$$g_t = \phi \ (1 + \lambda \ (Z_{D_t} + V_{D_t} - 1)) \tag{1}$$

$$Z_{Dt} g_{t-1} = \phi \left( Z_{Dt-1} + (1 - \lambda) V_{Dt-1} \right)$$
 (2)

$$V_{Dt} = \zeta_t \, Z_{Dt}^{1-\eta} \, N_{Dt}^{\eta} \tag{3}$$

$$J_t = \lambda H_t + \phi (1 - \lambda) \Lambda_{t+1} J_{t+1} \tag{4}$$

$$H_t = \Pi_t + \phi \Lambda_{t+1} H_{t+1} \tag{5}$$

$$\Pi_t = \frac{1}{2} \frac{1}{M} Y_{D_t}^W \tag{6}$$

$$\zeta_{t} \eta J_{t} \left( \frac{Z_{Dt}}{N_{Dt}} \right)^{1-\eta} = 1 + \log \left( f'(\cdot)|_{t} \right) \frac{g_{t-1} N_{Dt}}{N_{Dt-1}} + \log \left( f(\cdot)|_{t} \right) - \Lambda_{t+1} \log \left( f'(\cdot)|_{t+1} \right) \left( \frac{g_{t} N_{Dt+1}}{N_{Dt}} \right)^{2}$$

$$(7)$$

$$Y_{Dt} = Y_{Dt}^{W} \tag{8}$$

$$Y_{D_t}^W = \left(\frac{K_{D_{t-1}}}{g_{t-1}}\right)^{\alpha} L_t^{1-\alpha} \tag{9}$$

$$Y_{Dt} = N_{Dt} + C_{Dt} + \left(1 + \log\left(g\left(\cdot\right)|_{t}\right)\right) I_{Dt}$$

$$\tag{10}$$

$$\Lambda_t = \frac{\beta U_{CDt}}{U_{CDt-1}} g_{t-1}^{(-\rho)} \tag{11}$$

$$U_{CDt} = \left(C_{Dt} - \Gamma_{Dt} \frac{\chi}{1+\epsilon} L_t^{1+\epsilon}\right)^{(-\rho)} + \left(-\mu_{Dt}\right) \gamma \left(\frac{\Gamma_{Dt-1}}{g_{t-1}C_{Dt}}\right)^{1-\gamma} \tag{12}$$

$$\mu_{D_t} = \beta \ (1 - \gamma) \ g_t^{(-\rho)} \mu_{D_{t+1}} \left( \frac{g_t C_{D_{t+1}}}{\Gamma_{D_t}} \right)^{\gamma} + L_t^{1+\epsilon} \frac{\chi}{1+\epsilon} \left( C_{D_t} - \Gamma_{D_t} \frac{\chi}{1+\epsilon} L_t^{1+\epsilon} \right)^{(-\rho)}$$
(13)

$$\left(C_{Dt} - \Gamma_{Dt} \frac{\chi}{1+\epsilon} L_t^{1+\epsilon}\right)^{(-\rho)} \Gamma_{Dt} \chi L_t^{\epsilon} \frac{1}{U_{CDt}} = (1-\alpha) \frac{1}{\mathcal{M}} \frac{\vartheta - 1}{\vartheta} \frac{Y_{Dt}}{L_t} \tag{14}$$

$$\Gamma_{D_t} = C_{D_t^{\gamma}} \left(\frac{\Gamma_{D_{t-1}}}{g_{t-1}}\right)^{1-\gamma} \tag{15}$$

$$K_{Dt} = I_{Dt} + \frac{K_{Dt-1}}{g_{t-1}} \ (1 - \delta) \tag{16}$$

$$Q_{t} = 1 + \log\left(g\left(\cdot\right)|_{t}\right) + \frac{g_{t-1}I_{D_{t}}}{I_{D_{t-1}}}\log\left(g'\left(\cdot\right)|_{t}\right) - \Lambda_{t+1}\left(\frac{g_{t}I_{D_{t+1}}}{I_{D_{t}}}\right)^{2}\log\left(g'\left(\cdot\right)|_{t+1}\right)$$

$$(17)$$

$$Q_t = \Lambda_{t+1} \left( \frac{\alpha g_t \left( \vartheta - 1 \right) Y_{D t+1}^W}{\vartheta \mathcal{M} K_{Dt}} + (1 - \delta) Q_{t+1} \right)$$

$$\tag{18}$$

$$\log\left(\zeta_{t}\right) = \rho_{\zeta}\log\left(\zeta_{t-1}\right) + 0.1\,\epsilon_{t}^{\chi}\tag{19}$$

$$S_{Dt} = H_t + K_{Dt}Q_t + (Z_{Dt} + V_{Dt} - 1)J_t + X_{Dt}$$
(20)

$$X_{Dt} = g_t \Lambda_{t+1} \left( J_{t+1} V_{Dt+1} + X_{Dt+1} \right) \tag{21}$$

$$\mathcal{R}_{Dt} = V_{Dt} J_t \tag{22}$$

$$f(\cdot)|_{t} = exp\left(\frac{\psi_{N}}{2} \left(\frac{g_{t-1} N_{Dt}}{N_{Dt-1}} - g^{BGP}\right)^{2}\right)$$

$$(23)$$

$$f'(\cdot)|_{t} = exp\left(\psi_{N}\left(\frac{g_{t-1} N_{D_{t}}}{N_{D_{t-1}}} - g^{BGP}\right)\right)$$

$$(24)$$

$$g\left(\cdot\right)|_{t} = exp\left(\frac{\psi_{I}}{2}\left(\frac{g_{t-1}I_{Dt}}{I_{Dt-1}} - g^{BGP}\right)^{2}\right) \tag{25}$$

$$g'(\cdot)|_{t} = exp\left(\psi_{I}\left(\frac{g_{t-1}I_{Dt}}{I_{Dt-1}} - g^{BGP}\right)\right)$$
 (26)