

STAT 350 Final Project of predicting V-10

Xiaotian Ding, Jie Gu, De Lu, Huaiyi Liu

2019/3/10

```
# Import the data and pretreatment
load("~/Desktop/Study in NU/Winter/Regression analysis/Final/train & test.RData")
Zipcode= as.factor(train$`V-1`)
Zipcodetest=as.factor(test$`V-1`)
#strandized for train
y9=as.matrix(train$`V-9`)
colnames(y9)=c("V-9")
y10=as.matrix(train$`V-10`)
colnames(y10)=c("V-10")
train.v9<- cbind(Zipcode,train[2:27],y9)
train.v10<- cbind(Zipcode,train[2:27],y10)
for(i in 2:27)
{
  train.v9[,i] <-(train[,i]-mean(train[,i])) /sd(train[,i])
}
for(i in 2:27)
{
  train.v10[,i] <-(train[,i]-mean(train[,i])) /sd(train[,i])
}

#strandized for test data
yt9=as.matrix(test$`V-9`)
colnames(yt9)=c("V-9")
yt10=as.matrix(test$`V-10`)
colnames(yt10)=c("V-10")
test.v9<- cbind(test[1:27],yt9)
test.v10<- cbind(test[1:27],yt10)
for(i in 2:27)
{
  test.v9[,i] <-(test[,i]-mean(test[,i])) /sd(test[,i])
}
for(i in 2:27)
{
  test.v10[,i] <-(test[,i]-mean(test[,i])) /sd(test[,i])
}

# scatter plot & cor
fitv10 <- lm(train$`V-10`~ ., data = train.v10)
summary(fitv10)
```

```
##
## Call:
## lm(formula = train$`V-10` ~ ., data = train.v10)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -96.94  -11.10    0.13   11.22  195.69
##
```

```

## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) 235.4539      8.1451  28.907 < 2e-16 ***
## Zipcode2      3.2450      9.3795   0.346 0.72962
## Zipcode3     -9.8061      8.1755  -1.199 0.23134
## Zipcode4     -5.4482      9.8506  -0.553 0.58064
## Zipcode5     -0.7110     10.4575  -0.068 0.94584
## Zipcode6     -4.8886      9.8547  -0.496 0.62023
## Zipcode7    -12.5746     10.3617  -1.214 0.22591
## Zipcode8     -5.6590     10.5311  -0.537 0.59144
## Zipcode9     -7.8606     19.2677  -0.408 0.68360
## Zipcode10   -16.8070     16.3271  -1.029 0.30416
## Zipcode11   -14.2515     16.6566  -0.856 0.39293
## Zipcode12   -14.8322     12.3713  -1.199 0.23154
## Zipcode13   -17.3230     12.8140  -1.352 0.17747
## Zipcode14   -14.0094     11.3208  -1.237 0.21691
## Zipcode15   -26.3242     14.0832  -1.869 0.06261 .
## Zipcode16    -9.1743     14.7849  -0.621 0.53541
## Zipcode17   -15.7814     12.0238  -1.313 0.19039
## Zipcode18   -16.1880     12.8378  -1.261 0.20834
## Zipcode19   -11.4882     12.6624  -0.907 0.36502
## Zipcode20   -11.4787     11.4433  -1.003 0.31666
## `V-2`        4.1560      7.5873   0.548 0.58429
## `V-3`       -6.6246      5.9795  -1.108 0.26883
## `V-4`        7.5558      3.7532   2.013 0.04503 *
## `V-5`       150.2443      7.3503  20.441 < 2e-16 ***
## `V-6`       -7.3692      3.2394  -2.275 0.02365 *
## `V-7`       29.0769      1.7009  17.095 < 2e-16 ***
## `V-8`       -5.8754      4.2381  -1.386 0.16672
## `V-11`      -2.1577      3.9016  -0.553 0.58067
## `V-12`      -8.6235     41.5064  -0.208 0.83556
## `V-13`      17.5093     28.9961   0.604 0.54642
## `V-14`       4.0457      3.8376   1.054 0.29267
## `V-15`      63.3510     28.4569   2.226 0.02677 *
## `V-16`      14.3414      8.5742   1.673 0.09549 .
## `V-17`     -82.9451     15.5412  -5.337 1.92e-07 ***
## `V-18`     -11.6103      6.5866  -1.763 0.07901 .
## `V-19`      -4.9097      7.3955  -0.664 0.50730
## `V-20`      -0.8114      3.8823  -0.209 0.83460
## `V-21`      -2.9399     16.5997  -0.177 0.85955
## `V-22`     -55.8548     20.9688  -2.664 0.00816 **
## `V-23`      16.5962      7.3905   2.246 0.02549 *
## `V-24`     -13.1186      8.9559  -1.465 0.14407
## `V-25`      57.5260     78.4623   0.733 0.46405
## `V-26`      16.6635     62.8677   0.265 0.79116
## `V-27`     -11.0637      7.3525  -1.505 0.13348
## `V-28`       8.9552      4.6603   1.922 0.05565 .
## `V-29`      -7.1743     14.1937  -0.505 0.61362
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 27.61 on 288 degrees of freedom
## Multiple R-squared:  0.9729, Adjusted R-squared:  0.9687
## F-statistic: 229.7 on 45 and 288 DF,  p-value: < 2.2e-16

```

```
cor(train.v10[,c(2:28)])
```

| ## | V-2 | V-3 | V-4 | V-5 | V-6 |
|---------|--------------|--------------|--------------|-------------|--------------|
| ## V-2 | 1.000000000 | 0.945600958 | 0.77436762 | 0.23420508 | 0.21230859 |
| ## V-3 | 0.945600958 | 1.000000000 | 0.64019309 | 0.15528248 | 0.12979894 |
| ## V-4 | 0.774367618 | 0.640193087 | 1.000000000 | 0.57121240 | 0.33816723 |
| ## V-5 | 0.234205081 | 0.155282482 | 0.57121240 | 1.000000000 | 0.32722179 |
| ## V-6 | 0.212308594 | 0.129798937 | 0.33816723 | 0.32722179 | 1.000000000 |
| ## V-7 | 0.161547288 | 0.089225497 | 0.18086665 | 0.06782641 | 0.14136645 |
| ## V-8 | 0.226480811 | 0.145503571 | 0.47418223 | 0.80942131 | 0.16406550 |
| ## V-11 | -0.035418005 | -0.013619707 | 0.02290495 | 0.23425775 | -0.06469386 |
| ## V-12 | 0.089149149 | 0.082405943 | 0.32119612 | 0.79164543 | -0.19515942 |
| ## V-13 | 0.088261381 | 0.076359505 | 0.31999660 | 0.79468122 | -0.18162136 |
| ## V-14 | -0.031042870 | -0.007498359 | 0.05373985 | 0.24842339 | -0.06594751 |
| ## V-15 | 0.079502198 | 0.075962603 | 0.30494320 | 0.77237472 | -0.20802750 |
| ## V-16 | 0.092661957 | 0.094008848 | 0.29144067 | 0.70758556 | -0.17878957 |
| ## V-17 | 0.092216627 | 0.086045671 | 0.31811051 | 0.78139809 | -0.18702009 |
| ## V-18 | 0.067722258 | 0.051402223 | 0.20398832 | 0.48986363 | -0.05370173 |
| ## V-19 | 0.063634669 | 0.061394585 | 0.25013127 | 0.64261538 | -0.16845274 |
| ## V-20 | -0.007826318 | -0.030715653 | -0.04911039 | -0.21740676 | 0.11616290 |
| ## V-21 | 0.083525605 | 0.073809085 | 0.31314787 | 0.78345004 | -0.20180050 |
| ## V-22 | 0.100604965 | 0.092276694 | 0.32827391 | 0.78788394 | -0.19693094 |
| ## V-23 | 0.094428570 | 0.062129772 | 0.31781905 | 0.72055691 | -0.16593281 |
| ## V-24 | 0.082614838 | 0.062240681 | 0.26826007 | 0.64481091 | -0.08200588 |
| ## V-25 | 0.089286179 | 0.073363554 | 0.32671357 | 0.79833830 | -0.18004635 |
| ## V-26 | 0.090209687 | 0.074963521 | 0.32844952 | 0.79873355 | -0.18638055 |
| ## V-27 | 0.098501142 | 0.066699364 | 0.32827781 | 0.72016802 | -0.14959341 |
| ## V-28 | 0.081782289 | 0.065819345 | 0.15407731 | 0.30938116 | -0.01506138 |
| ## V-29 | 0.079099698 | 0.074670140 | 0.30292846 | 0.78219642 | -0.19173899 |
| ## V-10 | 0.263265794 | 0.166628000 | 0.59551162 | 0.96061711 | 0.31582150 |
| ## | V-7 | V-8 | V-11 | V-12 | V-13 |
| ## V-2 | 0.161547288 | 0.22648081 | -0.035418005 | 0.08914915 | 0.088261381 |
| ## V-3 | 0.089225497 | 0.14550357 | -0.013619707 | 0.08240594 | 0.076359505 |
| ## V-4 | 0.180866645 | 0.47418223 | 0.022904947 | 0.32119612 | 0.319996595 |
| ## V-5 | 0.067826410 | 0.80942131 | 0.234257753 | 0.79164543 | 0.794681216 |
| ## V-6 | 0.141366451 | 0.16406550 | -0.064693859 | -0.19515942 | -0.181621357 |
| ## V-7 | 1.000000000 | 0.01776631 | 0.002002689 | -0.01102056 | 0.001928748 |
| ## V-8 | 0.017766307 | 1.000000000 | 0.214791473 | 0.62970430 | 0.634816454 |
| ## V-11 | 0.002002689 | 0.21479147 | 1.000000000 | 0.31244811 | 0.344567028 |
| ## V-12 | -0.011020564 | 0.62970430 | 0.312448115 | 1.000000000 | 0.990115542 |
| ## V-13 | 0.001928748 | 0.63481645 | 0.344567028 | 0.99011554 | 1.000000000 |
| ## V-14 | -0.019721226 | 0.24596566 | 0.860365531 | 0.31564739 | 0.340203213 |
| ## V-15 | -0.024051443 | 0.61691478 | 0.332852738 | 0.98696187 | 0.965649585 |
| ## V-16 | -0.001528973 | 0.54631418 | 0.413873083 | 0.91047002 | 0.911852344 |
| ## V-17 | -0.007634694 | 0.61852139 | 0.360611448 | 0.98089806 | 0.976602879 |
| ## V-18 | 0.103500897 | 0.41133991 | 0.234032892 | 0.51878542 | 0.526198919 |
| ## V-19 | -0.006441351 | 0.54873449 | 0.299067350 | 0.80590755 | 0.775279122 |
| ## V-20 | 0.074979304 | -0.13666349 | -0.264273120 | -0.35712077 | -0.289603798 |
| ## V-21 | -0.001781932 | 0.61813693 | 0.327402884 | 0.99252339 | 0.983217541 |
| ## V-22 | 0.005911640 | 0.61471306 | 0.307851986 | 0.99291719 | 0.980110935 |
| ## V-23 | 0.046973086 | 0.56744724 | 0.111823359 | 0.85524646 | 0.868914803 |
| ## V-24 | 0.066728819 | 0.51811642 | 0.409866559 | 0.74751228 | 0.810329992 |
| ## V-25 | 0.017701519 | 0.63912703 | 0.346748048 | 0.98283160 | 0.993948015 |
| ## V-26 | 0.012712520 | 0.64038848 | 0.328935009 | 0.98773368 | 0.992846711 |

| | | | | | | |
|----|------|--------------|--------------|--------------|--------------|-------------|
| ## | V-27 | 0.041148951 | 0.58009504 | 0.101545061 | 0.83897307 | 0.859104077 |
| ## | V-28 | 0.097650836 | 0.27813186 | 0.104124516 | 0.29277178 | 0.286868723 |
| ## | V-29 | -0.020623125 | 0.63038431 | 0.302106965 | 0.98201195 | 0.970009704 |
| ## | V-10 | 0.246356641 | 0.77602067 | 0.216265318 | 0.75362621 | 0.758385544 |
| ## | | V-14 | V-15 | V-16 | V-17 | V-18 |
| ## | V-2 | -0.031042870 | 0.07950220 | 0.092661957 | 0.092216627 | 0.06772226 |
| ## | V-3 | -0.007498359 | 0.07596260 | 0.094008848 | 0.086045671 | 0.05140222 |
| ## | V-4 | 0.053739850 | 0.30494320 | 0.291440666 | 0.318110514 | 0.20398832 |
| ## | V-5 | 0.248423394 | 0.77237472 | 0.707585561 | 0.781398086 | 0.48986363 |
| ## | V-6 | -0.065947512 | -0.20802750 | -0.178789572 | -0.187020090 | -0.05370173 |
| ## | V-7 | -0.019721226 | -0.02405144 | -0.001528973 | -0.007634694 | 0.10350090 |
| ## | V-8 | 0.245965661 | 0.61691478 | 0.546314176 | 0.618521388 | 0.41133991 |
| ## | V-11 | 0.860365531 | 0.33285274 | 0.413873083 | 0.360611448 | 0.23403289 |
| ## | V-12 | 0.315647390 | 0.98696187 | 0.910470016 | 0.980898057 | 0.51878542 |
| ## | V-13 | 0.340203213 | 0.96564959 | 0.911852344 | 0.976602879 | 0.52619892 |
| ## | V-14 | 1.000000000 | 0.32141733 | 0.429650641 | 0.377683833 | 0.22975516 |
| ## | V-15 | 0.321417327 | 1.000000000 | 0.891777513 | 0.965041224 | 0.53798776 |
| ## | V-16 | 0.429650641 | 0.89177751 | 1.000000000 | 0.945888259 | 0.47463555 |
| ## | V-17 | 0.377683833 | 0.96504122 | 0.945888259 | 1.000000000 | 0.51550667 |
| ## | V-18 | 0.229755159 | 0.53798776 | 0.474635548 | 0.515506674 | 1.00000000 |
| ## | V-19 | 0.280428299 | 0.85592540 | 0.710762676 | 0.763396891 | 0.76005321 |
| ## | V-20 | -0.223180633 | -0.42477138 | -0.460695728 | -0.421048499 | -0.04807152 |
| ## | V-21 | 0.314238352 | 0.98479930 | 0.905593128 | 0.970529084 | 0.52651551 |
| ## | V-22 | 0.308650562 | 0.98188751 | 0.922203466 | 0.977496291 | 0.54096321 |
| ## | V-23 | 0.094598910 | 0.83560127 | 0.752719249 | 0.849345735 | 0.47191261 |
| ## | V-24 | 0.385324013 | 0.67979203 | 0.660607493 | 0.721302456 | 0.51287317 |
| ## | V-25 | 0.337258655 | 0.95920948 | 0.886957004 | 0.963501199 | 0.55244157 |
| ## | V-26 | 0.321973307 | 0.96848328 | 0.892081494 | 0.969094040 | 0.54969275 |
| ## | V-27 | 0.139606014 | 0.79419440 | 0.681317005 | 0.818461854 | 0.39502159 |
| ## | V-28 | 0.169608370 | 0.30630060 | 0.229200249 | 0.291059956 | 0.86463576 |
| ## | V-29 | 0.299937377 | 0.98315243 | 0.866570249 | 0.946223759 | 0.53018537 |
| ## | V-10 | 0.217431999 | 0.74070323 | 0.657945916 | 0.731985430 | 0.47370439 |
| ## | | V-19 | V-20 | V-21 | V-22 | V-23 |
| ## | V-2 | 0.063634669 | -0.007826318 | 0.083525605 | 0.10060497 | 0.09442857 |
| ## | V-3 | 0.061394585 | -0.030715653 | 0.073809085 | 0.09227669 | 0.06212977 |
| ## | V-4 | 0.250131268 | -0.049110392 | 0.313147874 | 0.32827391 | 0.31781905 |
| ## | V-5 | 0.642615376 | -0.217406759 | 0.783450035 | 0.78788394 | 0.72055691 |
| ## | V-6 | -0.168452740 | 0.116162896 | -0.201800496 | -0.19693094 | -0.16593281 |
| ## | V-7 | -0.006441351 | 0.074979304 | -0.001781932 | 0.00591164 | 0.04697309 |
| ## | V-8 | 0.548734491 | -0.136663489 | 0.618136933 | 0.61471306 | 0.56744724 |
| ## | V-11 | 0.299067350 | -0.264273120 | 0.327402884 | 0.30785199 | 0.11182336 |
| ## | V-12 | 0.805907545 | -0.357120769 | 0.992523387 | 0.99291719 | 0.85524646 |
| ## | V-13 | 0.775279122 | -0.289603798 | 0.983217541 | 0.98011094 | 0.86891480 |
| ## | V-14 | 0.280428299 | -0.223180633 | 0.314238352 | 0.30865056 | 0.09459891 |
| ## | V-15 | 0.855925405 | -0.424771384 | 0.984799301 | 0.98188751 | 0.83560127 |
| ## | V-16 | 0.710762676 | -0.460695728 | 0.905593128 | 0.92220347 | 0.75271925 |
| ## | V-17 | 0.763396891 | -0.421048499 | 0.970529084 | 0.97749629 | 0.84934574 |
| ## | V-18 | 0.760053214 | -0.048071518 | 0.526515511 | 0.54096321 | 0.47191261 |
| ## | V-19 | 1.000000000 | -0.277789904 | 0.817092309 | 0.81052043 | 0.63333981 |
| ## | V-20 | -0.277789904 | 1.000000000 | -0.359643069 | -0.36626055 | -0.22614493 |
| ## | V-21 | 0.817092309 | -0.359643069 | 1.000000000 | 0.99053656 | 0.84433800 |
| ## | V-22 | 0.810520432 | -0.366260547 | 0.990536564 | 1.00000000 | 0.84869783 |
| ## | V-23 | 0.633339813 | -0.226144932 | 0.844337998 | 0.84869783 | 1.00000000 |
| ## | V-24 | 0.531494188 | 0.097835932 | 0.745168073 | 0.73102304 | 0.65975292 |

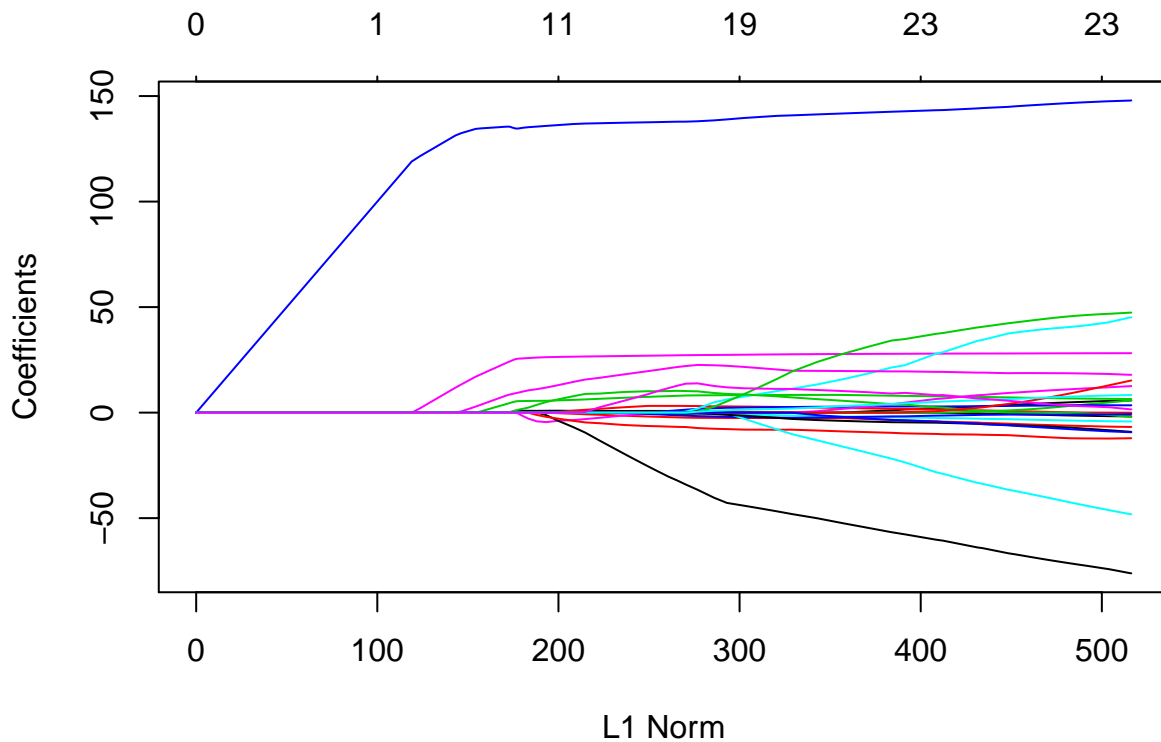
| | | | | | | |
|----|------|-------------|--------------|-------------|-------------|-------------|
| ## | V-25 | 0.781298186 | -0.248323465 | 0.977863958 | 0.97321585 | 0.88823633 |
| ## | V-26 | 0.792637630 | -0.283334553 | 0.981947612 | 0.97801582 | 0.89700001 |
| ## | V-27 | 0.570548168 | -0.069144581 | 0.824139284 | 0.81998426 | 0.91703848 |
| ## | V-28 | 0.561385894 | 0.037568332 | 0.296720859 | 0.31415987 | 0.25026572 |
| ## | V-29 | 0.828660567 | -0.330418745 | 0.975786332 | 0.97155143 | 0.83140014 |
| ## | V-10 | 0.625177036 | -0.188652528 | 0.748987995 | 0.74845738 | 0.72261514 |
| ## | | V-24 | V-25 | V-26 | V-27 | V-28 |
| ## | V-2 | 0.08261484 | 0.08928618 | 0.09020969 | 0.09850114 | 0.08178229 |
| ## | V-3 | 0.06224068 | 0.07336355 | 0.07496352 | 0.06669936 | 0.06581934 |
| ## | V-4 | 0.26826007 | 0.32671357 | 0.32844952 | 0.32827781 | 0.15407731 |
| ## | V-5 | 0.64481091 | 0.79833830 | 0.79873355 | 0.72016802 | 0.30938116 |
| ## | V-6 | -0.08200588 | -0.18004635 | -0.18638055 | -0.14959341 | -0.01506138 |
| ## | V-7 | 0.06672882 | 0.01770152 | 0.01271252 | 0.04114895 | 0.09765084 |
| ## | V-8 | 0.51811642 | 0.63912703 | 0.64038848 | 0.58009504 | 0.27813186 |
| ## | V-11 | 0.40986656 | 0.34674805 | 0.32893501 | 0.10154506 | 0.10412452 |
| ## | V-12 | 0.74751228 | 0.98283160 | 0.98773368 | 0.83897307 | 0.29277178 |
| ## | V-13 | 0.81032999 | 0.99394802 | 0.99284671 | 0.85910408 | 0.28686872 |
| ## | V-14 | 0.38532401 | 0.33725865 | 0.32197331 | 0.13960601 | 0.16960837 |
| ## | V-15 | 0.67979203 | 0.95920948 | 0.96848328 | 0.79419440 | 0.30630060 |
| ## | V-16 | 0.66060749 | 0.88695700 | 0.89208149 | 0.68131701 | 0.22920025 |
| ## | V-17 | 0.72130246 | 0.96350120 | 0.96909404 | 0.81846185 | 0.29105996 |
| ## | V-18 | 0.51287317 | 0.55244157 | 0.54969275 | 0.39502159 | 0.86463576 |
| ## | V-19 | 0.53149419 | 0.78129819 | 0.79263763 | 0.57054817 | 0.56138589 |
| ## | V-20 | 0.09783593 | -0.24832347 | -0.28333455 | -0.06914458 | 0.03756833 |
| ## | V-21 | 0.74516807 | 0.97786396 | 0.98194761 | 0.82413928 | 0.29672086 |
| ## | V-22 | 0.73102304 | 0.97321585 | 0.97801582 | 0.81998426 | 0.31415987 |
| ## | V-23 | 0.65975292 | 0.88823633 | 0.89700001 | 0.91703848 | 0.25026572 |
| ## | V-24 | 1.00000000 | 0.83419437 | 0.80279114 | 0.70242848 | 0.25925649 |
| ## | V-25 | 0.83419437 | 1.00000000 | 0.99785756 | 0.87754156 | 0.30716315 |
| ## | V-26 | 0.80279114 | 0.99785756 | 1.00000000 | 0.88162945 | 0.31251731 |
| ## | V-27 | 0.70242848 | 0.87754156 | 0.88162945 | 1.00000000 | 0.25408508 |
| ## | V-28 | 0.25925649 | 0.30716315 | 0.31251731 | 0.25408508 | 1.00000000 |
| ## | V-29 | 0.73163217 | 0.96492985 | 0.96786639 | 0.80227328 | 0.29412577 |
| ## | V-10 | 0.61612424 | 0.76984469 | 0.77157245 | 0.71050664 | 0.30221239 |
| ## | | V-29 | V-10 | | | |
| ## | V-2 | 0.07909970 | 0.2632658 | | | |
| ## | V-3 | 0.07467014 | 0.1666280 | | | |
| ## | V-4 | 0.30292846 | 0.5955116 | | | |
| ## | V-5 | 0.78219642 | 0.9606171 | | | |
| ## | V-6 | -0.19173899 | 0.3158215 | | | |
| ## | V-7 | -0.02062312 | 0.2463566 | | | |
| ## | V-8 | 0.63038431 | 0.7760207 | | | |
| ## | V-11 | 0.30210697 | 0.2162653 | | | |
| ## | V-12 | 0.98201195 | 0.7536262 | | | |
| ## | V-13 | 0.97000970 | 0.7583855 | | | |
| ## | V-14 | 0.29993738 | 0.2174320 | | | |
| ## | V-15 | 0.98315243 | 0.7407032 | | | |
| ## | V-16 | 0.86657025 | 0.6579459 | | | |
| ## | V-17 | 0.94622376 | 0.7319854 | | | |
| ## | V-18 | 0.53018537 | 0.4737044 | | | |
| ## | V-19 | 0.82866057 | 0.6251770 | | | |
| ## | V-20 | -0.33041874 | -0.1886525 | | | |
| ## | V-21 | 0.97578633 | 0.7489880 | | | |
| ## | V-22 | 0.97155143 | 0.7484574 | | | |

```
## V-23 0.83140014 0.7226151
## V-24 0.73163217 0.6161242
## V-25 0.96492985 0.7698447
## V-26 0.96786639 0.7715725
## V-27 0.80227328 0.7105066
## V-28 0.29412577 0.3022124
## V-29 1.00000000 0.7513661
## V-10 0.75136612 1.0000000
```

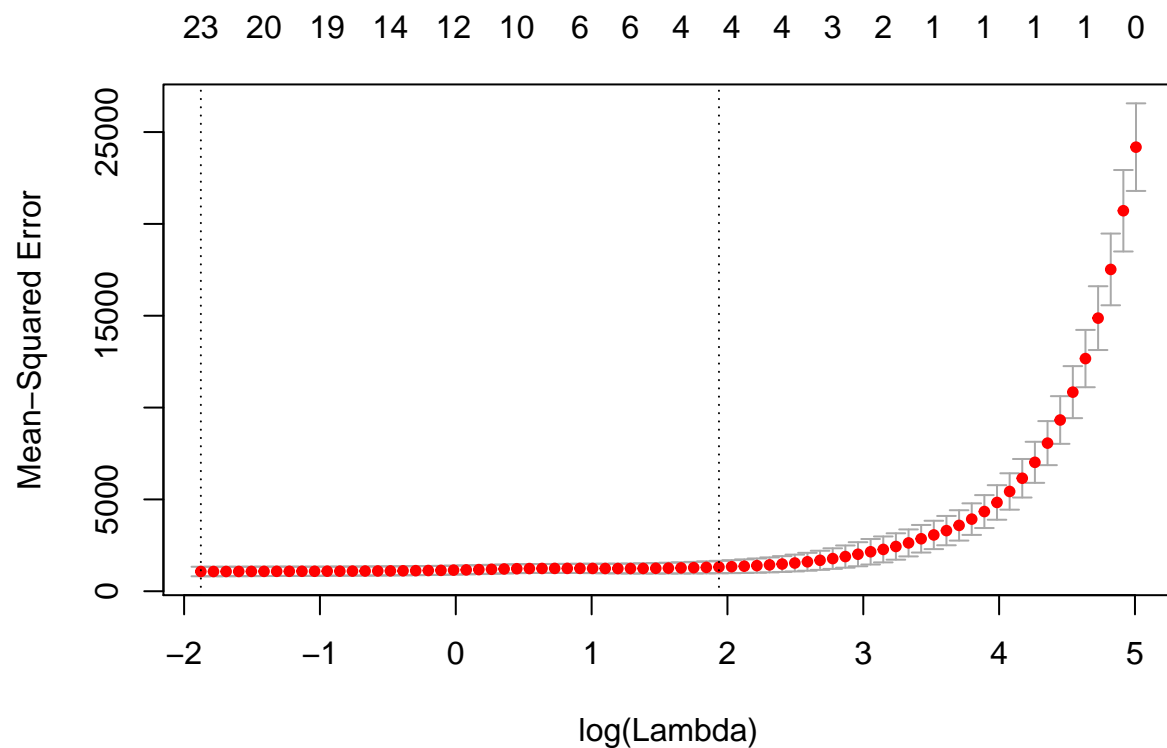
```
# Lasso to determine variable
library("glmnet")
```

```
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-16
```

```
x.simple=as.matrix(train.v10[,2:27])
y=train.v10$`V-10`
fitlasso=glmnet(x.simple,y,alpha = 1)
plot(fitlasso)
```



```
cv.lasso=cv.glmnet(x.simple,y)
plot(cv.lasso)
```



```
coef(cv.lasso)
```

```
## 27 x 1 sparse Matrix of class "dgCMatrix"
##              1
## (Intercept) 226.392216
## V-2         .
## V-3         .
## V-4         2.749670
## V-5        135.175905
## V-6         .
## V-7        21.494386
## V-8         .
## V-11        .
## V-12        .
## V-13        .
## V-14        .
## V-15        .
## V-16        .
## V-17        .
## V-18        .
## V-19        .
## V-20        .
## V-21        .
## V-22        .
## V-23        6.441003
## V-24        .
## V-25        .
## V-26        .
## V-27        .
## V-28        .
## V-29        .
```

```

# Model 3
# added variable factor to determine ^
datamodel3=data.frame(train.v10[,c(4,5,7,21,28)])
fitmodel3=lm(datamodel3$V.10~.,data = datamodel3)
colData3 <- list("`V-4`", "`V-5`", "`V-7`", "`V-23`")
names(colData3) <- c("`V-4`", "`V-5`", "`V-7`", "`V-23`")
removeXList <- colData3

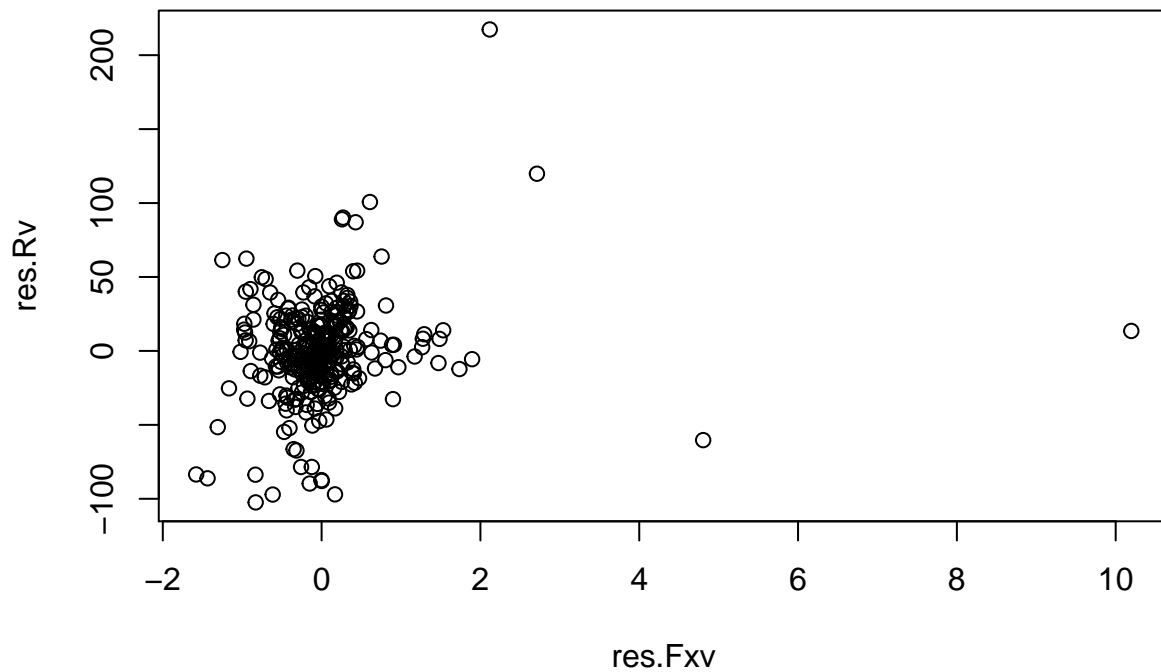
for (rmX in removeXList){
  tmpV <- colData3
  tmpV[[rmX]] = NULL
  test.Rv=lm(as.formula(paste("`V-10` ~", paste(tmpV, collapse = "+"))), data = train.v10)
  res.Rv= test.Rv$residuals

  test.Fxv=lm(as.formula(paste(paste(rmX," ~"), paste(tmpV, collapse = "+"))), data = train.v10)
  res.Fxv= test.Fxv$residuals

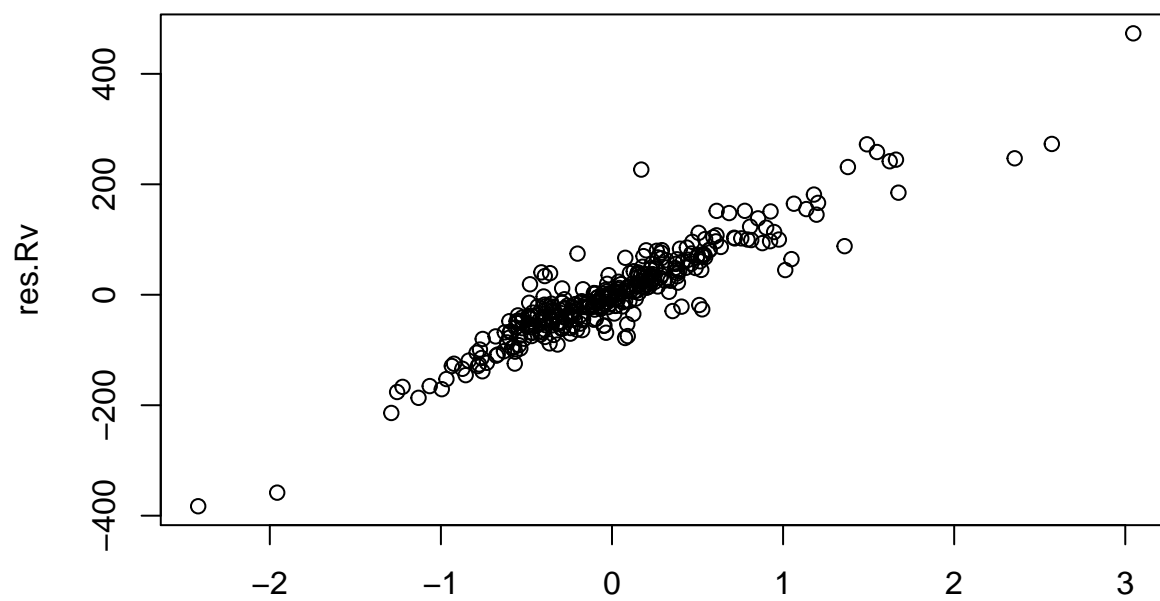
  plot(res.Fxv,res.Rv,main = rmX)
}

```

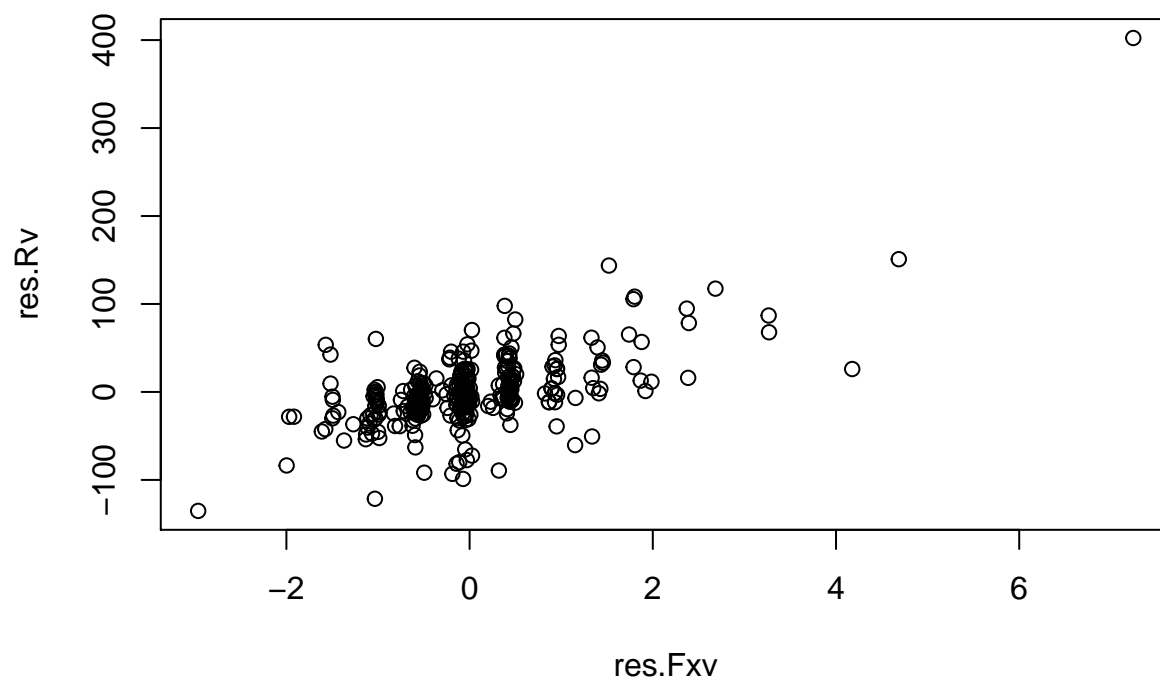
'V-4'

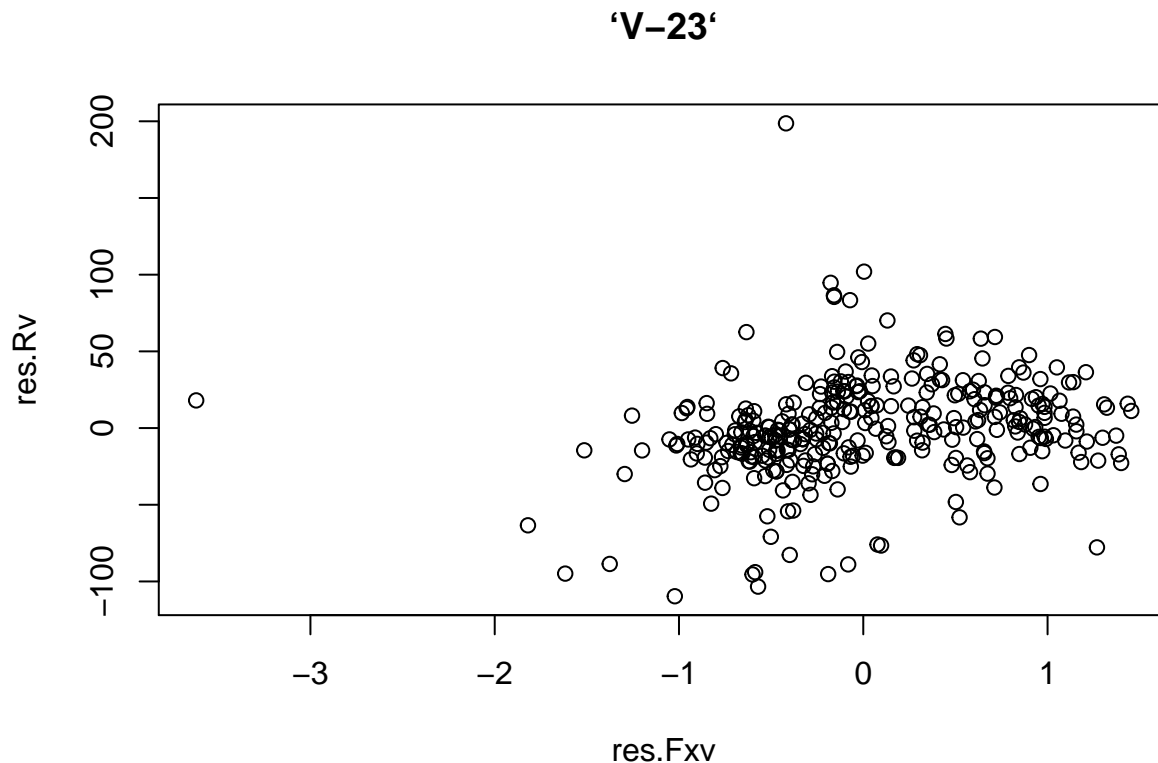


‘V-5’



res.Fxv
‘V-7’





```
summary(fitmodel3)$r.squared
```

```
## [1] 0.9588816
```

```
summary(fitmodel3)$adj.r.squared
```

```
## [1] 0.9583816
```

#Brown test whether constant variance and transformation for Model 3

```
resmodel3=fitmodel3$residuals
```

```
mmodel3=mean(datamodel3$V.10)
```

```
nmodel3=dim(datamodel3)[1]
```

```
p1=5
```

#1. Break the residuals into two groups.

```
Group1 <- resmodel3[datamodel3$V.10<mmodel3]
```

```
Group2 <-resmodel3[datamodel3$V.10>=mmodel3]
```

#2. Obtain the median of each group, using the commands:

```
M1 <- median(Group1)
```

```
M2 <- median(Group2)
```

#3. Obtain the mean absolute deviation for each group, using the commands:

```
D1 <- sum( abs( Group1 - M1 )) / length(Group1)
```

```
D2 <- sum( abs( Group2 - M2 )) / length(Group2)
```

#4. Calculate the pooled standard error, using the command:

```
s <- sqrt( ( sum( ( abs(Group1 - M1) - D1 )^2 ) + sum( ( abs(Group2 - M2) - D2 )^2 ) ) / (nmodel3-2) )
```

#5. Finally, calculate the Brown-Forsythe test statistic, using the command:

```
t <- ( D1 - D2 ) / ( s * sqrt( 1/length(Group1) + 1/length(Group2) ) )
```

```
t
```

```
## [1] -2.798773
```

#6 Once you obtain this value, you can compare it to the critical value for any given alpha level to decide if you can reject the null hypothesis or you can find its P-value.

```
alpha <- 0.05
```

```
qt(1-alpha/2, nmodel3-p1-1) # find the critical value
```

```
## [1] 1.967223
```

Weighted transformation for model 3

```
wts <- 1/fitted(lm(abs(residuals(fitmodel3)) ~ ., data = datamodel3))^2
```

```
fitmodel3weight <- lm(datamodel3$V.10 ~ ., data = datamodel3, weights=wts)
```

```
datamodel3weight=cbind(datamodel3[1:4], datamodel3$V.10*wts)
```

```
summary(fitmodel3weight)$r.squared
```

```
## [1] 0.9615326
```

```
summary(fitmodel3weight)$adj.r.squared
```

```
## [1] 0.961065
```

#Brown test whether constant variance and transformation for Model 3 after transformation

```
resmodel3b=fitmodel3weight$residuals
```

```
mmodel3=mean(datamodel3weight$`datamodel3$V.10 * wts`)
```

```
nmodel3=dim(datamodel3weight)[1]
```

#1. Break the residuals into two groups.

```
Group1 <- resmodel3b[datamodel3weight$`datamodel3$V.10 * wts`<mmodel3]
```

```
Group2 <- resmodel3b[datamodel3weight$`datamodel3$V.10 * wts`>=mmodel3]
```

#2. Obtain the median of each group, using the commands:

```
M1 <- median(Group1)
```

```
M2 <- median(Group2)
```

#3. Obtain the mean absolute deviation for each group, using the commands:

```
D1 <- sum( abs( Group1 - M1 )) / length(Group1)
```

```
D2 <- sum( abs( Group2 - M2 )) / length(Group2)
```

#4. Calculate the pooled standard error, using the command:

```
s <- sqrt( ( sum( ( abs(Group1 - M1) - D1 )^2 ) + sum( ( abs(Group2 - M2) - D2 )^2 ) ) / (nmodel3-2) )
```

#5. Finally, calculate the Brown-Forsythe test statistic, using the command:

```
t <- ( D1 - D2 ) / ( s * sqrt( 1/length(Group1) + 1/length(Group2) ) )
```

```
t
```

```
## [1] 0.3504877
```

#6 Once you obtain this value, you can compare it to the critical value for any given alpha level to decide if you can reject the null hypothesis or you can find its P-value.

```
alpha <- 0.05
```

```
qt(1-alpha/2, nmodel3-p1-1) # find the critical value
```

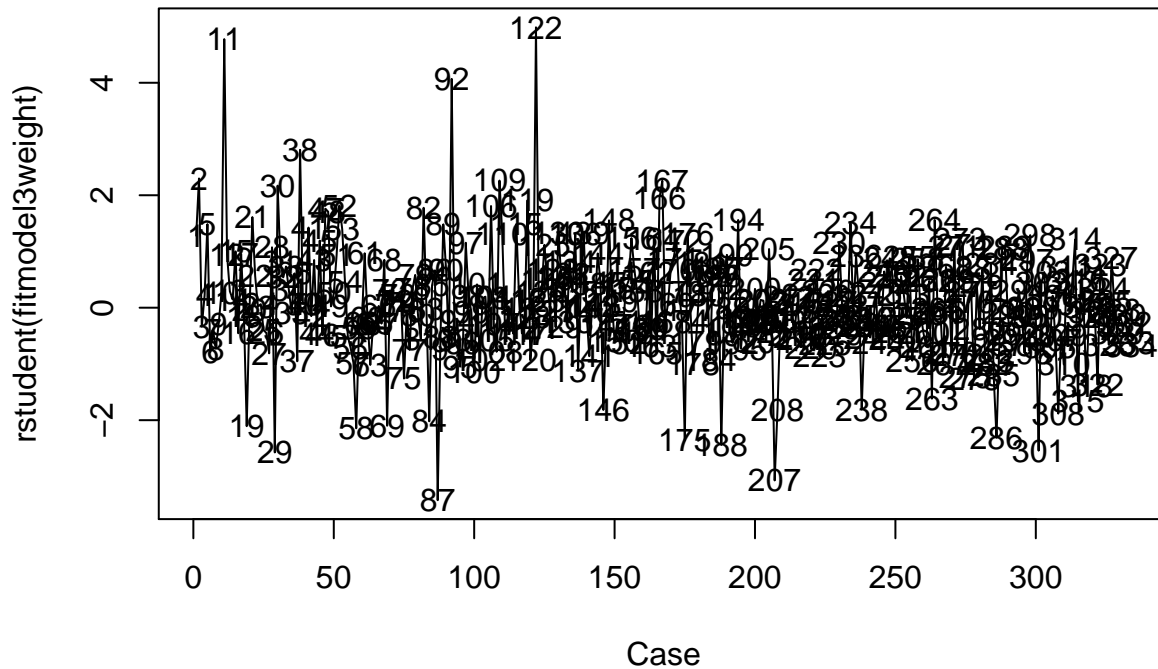
```
## [1] 1.967223
```

And the P-value can be found by typing:

```
2*(1-pt( abs(t), nmodel3-p1-1))
```

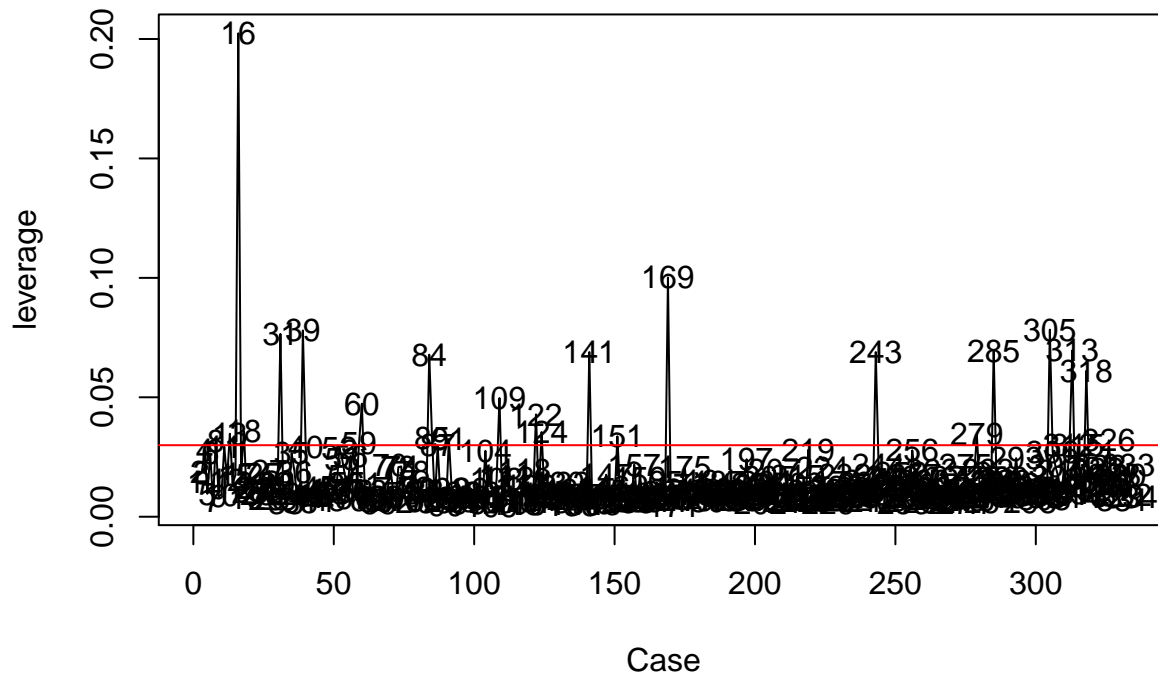
```
## [1] 0.7261977
```

```
#y outlier for model3
Case <- c(1:nmodel3)
plot(Case, rstudent(fitmodel3weight), type="l")
text(Case, rstudent(fitmodel3weight), Case)
```



```
alpha <- 0.05
crit <- qt(1-alpha/2/nmodel3, nmodel3-p1-1)
youtlier3=which(abs(rstudent(fitmodel3weight)) >=crit )
```

```
#x outlier for model3
X <- as.matrix(cbind(rep(1,nmodel3), datamodel3[1:4]))
H <- X%*%solve(t(X)%*%X, tol=1e-20)%*%t(X)
leverage <- hatvalues(fitmodel3weight)
plot(Case, leverage, type="l")
text(Case, leverage, Case)
abline(h=2*p1/nmodel3, col=2)
```



```
xoutlier1=data.frame(which(leverage>2*p1/nmodel3) )
xoutlier1
```

```
##      which.leverage...2...p1.nmodel3.
## 8                                     8
## 13                                    13
## 16                                    16
## 18                                    18
## 31                                    31
## 39                                    39
## 59                                    59
## 60                                    60
## 84                                    84
## 85                                    85
## 87                                    87
## 91                                    91
## 109                                  109
## 122                                  122
## 124                                  124
## 141                                  141
## 151                                  151
## 169                                  169
## 243                                  243
## 279                                  279
## 285                                  285
## 305                                  305
## 312                                  312
## 313                                  313
## 315                                  315
## 318                                  318
## 326                                  326
```

```

#test whether outlier in the extend of the model3
IM3=influence.measures(fitmodel3weight)
dxoutlier3=union(which(IM3$infmat[,8]>0.2),which(IM3$infmat[,6]>2*sqrt(p1/nmodel3)))
#combine x and y outlier
finaloutlier3=union(dxoutlier3,youtlier3)
datamodel3Final=datamodel3[-c(finaloutlier3),]
# get model1 without x y outlier
fitmodel3x1=lm(datamodel3Final$V.10~.,data = datamodel3Final)
wtsx3 <- 1/fitted(lm(abs(residuals(fitmodel3x1)) ~ ., data = datamodel3Final))^2
Fmodel3=lm(datamodel3Final$V.10~., data = datamodel3Final,weights =wtsx3)
# R2 & adj R2 for model3 test
summary(Fmodel3)$r.squared

```

```
## [1] 0.9768281
```

```
summary(Fmodel3)$adj.r.squared
```

```
## [1] 0.9765403
```

```

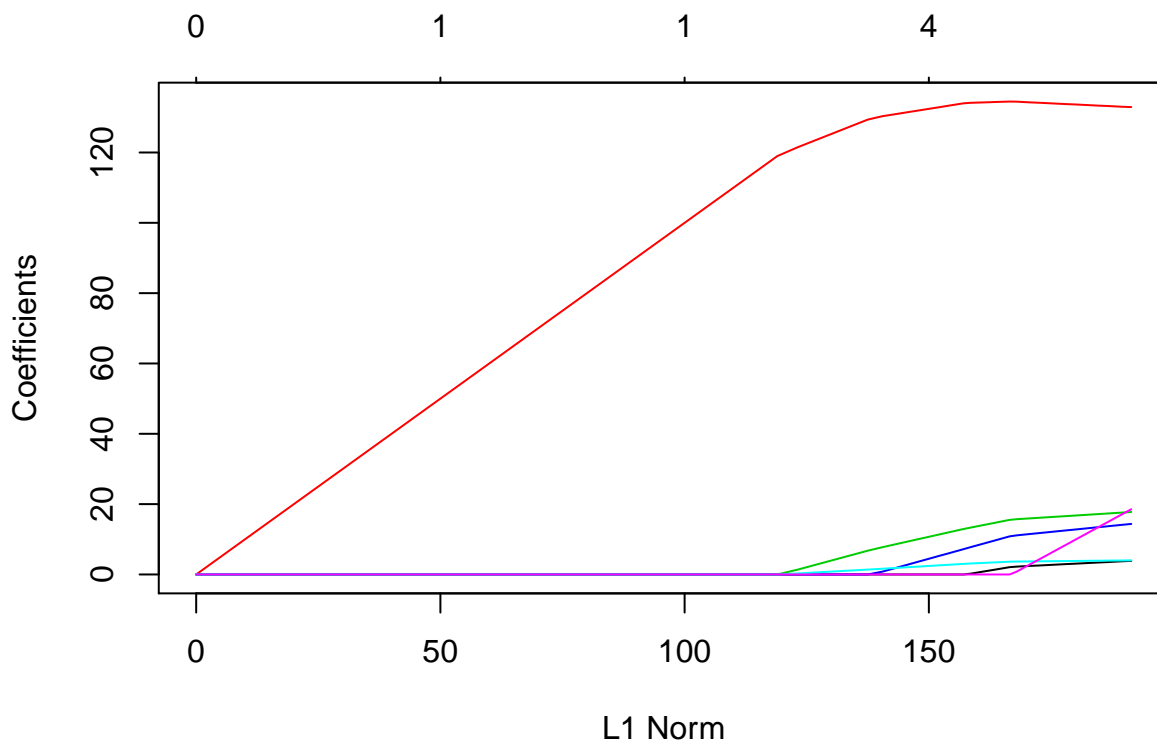
# add ~2 for model4
Data.new3 <- cbind(train.v10$`V-4`, train.v10$`V-5`, train.v10$`V-7`, train.v10$`V-23`)
x3.new=as.matrix(cbind(Data.new3,((Data.new3)^2)[,-2]))
colnames(x3.new)=c("V-4","V-5","V-7","V-23","V-4.2","V-7.2","V-23.2")

```

```

#lasso test x~2
library("glmnet")
fitlasso.x3add=glmnet(x3.new,y,alpha = 1)
plot(fitlasso.x3add)

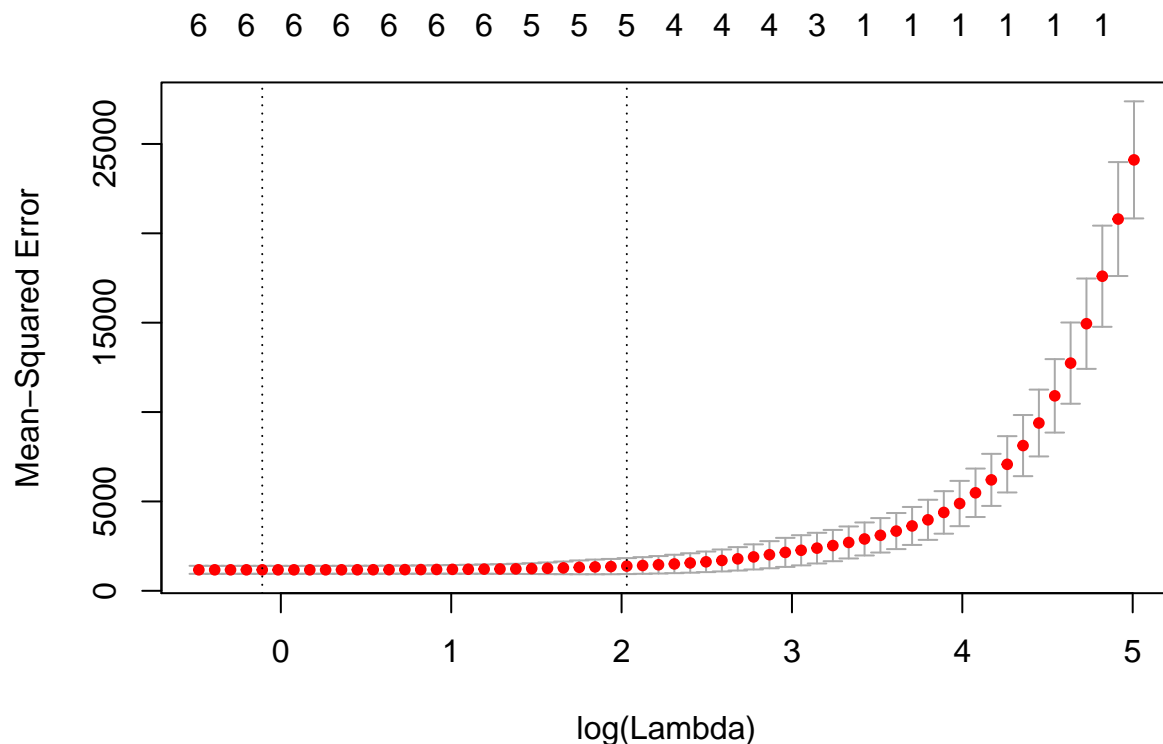
```



```

cv.lasso.x3add=cv.glmnet(x3.new,y)
plot(cv.lasso.x3add)

```



```
coef(cv.lasso.x3add)
```

```
## 8 x 1 sparse Matrix of class "dgCMatrix"
```

```
##              1
## (Intercept) 223.2886614
## V-4         0.2221622
## V-5        134.1264851
## V-7        13.3285514
## V-23        7.7699144
## V-4.2       .
## V-7.2       3.1128741
## V-23.2     .
```

```
# Model 4
```

```
trainv14 = data.frame(x3.new,y)
datamodel4=data.frame(trainv14[,c(2,8)])
fitmodel4=lm(datamodel4$y~.,data = datamodel4)
summary(fitmodel4)$r.squared
```

```
## [1] 0.9227852
```

```
summary(fitmodel4)$adj.r.squared
```

```
## [1] 0.9225527
```

```
#Brown test whether constant variance and transformation for Model 4
```

```
fitmodel4=lm(datamodel4$y~.,data = datamodel4)
resmodel4=fitmodel4$residuals
mmodel4=mean(datamodel4$y)
nmodel4=dim(datamodel4)[1]
```

```
#1. Break the residuals into two groups.
```

```
Group3 <- resmodel4[datamodel4$y<mmodel4]
Group4 <-resmodel4[datamodel4$y>=mmodel4]
```

```

#2. Obtain the median of each group, using the commands:
M3 <- median(Group3)
M4 <- median(Group4)

#3. Obtain the mean absolute deviation for each group, using the commands:
D3 <- sum( abs( Group3 - M3 )) / length(Group3)
D4 <- sum( abs( Group4 - M4 )) / length(Group4)

#4. Calculate the pooled standard error, using the command:
s <- sqrt( ( sum( ( abs(Group3 - M3) - D3 )^2 ) + sum( ( abs(Group4 - M4) - D4 )^2 ) ) / (nmodel4-2) )

#5. Finally, calculate the Brown-Forsythe test statistic, using the command:
t <- ( D3 - D4 ) / ( s * sqrt( 1/length(Group3) + 1/length(Group4) ) )
t

## [1] -5.216066

#6 Once you obtain this value, you can compare it to the critical value for any given alpha level to de
# or you can find its P-value.
alpha <- 0.05
qt(1-alpha/2, nmodel4-p1-1) # find the catical value

## [1] 1.967223

# And the P-value can be found by typing:
2*(1-pt( abs(t), nmodel4-p1-1))

## [1] 3.244961e-07

# Weighted transformation for model 4
wts <- 1/fitted(lm(abs(residuals(fitmodel4)) ~ ., data = datamodel4))^2

fitmodel4weight <- lm(datamodel4$y~ .,data = datamodel4, weights=wts)
datamodel4weight=cbind(datamodel4[1],datamodel4$y*wts)
summary(fitmodel4weight)$r.squared

## [1] 0.8608815

summary(fitmodel4weight)$adj.r.squared

## [1] 0.8604625

#Brown test whether constant variance and transformation for Model 2 after transformation
resmode22b=fitmodel4weight$residuals
mmodel4=mean(datamodel4weight$`datamodel4$y * wts`)
nmodel4=dim(datamodel4weight)[1]

#1. Break the residuals into two groups.
Group6 <- resmode22b[datamodel4weight$`datamodel4$y * wts`<mmodel4]
Group7 <- resmode22b[datamodel4weight$`datamodel4$y * wts`>=mmodel4]

#2. Obtain the median of each group, using the commands:
M1 <- median(Group6)
M2 <- median(Group7)

#3. Obtain the mean absolute deviation for each group, using the commands:
D1 <- sum( abs( Group6 - M1 )) / length(Group6)
D2 <- sum( abs( Group7 - M2 )) / length(Group7)

```



```
#4. Calculate the pooled standard error, using the command:
s <- sqrt( ( sum( ( abs(Group6 - M1) - D1 )^2 ) + sum( ( abs(Group7 - M2) - D2 )^2 ) ) / (nmodel4-2) )

#5. Finally, calculate the Brown-Forsythe test statistic, using the command:
t <- ( D1 - D2 ) / ( s * sqrt( 1/length(Group6) + 1/length(Group7) ) )
t
```

```
## [1] 1.5684
```

#6 Once you obtain this value, you can compare it to the critical value for any given alpha level to determine if there is a significant difference between the two groups or you can find its P-value.

```
alpha <- 0.05
qt(1-alpha/2, nmodel4-5) # find the critical value
```

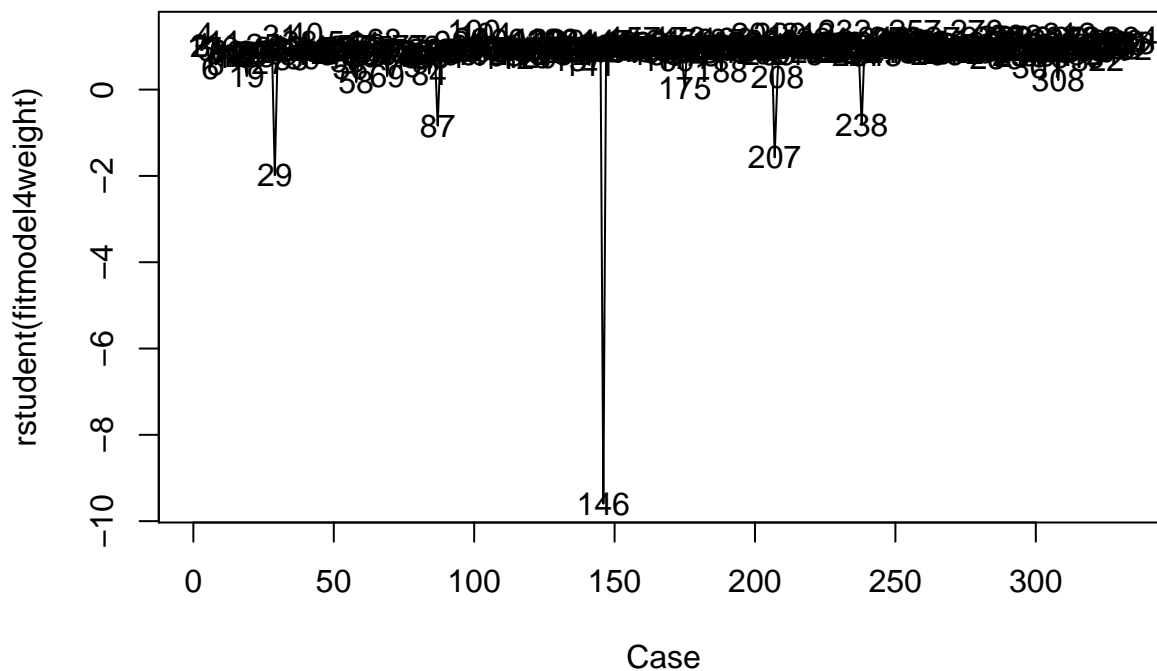
```
## [1] 1.967201
```

And the P-value can be found by typing:

```
2*(1-pt( abs(t), nmodel4-5))
```

```
## [1] 0.1177491
```

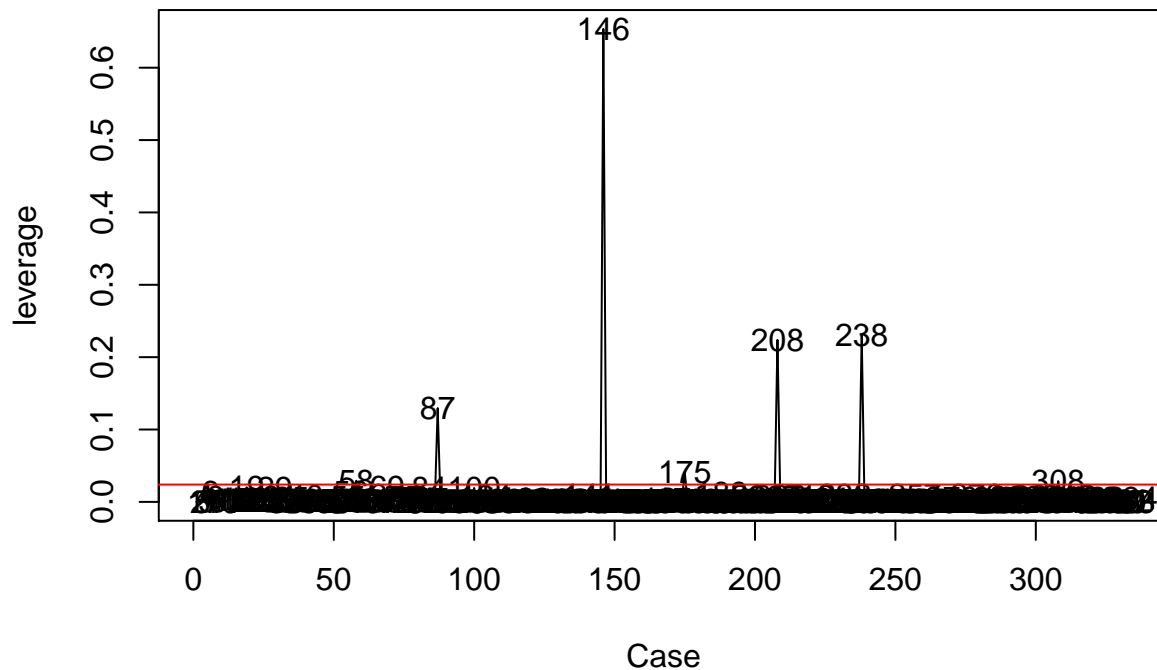
```
#y outlier
Case <- c(1:nmodel4)
plot(Case, rstudent(fitmodel4weight), type="n")
text(Case, rstudent(fitmodel4weight), Case)
```



```
alpha <- 0.01
p=4
crit <- qt(1-alpha/2/nmodel4, nmodel4-p-1)
youtlier=which(abs(rstudent(fitmodel4weight)) >=crit )
```

```
#x outlier
X <- as.matrix(cbind(rep(1,nmodel4), datamodel4weight[1]))
H <- X%*%solve(t(X)%*%X,tol=1e-30)%*%t(X)
leverage <- hatvalues(fitmodel4weight)
```

```
plot(Case, leverage, type="l")
text(Case, leverage, Case)
abline(h=2*p/nmodel4, col=2)
```



```
xoutlier=data.frame(which(leverage>2*p/nmodel4) )
xoutlier
```

```
##      which.leverage...2...p.nmodel4.
## 58                                     58
## 87                                     87
## 146                                    146
## 175                                    175
## 208                                    208
## 238                                    238
## 308                                    308
```

```
#test whether outlier in the extend of the model
IM4=influence.measures(fitmodel4weight)
dxoutlier=union(which(IM4$infmat[,5]>0.2),which(IM4$infmat[,3]>2*sqrt(p/nmodel4)))
#combine x and y outlier
finaloutlier=union(dxoutlier,youtlier)
datamodel4Final=datamodel4[-c(finaloutlier),]
# get model2 without x y outlier
fitmodel4x2=lm(datamodel4Final$y~.,data = datamodel4Final)
wtsx2 <- 1/fitted(lm(abs(residuals(fitmodel4x2)) ~ ., data = datamodel4Final))^2
Fmodel4=lm(datamodel4Final$y~., data = datamodel4Final,weights =wtsx2)
# R2 & adj R2 for model1
summary(Fmodel4)$r.squared
```

```
## [1] 0.8804859
```

```
summary(Fmodel4)$adj.r.squared
```

```
## [1] 0.8801249
```

```

# Test the model
#strandized for test data
yt9=as.matrix(test$`V-9`)
colnames(yt9)=c("V-9")
yt10=as.matrix(test$`V-10`)
colnames(yt10)=c("V-10")
test.v9<- cbind(test[1:27],yt9)
test.v10<- cbind(test[1:27],yt10)
for(i in 2:27)
{
  test.v9[,i] <-(test[,i]-mean(test[,i])) /sd(test[,i])
}
for(i in 2:27)
{
  test.v10[,i] <-(test[,i]-mean(test[,i])) /sd(test[,i])
}

```

```

# scatter plot & cor
fitv10 <- lm(test$`V-10`~ ., data = test.v10)
summary(fitv10)

```

```

##
## Call:
## lm(formula = test$`V-10` ~ ., data = test.v10)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.870  -3.670   1.169   4.338  11.544
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  272.4457    11.3144   24.080 3.47e-10 ***
## `V-1`         1.5941     1.1706    1.362 0.203165
## `V-2`        -6.6147    24.4522   -0.271 0.792266
## `V-3`        40.1613    23.9268    1.679 0.124174
## `V-4`       -66.8744    22.6169   -2.957 0.014366 *
## `V-5`       233.8802    26.8405    8.714 5.53e-06 ***
## `V-6`        -6.9412    11.2577   -0.617 0.551292
## `V-7`        32.3178     3.2195   10.038 1.53e-06 ***
## `V-8`        30.6192     7.2639    4.215 0.001785 **
## `V-11`       -0.7395    14.8773   -0.050 0.961338
## `V-12`      113.1887   118.3086    0.957 0.361264
## `V-13`      140.3495    83.2022    1.687 0.122527
## `V-14`        1.3866    17.1699    0.081 0.937228
## `V-15`      169.7870    99.9927    1.698 0.120356
## `V-16`       10.0250    50.4989    0.199 0.846616
## `V-17`        9.1391    70.3806    0.130 0.899258
## `V-18`      -21.7666    18.2804   -1.191 0.261266
## `V-19`      -30.6981    21.3410   -1.438 0.180857
## `V-20`       77.3476    21.1456    3.658 0.004405 **
## `V-21`      -60.7189    42.0521   -1.444 0.179357
## `V-22`     -120.0430    66.2118   -1.813 0.099910 .
## `V-23`       73.7604    31.4409    2.346 0.040919 *
## `V-24`       11.8816    33.0547    0.359 0.726731

```

```
## `V-25`      -225.4046   268.3902  -0.840  0.420624
## `V-26`       66.3399   165.9609   0.400  0.697758
## `V-27`     -103.7999    22.2297  -4.669  0.000882 ***
## `V-28`       32.9507    15.8271   2.082  0.063992 .
## `V-29`     -19.0591    27.0856  -0.704  0.497699
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.78 on 10 degrees of freedom
## Multiple R-squared:  0.9991, Adjusted R-squared:  0.9968
## F-statistic: 423 on 27 and 10 DF, p-value: 3.708e-12
```

```
cor(test.v10[,c(2:28)])
```

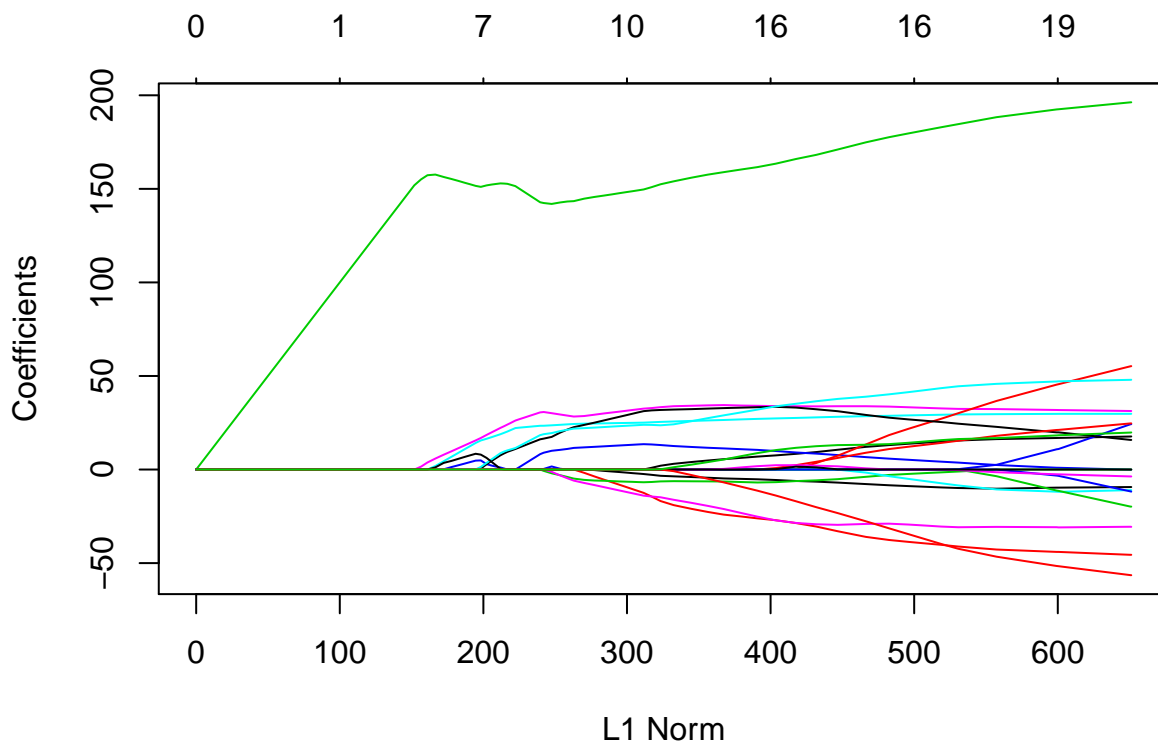
```
##           V-2           V-3           V-4           V-5           V-6
## V-2  1.00000000  0.98760515  0.73160086  0.37670831  0.22600652
## V-3  0.98760515  1.00000000  0.71209140  0.37228924  0.21567025
## V-4  0.73160086  0.71209140  1.00000000  0.84671012  0.24922766
## V-5  0.37670831  0.37228924  0.84671012  1.00000000  0.30351159
## V-6  0.22600652  0.21567025  0.24922766  0.30351159  1.00000000
## V-7 -0.02292599 -0.02186071  0.24412674  0.33620300  0.29322017
## V-8  0.53953700  0.53344562  0.86489429  0.82822710  0.30041366
## V-11 0.36533757  0.36353757  0.56934023  0.61657479  0.16658200
## V-12 0.33139692  0.31593503  0.73920733  0.86156959 -0.08532251
## V-13 0.32272403  0.30183748  0.73328812  0.85294637 -0.08492403
## V-14 0.28741154  0.26035082  0.55247646  0.64418155  0.26248596
## V-15 0.33136935  0.32684742  0.72021209  0.84528427 -0.09394580
## V-16 0.35132989  0.32660843  0.77856486  0.82834474 -0.03979719
## V-17 0.32506928  0.29793012  0.77490951  0.87052243 -0.05195761
## V-18 -0.13142833 -0.11399440  0.03433714  0.19025481 -0.24756714
## V-19 0.17836347  0.20812630  0.38801002  0.50391639 -0.18251913
## V-20 -0.29988016 -0.30073657 -0.69239049 -0.77660353 -0.05539371
## V-21 0.30817051  0.30110642  0.72947167  0.85704711 -0.10059098
## V-22 0.34513510  0.32903710  0.75979981  0.86558255 -0.08782856
## V-23 0.21719020  0.19529788  0.47802378  0.62976351 -0.21996723
## V-24 0.09327267  0.06689985  0.41470723  0.59337340 -0.12706560
## V-25 0.29584548  0.27747458  0.68387755  0.82511693 -0.12111300
## V-26 0.29535671  0.27861968  0.68366366  0.82505364 -0.13107651
## V-27 0.17990392  0.15830678  0.46120831  0.63685096 -0.13050909
## V-28 -0.22409534 -0.20295458 -0.13124054  0.04877237 -0.06067612
## V-29 0.35241519  0.33821433  0.74379471  0.84233751 -0.06839656
## V-10 0.37440101  0.37524116  0.81522709  0.97470602  0.31052398
##           V-7           V-8           V-11           V-12           V-13
## V-2 -0.02292599  0.53953700  0.36533757  0.33139692  0.32272403
## V-3 -0.02186071  0.53344562  0.36353757  0.31593503  0.30183748
## V-4  0.24412674  0.86489429  0.56934023  0.73920733  0.73328812
## V-5  0.33620300  0.82822710  0.61657479  0.86156959  0.85294637
## V-6  0.29322017  0.30041366  0.16658200 -0.08532251 -0.08492403
## V-7  1.00000000  0.30105455  0.11998472  0.22570889  0.23497926
## V-8  0.30105455  1.00000000  0.50374408  0.66459443  0.66941953
## V-11 0.11998472  0.50374408  1.00000000  0.57709819  0.58573941
## V-12 0.22570889  0.66459443  0.57709819  1.00000000  0.99284343
## V-13 0.23497926  0.66941953  0.58573941  0.99284343  1.00000000
## V-14 0.17104439  0.43539652  0.86567836  0.62321257  0.62133723
## V-15 0.24442844  0.65639165  0.60763465  0.98837433  0.97541628
```

| | | | | | | |
|----|------|---------------|-------------|-------------|-------------|-------------|
| ## | V-16 | 0.14701985 | 0.63479608 | 0.66093890 | 0.91934038 | 0.91825536 |
| ## | V-17 | 0.22603833 | 0.65035736 | 0.60781001 | 0.97411641 | 0.97099506 |
| ## | V-18 | 0.28047450 | -0.04531235 | 0.16643626 | 0.35935593 | 0.36469287 |
| ## | V-19 | 0.24933678 | 0.30909345 | 0.48169384 | 0.71663431 | 0.70108747 |
| ## | V-20 | -0.09126864 | -0.60965008 | -0.71249914 | -0.75710367 | -0.72547131 |
| ## | V-21 | 0.24458981 | 0.67387434 | 0.61143932 | 0.98660922 | 0.97896018 |
| ## | V-22 | 0.21226792 | 0.65935680 | 0.59549118 | 0.99072373 | 0.98163857 |
| ## | V-23 | 0.21822375 | 0.46259694 | 0.38352358 | 0.79635337 | 0.82352013 |
| ## | V-24 | 0.18430826 | 0.47278839 | 0.42093001 | 0.72829040 | 0.77718417 |
| ## | V-25 | 0.24865855 | 0.63793373 | 0.56071173 | 0.98150465 | 0.99143887 |
| ## | V-26 | 0.24245434 | 0.63248576 | 0.54894643 | 0.98406695 | 0.99057436 |
| ## | V-27 | 0.29543427 | 0.44939056 | 0.22949717 | 0.77103403 | 0.79436596 |
| ## | V-28 | 0.29970449 | -0.19043096 | -0.07412328 | 0.13729518 | 0.13530408 |
| ## | V-29 | 0.23998363 | 0.66416219 | 0.57442695 | 0.98710408 | 0.97929565 |
| ## | V-10 | 0.45747334 | 0.84754453 | 0.57655860 | 0.85482795 | 0.85117572 |
| ## | | V-14 | V-15 | V-16 | V-17 | V-18 |
| ## | V-2 | 0.2874115436 | 0.3313694 | 0.35132989 | 0.32506928 | -0.13142833 |
| ## | V-3 | 0.2603508218 | 0.3268474 | 0.32660843 | 0.29793012 | -0.11399440 |
| ## | V-4 | 0.5524764595 | 0.7202121 | 0.77856486 | 0.77490951 | 0.03433714 |
| ## | V-5 | 0.6441815499 | 0.8452843 | 0.82834474 | 0.87052243 | 0.19025481 |
| ## | V-6 | 0.2624859638 | -0.0939458 | -0.03979719 | -0.05195761 | -0.24756714 |
| ## | V-7 | 0.1710443906 | 0.2444284 | 0.14701985 | 0.22603833 | 0.28047450 |
| ## | V-8 | 0.4353965238 | 0.6563916 | 0.63479608 | 0.65035736 | -0.04531235 |
| ## | V-11 | 0.8656783621 | 0.6076346 | 0.66093890 | 0.60781001 | 0.16643626 |
| ## | V-12 | 0.6232125688 | 0.9883743 | 0.91934038 | 0.97411641 | 0.35935593 |
| ## | V-13 | 0.6213372286 | 0.9754163 | 0.91825536 | 0.97099506 | 0.36469287 |
| ## | V-14 | 1.0000000000 | 0.6215299 | 0.72533932 | 0.69452099 | 0.15605408 |
| ## | V-15 | 0.6215298730 | 1.0000000 | 0.90209227 | 0.94941667 | 0.40458450 |
| ## | V-16 | 0.7253393223 | 0.9020923 | 1.0000000 | 0.96611641 | 0.27203608 |
| ## | V-17 | 0.6945209943 | 0.9494167 | 0.96611641 | 1.0000000 | 0.31791123 |
| ## | V-18 | 0.1560540827 | 0.4045845 | 0.27203608 | 0.31791123 | 1.0000000 |
| ## | V-19 | 0.4083245027 | 0.7873891 | 0.59859493 | 0.62986553 | 0.73216288 |
| ## | V-20 | -0.7741418013 | -0.7665163 | -0.86187965 | -0.80850985 | -0.09154056 |
| ## | V-21 | 0.6066935538 | 0.9906373 | 0.90719355 | 0.95103770 | 0.39962450 |
| ## | V-22 | 0.6429662142 | 0.9786266 | 0.95341013 | 0.98380933 | 0.36255471 |
| ## | V-23 | 0.4161109177 | 0.7774443 | 0.67084502 | 0.75610551 | 0.42932245 |
| ## | V-24 | 0.4312455544 | 0.6872105 | 0.59685074 | 0.66803579 | 0.38651934 |
| ## | V-25 | 0.5844609203 | 0.9675719 | 0.87566108 | 0.94225312 | 0.42548625 |
| ## | V-26 | 0.5756684522 | 0.9713055 | 0.87711897 | 0.94478814 | 0.42811196 |
| ## | V-27 | 0.3008578736 | 0.7255657 | 0.56500768 | 0.72278276 | 0.38691850 |
| ## | V-28 | 0.0005952779 | 0.1613507 | 0.02801824 | 0.10393714 | 0.86355056 |
| ## | V-29 | 0.5885690773 | 0.9831633 | 0.89956429 | 0.95135608 | 0.37296130 |
| ## | V-10 | 0.5900117992 | 0.8516274 | 0.78108086 | 0.83674718 | 0.22666142 |
| ## | | V-19 | V-20 | V-21 | V-22 | V-23 |
| ## | V-2 | 0.1783635 | -0.29988016 | 0.3081705 | 0.34513510 | 0.2171902 |
| ## | V-3 | 0.2081263 | -0.30073657 | 0.3011064 | 0.32903710 | 0.1952979 |
| ## | V-4 | 0.3880100 | -0.69239049 | 0.7294717 | 0.75979981 | 0.4780238 |
| ## | V-5 | 0.5039164 | -0.77660353 | 0.8570471 | 0.86558255 | 0.6297635 |
| ## | V-6 | -0.1825191 | -0.05539371 | -0.1005910 | -0.08782856 | -0.2199672 |
| ## | V-7 | 0.2493368 | -0.09126864 | 0.2445898 | 0.21226792 | 0.2182237 |
| ## | V-8 | 0.3090934 | -0.60965008 | 0.6738743 | 0.65935680 | 0.4625969 |
| ## | V-11 | 0.4816938 | -0.71249914 | 0.6114393 | 0.59549118 | 0.3835236 |
| ## | V-12 | 0.7166343 | -0.75710367 | 0.9866092 | 0.99072373 | 0.7963534 |
| ## | V-13 | 0.7010875 | -0.72547131 | 0.9789602 | 0.98163857 | 0.8235201 |
| | | | | | | 0.77718417 |

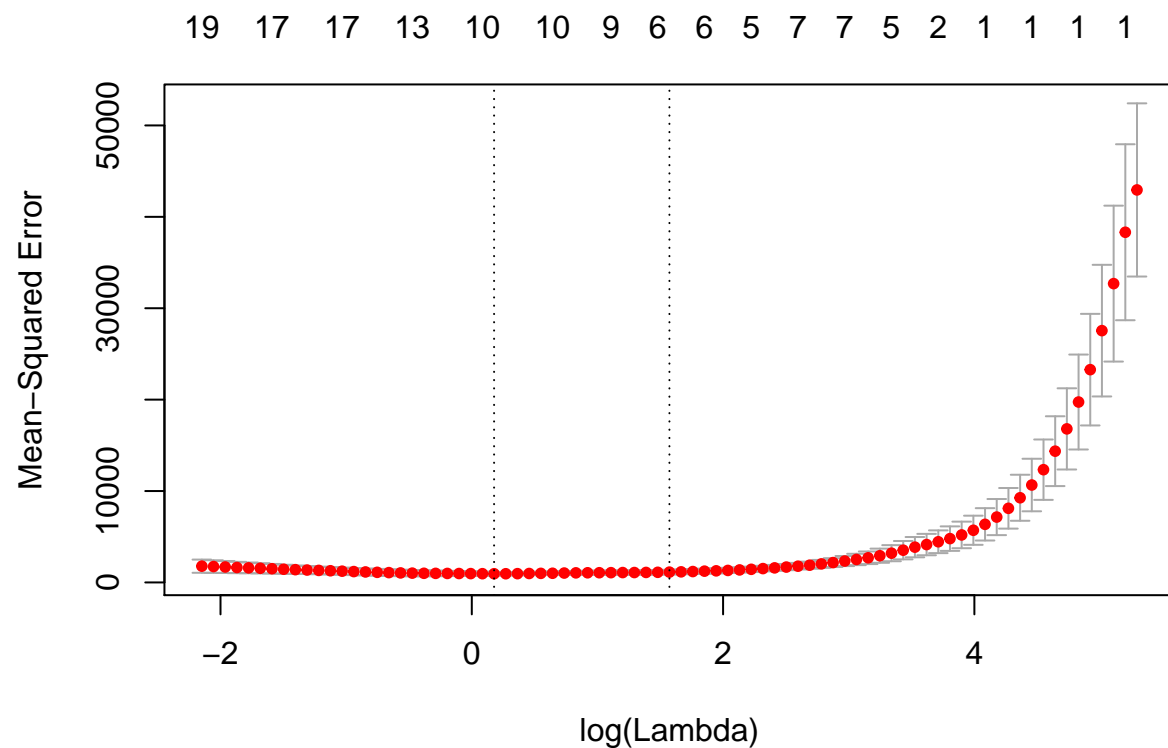
| | | | | | | | |
|----|------|------------|-------------|------------|---------------|-------------|-------------|
| ## | V-14 | 0.4083245 | -0.77414180 | 0.6066936 | 0.64296621 | 0.4161109 | 0.43124555 |
| ## | V-15 | 0.7873891 | -0.76651634 | 0.9906373 | 0.97862664 | 0.7774443 | 0.68721053 |
| ## | V-16 | 0.5985949 | -0.86187965 | 0.9071935 | 0.95341013 | 0.6708450 | 0.59685074 |
| ## | V-17 | 0.6298655 | -0.80850985 | 0.9510377 | 0.98380933 | 0.7561055 | 0.66803579 |
| ## | V-18 | 0.7321629 | -0.09154056 | 0.3996245 | 0.36255471 | 0.4293224 | 0.38651934 |
| ## | V-19 | 1.0000000 | -0.41602353 | 0.7641967 | 0.70151754 | 0.5605578 | 0.51266245 |
| ## | V-20 | -0.4160235 | 1.00000000 | -0.7545829 | -0.79468355 | -0.4487491 | -0.38553819 |
| ## | V-21 | 0.7641967 | -0.75458293 | 1.0000000 | 0.97974383 | 0.7731228 | 0.70924978 |
| ## | V-22 | 0.7015175 | -0.79468355 | 0.9797438 | 1.00000000 | 0.7662124 | 0.68447330 |
| ## | V-23 | 0.5605578 | -0.44874905 | 0.7731228 | 0.76621244 | 1.0000000 | 0.73658929 |
| ## | V-24 | 0.5126625 | -0.38553819 | 0.7092498 | 0.68447330 | 0.7365893 | 1.00000000 |
| ## | V-25 | 0.7283520 | -0.67082997 | 0.9695914 | 0.96181713 | 0.8723698 | 0.81802957 |
| ## | V-26 | 0.7337861 | -0.67297063 | 0.9715537 | 0.96501751 | 0.8762817 | 0.79843537 |
| ## | V-27 | 0.4897397 | -0.29678603 | 0.7330601 | 0.72350793 | 0.9020787 | 0.71872893 |
| ## | V-28 | 0.5019291 | 0.13628274 | 0.1724028 | 0.13522069 | 0.2075548 | 0.13663264 |
| ## | V-29 | 0.7447778 | -0.73530060 | 0.9807783 | 0.97404091 | 0.7658337 | 0.71177550 |
| ## | V-10 | 0.5596538 | -0.70418735 | 0.8563429 | 0.84520316 | 0.6688126 | 0.61045344 |
| ## | | V-25 | V-26 | V-27 | V-28 | V-29 | |
| ## | V-2 | 0.2958455 | 0.2953567 | 0.1799039 | -0.2240953363 | 0.35241519 | |
| ## | V-3 | 0.2774746 | 0.2786197 | 0.1583068 | -0.2029545779 | 0.33821433 | |
| ## | V-4 | 0.6838775 | 0.6836637 | 0.4612083 | -0.1312405395 | 0.74379471 | |
| ## | V-5 | 0.8251169 | 0.8250536 | 0.6368510 | 0.0487723702 | 0.84233751 | |
| ## | V-6 | -0.1211130 | -0.1310765 | -0.1305091 | -0.0606761209 | -0.06839656 | |
| ## | V-7 | 0.2486585 | 0.2424543 | 0.2954343 | 0.2997044861 | 0.23998363 | |
| ## | V-8 | 0.6379337 | 0.6324858 | 0.4493906 | -0.1904309611 | 0.66416219 | |
| ## | V-11 | 0.5607117 | 0.5489464 | 0.2294972 | -0.0741232850 | 0.57442695 | |
| ## | V-12 | 0.9815047 | 0.9840670 | 0.7710340 | 0.1372951846 | 0.98710408 | |
| ## | V-13 | 0.9914389 | 0.9905744 | 0.7943660 | 0.1353040806 | 0.97929565 | |
| ## | V-14 | 0.5844609 | 0.5756685 | 0.3008579 | 0.0005952779 | 0.58856908 | |
| ## | V-15 | 0.9675719 | 0.9713055 | 0.7255657 | 0.1613506662 | 0.98316326 | |
| ## | V-16 | 0.8756611 | 0.8771190 | 0.5650077 | 0.0280182377 | 0.89956429 | |
| ## | V-17 | 0.9422531 | 0.9447881 | 0.7227828 | 0.1039371380 | 0.95135608 | |
| ## | V-18 | 0.4254862 | 0.4281120 | 0.3869185 | 0.8635505633 | 0.37296130 | |
| ## | V-19 | 0.7283520 | 0.7337861 | 0.4897397 | 0.5019290952 | 0.74477779 | |
| ## | V-20 | -0.6708300 | -0.6729706 | -0.2967860 | 0.1362827396 | -0.73530060 | |
| ## | V-21 | 0.9695914 | 0.9715537 | 0.7330601 | 0.1724027847 | 0.98077831 | |
| ## | V-22 | 0.9618171 | 0.9650175 | 0.7235079 | 0.1352206913 | 0.97404091 | |
| ## | V-23 | 0.8723698 | 0.8762817 | 0.9020787 | 0.2075548473 | 0.76583369 | |
| ## | V-24 | 0.8180296 | 0.7984354 | 0.7187289 | 0.1366326393 | 0.71177550 | |
| ## | V-25 | 1.0000000 | 0.9989211 | 0.8352226 | 0.1848733515 | 0.96894426 | |
| ## | V-26 | 0.9989211 | 1.0000000 | 0.8395187 | 0.1902107103 | 0.97039969 | |
| ## | V-27 | 0.8352226 | 0.8395187 | 1.0000000 | 0.2995912846 | 0.73230796 | |
| ## | V-28 | 0.1848734 | 0.1902107 | 0.2995913 | 1.0000000000 | 0.14344307 | |
| ## | V-29 | 0.9689443 | 0.9703997 | 0.7323080 | 0.1434430723 | 1.00000000 | |
| ## | V-10 | 0.8365705 | 0.8355670 | 0.6675232 | 0.0919203396 | 0.84459157 | |
| ## | | V-10 | | | | | |
| ## | V-2 | 0.37440101 | | | | | |
| ## | V-3 | 0.37524116 | | | | | |
| ## | V-4 | 0.81522709 | | | | | |
| ## | V-5 | 0.97470602 | | | | | |
| ## | V-6 | 0.31052398 | | | | | |
| ## | V-7 | 0.45747334 | | | | | |
| ## | V-8 | 0.84754453 | | | | | |
| ## | V-11 | 0.57655860 | | | | | |

```
## V-12 0.85482795
## V-13 0.85117572
## V-14 0.59001180
## V-15 0.85162743
## V-16 0.78108086
## V-17 0.83674718
## V-18 0.22666142
## V-19 0.55965376
## V-20 -0.70418735
## V-21 0.85634287
## V-22 0.84520316
## V-23 0.66881263
## V-24 0.61045344
## V-25 0.83657051
## V-26 0.83556696
## V-27 0.66752317
## V-28 0.09192034
## V-29 0.84459157
## V-10 1.00000000
```

```
# Lasso to determine variable
library("glmnet")
x.simple=as.matrix(test.v10[,2:27])
y=test.v10$`V-10`
fitlasso=glmnet(x.simple,y,alpha = 1)
plot(fitlasso)
```



```
cv.lasso=cv.glmnet(x.simple,y)
plot(cv.lasso)
```



```
coef(cv.lasso)
```

```
## 27 x 1 sparse Matrix of class "dgCMatrix"
##              1
## (Intercept) 287.631579
## V-2         .
## V-3         .
## V-4         .
## V-5         144.960511
## V-6          6.192732
## V-7         23.099944
## V-8         29.472063
## V-11        .
## V-12        .
## V-13        .
## V-14        .
## V-15        .
## V-16        .
## V-17        .
## V-18        .
## V-19        14.891914
## V-20        .
## V-21        .
## V-22        .
## V-23        16.689107
## V-24        .
## V-25        .
## V-26        .
## V-27        .
## V-28        .
## V-29        .
```



```

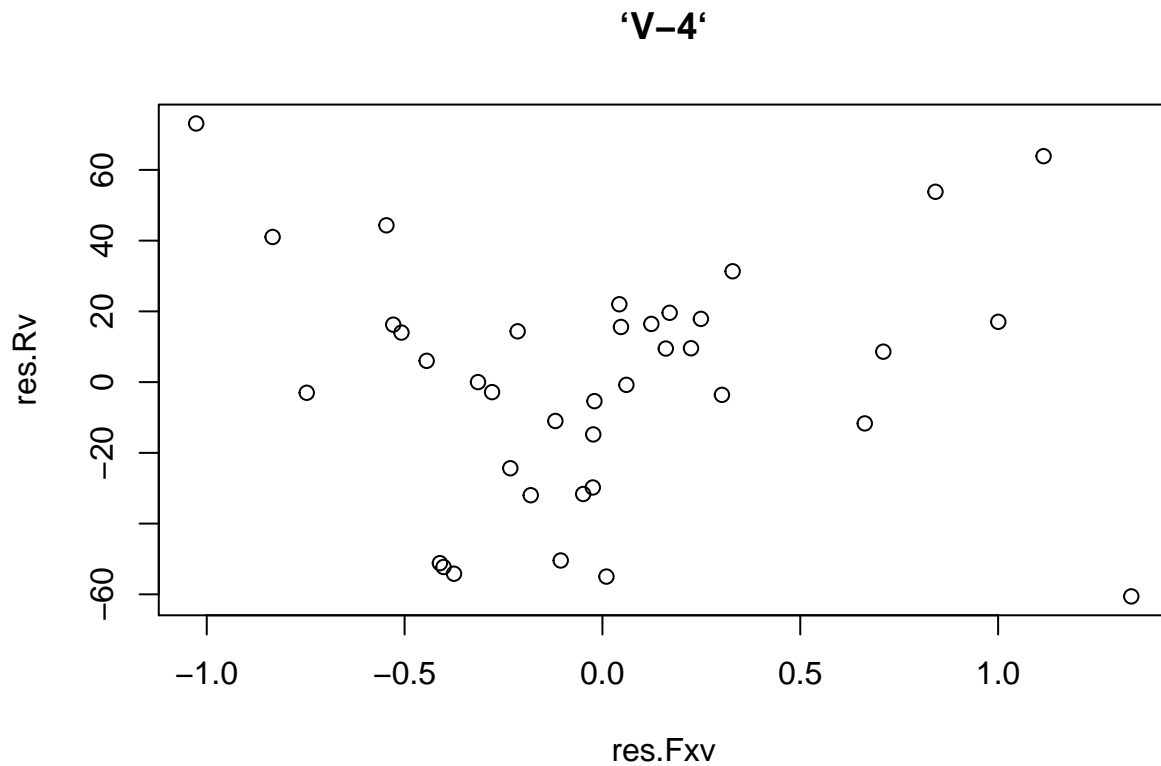
# Model 3
# added variable factor to determine ~
datamodel3=data.frame(test.v10[,c(4,5,7,21,28)])
fitmodel3=lm(datamodel3$V.10~.,data = datamodel3)
colData3 <- list("`V-4`", "`V-5`", "`V-7`", "`V-23`")
names(colData3) <- c("`V-4`", "`V-5`", "`V-7`", "`V-23`")
removeXList <- colData3

for (rmX in removeXList){
  tmpV <- colData3
  tmpV[[rmX]] = NULL
  test.Rv=lm(as.formula(paste("`V-10` ~", paste(tmpV, collapse = "+"))), data = test.v10)
  res.Rv= test.Rv$residuals

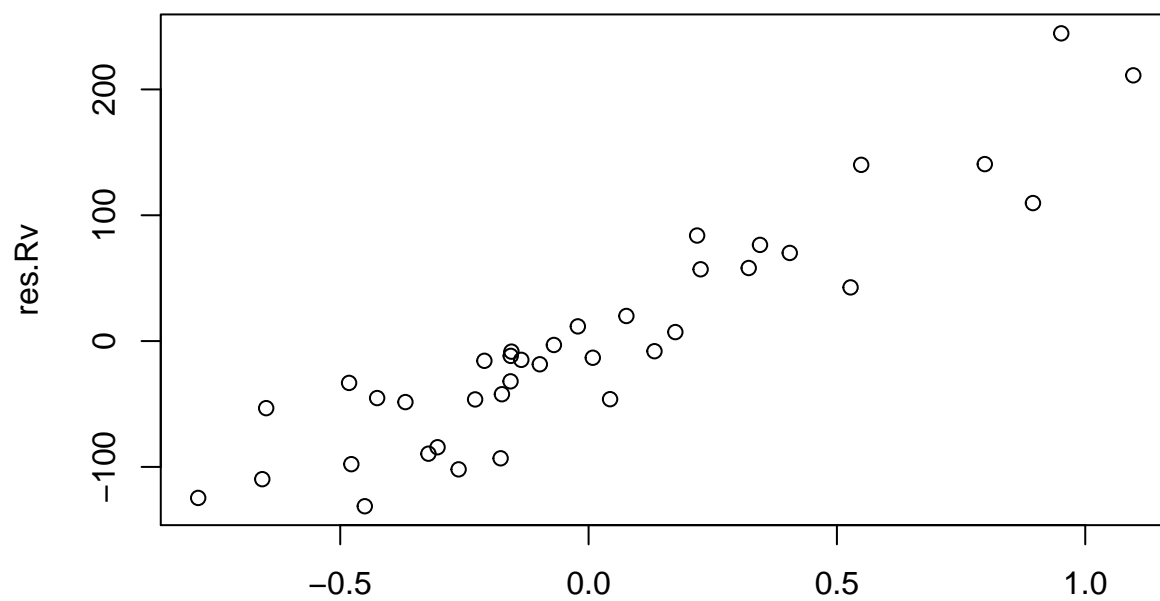
  test.Fxv=lm(as.formula(paste(paste(rmX, " ~"), paste(tmpV, collapse = "+"))), data = test.v10)
  res.Fxv= test.Fxv$residuals

  plot(res.Fxv,res.Rv,main = rmX)
}

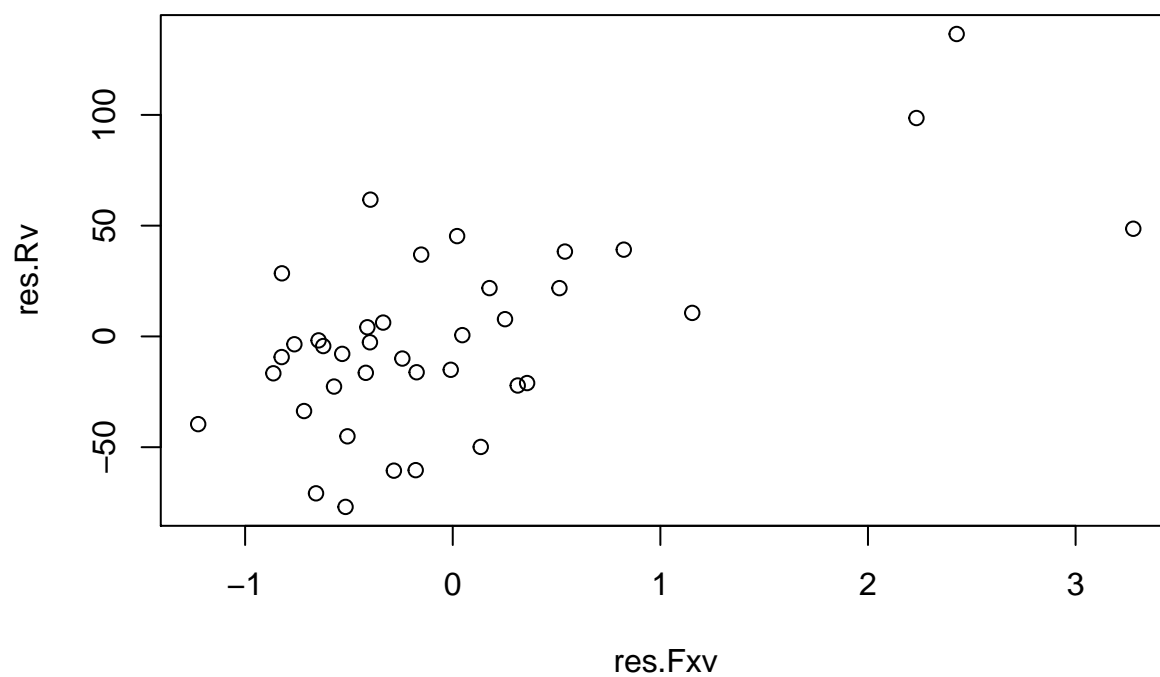
```

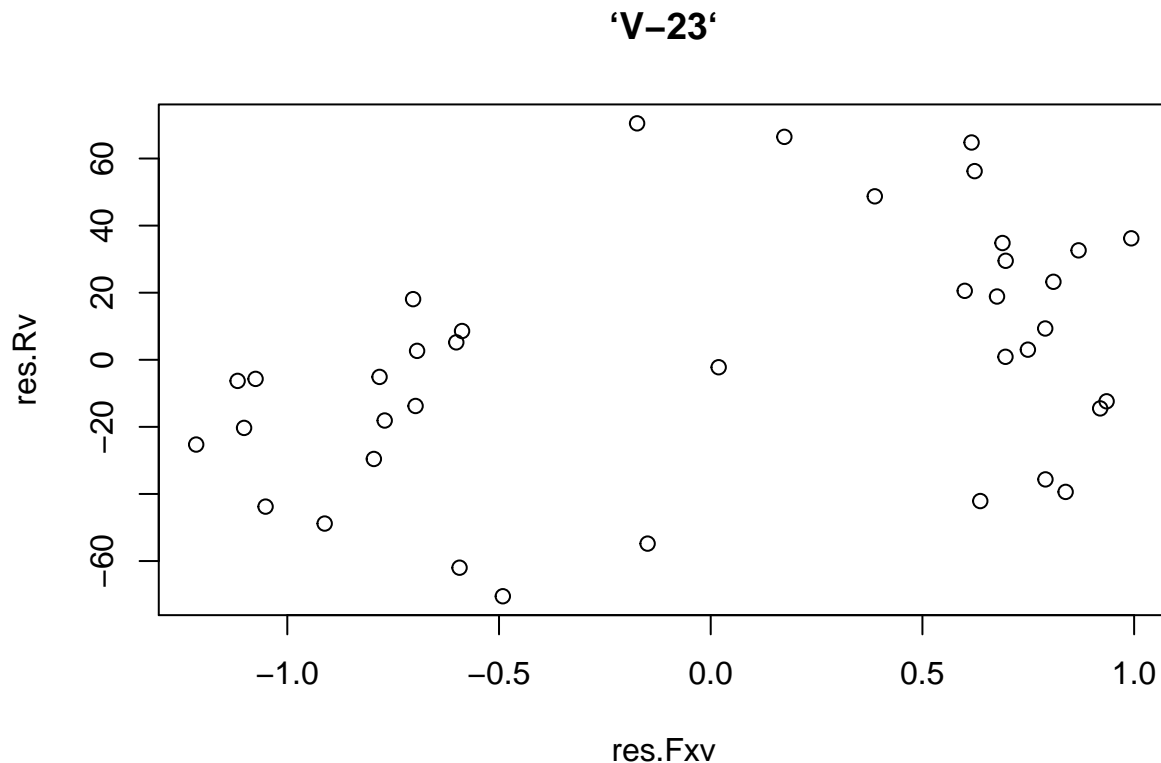


‘V-5’



‘V-7’





```
# Weighted transformation for model 3
wts <- 1/fitted(lm(abs(residuals(fitmodel3)) ~ ., data = datamodel3))^2

fitmodel3weight <- lm(datamodel3$V.10~ .,data = datamodel3, weights=wts)
datamodel3weight=cbind(datamodel3[1:4],datamodel3$V.10*wts)
summary(fitmodel3weight)$r.squared
```

```
## [1] 0.9776405
```

```
summary(fitmodel3weight)$adj.r.squared
```

```
## [1] 0.9749303
```

```
#Brown test whether constant variance and transformation for Model 3 after tranformation
resmodel3b=fitmodel3weight $residuals
mmodel3=mean(datamodel3weight$`datamodel3$V.10 * wts`)
nmodel3=dim(datamodel3weight)[1]
```

```
#1. Break the residuals into two groups.
```

```
Group1 <- resmodel3b[datamodel3weight$`datamodel3$V.10 * wts`<mmodel3]
```

```
Group2 <-resmodel3b[datamodel3weight$`datamodel3$V.10 * wts`>=mmodel3]
```

```
#2. Obtain the median of each group, using the commands:
```

```
M1 <- median(Group1)
```

```
M2 <- median(Group2)
```

```
#3. Obtain the mean absolute deviation for each group, using the commands:
```

```
D1 <- sum( abs( Group1 - M1 )) / length(Group1)
```

```
D2 <- sum( abs( Group2 - M2 )) / length(Group2)
```

```
#4. Calculate the pooled standard error, using the command:
```

```
s <- sqrt( ( sum( ( abs(Group1 - M1) - D1 )^2 ) + sum( ( abs(Group2 - M2) - D2 )^2 ) ) / (nmodel3-2) )
```

#5. Finally, calculate the Brown-Forsythe test statistic, using the command:

```
t <- ( D1 - D2 ) / ( s * sqrt( 1/length(Group1) + 1/length(Group2) ) )
t
```

```
## [1] 1.422665
```

*#6 Once you obtain this value, you can compare it to the critical value for any given alpha level to de
or you can find its P-value.*

```
alpha <- 0.05
```

```
qt(1-alpha/2, nmodel3-p1-1) # find the catical value
```

```
## [1] 2.036933
```

And the P-value can be found by typing:

```
2*(1-pt( abs(t), nmodel3-p1-1))
```

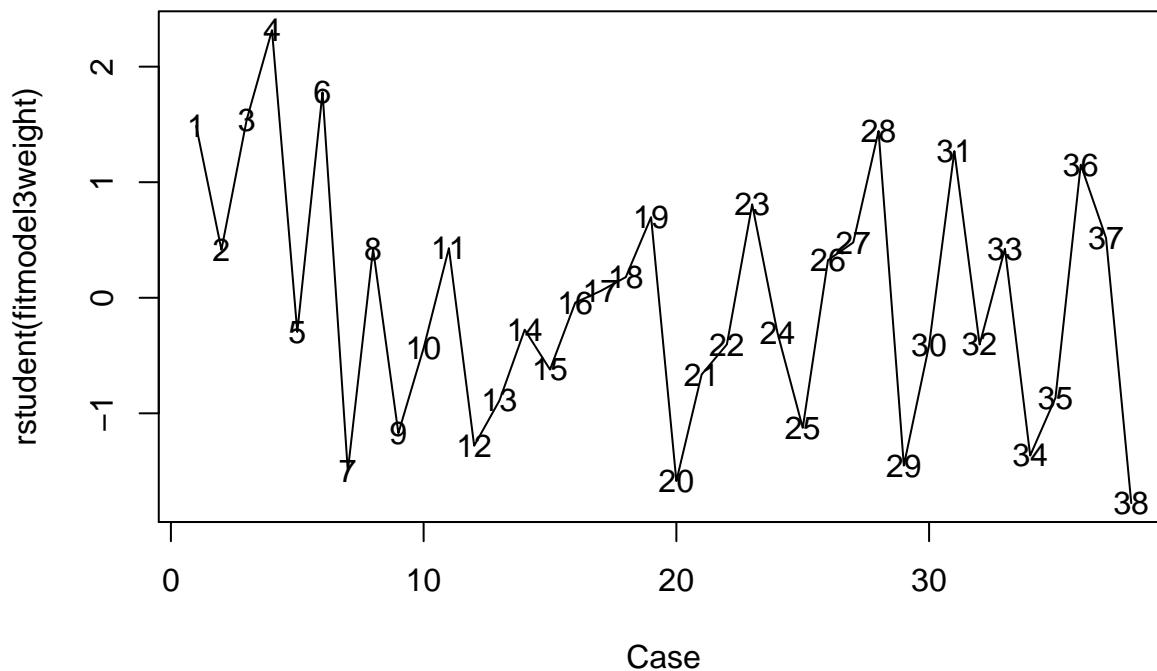
```
## [1] 0.1645093
```

#y outlier for model3

```
Case <- c(1:nmodel3)
```

```
plot(Case, rstudent(fitmodel3weight), type="l")
```

```
text(Case, rstudent(fitmodel3weight), Case)
```



```
alpha <- 0.05
```

```
crit <- qt(1-alpha/2/nmodel3, nmodel3-p1-1)
```

```
youtlier3=which(abs(rstudent(fitmodel3weight)) >=crit )
```

#x outlier for model3

```
X <- as.matrix(cbind(rep(1,nmodel3), datamodel3[1:4]))
```

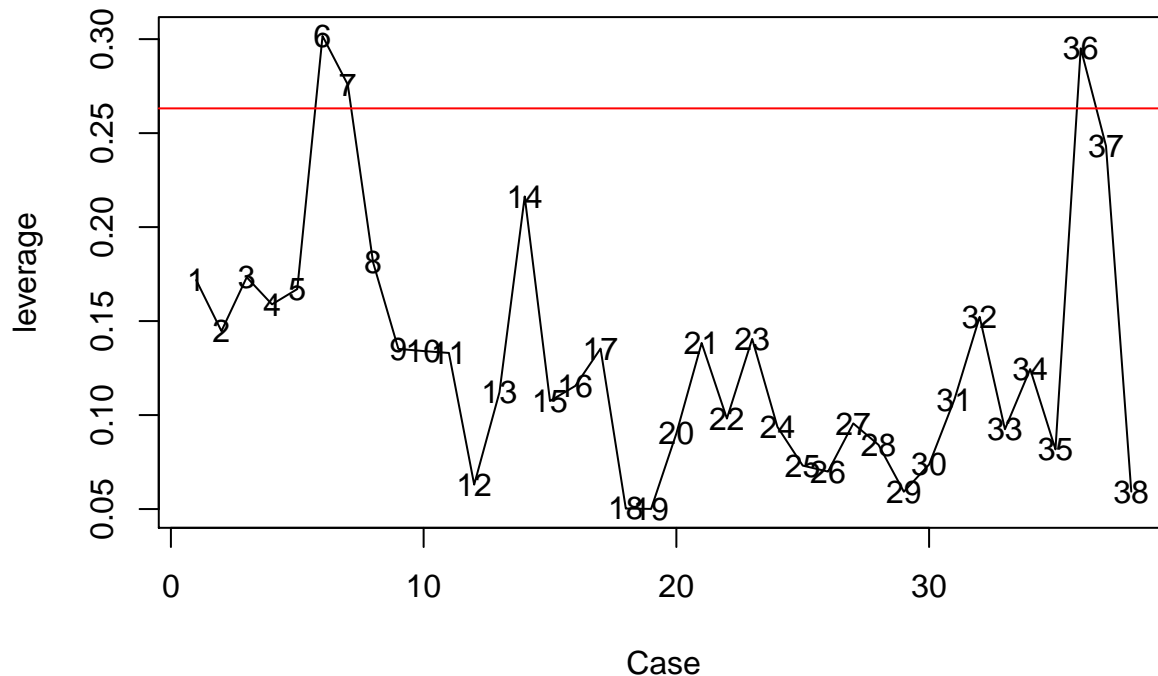
```
H <- X%*%solve(t(X)%*%X, tol=1e-20)%*%t(X)
```

```
leverage <- hatvalues(fitmodel3weight)
```

```
plot(Case, leverage, type="l")
```

```
text(Case, leverage, Case)
```

```
abline(h=2*p1/nmodel3, col=2)
```



```
xoutlier1=data.frame(which(leverage>2*p1/nmodel3) )
xoutlier1
```

```
##      which.leverage...2...p1.nmodel3.
## 6
## 7
## 36
```

```
#test whether outlier in the extend of the model3
IM3=influence.measures(fitmodel3weight)
dxoutlier3=union(which(IM3$infmat[,8]>0.2),which(IM3$infmat[,6]>2*sqrt(p1/nmodel3)))
#combine x and y outlier
finaloutlier3=union(dxoutlier3,youtlier3)
datamodel3Final=datamodel3[-c(finaloutlier3),]
# get model1 without x y outlier
fitmodel3x1=lm(datamodel3Final$V.10~.,data = datamodel3Final)
wtsx3 <- 1/fitted(lm(abs(residuals(fitmodel3x1)) ~ ., data = datamodel3Final))^2
Fmodel3=lm(datamodel3Final$V.10~., data = datamodel3Final,weights =wtsx3)
# R2 & adj R2 for model3 test
summary(Fmodel3)$r.squared
```

```
## [1] 0.9797508
```

```
summary(Fmodel3)$adj.r.squared
```

```
## [1] 0.9770509
```

```
# add ~2 for model4
Data.new3 <- cbind(test.v10$`V-4`, test.v10$`V-5`, test.v10$`V-7`, test.v10$`V-23`)
x3.new=as.matrix(cbind(Data.new3,((Data.new3)^2)[-2]))
colnames(x3.new)=c("V-4", "V-5", "V-7", "V-23", "V-4.2", "V-7.2", "V-23.2")
```

```
# Model 4
testv14 = data.frame(x3.new,y)
datamodel4=data.frame(testv14[,c(2,8)])
```

```

fitmodel4=lm(datamodel4$y~.,data = datamodel4)
summary(fitmodel4)$r.squared

## [1] 0.9500518

summary(fitmodel4)$adj.r.squared

## [1] 0.9486644

# Weighted transformation for model 4
wts <- 1/fitted(lm(abs(residuals(fitmodel4)) ~ ., data = datamodel4))^2

fitmodel4weight <- lm(datamodel4$y~ .,data = datamodel4, weights=wts)
datamodel4weight=cbind(datamodel4[1],datamodel4$y*wts)
summary(fitmodel4weight)$r.squared

## [1] 0.9524123

summary(fitmodel4)$adj.r.squared

## [1] 0.9486644

#Brown test whether constant variance and transformation for Model 2 after transformation
resmode22b=fitmodel4weight$residuals
mmodel4=mean(datamodel4weight$`datamodel4$y * wts`)
nmodel4=dim(datamodel4weight)[1]
#1. Break the residuals into two groups.
Group6 <- resmode22b[datamodel4weight$`datamodel4$y * wts`<mmodel4]
Group7 <- resmode22b[datamodel4weight$`datamodel4$y * wts`>=mmodel4]

#2. Obtain the median of each group, using the commands:
M1 <- median(Group6)
M2 <- median(Group7)

#3. Obtain the mean absolute deviation for each group, using the commands:
D1 <- sum( abs( Group6 - M1 )) / length(Group6)
D2 <- sum( abs( Group7 - M2 )) / length(Group7)

#4. Calculate the pooled standard error, using the command:
s <- sqrt( ( sum( ( abs(Group6 - M1) - D1 )^2 ) + sum( ( abs(Group7 - M2) - D2 )^2 ) ) / (nmodel4-2) )

#5. Finally, calculate the Brown-Forsythe test statistic, using the command:
t <- ( D1 - D2 ) / ( s * sqrt( 1/length(Group6) + 1/length(Group7) ) )
t

## [1] 1.582472

#6 Once you obtain this value, you can compare it to the critical value for any given alpha level to de
# or you can find its P-value.
alpha <- 0.05
qt(1-alpha/2, nmodel4-5) # find the catical value

## [1] 2.034515

# And the P-value can be found by typing:
2*(1-pt( abs(t), nmodel4-5))

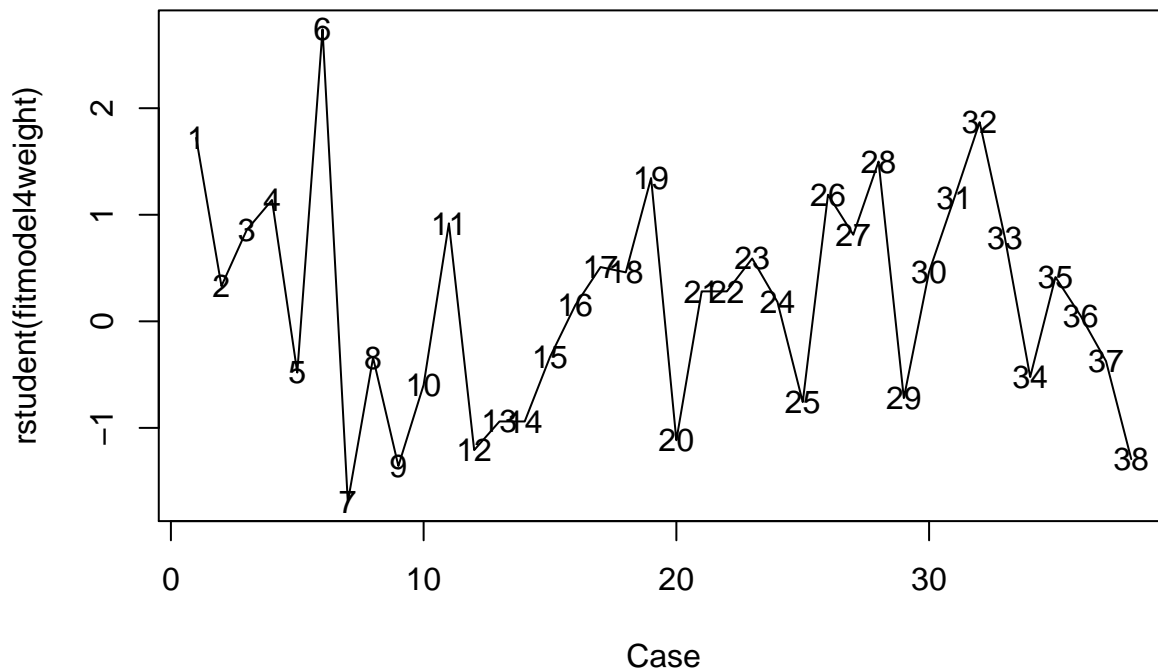
## [1] 0.1230801

```

```

#y outlier
Case <- c(1:nmodel4)
plot(Case, rstudent(fitmodel4weight), type="l")
text(Case, rstudent(fitmodel4weight), Case)

```



```

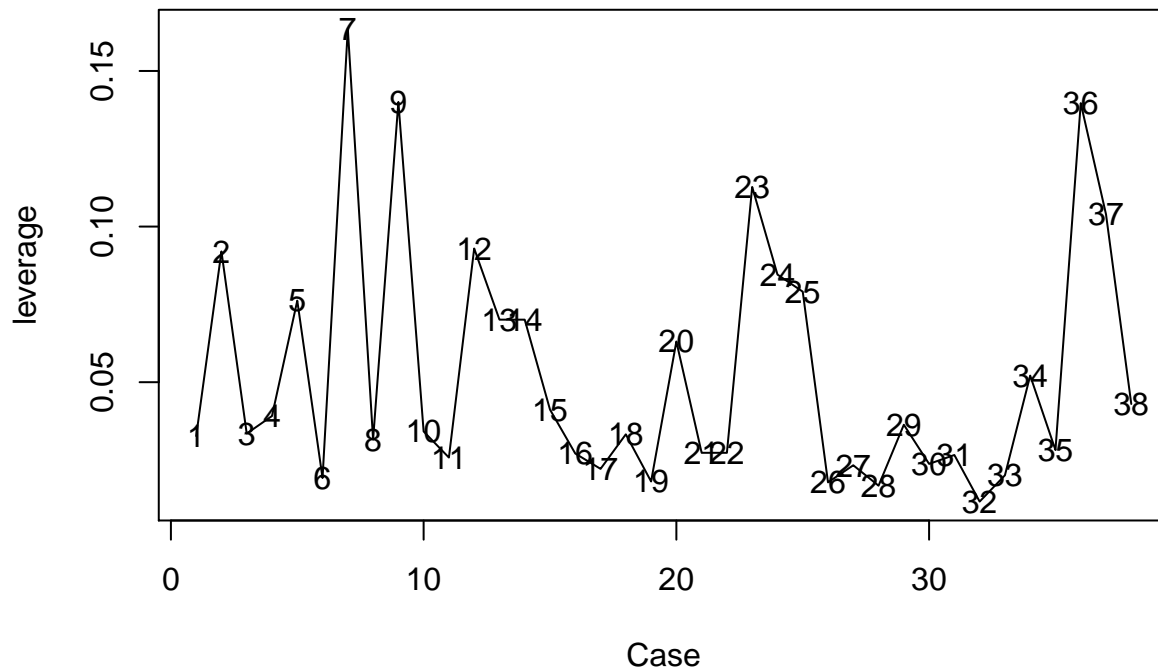
alpha <- 0.01
p=4
crit <- qt(1-alpha/2/nmodel4, nmodel4-p-1)
youtlier=which(abs(rstudent(fitmodel4weight)) >=crit )

```

```

#x outlier
X <- as.matrix(cbind(rep(1,nmodel4), datamodel4weight[1]))
H <- X%*%solve(t(X)%*%X,tol=1e-30)%*%t(X)
leverage <- hatvalues(fitmodel4weight)
plot(Case, leverage, type="l")
text(Case, leverage, Case)
abline(h=2*p/nmodel4, col=2)

```



```
xoutlier=data.frame(which(leverage>2*p/nmodel4) )
xoutlier

## [1] which.leverage...2...p.nmodel4.
## <0 rows> (or 0-length row.names)

#test whether outlier in the extend of the model
IM4=influence.measures(fitmodel4weight)
dxoutlier=union(which(IM4$infmat[,5]>0.2),which(IM4$infmat[,3]>2*sqrt(p/nmodel4)))
#combine x and y outlier
finaloutlier=union(dxoutlier,youtlier)
datamodel4Final=datamodel4[-c(finaloutlier),]
# get model2 without x y outlier
fitmodel4x2=lm(datamodel4Final$y~.,data = datamodel4Final)
wtsx2 <- 1/fitted(lm(abs(residuals(fitmodel4x2)) ~ ., data = datamodel4Final))^2
Fmodel4=lm(datamodel4Final$y~., data = datamodel4Final,weights =wtsx2)
# R2 & adj R2 for model1
summary(Fmodel4)$r.squared

## [1] 0.9516841

summary(Fmodel4)$adj.r.squared

## [1] 0.9503037
```