$$g = \phi + \phi \lambda (Z_D - 1) \tag{1}$$

$$g Z_D = \phi Z_D + V_D \tag{2}$$

$$V_D = Z_D \,\overline{\zeta} \,\zeta \,\left(\frac{g \,N_D}{K_D}\right)^{\eta} \tag{3}$$

$$J = (-M) + \phi \Lambda \left(\lambda H + J \left(1 - \lambda\right)\right) \tag{4}$$

$$H = \Pi + \phi \Lambda H \tag{5}$$

$$\Pi = \frac{1}{\vartheta} \frac{1}{\mathcal{M}} Y_D^W \tag{6}$$

$$Z_{D}\zeta\overline{\zeta}J\Lambda\frac{1}{\left(\frac{K_{D}}{g}\right)^{\eta}}\frac{1}{N_{D}^{1-\eta}} = 1 + \log\left(f'(\cdot)\right)\left(\frac{gN_{D}}{N_{D}} + \log\left(f(\cdot)\right)\right) - \Lambda\log\left(f'(\cdot)\right)\left(\frac{gN_{D}}{N_{D}}\right)^{2}$$

$$\tag{7}$$

$$\Lambda \phi \rho_{\lambda} \bar{\lambda} (H - J) = M^{1 - \rho_{\lambda}} \tag{8}$$

$$\lambda = \bar{\lambda} M^{\rho_{\lambda}} \tag{9}$$

$$Y_D = Y_D^W \tag{10}$$

$$Y_D^W = \left(\frac{K_D}{g}\right)^{\alpha} L^{1-\alpha} \tag{11}$$

$$Y_{D} = C_{D} + (1 + \log(g(\cdot)|)) I_{D} + N_{D} (1 + \log(f(\cdot)|)) + (Z_{D} - 1) M$$
(12)

$$\Lambda = \frac{\beta U_{CD}}{U_{CD}} g^{(-\rho)} \tag{13}$$

$$U_{CD} = \left(C_D - \Gamma_D \frac{\chi}{1+\epsilon} L^{1+\epsilon}\right)^{(-\rho)} + (-\mu_D) \gamma \left(\frac{\Gamma_D}{g C_D}\right)^{1-\gamma}$$
(14)

$$\mu_D = \beta \left(1 - \gamma\right) g^{(-\rho)} \mu_D \left(\frac{gC_D}{\Gamma_D}\right)^{\gamma} + L^{1+\epsilon} \frac{\chi}{1+\epsilon} \left(C_D - \Gamma_D \frac{\chi}{1+\epsilon} L^{1+\epsilon}\right)^{(-\rho)}$$
(15)

$$\left(C_D - \Gamma_D \frac{\chi}{1+\epsilon} L^{1+\epsilon}\right)^{(-\rho)} \Gamma_D \chi L^{\epsilon} \frac{1}{U_{CD}} = (1-\alpha) \frac{1}{\mathcal{M}} \frac{\vartheta - 1}{\vartheta} \frac{Y_D}{L} \tag{16}$$

$$\Gamma_D = C_D{}^{\gamma} \left(\frac{\Gamma_D}{g}\right)^{1-\gamma} \tag{17}$$

$$K_D = I_D + \frac{K_D}{q} (1 - \delta) \tag{18}$$

$$Q = 1 + \log\left(\left.g\left(\cdot\right)\right|\right) + \frac{g\,I_{D}}{I_{D}}\log\left(\left.g'\left(\cdot\right)\right|\right) - \log\left(\left.g'\left(\cdot\right)\right|\right)\,\Lambda\,\left(\frac{g\,I_{D}}{I_{D}}\right)^{2} \tag{19}$$

$$Q = \Lambda \left( \frac{\alpha Y_D^W g (\vartheta - 1)}{\vartheta K_D \mathcal{M}} + (1 - \delta) Q \right)$$
 (20)

$$log(\zeta) = \sigma_{\zeta} \epsilon^{\chi} + log(\zeta) \rho_{\zeta} - \rho_{\zeta 2} log(AUX\_ENDO\_LAG\_20\_1)$$
(21)

$$S_D = H + K_D Q + J (Z_D + V_D - 1) + X_D$$
(22)

$$X_D = g \Lambda (X_D + V_D J) \tag{23}$$

$$\mathcal{R}_D = N_D \tag{24}$$

$$f(\cdot)| = exp\left(\frac{\psi_N}{2} \left(\frac{gN_D}{N_D} - g^{BGP}\right)^2\right)$$
 (25)

$$f'(\cdot)| = exp\left(\psi_N\left(\frac{gN_D}{N_D} - g^{BGP}\right)\right)$$
 (26)

$$g(\cdot)| = exp\left(\frac{\psi_I}{2} \left(\frac{gI_D}{I_D} - g^{BGP}\right)^2\right)$$
(27)

$$g'(\cdot)| = exp\left(\psi_I\left(\frac{gI_D}{I_D} - g^{BGP}\right)\right)$$
 (28)

$$\pi^{1-\omega} = \theta + (1-\theta) \ \pi^{*1-\omega} \tag{29}$$

$$\pi^* = \pi \frac{\omega}{\omega - 1} \frac{x_{1D}}{x_{2D}} \tag{30}$$

$$x_{1D} = Y_D \frac{1}{M} U_{CD} + x_{1D} \beta \theta g^{1-\rho} \pi^{\omega}$$
(31)

$$x_{2D} = Y_D U_{CD} + x_{2D} \beta \theta g^{1-\rho} \pi^{\omega - 1}$$
(32)

$$1 = \frac{\Lambda R}{\pi} \tag{33}$$

$$\frac{R}{R^{ss}} = \pi^{\gamma_{\pi}} \left( \frac{\frac{1}{\mathcal{M}}}{\frac{1}{\mathcal{M}^{ss}}} \right)^{\gamma_{y}} \tag{34}$$

$$AUX\_ENDO\_LAG\_20.1 = \zeta \tag{35}$$