

# Time Complexity Analysis

1. (1Pts) For each of the following expressions, what is the order of growth (in  $\Theta$ (Theta) notation) that best describes it?

For example:  $10 \cdot n \rightarrow \Theta(n)$

- 1)  $3n^2 + 7n^3 + 4 \rightarrow \Theta(n^3)$
- 2)  $10\log(n) + 5n \rightarrow \Theta(n)$
- 3)  $3^n + n^2 \rightarrow \Theta(3^n)$
- 4)  $100n + n\log(n) \rightarrow \Theta(n \log(n))$
- 5)  $5 + 40 \rightarrow \Theta(1)$
- 6)  $\log(n) + 4n \rightarrow \Theta(n)$

2. (2Pts) Please specify the time complexity for the following programs.

```
def program1():  
    list = [1,2,3,4,5,6,7,8]  
    even_list = []  
    for i in range(len(list)):  
        if i % 2 == 0:  
            even_list.append(i)  
  
    return even_list  
  
 $\Theta(n)$ 
```

```
def program2():  
    list1 = [1,2,3,4,5,7]  
    list2 = [3,4,5,7,8,9]  
  
    output_list1 = [i for i in list1]  
  
    output_list2 = []  
    for i in list1:  
        for j in list2:  
            output_list2 += [i,j]
```

```
return (output_list1, output_list2)
```

$\Theta(n^2)$

```
def program3(n):
```

```
    epsilon = 0.01
```

```
    low = 0
```

```
    high = n
```

```
    ans = (high + low) / 2
```

```
    while abs(ans**4 - n) >= epsilon:
```

```
        if ans**4 > n:
```

```
            high = ans
```

```
        else:
```

```
            low = ans
```

```
        ans = (high + low) / 2
```

```
    return ans
```

$\Theta(\log n)$

```
def program4(n):
```

```
    """ n > 0 """
```

```
    answer = 0
```

```
    while n > 0:
```

```
        answer += n%10
```

```
        n = int(n/10)
```

```
    return answer
```

$\Theta(\log n)$