

# Predictive Hebbian Learning

## Computational Models of Neural Systems

### Lecture 5.2

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Based on slides by Mirella Lapata

November, 2017

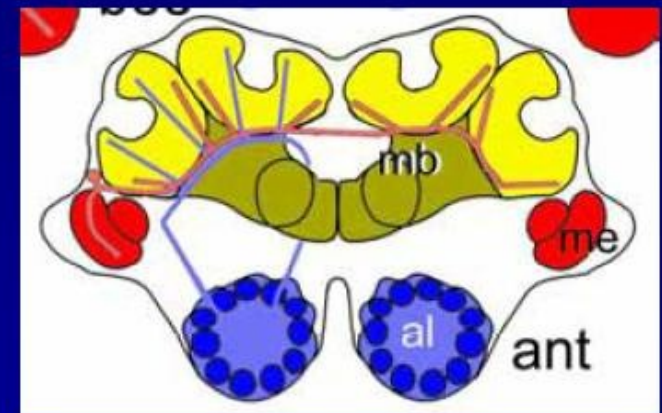
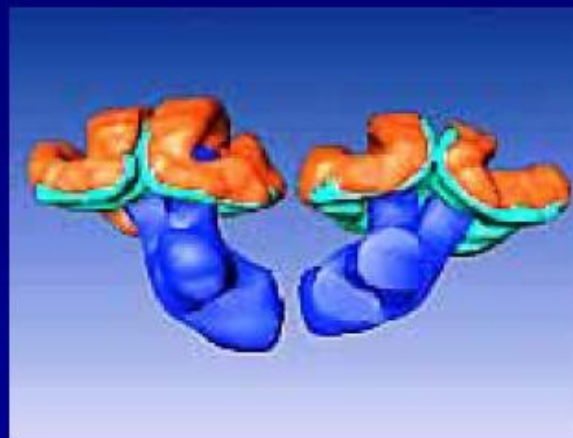
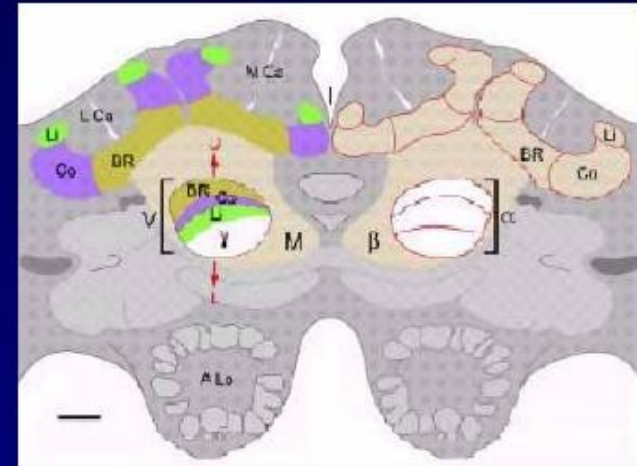
# Outline

- The bee brain
- Classical conditioning in honeybees
  - identification of VUMmx1
  - properties of VUMmx1
- Bee foraging in uncertain environments
  - model of bee foraging
  - theory of predictive Hebbian learning
- Dopamine neurons in the macaque monkey
  - activity of dopamine neurons
  - generalized theory of predictive Hebbian learning
  - modeling predictions

# The Bee Brain

- Honeybees have about one million neurons in about 1 mm<sup>3</sup>.
  - Fruit flies have only about 100,000 neurons
  - Ants have about 250,000 neurons.
- The mushroom bodies are thought to be involved in learning and memory.

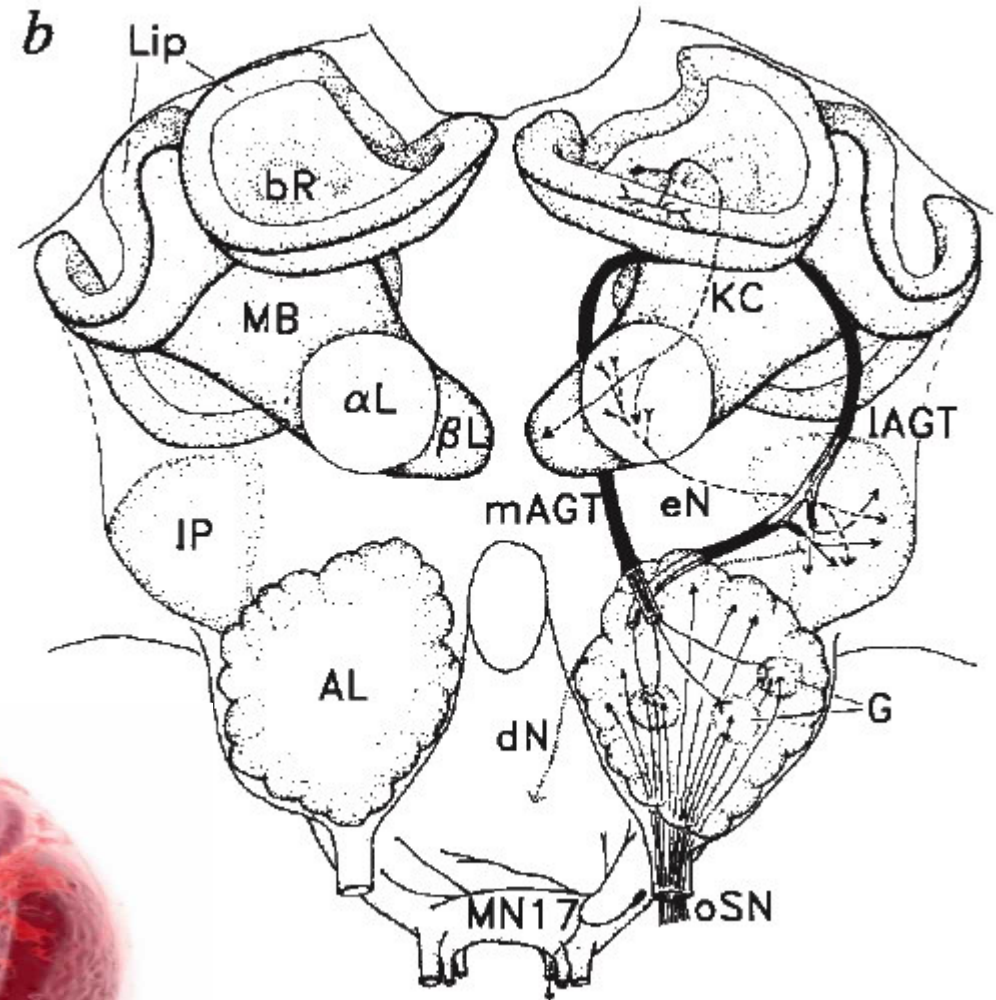
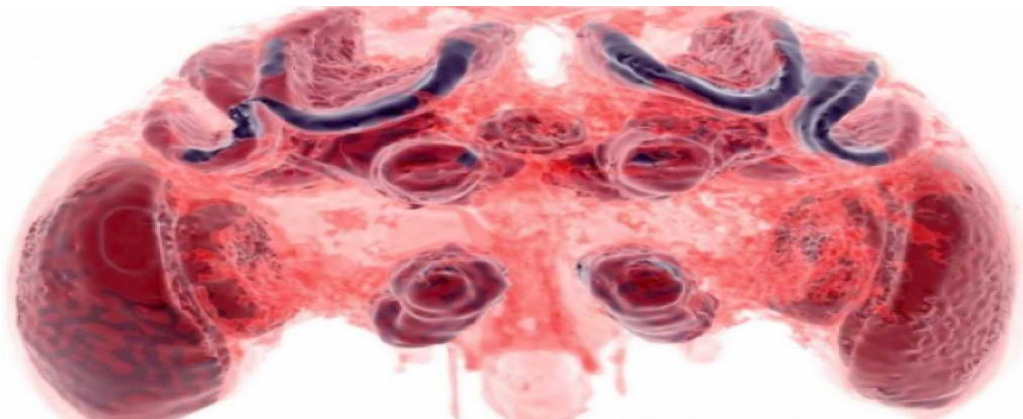
# Where is memory located in the honey bee brain?



<http://web.neurobio.arizona.edu/gronenberg/nrsc581>

# Anatomy of the Bee Brain

- MB: Mushroom body
- AL: Antenna lobe
- KC: Kenyon cells
- oSN: Olfactory sensory neurons
- MN17: motor neuron involved in PER



# Questions

- What are the cellular mechanisms responsible for classical conditioning?
- How is information about the unconditioned stimulus (US) represented at the neuronal level?
- What are the properties of neurons mediating the US?
  - Response to US
  - Convergence with the conditioned stimulus (CS) pathway
  - Reinforcement in conditioning
- How to identify such neurons?



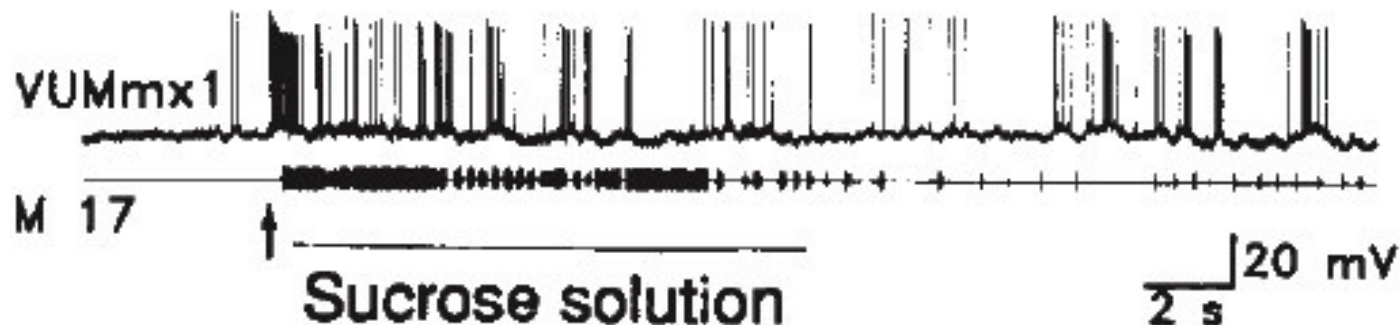
# Experiments on Honeybees

- Bees fixed by waxing dorsal thorax to small metal table.
- Odors were presented in a gentle air stream.
- Sucrose solution applied briefly to antenna and proboscis.
- Proboscis extension was seen after a *single pairing* of the odor (CS) with sucrose (US).



# Measuring Responses

- Proboscis extension reflex (PER) was recorded as an electromyogram from the M17 muscle involved in the reflex.
- Neurons were tested for responsiveness to the US.

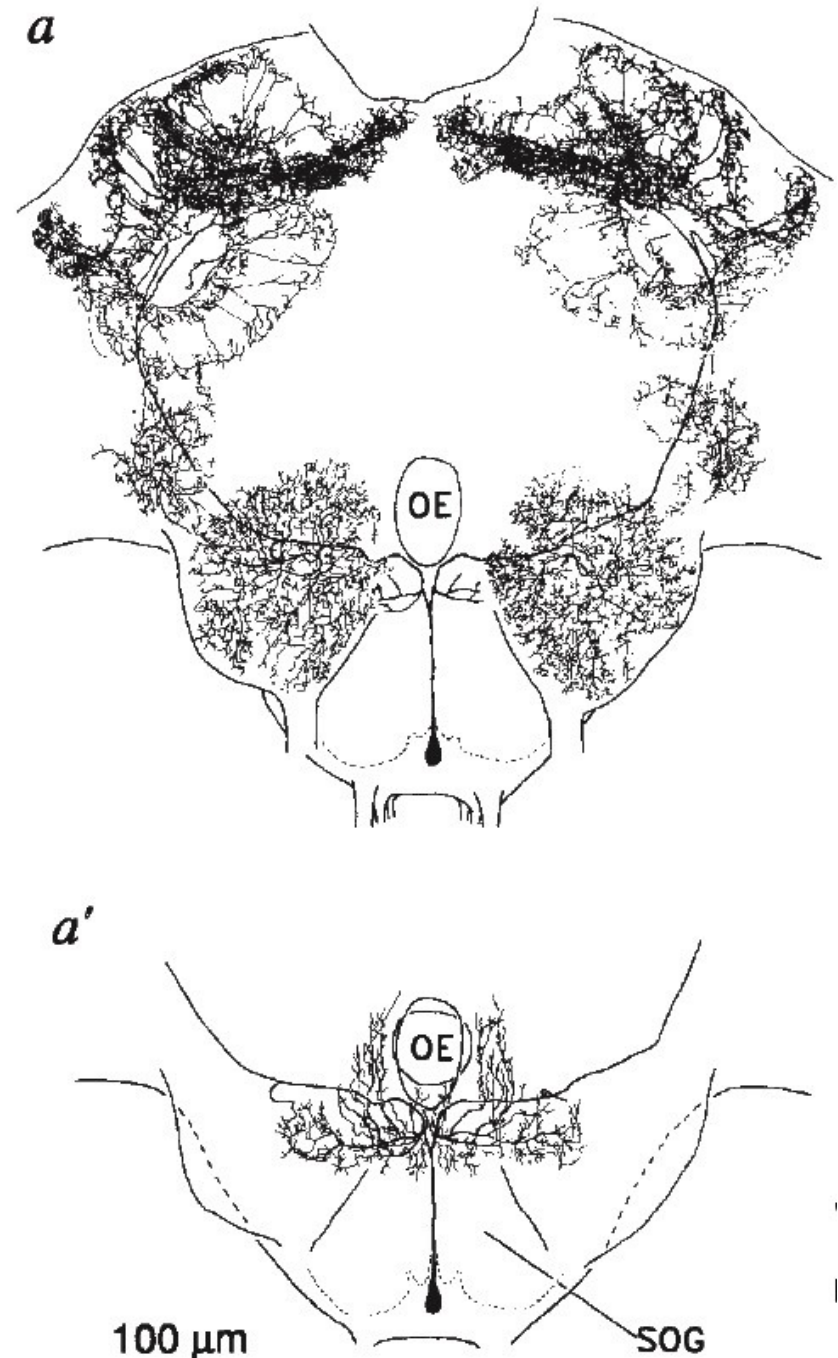




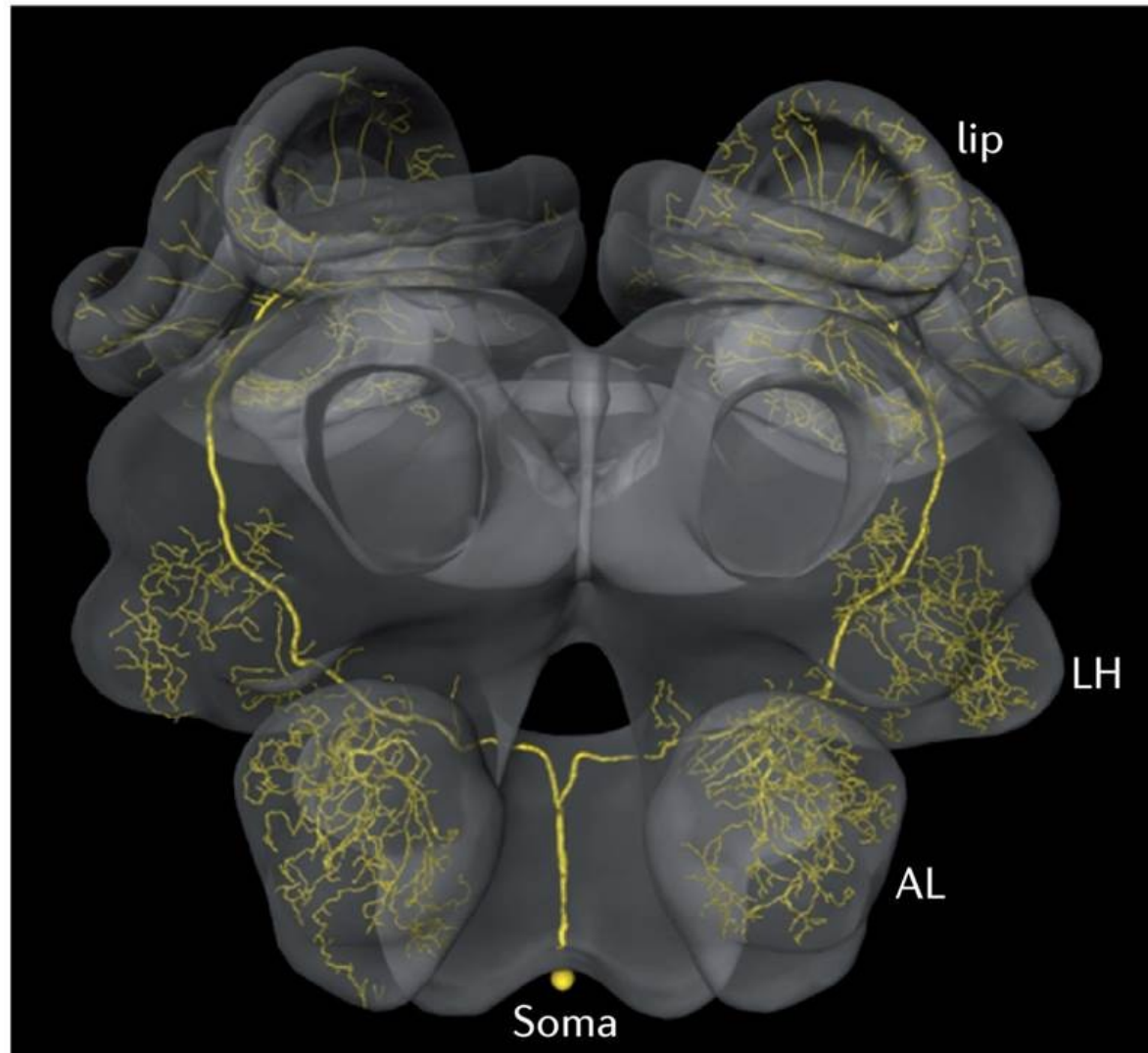
# VUMmx1 Responds to US

- Unique morphology: arborizes in the suboesophageal ganglion (SOG) and projects widely in regions involved in odor (CS) processing
- Responds to sucrose with a long burst of action potentials which outlasts the sucrose US.
- Neurotransmitter is octopamine: related to dopamine.

OE = Oesophagus



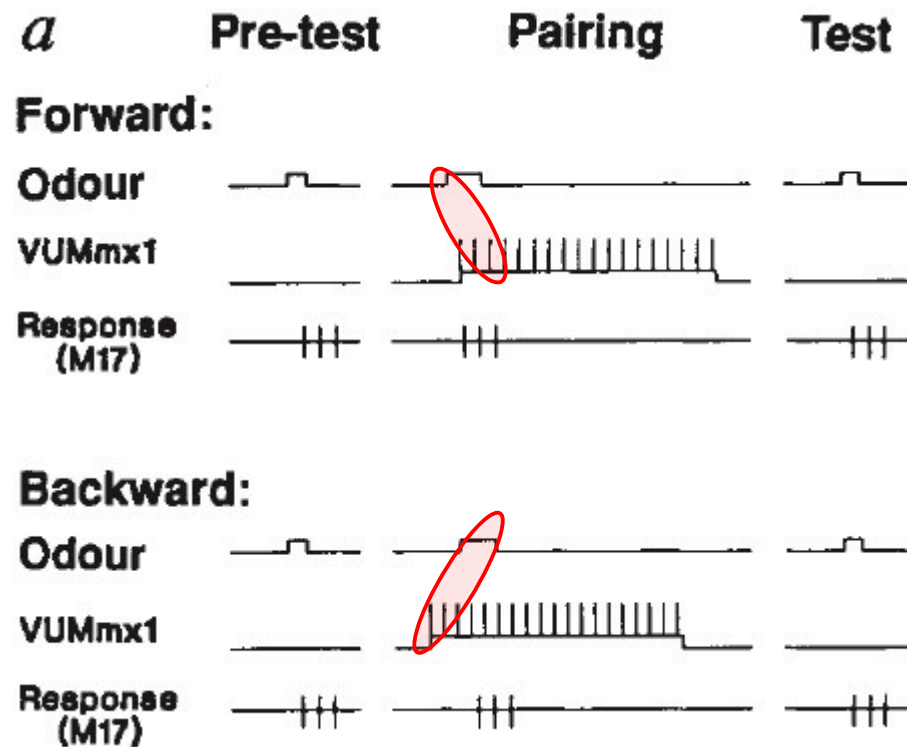
# VUMmx1



Nature Reviews | Neuroscience

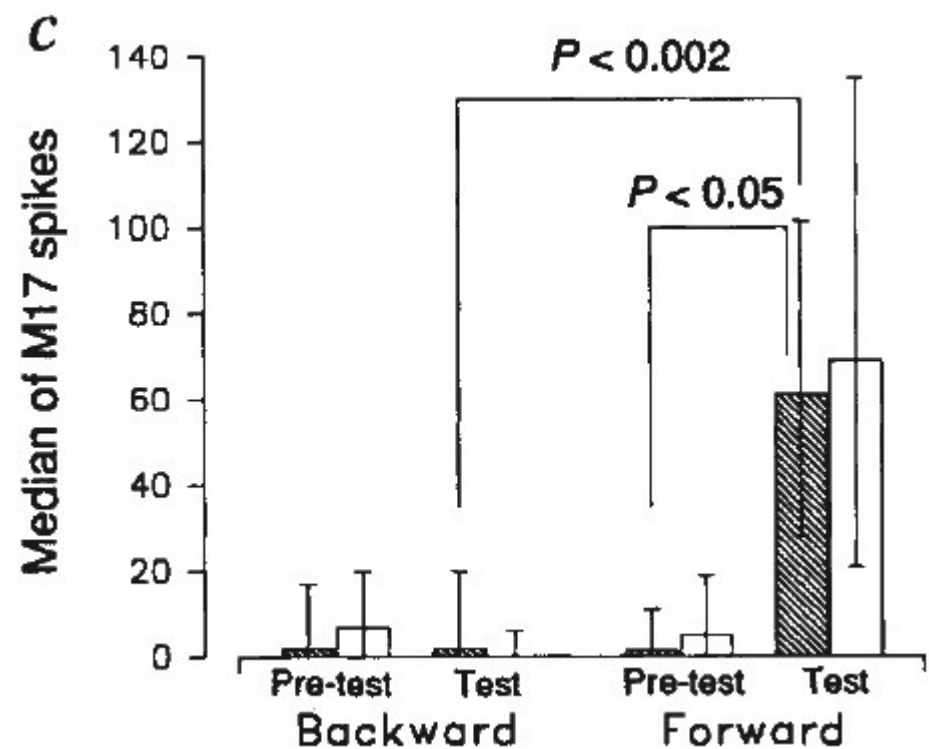
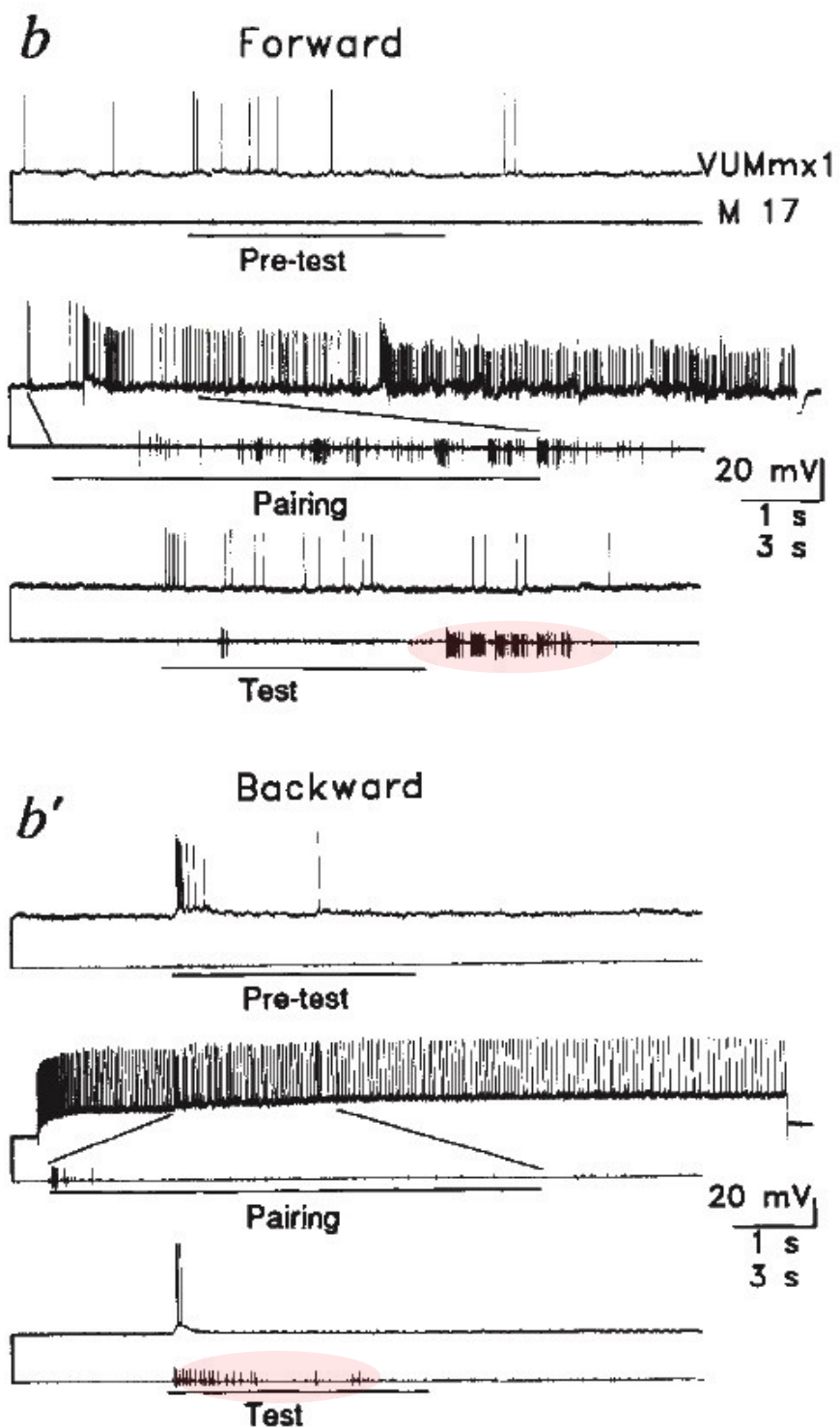
# Stimulating VUMmx1 Simulates a US

- Introduce CS then inject depolarizing current into VUMmx1 in lieu of applying sucrose.
- Try both forward and backward conditioning paradigms.



**Schematic diagram.**

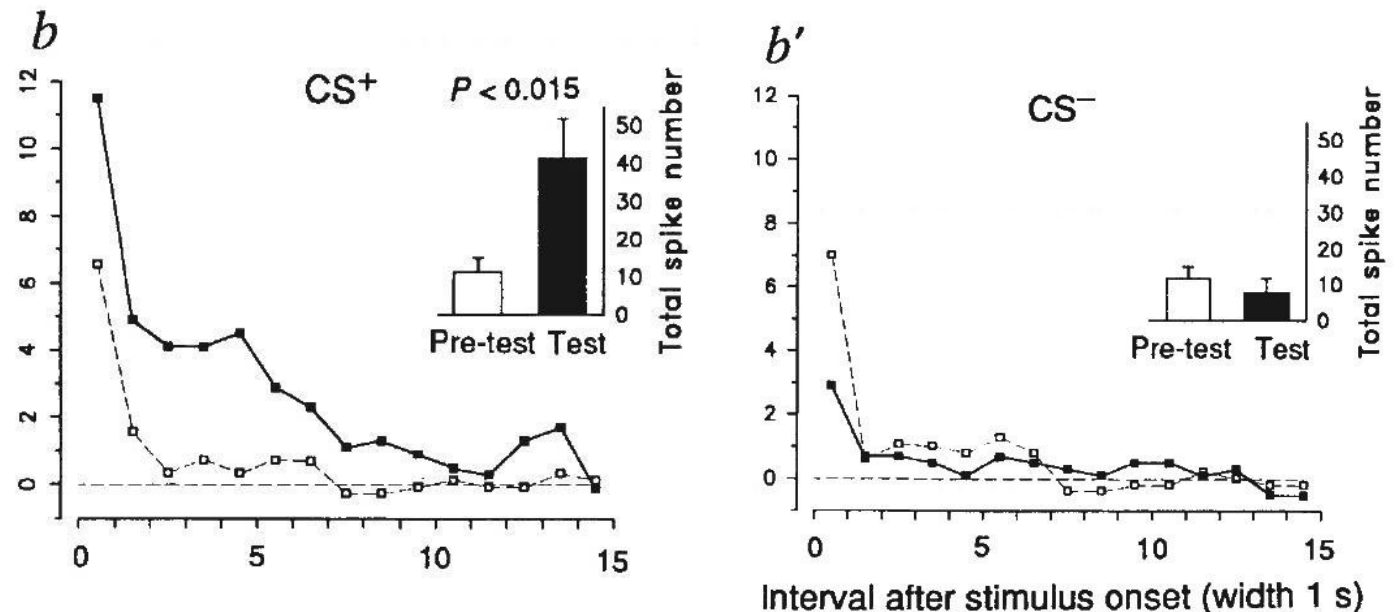
**Not real data!**



Open bars: sucrose US  
Shaded bars: VUMmx1 stimulation

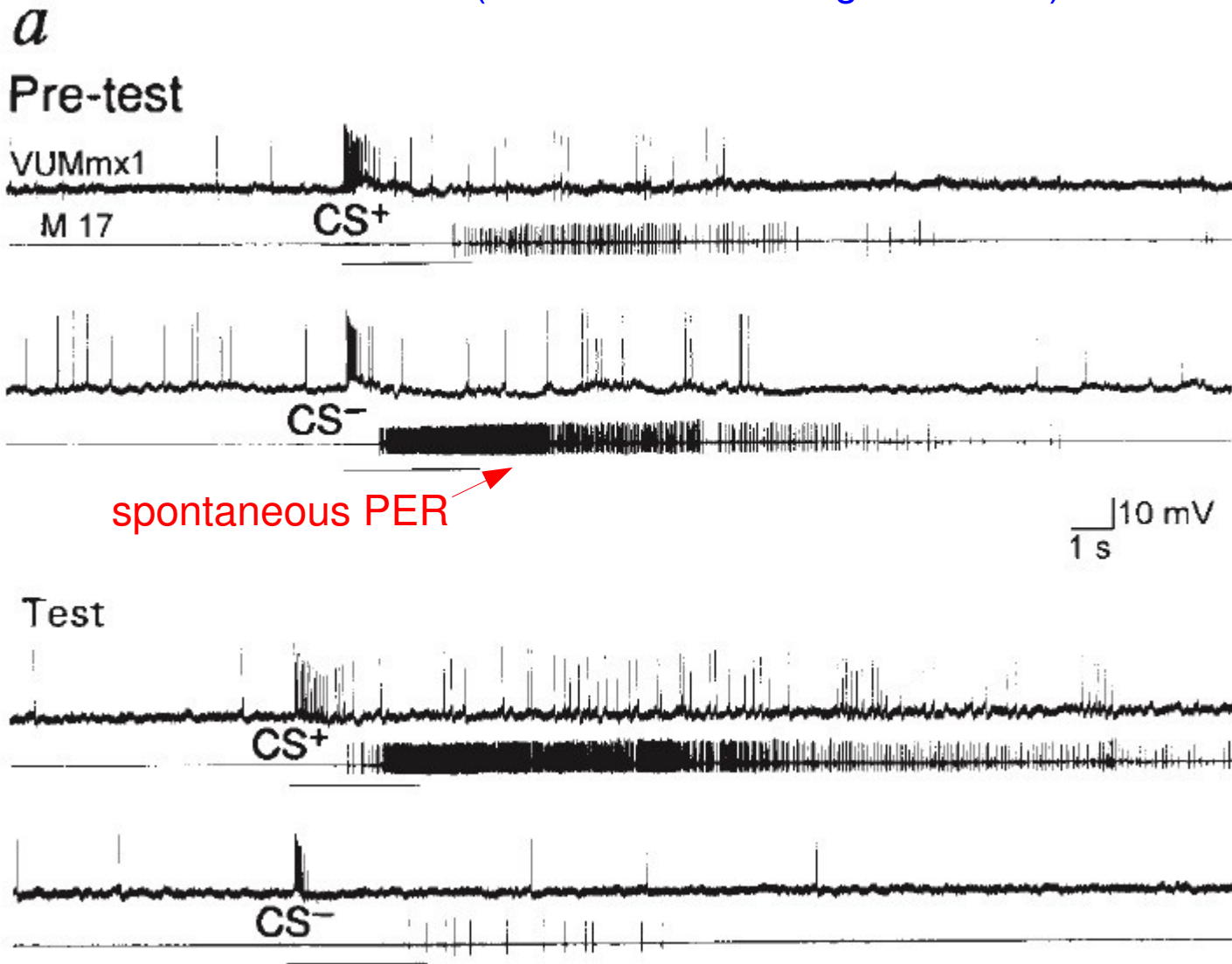
# Learning Effects of VUMmx1 Stimulation

- After learning, the odor alone stimulates VUMmx1 activity.
- Temporal contiguity effect: forward pairing causes a larger increase in spiking than backward pairing.
- Differential conditioning effect:
  - Differentially conditioned bees respond strongly to an odor (CS+) specifically paired with the US, and significantly less to an unpaired odor (CS–).



# Differential Conditioning of Two Odors

(carnation and orange blossom)





# Discussion

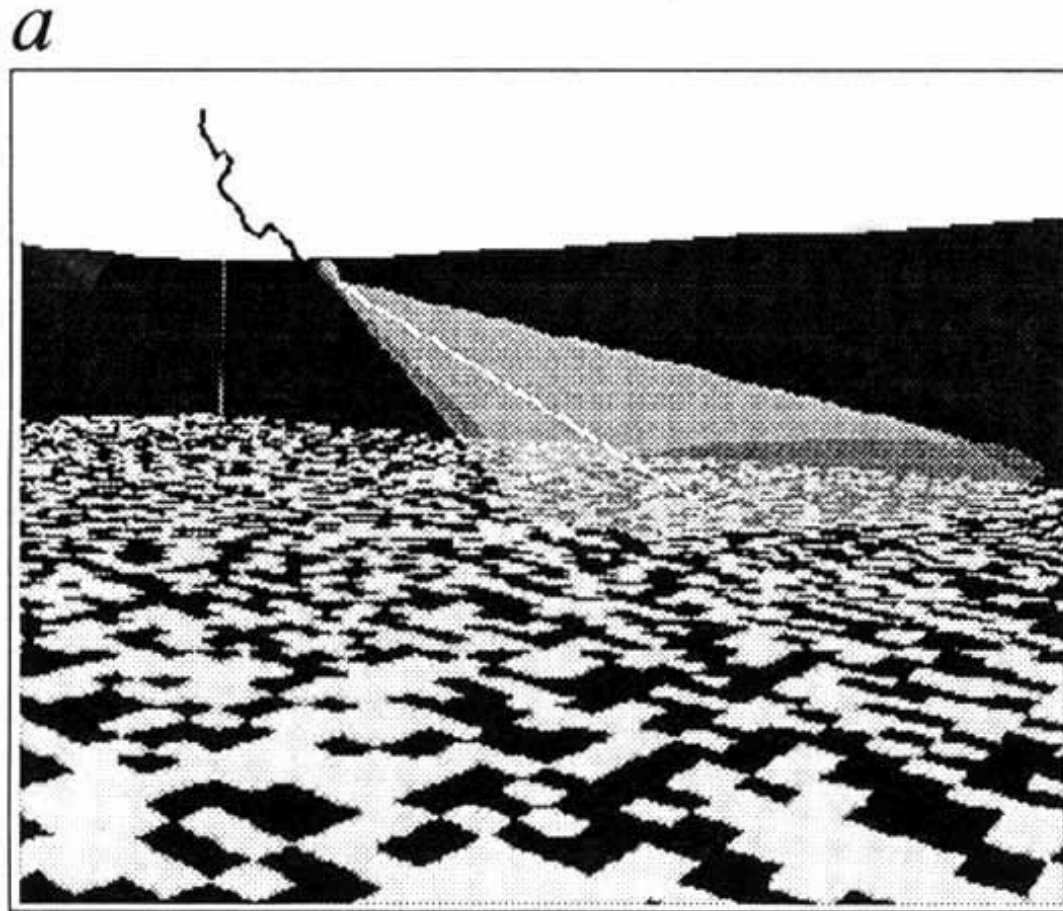
- Main claims:
  - VUMmx1 mediates the US in associative learning
  - A learned CS also activates VUMmx1.
  - Physiology is compatible with structures involved in complex forms of learning.
- Questions:
  - Is VUMmx1 the only neuron mediating the US?
    - Serial homologue of VUMmx1 has almost identical branching pattern.
    - Response to electrical stimulation is less than response to sucrose, so perhaps other neurons also contribute to the US signal.
  - Can VUMmx1 mediate other conditioning phenomena, e.g., blocking, overshadowing, extinction?
  - Do different stimuli induce similar responses?

# Bee Foraging

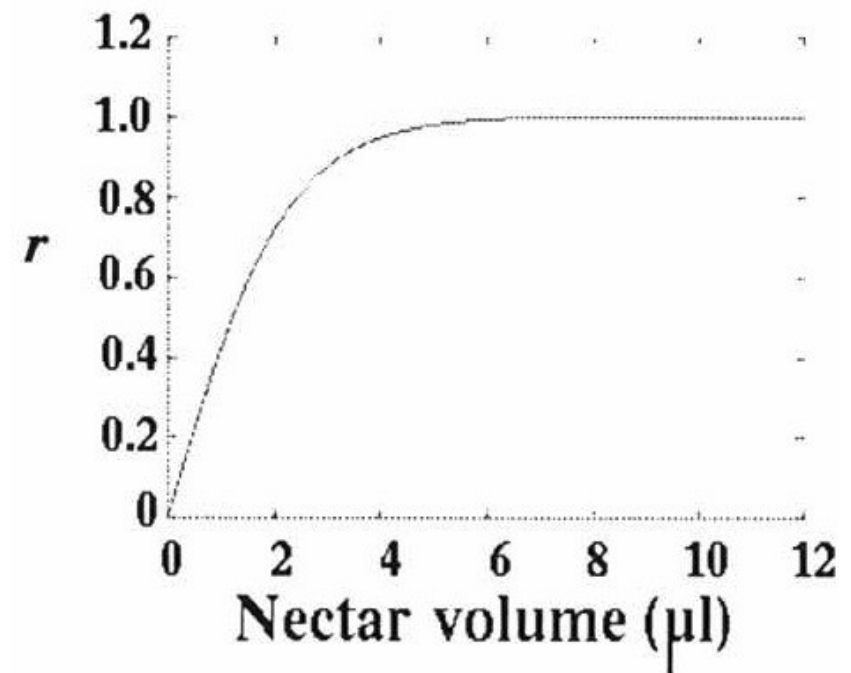
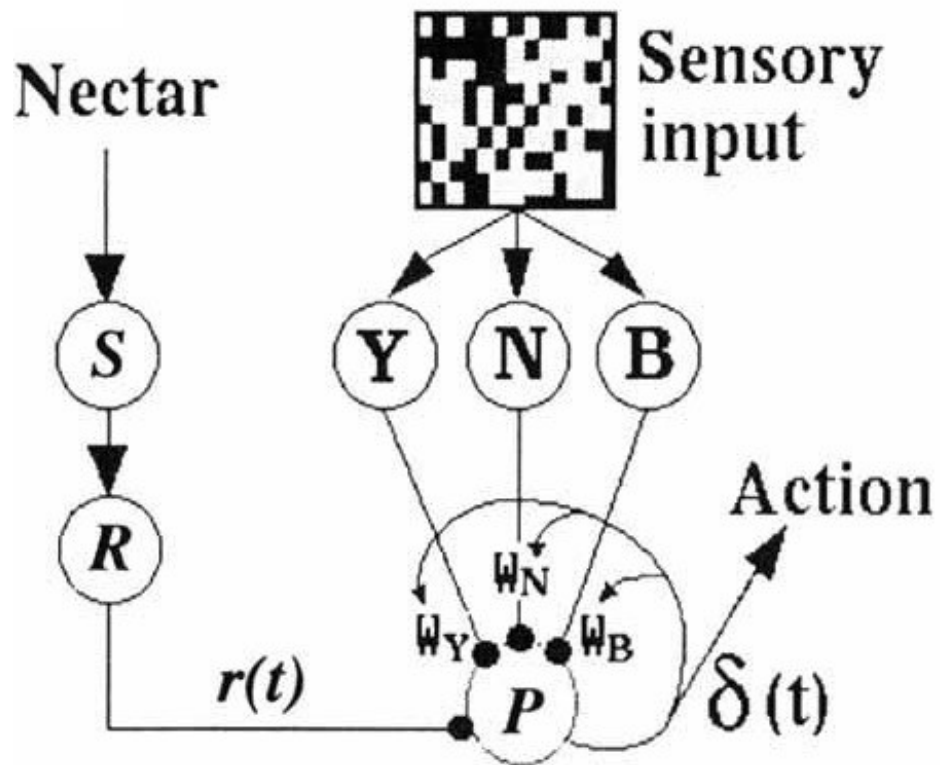
- Real's (1991) experiment:
  - Bumblebees foraged on artificial blue and yellow flowers.
  - Blue flowers contained 2  $\mu\text{l}$  of nectar.
  - Yellow flowers contained 6  $\mu\text{l}$  in one third of the flowers and no nectar in the remaining two thirds.
  - Blue and yellow flowers contained the same *average* amount of nectar.
- Results:
  - Bees favored the constant blue over the variable yellow flowers even though the mean reward was the same.
  - Bees forage equally from both flower types if the mean reward from yellow is made sufficiently large.

# Montague, Dayan, and Sejnowski (1995)

- Model of bee foraging behavior based on VUMmx1.
- Bee decides at each time step whether to randomly reorient.



# Neural Network Model



S: sucrose sensitive neuron; R: reward neuron;  
P: reward predicting neuron;  $\delta$ : prediction error signal

# TD Equations

$$\delta(t) = r(t) + \gamma V(t) - V(t-1)$$

Let  $\gamma = 1$ : no discounting

$$\begin{aligned}\delta(t) &= r(t) + \overset{i}{V}(t) - V(t-1) \\ &= r(t) + \dot{V}(t)\end{aligned}$$

$$V(t) = \sum_i w_i x_i(t)$$

$$\begin{aligned}\dot{V}(t) &= \sum_i w_i [x_i(t) - x_i(t-1)] \\ &= \sum_i w_i \dot{x}_i(t)\end{aligned}$$

$$\delta(t) = r(t) + \sum_i w_i \dot{x}_i(t)$$

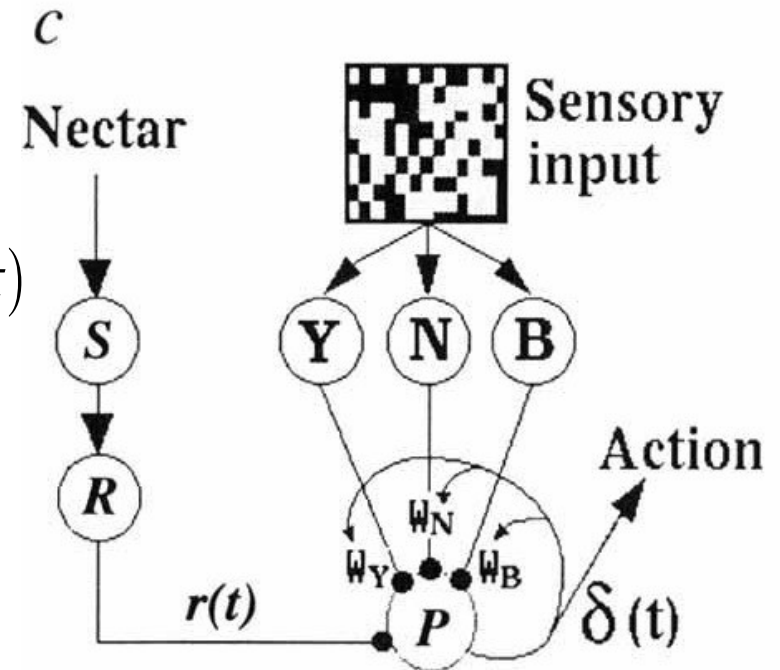
# Bee Foraging Model

$x_Y, x_B, x_N$  encode change in scene

$$\dot{V}(t) = w_b x_b(t) + w_y x_y(t) + w_n x_n(t)$$

$$\delta(t) = r(t) + \dot{V}(t)$$

$$\Delta w_i(t) = \lambda x_i(t-1) \cdot \delta(t)$$





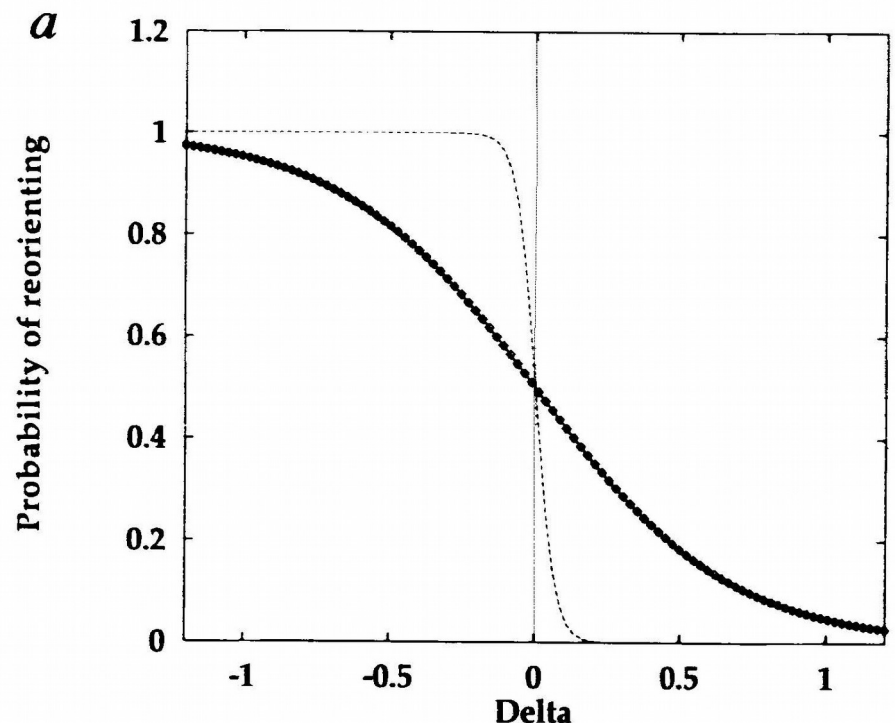
# Parameters

$w_B$  and  $w_Y$  are adaptable;  $w_N$  fixed at -0.5

Probability of reorienting:  $P_r(\delta(t)) = \frac{1}{1 + \exp(m \cdot \delta(t) + b)}$

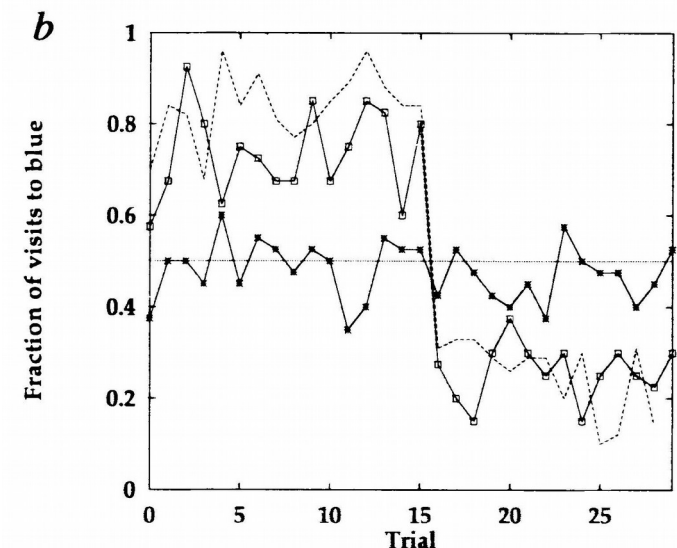
Learning rate  $\lambda = 0.9$

Volume of nectar reward determined by empirically derived utility curve.



# Theoretical Idea

- Unit P is analogous to VUMmx1.
- Nectar  $r(t)$  represents the reward, which can vary over time.
- At each time  $t$ ,  $\delta(t)$  determines the bee's next action: continue on present heading, or reorient.
- Weights are adjusted on encounters with flowers: they are updated according to the nectar reward.
- Model best matches the bee when  $\lambda = 0.9$ .
- Graph shows bee response to switch in contingencies on trial 15.



# An Aside: Honeybee Operant Learning

Honey bees can learn visual cues associated with nectar rewards

- Colors



- Shapes



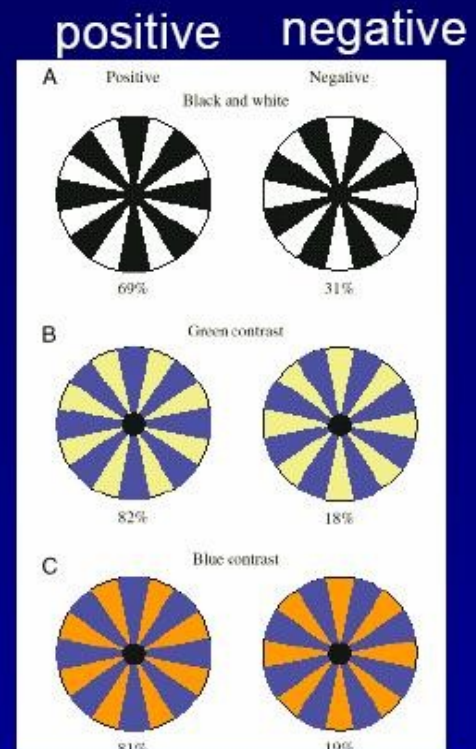
- Symmetry



- Complex patterns

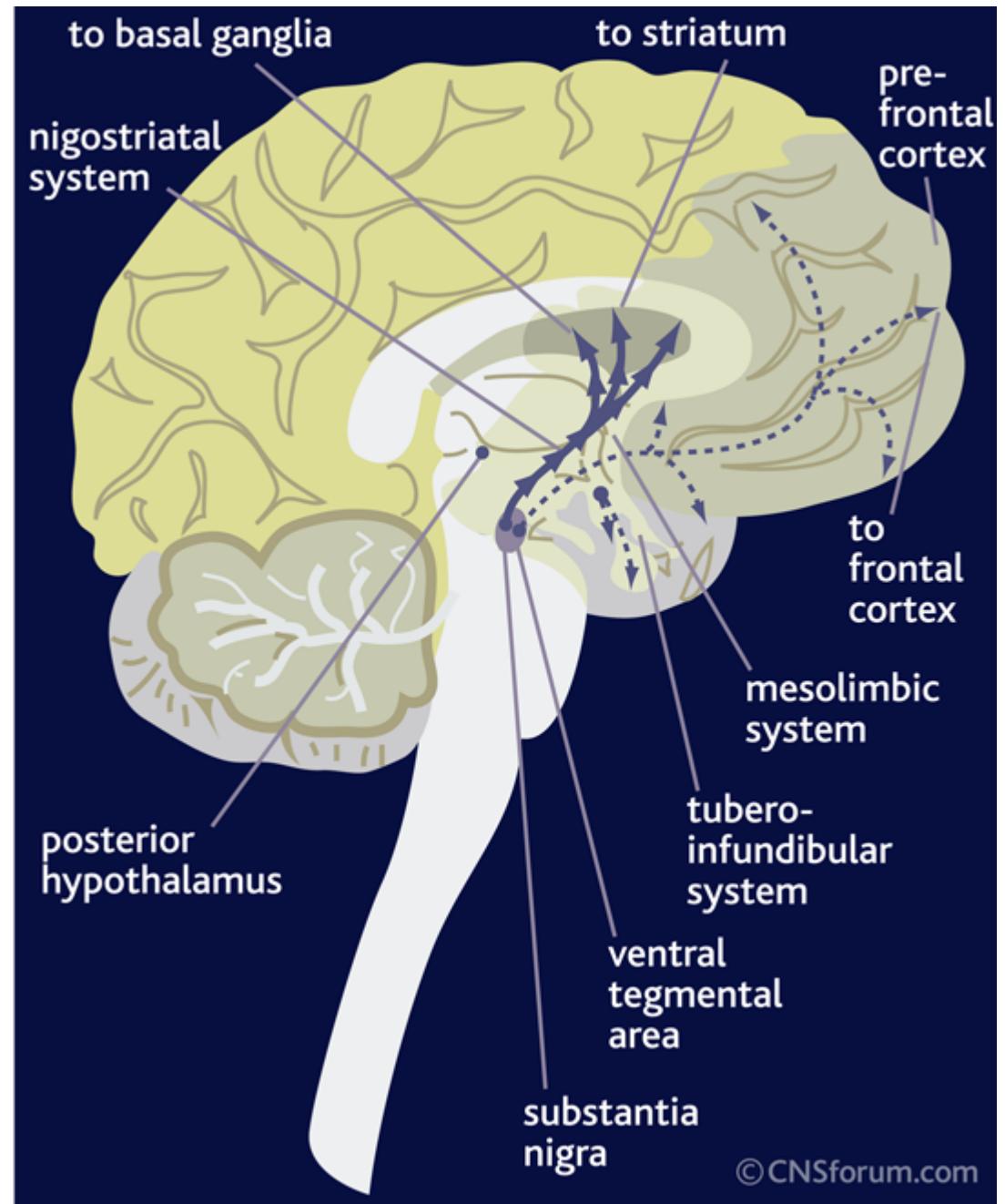


<http://web.neurobio.arizona.edu/gronenberg/nrsc581>



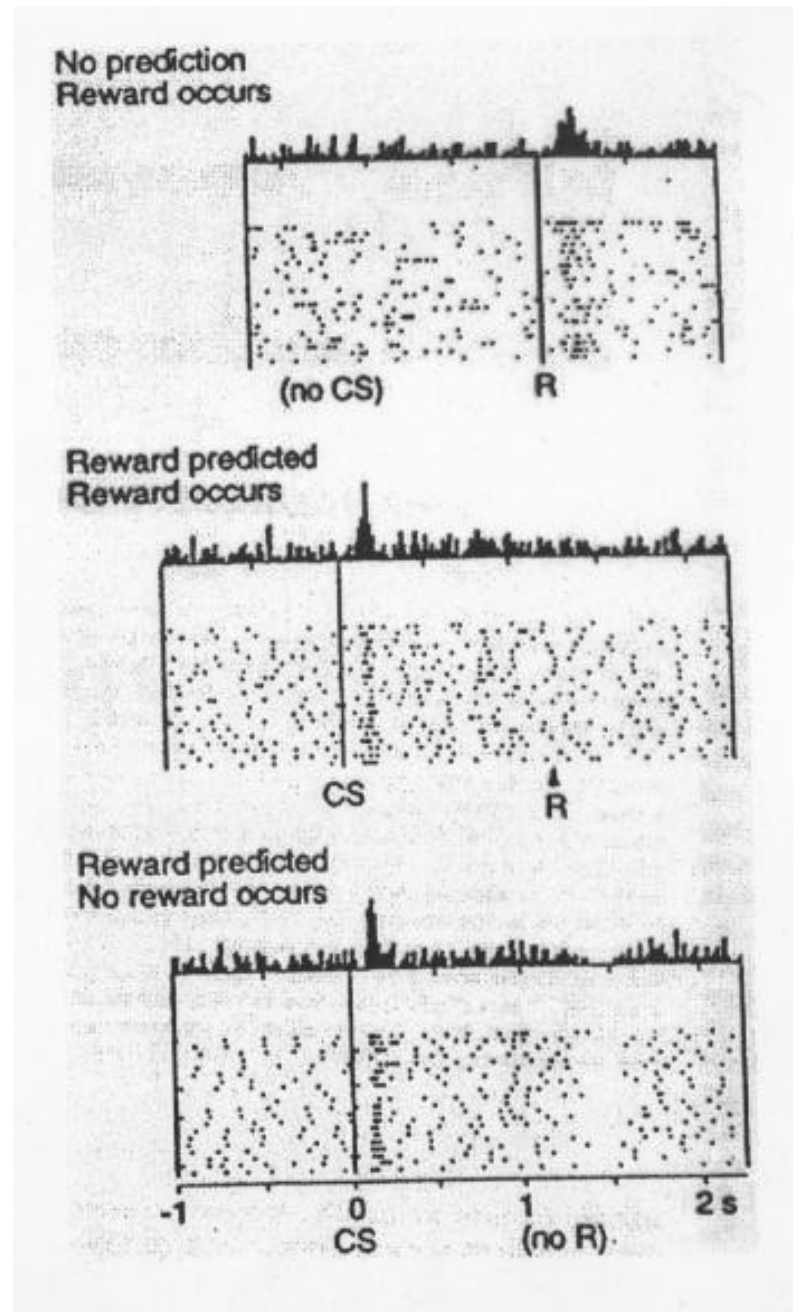
# Dopamine

- Involved in:
  - Addiction
  - Self-stimulation
  - Learning
  - Motor actions
  - Rewarding situations



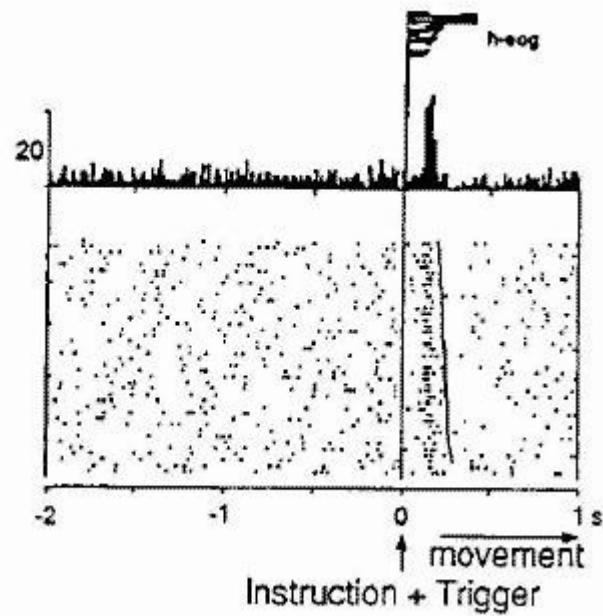
# Responses of Dopamine Neurons in Macaques

- Burst for unexpected reward
- Response transfers to reward predictors
- Pause at time of missed reward

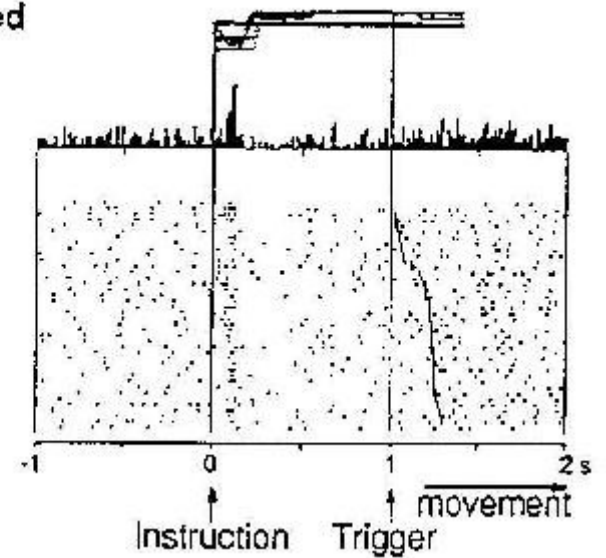




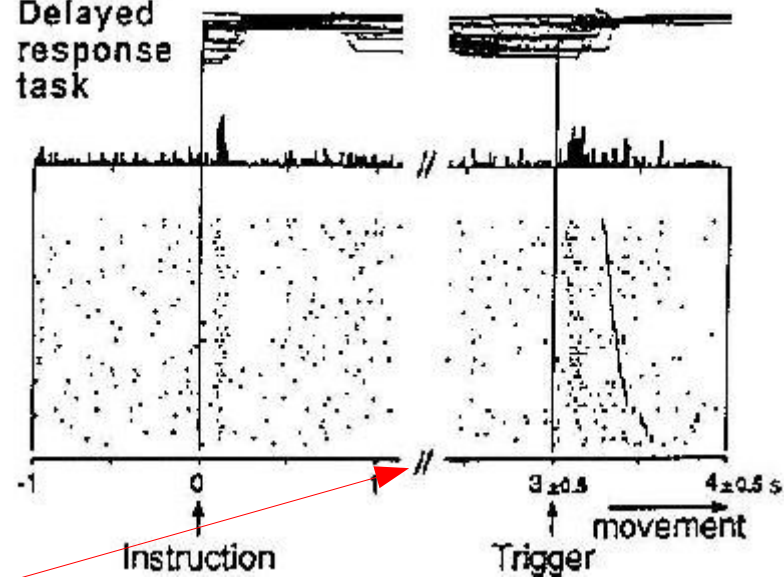
Spatial choice task



Instructed spatial task



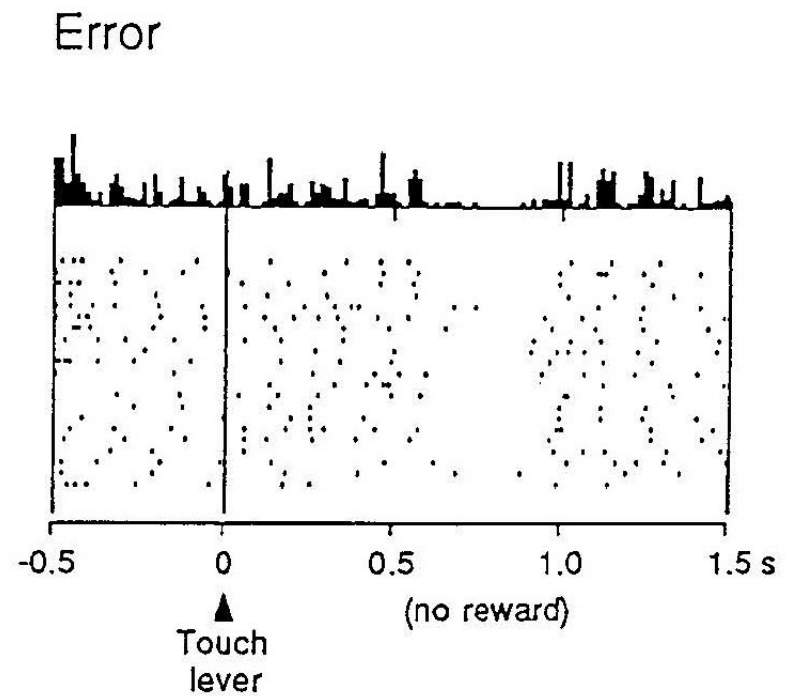
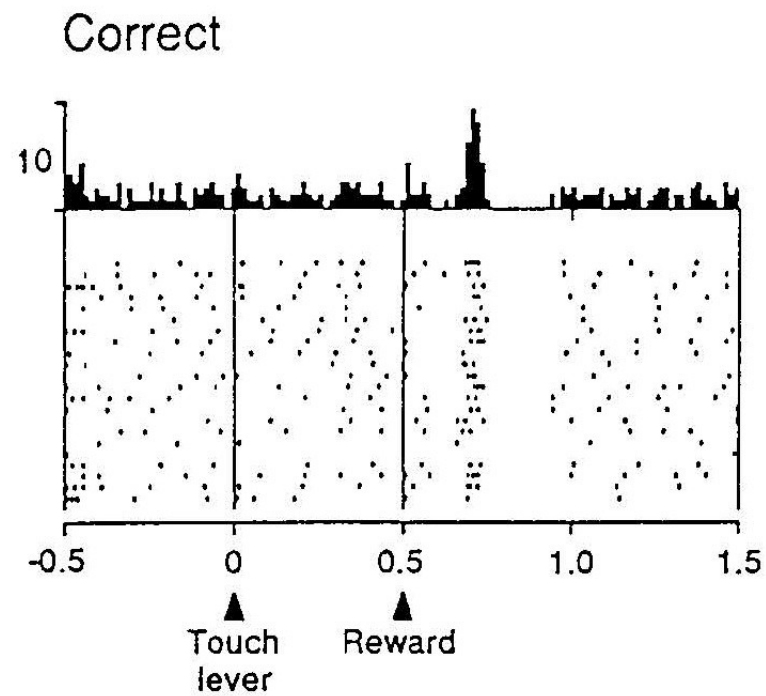
Delayed response task



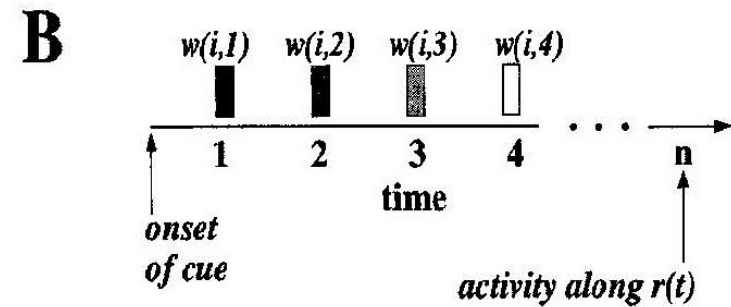
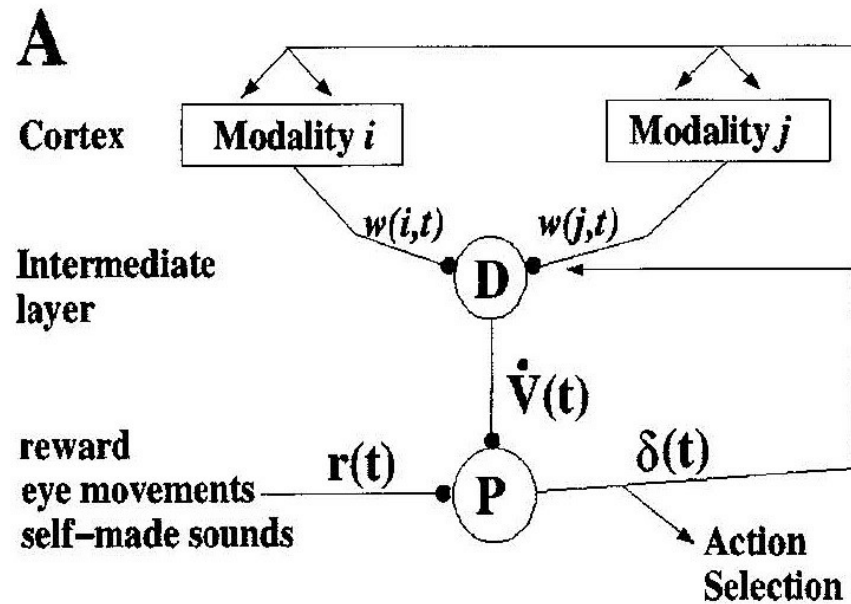
1.5 to 3.5 second delay



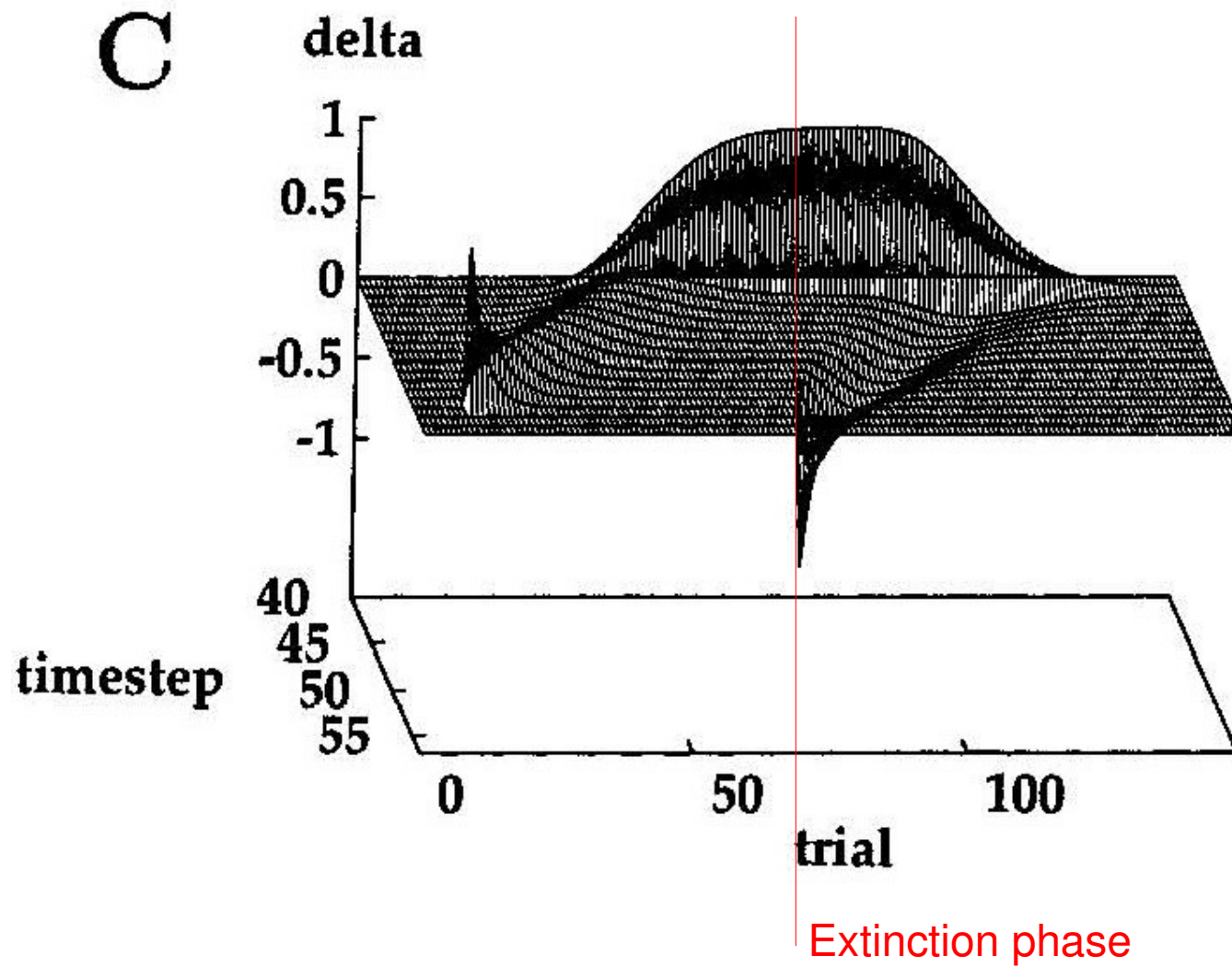
# Correct and Error Trials



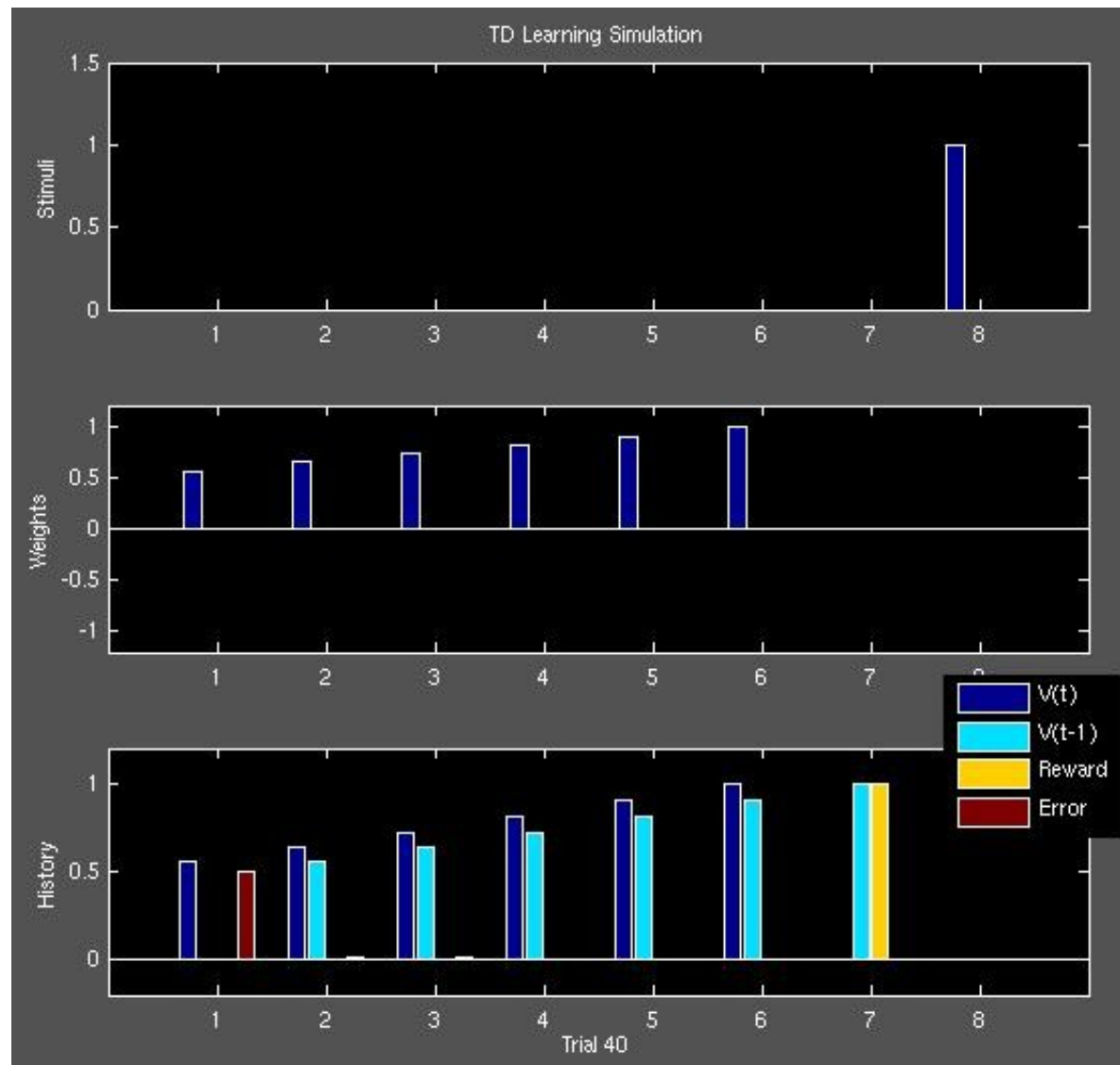
# Predictive Hebbian Learning Model



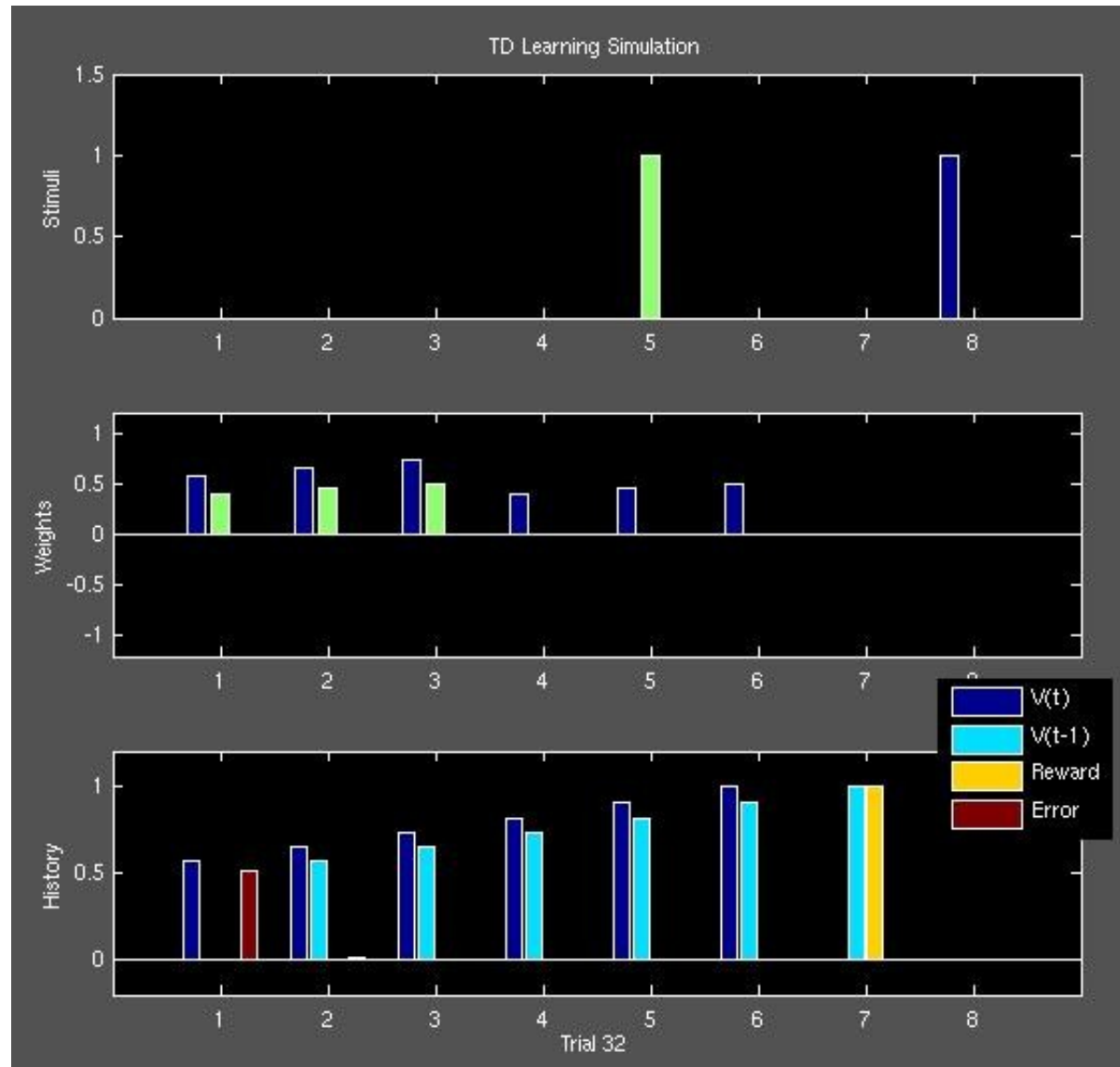
# Model Behavior



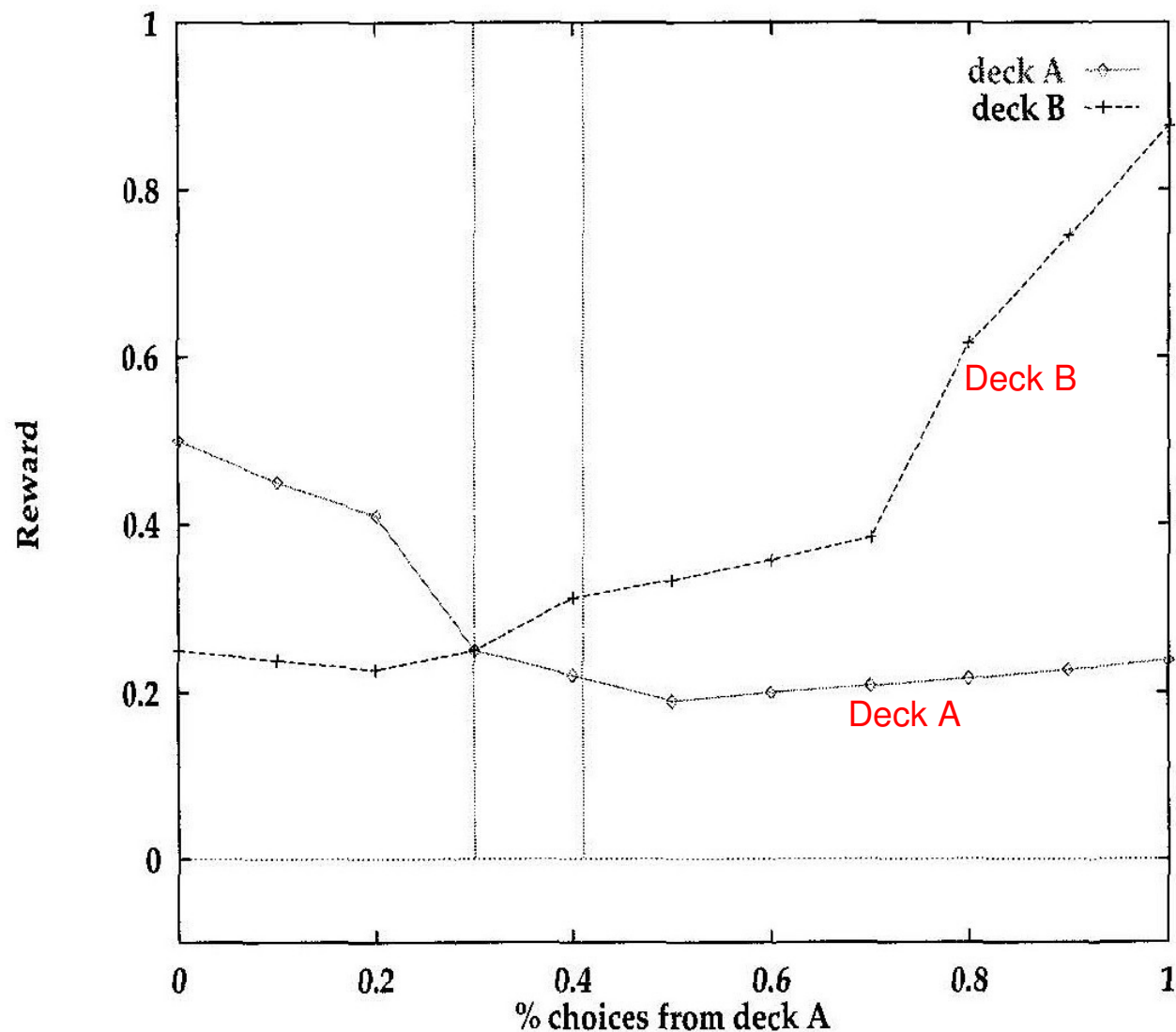
# TD Simulation 1



# TD Simulation 2



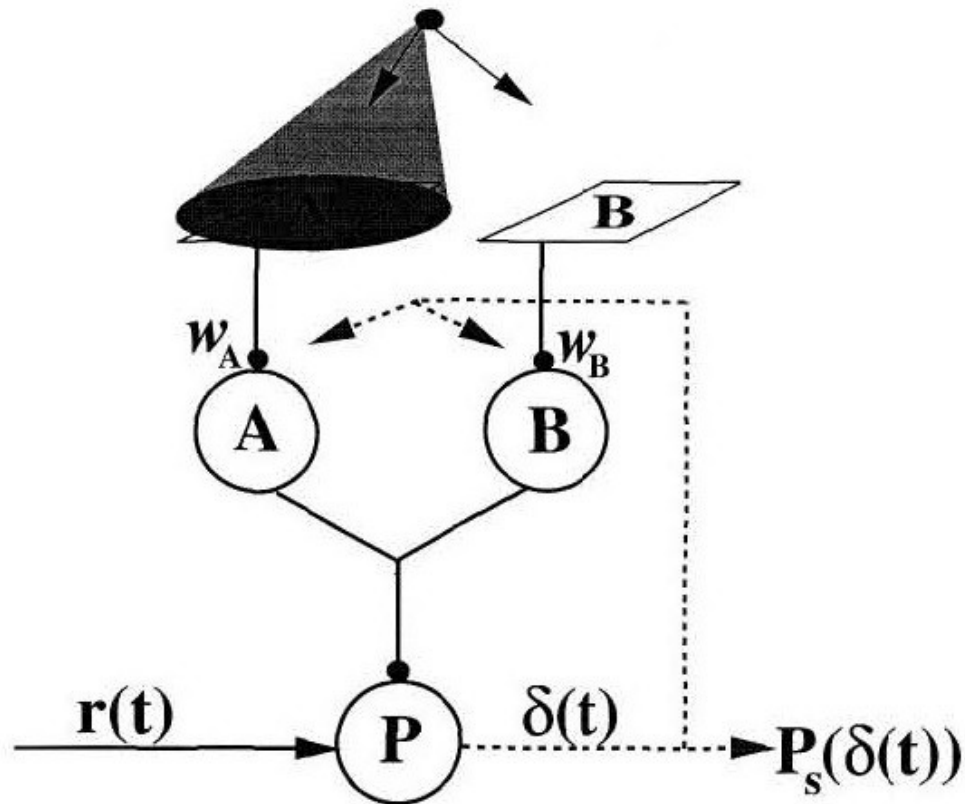
# Card Choice Task



Magnitude of reward is a function of the % choices from deck A in the last 40 draws. Optimal strategy lies to the right of the crossover point, but human subjects generally get stuck around the crossover point



# Card Choice Model



“Attention” alternates between decks A and B. Change in predicted reward determines  $P_s$ , the probability of selecting the current deck. The model tends to get stuck at the crossover point, as humans do.

# Conclusions

- Specific neurons distribute a signal that represents information about future expected reward (VUMmx1; dopamine neurons).
- These neurons have access to the precise time at which a reward will be delivered.
  - Serial compound stimulus makes this possible.
- Fluctuations in activity levels of these neurons represent errors in predictions about future reward.
- Montague et al. (1996) present a model of how such errors could be computed in a real brain.
- The theory makes predictions about human choice behaviors in simple decision-making tasks.