

# Lab 06

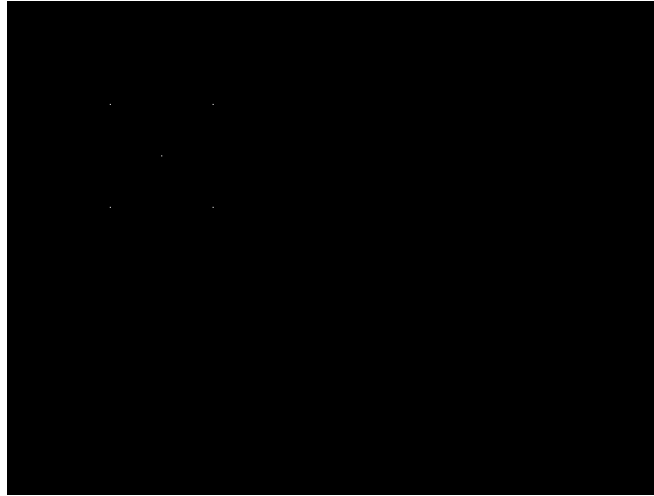
Hough Transform

# Contents

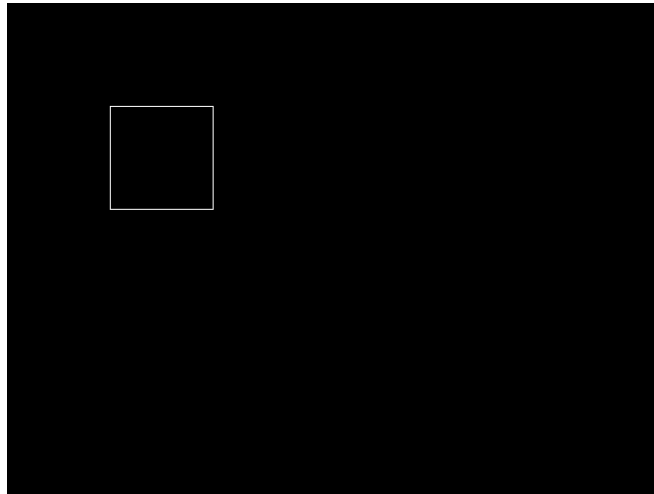
- images
- Prepare Hough Space
- Hough Transform
- Find Peak

# images

- 5 points

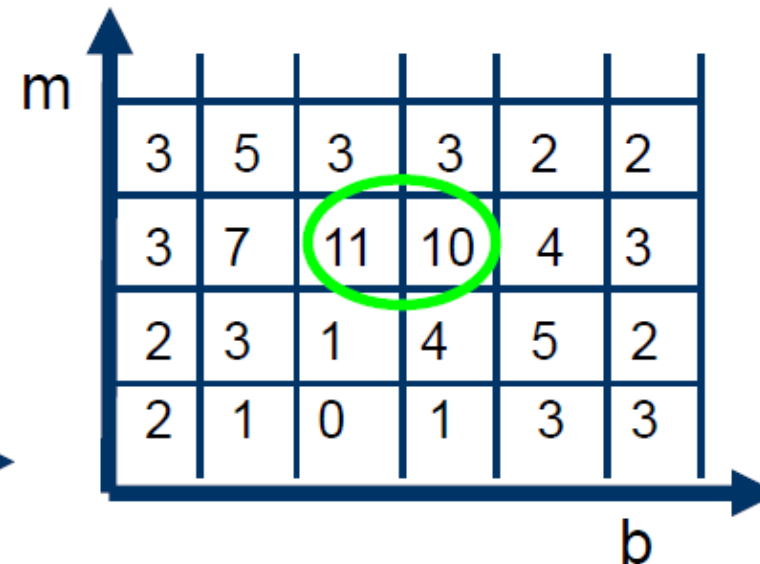
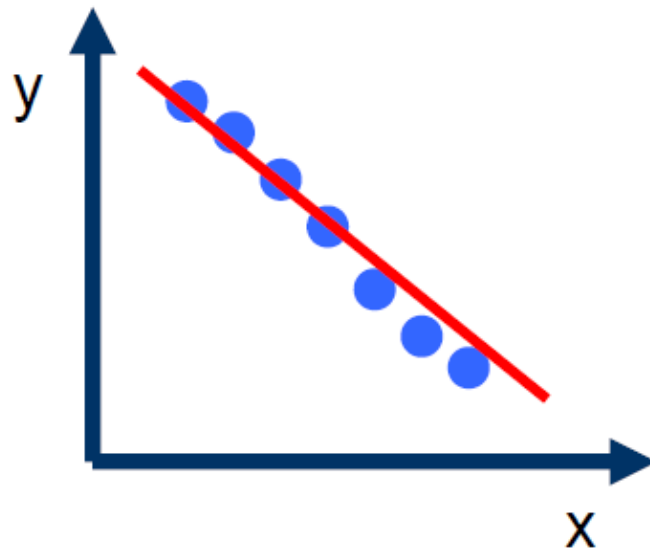
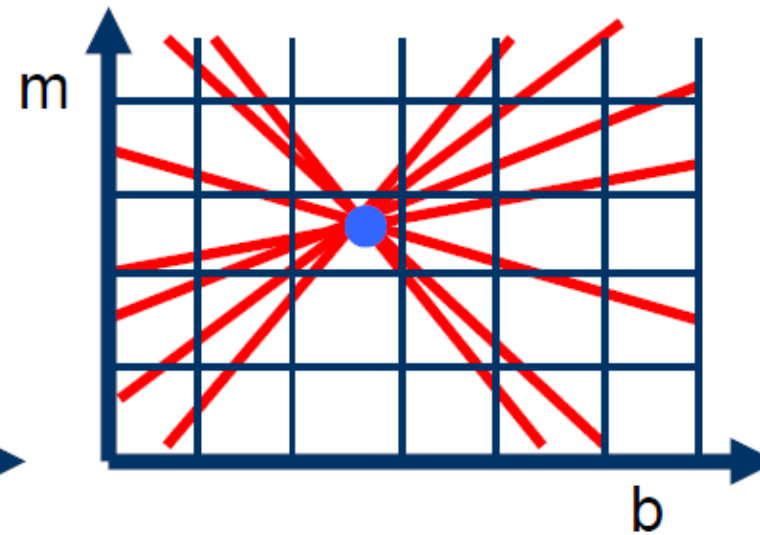
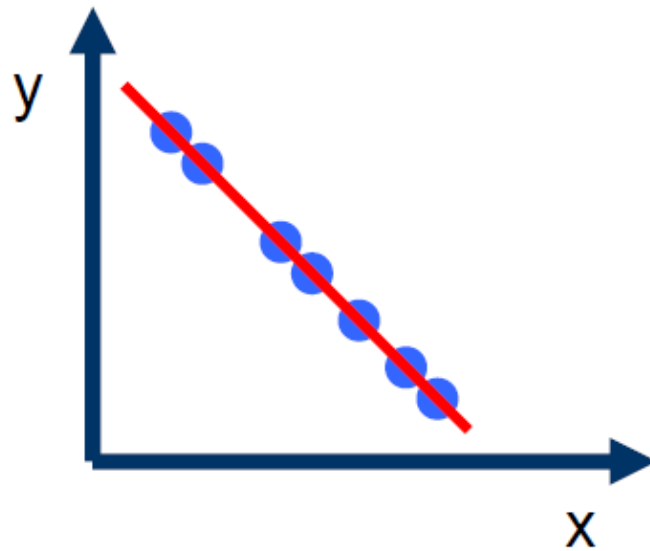


- rectangle



# Hough transform

$$Y = mx + b$$

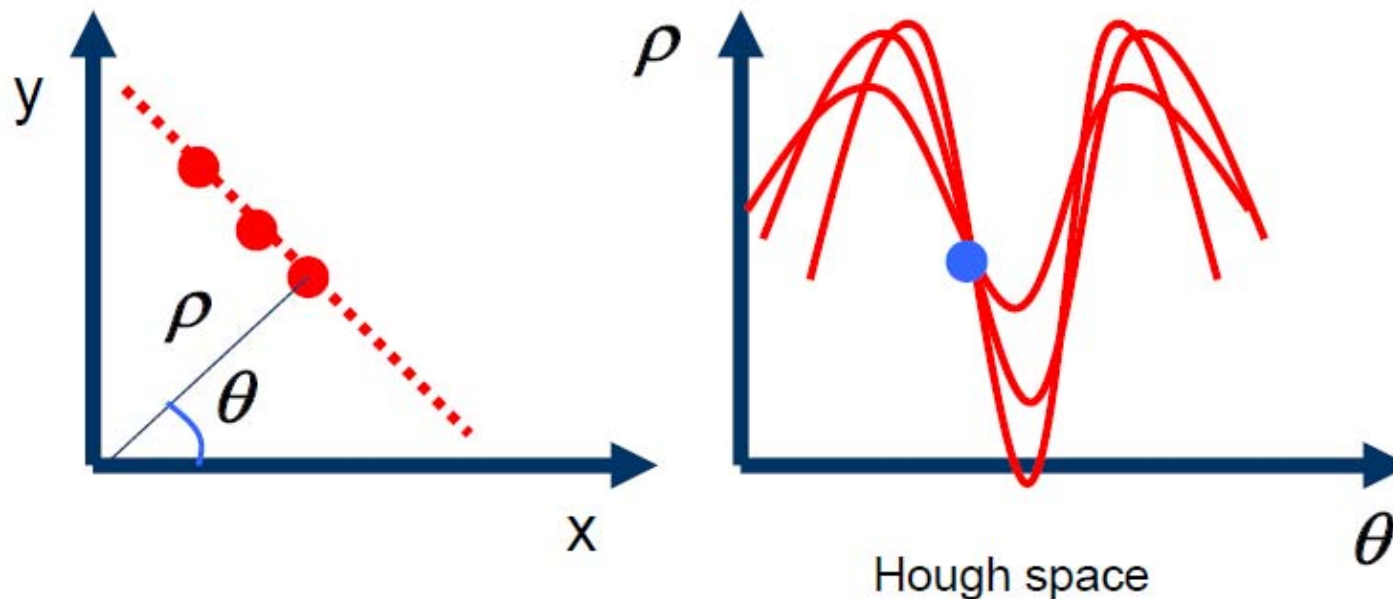


# Hough transform

P.V.C. Hough, *Machine Analysis of Bubble Chamber Pictures*, Proc. Int. Conf. High Energy Accelerators and Instrumentation, 1959

Issue : parameter space  $[m,b]$  is unbounded...

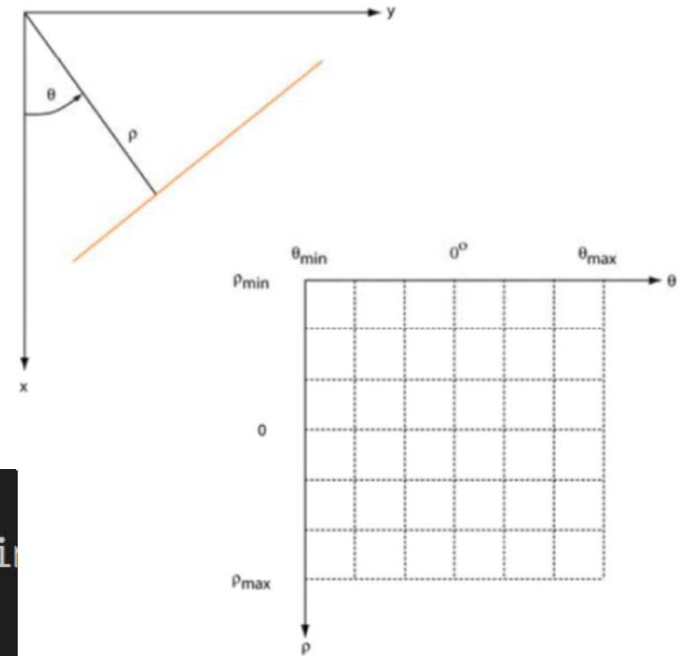
Use a polar representation for the parameter space



$$x \cos \theta + y \sin \theta = \rho$$

# Prepare Hough Space

- (=accumulator cells)



Polar representation of lines

```
// prepare Hough space
int RhoLimit = sqrt( img_edge.cols*img_edge.cols + i
int nRho = RhoLimit*2+1;
double thetaSamplingFreq = 0.0025;
int nTheta = CV_PI / thetaSamplingFreq + 5;
Mat canvas_HoughSpace = Mat::zeros( nRho, nTheta, CV_32FC1 );
```

# Prepare Hough Space

- (=accumulator cells)

```
# prepare Hough space
RhoLimit = math.floor(np.linalg.norm( image.shape ))
nRho = RhoLimit*2+1 # -limit to +limit
thetaSamplingFreq = 0.0025
nTheta = math.floor( math.pi / thetaSamplingFreq )
canvas_HoughSpace = np.zeros( (nRho, nTheta ) )
```

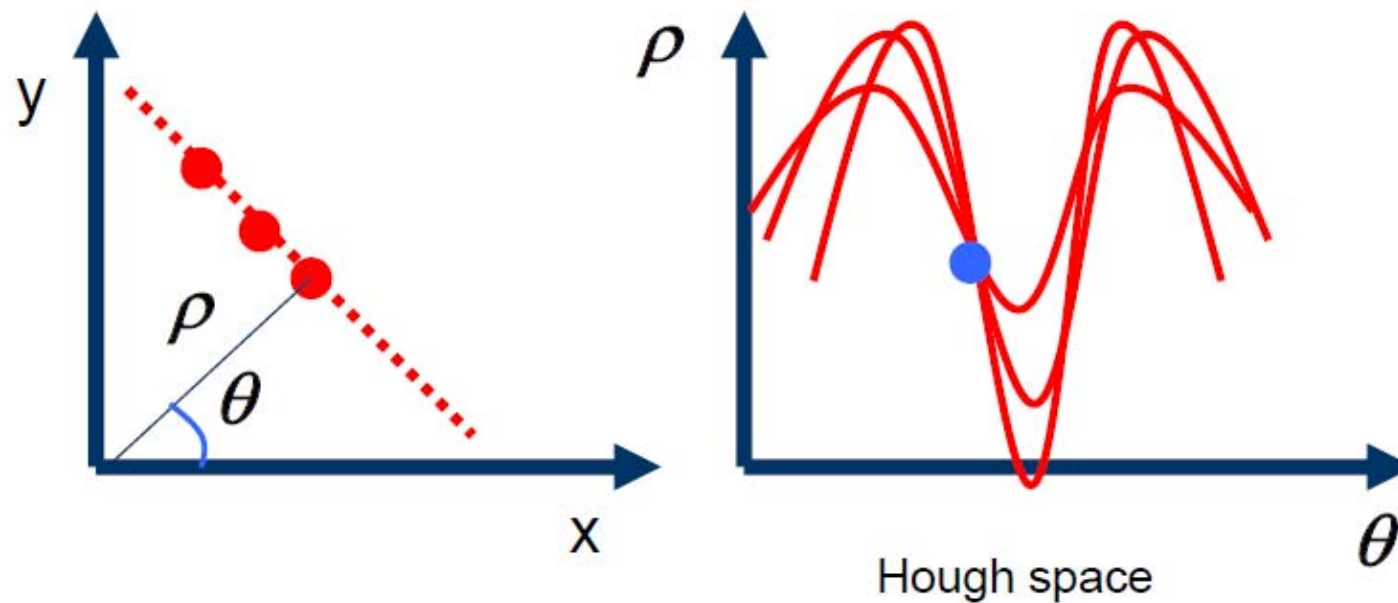
# Pre-calculate trigonometric functions

```
# pre-calculated trigonometric functions
cosine = np.zeros(nTheta)
sine = np.zeros(nTheta)
for theta in range(nTheta):
    cosine[theta] = math.cos(theta*thetaSamplingFreq)
    sine[theta] = math.sin(theta*thetaSamplingFreq)
```



# Hough Transform

- Find possible polar coordinates of each point



$$x \cos \theta + y \sin \theta = \rho$$

# Hough Transform

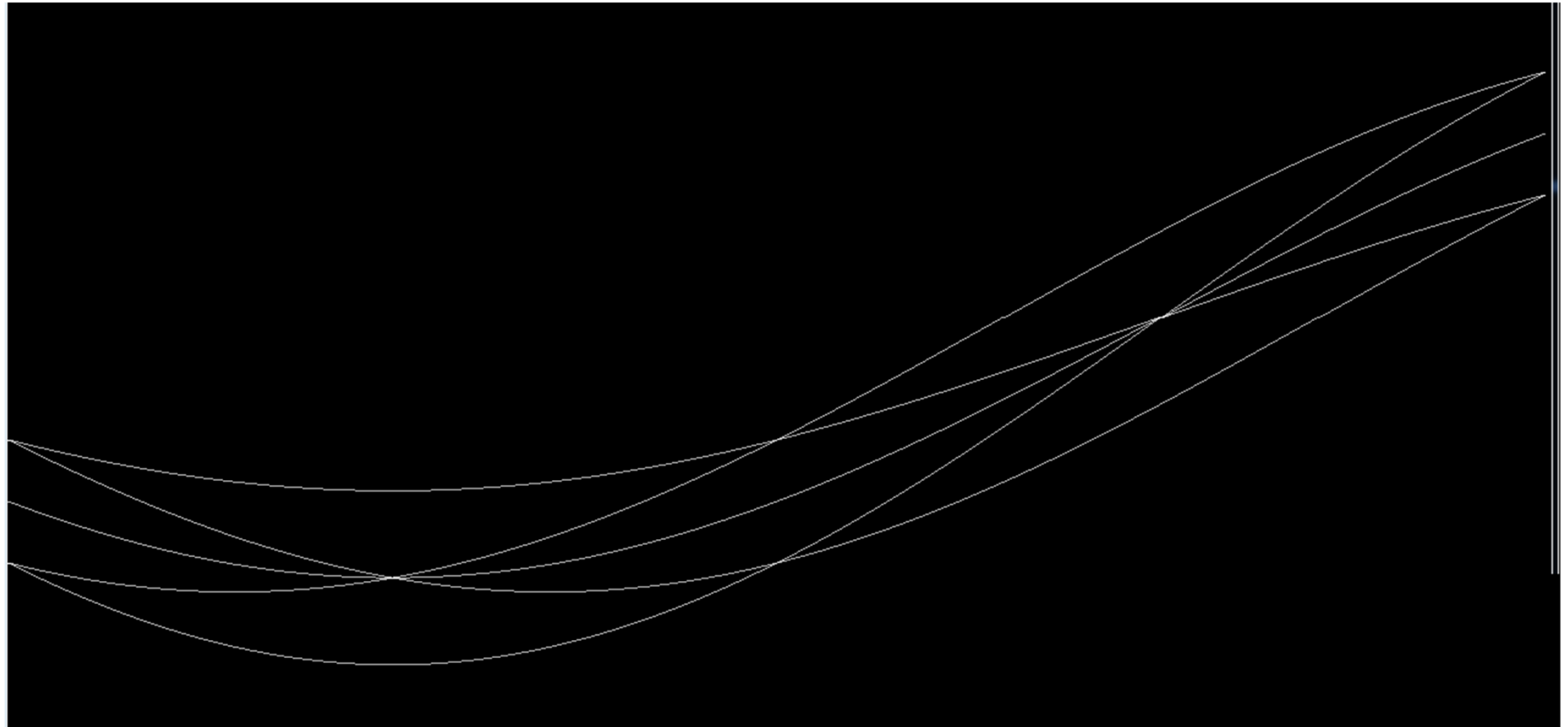
For each point, vote on polar coordinates (c code)

# Hough Transform

For each point, vote on polar coordinates

normalize

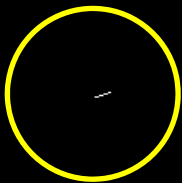
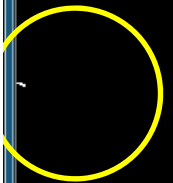
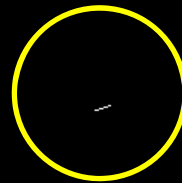
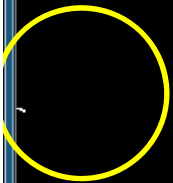
# Hough Transform



# Find Peak

```
// find peaks  
Mat canvas_HoughSpace_peak;  
threshold( canvas_HoughSpace, canvas_HoughSpace_peak, 0.3, 1, THRESH_BINARY );  
imshow( "canvas_HoughSpace_peak", canvas_HoughSpace_peak );  
waitKey();
```

$$\text{dst}(x, y) = \begin{cases} \text{maxval} & \text{if } \text{src}(x, y) > \text{thresh} \\ 0 & \text{otherwise} \end{cases}$$



# Hough Transform

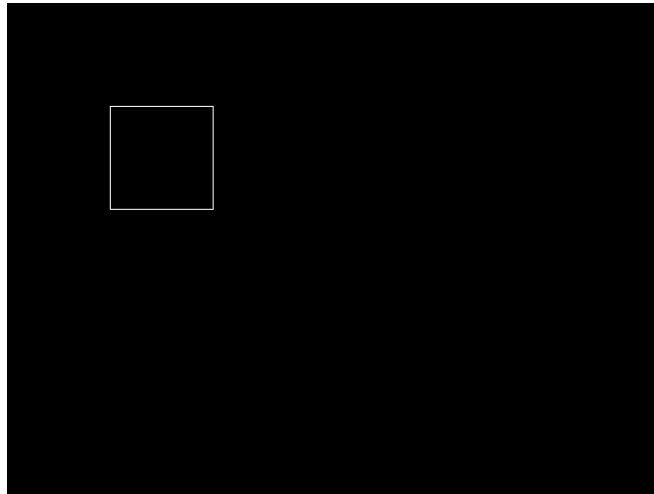
Threshold  
Convert back  
Draw lines

# images

- 5 points



- rectangle



# Hough Transform





# results

