Feedforward Neural Networks: Revisiting Word Vectors and Text Classification

COM4513/6513 Natural Language Processing

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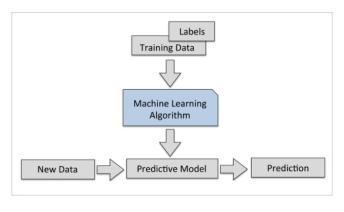
Week 6 Spring 2020



Admin

- The deadline for submitting Assignment 1 is now Friday 27/3, 23:59:59. Note that for people working on Windows, there is no need to test on Linux;
- Assignment 2 will be released on Monday 30/3 (deadline after Easter holidays) instead of next week;
- Labs have been suspended. For any questions, please use the Google Group. The TAs and me will try to provide answers as quickly as possible;
- Lectures are online from now via Blackboard Collaborate (MOLE)

In lecture 2...



Supervised ML

In lecture 2...

- Machine Learning Algorithm: Logistic Regression
- Binary and Multi-class

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Predict the class with the highest probability:

$$\hat{y} := \begin{cases} 0 & \text{if } P(y = 1 | \mathbf{x}; \mathbf{w}) < 0.5 \\ 1 & \text{otherwise} \end{cases}$$

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- LR directly maps input to output and only captures linear relationships in the data

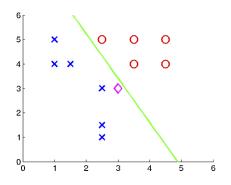
 Feedforward neural networks or deep feedforward networks or multilayer perceptrons

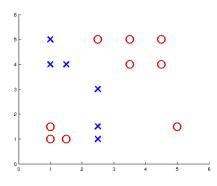
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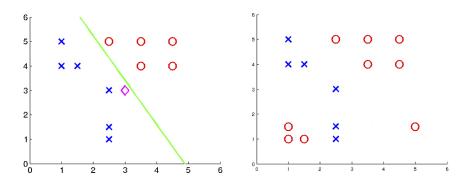
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- NLP applications: word vectors and text classification

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The righthand dataset is not linearly separable and cannot be learned with a linear model.

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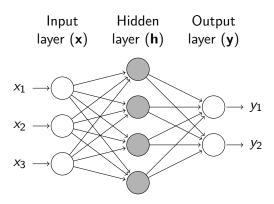
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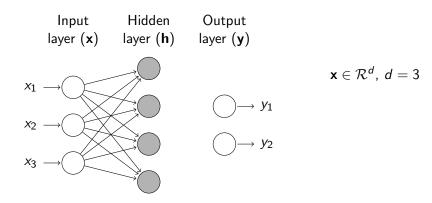
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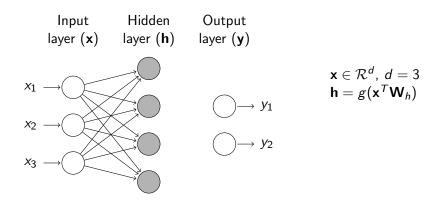
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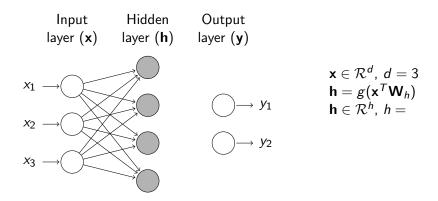
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- f_1 is the first **hidden layer** of the model, f_2 the second and so on. Number of hidden layers denote the **depth** of the model.
- Input denote the input layer
- The final layer to obtain the prediction is called the output layer (e.g. sigmoid, softmax)

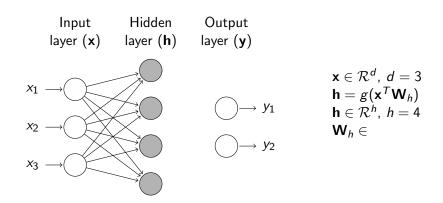
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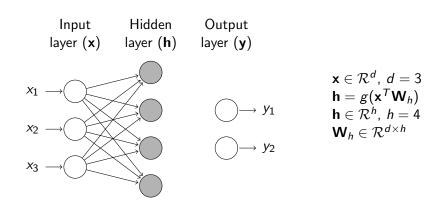


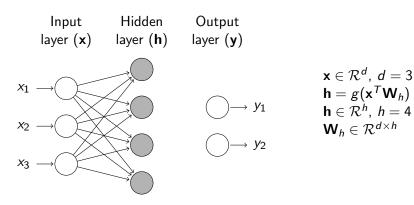






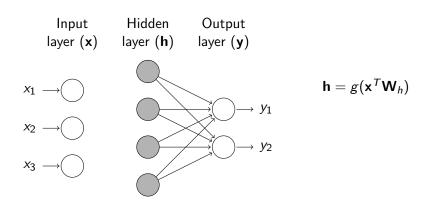


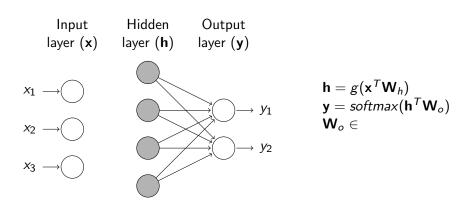


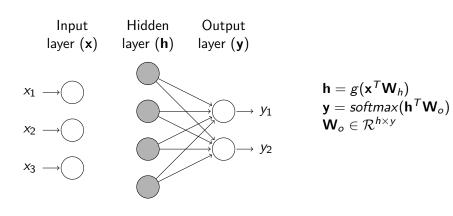


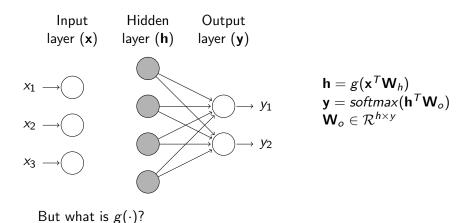
Extended to deeper architectures:

$$\mathbf{h_i} = g(\mathbf{h}_{i-1}^T \mathbf{W}_{h_i})$$









■ Applied on **hidden units**: elements of *h*

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Activation Functions

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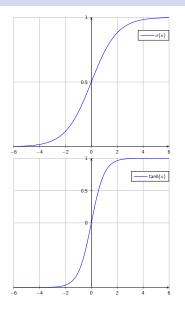
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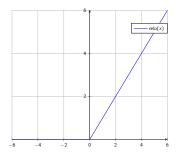
Rectified Linear Unit (ReLU):

$$g(z) = max(0, z)$$

And many more...

Activation Functions





Training: Stochastic Gradient Descent (SGD) recap

```
Input: D_{train} = \{(x_1, y_1)...(x_M, y_M)\}, D_{val} = \{(x_1, y_1)...(x_D, y_D)\},
         learning rate \eta, epochs e, tolerance t
initialize w with zeros
for each epoch e do
   randomise order in D<sub>train</sub>
  for each (x_i, y_i) in D_{train} do
      update \mathbf{w} = \mathbf{w} - \eta \nabla_{\mathbf{w}} L(\mathbf{w}; x_i; y_i)
   monitor training and validation loss
   if previous validation loss — current validation loss; smaller than t
      break
return w
```

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How to compute the gradient for the weights of the hidden layers?

Training: Backpropagation Algorithm

■ Forward Pass: Compute and store all the output values of all the hidden units (for each hidden layer) and the output layer

Training: Backpropagation Algorithm

- Forward Pass: Compute and store all the output values of all the hidden units (for each hidden layer) and the output layer
- **Backward Pass:** Compute the gradients for the output and hidden layers with respect to the cost function *L* and update the weights for each layer

Training: SGD and Backpropagation

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Input: D_{train} = \{(x_1, y_1)...(x_M, y_M)\}, D_{val} = \{(x_1, y_1)...(x_D, y_D)\},
       learning rate \eta, epochs e, tolerance t
initialise W_i \in W = \{W_1, ..., W_l\} for each layer (small random values)
for each epoch e do
  randomise order in Dtrain
  for each (x_i, y_i) in D_{train} do
     layer_outputs = forward_pass((x_i, y_i), W)
     W = backward_pass((x_i, y_i), W, L, layer_outputs)
  monitor training and validation loss
  if prev val loss — current val loss; smaller than t : break
return W
```

$$\boldsymbol{h}_0 \leftarrow \boldsymbol{x} \; (\text{input layer})$$

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 (input layer) for layer $k = 1, ..., l$ do

```
\begin{aligned} \mathbf{h}_0 \leftarrow \mathbf{x} \text{ (input layer)} \\ \mathbf{for layer} \ k = 1,.., \textit{I} \ \mathbf{do} \\ \mathbf{z}_k \leftarrow \mathbf{W_k} \mathbf{h}_{k-1} \\ \mathbf{h}_k \leftarrow g(\mathbf{z}) \\ \mathbf{end for} \end{aligned}
```

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\begin{aligned} \mathbf{h}_0 &\leftarrow \mathbf{x} \text{ (input layer)} \\ \mathbf{for} \text{ layer } k = 1, ..., I \text{ do} \\ \mathbf{z}_k &\leftarrow \mathbf{W_k} \mathbf{h}_{k-1} \\ \mathbf{h}_k &\leftarrow g(\mathbf{z}) \\ \mathbf{end for} \\ \text{Get prediction } \mathbf{\hat{y}} = \mathbf{h}_I \\ \text{Compute cross-entropy loss } L(\hat{y}, y) \\ \mathbf{return} \quad \mathbf{h}, \mathbf{z} \text{ for all layers} \end{aligned}
```

Propagate the gradients backwards from the loss to the input layer (i.e. how each layer's output should change to reduce error):

Compute gradient on the output layer $\mathbf{g} \leftarrow \nabla_{\hat{y}} L$

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for layer
$$k = I, I - 1, ..., 1$$
 do

Convert the gradient on the layer's output (h) into a gradient before the activation function (z):

$$\mathbf{g} \leftarrow \nabla_{\mathbf{z}_k} L = \mathbf{g} \odot f'(\mathbf{z}_k) \ (\odot \text{ element-wise, } f'(\cdot) \text{ deriv.})$$

Propagate the gradients backwards from the loss to the input layer (i.e. how each layer's output should change to reduce error):

Compute gradient on the output layer $\mathbf{g} \leftarrow \nabla_{\hat{y}} L$ for layer k = l, l - 1, ..., 1 do

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Compute gradients on weights:

$$\nabla_{W_k} L = \mathbf{g} h_{k-1}$$

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Compute gradients on weights:

$$\nabla_{W_k} L = \mathbf{g} h_{k-1}$$

Compute the gradients w.r.t. the next hidden layer:

$$\mathbf{g} \leftarrow \nabla_{h_{k-1}} L = \mathbf{g} W_k$$

return W

Propagate the gradients backwards from the loss to the input layer (i.e. how each layer's output should change to reduce error):

```
Compute gradient on the output layer \mathbf{g} \leftarrow \nabla_{\hat{\mathbf{v}}} L
for layer k = 1, 1 - 1, ..., 1 do
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    before the activation function (z):
    \mathbf{g} \leftarrow \nabla_{z_k} \mathbf{L} = \mathbf{g} \odot f'(\mathbf{z}_k) \ (\odot \text{ element-wise, } f'(\cdot) \text{ deriv.})
    Compute gradients on weights:
    \nabla_{W_k} L = \mathbf{g} h_{k-1}
    Compute the gradients w.r.t. the next hidden layer:
    \mathbf{g} \leftarrow \nabla_{h_k}, L = \mathbf{g} W_k
    Update current weights:
    W_k \leftarrow W_k - \eta \nabla_{W_k} L
end for
```

Regularisation

■ L2-regularisation in the weights of each layer (added in the loss function of each layer)

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- **Dropout**: randomly ignore a percentage (e.g. 20% or 50%) of layer outputs during training:
 - Apply a random binary mask after the activation function, i.e. elementwise multiplication with vector containing %20 0s in random positions

Design Choices

- How many layers?
- How many units per layer?
- What activation function(s)?

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- How many layers?
- How many units per layer?
- What activation function(s)?
- Architecture engineering vs feature engineering
- Theory says that we can approximate any function with one hidden layer, practice says different architectures work well for different problems

Implementation tips

- Learning objective non-convex: initialisation matters
 - start with small non-zero values
 - random restarts to escape local optima
- Greater learning capacity makes overfitting more likely: regularise
- Many open libraries are available: PyTorch, Tensorflow, MxNet, Keras etc.

Applications: Word Vectors

■ Lecture 1: word vectors by **counting** co-occurrences with context words

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- Lecture 1: word vectors by counting co-occurrences with context words
- Instead, use a feedforward network to predict a context word for a given word (and vice versa)
- Word2Vec (Mikolov et al., 2013) family, more recently supporting char n-grams (e.g. FastText)

■ Skip-gram model: Given a word predict its context word

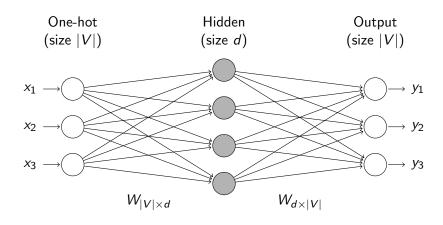
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- **Hidden layer**: One hidden layer of size vocabulary × hidden size (usually 300), linear activation function
- Output: softmax over the vocabulary to predict the correct context/target word respectively

Word2Vec Architecture



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- **Vector** of a word $x_i = W_i$, from the network weights
- Evaluation: standard approaches for word representation (see Lecture 1)
- Pre-trained word embeddings are widely re-used in other NLP tasks, i.e. transfer learning (more in Lecture 10)

Word2Vec: Implementation Details

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 - **Negative Sampling:** Update the weights for the positive word, plus the weights for a small number (5-20) other words that we want to output 0
 - Subsampling frequent words to decrease the number of training examples

Applications: Text Classification

■ **Approach 1:** Pass BOW vectors into a series of hidden layers (extending the LR model in Lecture 2)

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Applications: Text Classification

- **Approach 1:** Pass BOW vectors into a series of hidden layers (extending the LR model in Lecture 2)
- Approach 2: Pass one-hot word vectors through an embedding layer to obtain embeddings for each word in a document which are subsequently concatenated (or added/averaged) and passed through a series of hidden layers
- Approach 2 is more contemporary and usually the embedding layer is pre-trained (e.g. using Word2Vec) and is not updated during training (Lecture 10: transfer learning)

Bibliographhy

- Chapters 6-8 from Goodfellow et al.
- Sections 3-6 from Goldberg
- Tutorial on backprop by D. Stansbury
- Word2vec tutorial by Chris McCormick

Coming up next..

Information extraction and Ethics by Prof. Jochen Leidner