

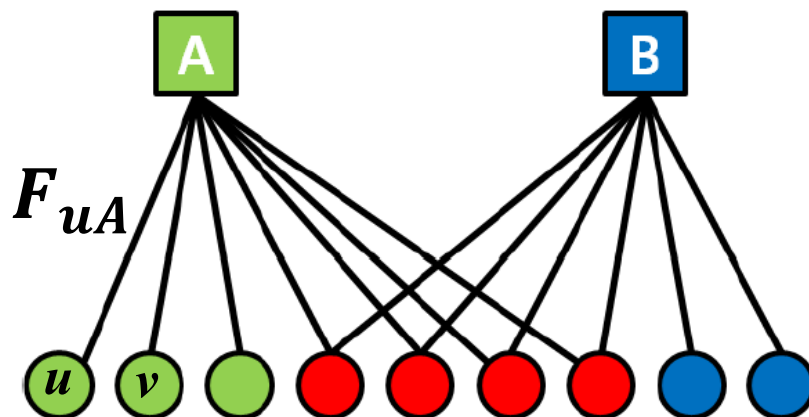
From AGM to BIGCLAM

Mining of Massive Datasets
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From AGM to BigCLAM

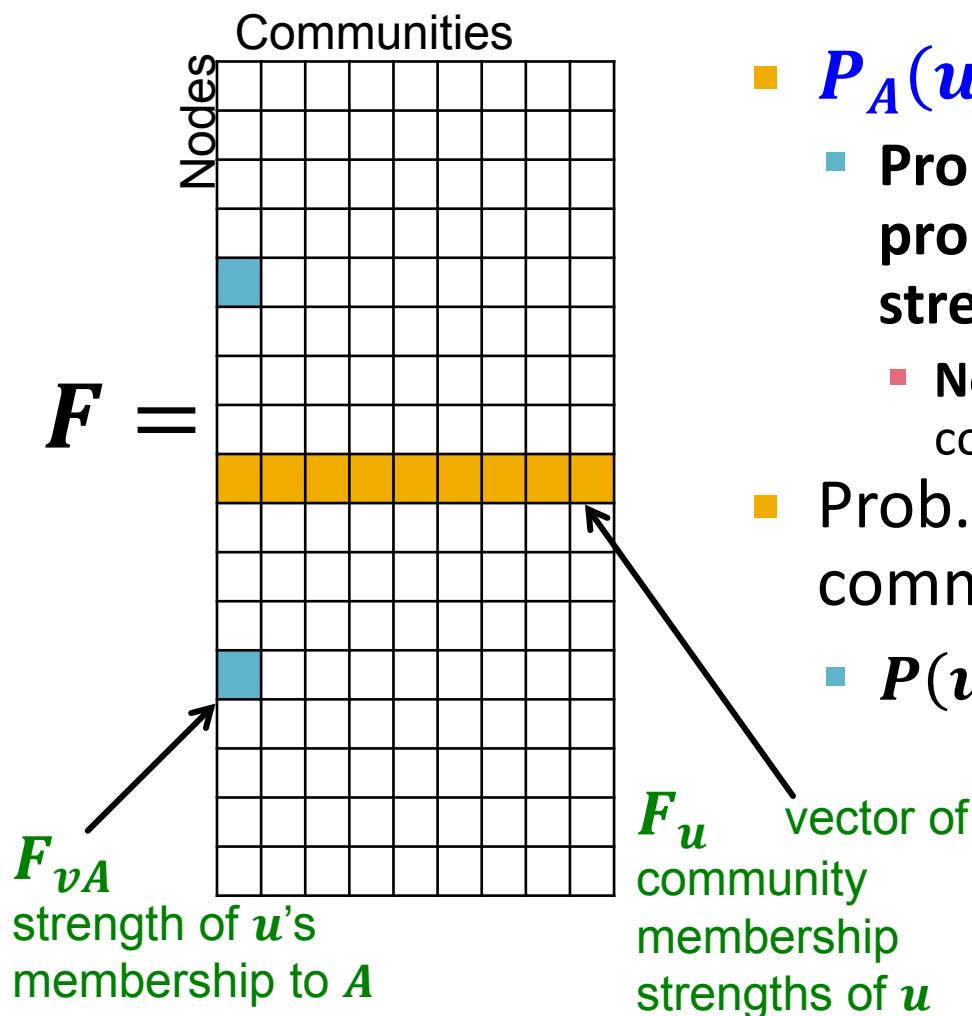
- **Relaxation: Memberships have strengths**



- F_{uA} : The membership strength of node u to community A ($F_{uA} = 0$: no membership)
- Each community A links nodes independently:
$$P_A(u, v) = 1 - \exp(-F_{uA} \cdot F_{vA})$$

Factor Matrix F

■ Community membership strength matrix F



- $P_A(u, v) = 1 - \exp(-F_{uA} \cdot F_{vA})$
 - Probability of connection is proportional to the product of strengths
 - Notice: If one node doesn't belong to the community ($F_{uC} = 0$) then $P(u, v) = 0$
- Prob. that **at least one** common community C links the nodes:
 - $P(u, v) = 1 - \prod_C (1 - P_C(u, v))$

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- Community **A** links nodes **u**, **v** independently:

$$P_A(u, v) = 1 - \exp(-F_{uA} \cdot F_{vA})$$

- Then prob. at least one common **C** links them:

$$\begin{aligned} P(u, v) &= 1 - \prod_C (1 - P_C(u, v)) \\ &= 1 - \exp(-\sum_C F_{uC} \cdot F_{vC}) \\ &= 1 - \exp(-F_u \cdot F_v^T) \end{aligned}$$

- For example:

$$F_u: \begin{array}{|c|c|c|c|} \hline 0 & 1.2 & 0 & 0.2 \\ \hline \end{array}$$

$$F_v: \begin{array}{|c|c|c|c|} \hline 0.5 & 0 & 0 & 0.8 \\ \hline \end{array}$$

$$F_w: \begin{array}{|c|c|c|c|} \hline 0 & 1.8 & 1 & 0 \\ \hline \end{array}$$

Then: $F_u \cdot F_v^T = 0.16$

And: $P(u, v) = 1 - \exp(-0.16) = 0.14$

But: $P(u, w) = 0.88$

$$P(v, w) = 0$$

Node community
membership strengths