

## 1. $\alpha_R$ for different types of equations

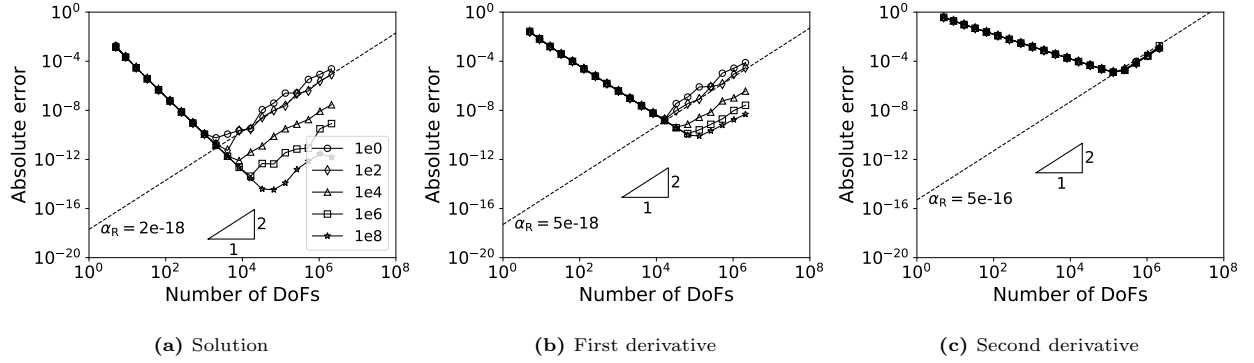
We consider the benchmark Poisson equation, i.e.  $u = e^{-(x-1/2)^2}$ , but we extend it to diffusion and Helmholtz equations by choosing different  $d(x)$  and  $r(x)$ , see Table 1 for the settings. The variables in  $d(x)$  and  $r(x)$  are denoted as  $c_d$  and  $c_h$ , respectively, for which the values of the former ranges from 1 to  $10^4$ , and that of the latter is equal to 1.

**Table 1** Settings of the Poisson, diffusion and Helmholtz equations.

	“Poisson”	“diffusion”	“Helmholtz”
$d(x)$	1	$1 + 0.5 \sin(c_d x)$	$1 + 0.5 \sin(x)$
$r(x)$	0	0	$c_h$

The offset  $\alpha_R$  for the three types of equations using the standard FEM ( $P_2$  elements) and the mixed FEM ( $P_4/P_3^{\text{disc}}$  elements) are shown in 2 writing 1 1d summary of offsets.

It shows that the offset  $\alpha_R$  is generally not affected by the types of equations considered. However, if we increase  $c_h$  for the Helmholtz equation,  $\alpha_R$  for the solution and first derivative would decrease, see Fig. 1.



**Fig. 1.** Absolute errors for the Helmholtz equation using the standard FEM for different  $c_h$ .