummy_pq.designLevelForEvals(max_evals, prod_level, prod_evals);
  bool take\_smolyak = (smol\_evals < prod\_evals) \land (smol\_level \ge prod\_level - 1);
This code is used in section 305.
```

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```
307.
\langle create the quadrature and report the decision 307\rangle \equiv
  if (take_smolyak) {
     quad = new SmolyakQuadrature(model.nexoq(), smol_level, qh);
     lev = smol\_level;
     JournalRecord rec(journal);
     rec \ll "Selected_{\sqcup}Smolyak_{\sqcup}(level,evals) = (" \ll smol\_level \ll "," \ll smol\_evals \ll "
          ")_{\sqcup}over_{\sqcup}product_{\sqcup}(" \ll prod\_level \ll "," \ll prod\_evals \ll ")" \ll endrec;
  else {
     quad = new ProductQuadrature(model.nexog(), gh);
     lev = prod\_level;
     JournalRecord rec(journal);
     rec \ll "Selected_{\sqcup}product_{\sqcup}(level,evals) = (" \ll prod\_level \ll "," \ll prod\_evals \ll ")
          ")_{\sqcup}over_{\sqcup}Smolyak_{\sqcup}(" \ll smol\_level \ll "," \ll smol\_evals \ll ")" \ll endrec;
  }
This code is used in section 305.
308.
\langle \text{ check all column of } y \text{ and } x \text{ 308} \rangle \equiv
  int first\_row = (y.nrows() \equiv model.numeq())? model.nstat():0;
  ConstTwoDMatrix\ ysmat(y, first\_row, 0, model.npred() + model.nboth(), y.ncols());
  for (int j = 0; j < y.ncols(); j ++ ) {
     {\bf ConstVector}\ yj(ysmat,j);
     ConstVector xj(x, j);
     Vector outj(out, j);
     check(*quad, lev, yj, xj, outj);
This code is used in section 305.
309. This method checks an error of the approximation by evaluating residual E[F(y^*, u, u')|y^*, u] for y^*
being the steady state, and changing u. We go through all elements of u and vary them from -mult \cdot \sigma to
mult \cdot \sigma in m steps.
\langle GlobalChecker :: checkAlongShocksAndSave code 309 \rangle \equiv
  void GlobalChecker::checkAlongShocksAndSave(mat_t * fd, const char *prefix, int m, double
            mult, int max_evals)
     JournalRecordPair pa(journal);
     pa \ll "Calculating_errors_along_shocks_+/-_" \ll mult \ll "_std_errors,_granularity_" \ll
          m \ll endrec;
     \langle \text{ setup } y\_mat \text{ of steady states for checking } 310 \rangle;
     \langle \text{ setup } exo\_mat \text{ for checking } 311 \rangle;
     TwoDMatrix errors(model.numeq(), 2*m*model.nexog() + 1);
     check(max_evals, y_mat, exo_mat, errors);
     (report errors along shock and save them 312);
  }
This code is used in section 294.
```

138 GLOBAL CHECK Dynare++ §310

```
310.
\langle \text{ setup } y\_mat \text{ of steady states for checking } 310 \rangle \equiv
  TwoDMatrix y_mat(model.numeq(), 2*m*model.nexog()+1);
  for (int j = 0; j < 2 * m * model.nexog() + 1; j++) {
    Vector yj(y_{-}mat, j);
    yj = (\mathbf{const\ Vector\ }\&)\ model.getSteady();
This code is used in section 309.
311.
\langle \text{ setup } exo\_mat \text{ for checking } 311 \rangle \equiv
  TwoDMatrix exo\_mat(model.nexog(), 2*m*model.nexog() + 1);
  exo_mat.zeros();
  for (int ishock = 0; ishock < model.nexog(); ishock +++) {
    double max\_sigma = sqrt(model.getVcov().get(ishock, ishock));
    for (int j = 0; j < 2 * m; j \leftrightarrow) {
       int jmult = (j < m) ? j - m : j - m + 1;
       exo\_mat.get(ishock, 1 + 2 * m * ishock + j) = mult * jmult * max\_sigma/m;
  }
This code is used in section 309.
312.
\langle report errors along shock and save them 312\rangle \equiv
  TwoDMatrix res(model.nexog(), 2*m+1);
  JournalRecord rec(journal);
  rec \ll "Shock_{\cutum}value_{\cutum}error" \ll endrec;
  ConstVector err0 (errors, 0);
  char shock[9];
  char erbuf[17]; for (int ishock = 0; ishock < model.nexog(); ishock +++) { TwoDMatrix
       err\_out(model.numeq(), 2*m+1);
  sprintf(shock, "\%-8s", model.getExogNames().getName(ishock)); for (int j=0; j<2*m+1; j++) {
       int jj; Vector
  error (err\_out, j) ;
  if (j \neq m) {
  if (j < m) jj = 1 + 2 * m * ishock + j;
  else jj = 1 + 2 * m * ishock + j - 1;
  ConstVector colij(errors, jj); error = colij; } else { jj = 0; error = err\theta; } JournalRecord
       rec1 (journal); sprintf (erbuf, "%12.7g_{ | | | | | | |}", error . getMax());
  rec1 \ll shock \ll " " = exo\_mat.get(ishock, jj) \ll " t" \ll erbuf \ll endrec; } char tmp[100];
  sprintf(tmp, "%s_shock_%s_errors", prefix, model.getExoqNames().getName(ishock));
  err\_out.writeMat(fd, tmp);  }
This code is used in section 309.
```

§313 Dynare++ GLOBAL CHECK 139

**313.** This method checks errors on ellipse of endogenous states (predetermined variables). The ellipse is shaped according to covariance matrix of endogenous variables based on the first order approximation and scaled by *mult*. The points on the ellipse are chosen as polar images of the low discrepancy grid in a cube.

The method works as follows: First we calculate symmetric Schur factor of covariance matrix of the states. Second we generate low discrepancy points on the unit sphere. Third we transform the sphere with the variance-covariance matrix factor and multiplier mult and initialize matrix of  $u_t$  to zeros. Fourth we run the check method and save the results.

```
\langle GlobalChecker :: checkOnEllipseAndSave code 313 \rangle \equiv
  void GlobalChecker:: checkOnEllipseAndSave(mat_t*fd, const. char*prefix, int. m, double. mult, int.
            max_evals)
     {\bf Journal Record Pair}\ pa(journal);
     pa \ll "Calculating = rors = t = m \ll "lellipse = points = scaled = by = mult \ll endrec;
     \langle make factor of covariance of variables 314\rangle;
     \langle \text{ put low discrepancy sphere points to } ymat 315 \rangle;
     \langle \text{transform sphere } ymat \text{ and prepare } umat \text{ for checking } 316 \rangle;
     \langle \text{ check on ellipse and save } 317 \rangle;
This code is used in section 294.
314. Here we set ycovfac to the symmetric Schur decomposition factor of a submatrix of covariances of all
endogenous variables. The submatrix corresponds to state variables (predetermined plus both).
\langle make factor of covariance of variables 314\rangle \equiv
  \mathbf{TwoDMatrix} *ycov = approx.calcYCov();
  TwoDMatrix ycovpred((const TwoDMatrix &) *ycov, model.nstat(), model.nstat(),
       model.npred() + model.nboth(), model.npred() + model.nboth());
  delete ycov;
  SymSchurDecompssd(ycovpred);
  ssd.correctDefinitness(1.\cdot 10^{-05});
  TwoDMatrix ycovfac(ycovpred.nrows(), ycovpred.ncols());
  KORD\_RAISE\_IF(\neg ssd.isPositiveSemidefinite(), "Covariance\_matrix\_of\_the\_states\_not\_pos\
       itive___semidefinite_in_GlobalChecker::checkOnEllipseAndSave");
  ssd.getFactor(ycovfac);
```

140 GLOBAL CHECK Dynare++ §315

**315.** Here we first calculate dimension d of the sphere, which is a number of state variables minus one. We go through the d-dimensional cube  $(0,1)^d$  by **QMCarloCubeQuadrature** and make a polar transformation to the sphere. The polar transformation  $f^i$  can be written recursively wrt. the dimension i as:

$$f^{0}() = [1]$$

$$f^{i}(x_{1},...,x_{i}) = \begin{bmatrix} cos(2\pi x_{i}) \cdot f^{i-1}(x_{1},...,x_{i-1}) \\ sin(2\pi x_{i}) \end{bmatrix}$$

```
\langle put low discrepancy sphere points to ymat 315\rangle \equiv
  int d = model.npred() + model.nboth() - 1;
  TwoDMatrix ymat(model.npred() + model.nboth(), (d \equiv 0) ? 2 : m);
  if (d \equiv 0) {
    ymat.get(0,0) = 1;
    ymat.get(0,1) = -1;
  }
  else {
    int icol = 0;
    ReversePerScheme ps;
    QMCarloCubeQuadrature qmc(d, m, ps);
    qmcpitbeg = qmc.start(m);
    qmcpitend = qmc.end(m);
    for (qmcpitrun = beg; run \neq end; ++run, icol++) {
      Vector ycol(ymat, icol);
      Vector x(run.point());
      x.mult(2 * M_PI);
      ycol[0] = 1;
      for (int i = 0; i < d; i ++) {
         Vector subsphere(ycol, 0, i + 1);
         subsphere.mult(cos(x[i]));
         ycol[i+1] = sin(x[i]);
    }
  }
This code is used in section 313.
```

**316.** Here we multiply the sphere points in ymat with the Cholesky factor to obtain the ellipse, scale the ellipse by the given mult, and initialize matrix of shocks umat to zero.

```
⟨ transform sphere ymat and prepare umat for checking 316⟩ ≡
TwoDMatrix umat(model.nexog(), ymat.ncols());
umat.zeros();
ymat.mult(mult);
ymat.multLeft(ycovfac);
ConstVector ys(model.getSteady(), model.nstat(), model.npred() + model.nboth());
for (int icol = 0; icol < ymat.ncols(); icol++) {
    Vector ycol(ymat, icol);
    ycol.add(1.0, ys);
}</pre>
This code is used in section 313.
```

§317 Dynare++ GLOBAL CHECK 141

```
317.
       Here we check the points and save the results to MAT-4 file.
\langle check on ellipse and save 317\rangle \equiv
  TwoDMatrix out(model.numeq(), ymat.ncols());
  check(max_evals, ymat, umat, out);
  char tmp[100];
  sprintf(tmp, "%s_ellipse_points", prefix);
  ymat.writeMat(fd, tmp);
  sprintf(tmp, "%s_ellipse_errors", prefix);
  out.writeMat(fd, tmp);
This code is used in section 313.
318. Here we check the errors along a simulation. We simulate, then set x to zeros, check and save results.
\langle GlobalChecker :: checkAlongSimulationAndSave code 318 \rangle \equiv
  void GlobalChecker:: checkAlongSimulationAndSave(mat_t * fd, const char * prefix, int m, int
           max_evals)
    JournalRecordPair pa(journal);
    pa \ll "Calculating = rrors = at = " \ll m \ll " = simulated = points" \ll endrec;
    RandomShockRealization \ sr(model.getVcov(), system\_random\_generator.int\_uniform());
    \mathbf{TwoDMatrix} *y = approx.getFoldDecisionRule().simulate(\mathbf{DecisionRule} :: horner, m,
         model.getSteady(), sr);
    TwoDMatrix x(model.nexog(), m);
    x.zeros();
    TwoDMatrix out(model.numeq(), m);
    check(max\_evals, *y, x, out);
    char tmp[100];
    sprintf(tmp, "%s_simul_points", prefix);
    y \rightarrow writeMat(fd, tmp);
    sprintf(tmp, "%s_simul_errors", prefix);
    out.writeMat(fd, tmp);
    delete y;
This code is used in section 294.
319. End of global_check.cpp file.
```

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