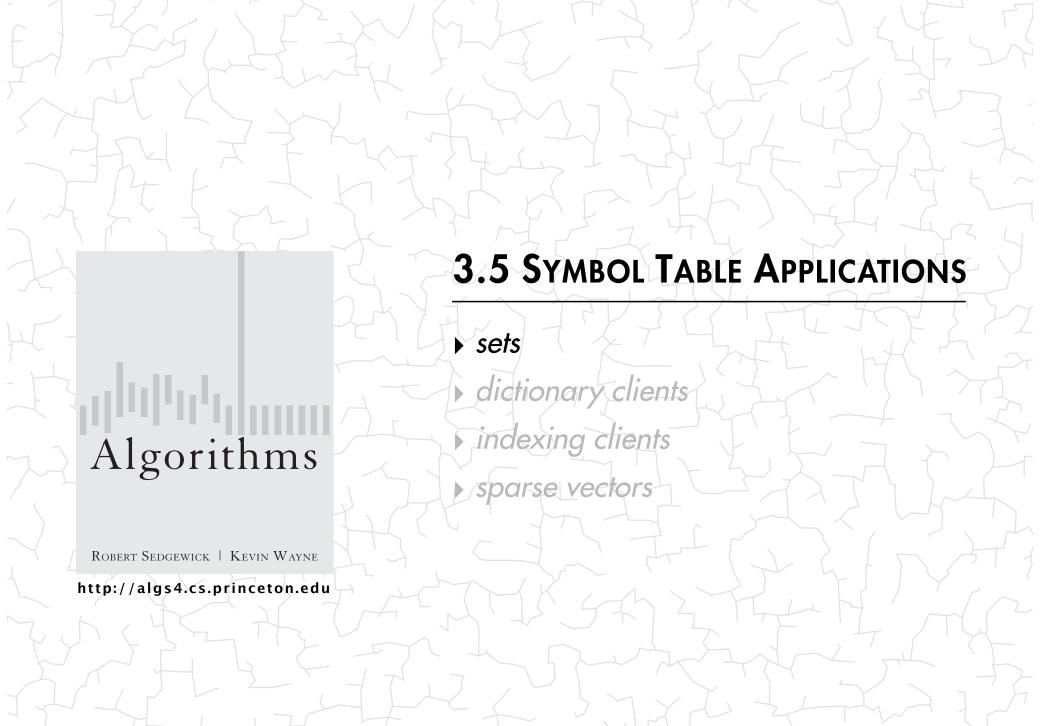


- sets
- dictionary clients
- indexing clients
- sparse vectors



Set API

Mathematical set. A collection of distinct keys.

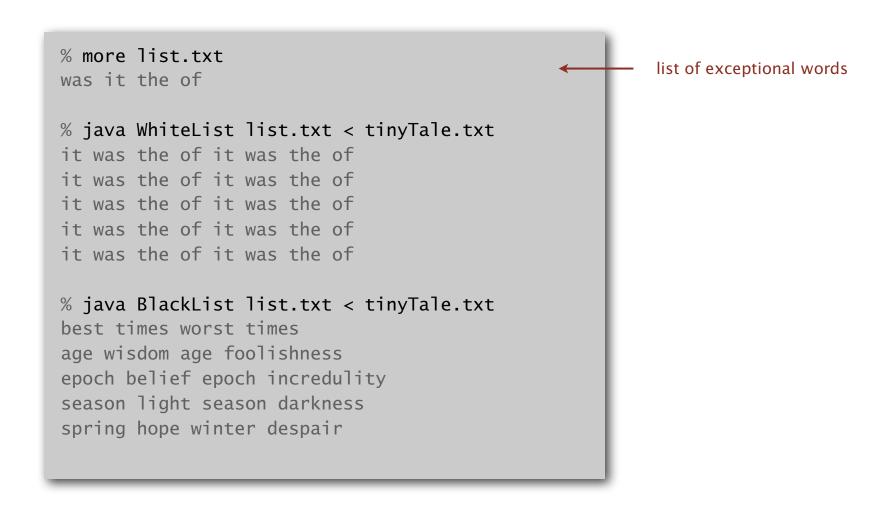
public class SET <k< th=""><th>y extends</th><th>Comparable<key>></key></th></k<>	y extends	Comparable <key>></key>
--	-----------	----------------------------

	SET()	create an empty set	
void	add(Key key)	add the key to the set	
boolean	<pre>contains(Key key)</pre>	is the key in the set?	
void	remove(Key key)	remove the key from the set	
int	size()	return the number of keys in the set	
Iterator <key></key>	iterator()	iterator through keys in the set	

Q. How to implement?

Exception filter

- Read in a list of words from one file.
- Print out all words from standard input that are { in, not in } the list.



Exception filter applications

- · Read in a list of words from one file.
- Print out all words from standard input that are { in, not in } the list.

application	purpose	key	in list
spell checker	identify misspelled words	word	dictionary words
browser	mark visited pages	URL	visited pages
parental controls	block sites	URL	bad sites
chess	detect draw	board	positions
spam filter	eliminate spam	IP address	spam addresses
credit cards	check for stolen cards	number	stolen cards

Exception filter: Java implementation

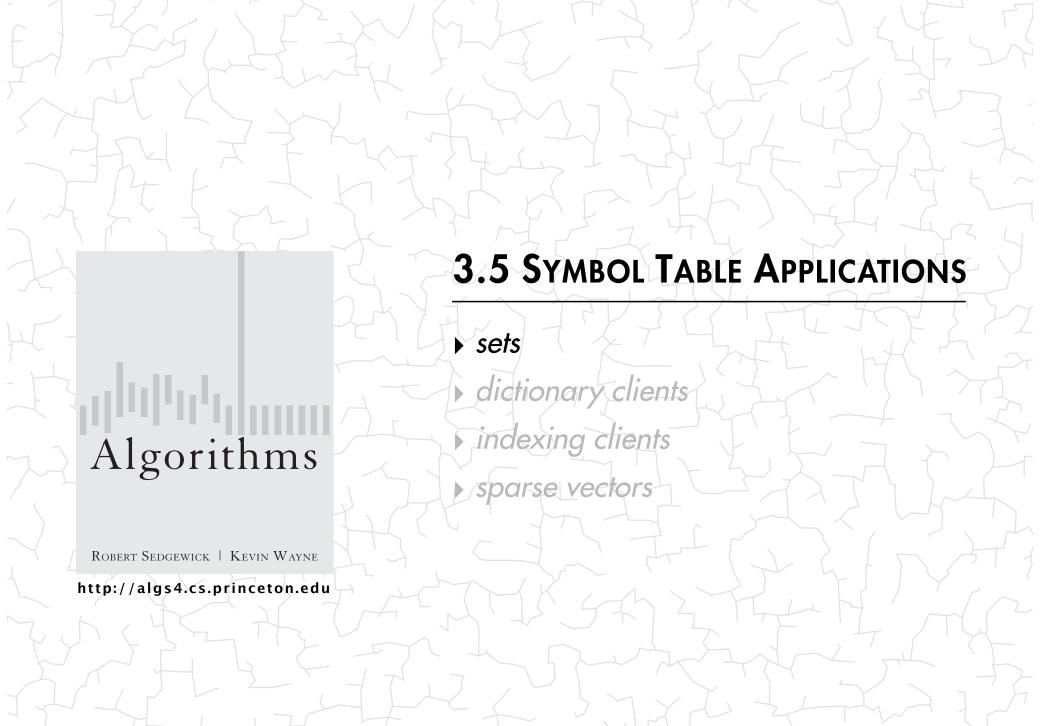
- Read in a list of words from one file.
- Print out all words from standard input that are in the list.

```
public class WhiteList
   public static void main(String[] args)
                                                            create empty set of strings
      SET<String> set = new SET<String>();
      In in = new In(args[0]);
      while (!in.isEmpty())
                                                            read in whitelist
         set.add(in.readString());
      while (!StdIn.isEmpty())
         String word = StdIn.readString();
                                                            print words not in list
         if (set.contains(word))
             StdOut.println(word);
```

Exception filter: Java implementation

- Read in a list of words from one file.
- Print out all words from standard input that are not in the list.

```
public class BlackList
   public static void main(String[] args)
                                                           create empty set of strings
      SET<String> set = new SET<String>();
      In in = new In(args[0]);
      while (!in.isEmpty())
                                                            read in whitelist
         set.add(in.readString());
      while (!StdIn.isEmpty())
         String word = StdIn.readString();
                                                            print words not in list
         if (!set.contains(word))
             StdOut.println(word);
```



- dictionary clients
- indexing clients
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Algorithms

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Dictionary lookup

Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

Ex 1. DNS lookup.

domain name is key IP is value % java LookupCSV ip.csv 0 1 adobe.com 192.150.18.60 www.princeton.edu 128.112.128.15 domain name ebay.edu IP is kev is value Not found % java LookupCSV ip.csv 1 0 128.112.128.15 www.princeton.edu 999.999.999.99 Not found

```
% more ip.csv
www.princeton.edu,128.112.128.15
www.cs.princeton.edu,128.112.136.35
www.math.princeton.edu,128.112.18.11
www.cs.harvard.edu,140.247.50.127
www.harvard.edu,128.103.60.24
www.yale.edu,130.132.51.8
www.econ.yale.edu,128.36.236.74
www.cs.yale.edu,128.36.229.30
espn.com,199.181.135.201
yahoo.com,66.94.234.13
msn.com,207.68.172.246
google.com,64.233.167.99
baidu.com,202.108.22.33
yahoo.co.jp,202.93.91.141
sina.com.cn,202.108.33.32
ebay.com,66.135.192.87
adobe.com, 192.150.18.60
163.com, 220.181.29.154
passport.net,65.54.179.226
tom.com,61.135.158.237
nate.com, 203.226.253.11
cnn.com,64.236.16.20
daum.net,211.115.77.211
blogger.com, 66.102.15.100
fastclick.com, 205.180.86.4
wikipedia.org, 66.230.200.100
rakuten.co.jp,202.72.51.22
```

Dictionary lookup

Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

Ex 2. Amino acids.

% java LookupCSV amino.csv 0 3 ACT Threonine TAG Stop CAT Histidine

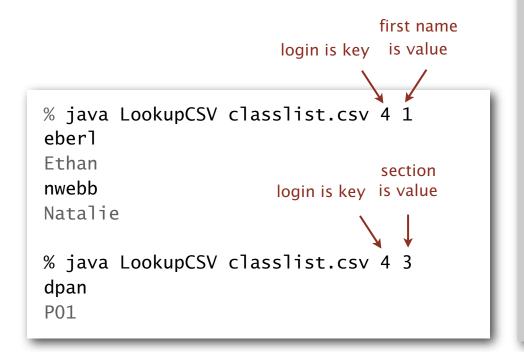
```
% more amino.csv
TTT, Phe, F, Phenylalanine
TTC, Phe, F, Phenylalanine
TTA, Leu, L, Leucine
TTG, Leu, L, Leucine
TCT, Ser, S, Serine
TCC, Ser, S, Serine
TCA, Ser, S, Serine
TCG, Ser, S, Serine
TAT, Tyr, Y, Tyrosine
TAC, Tyr, Y, Tyrosine
TAA, Stop, Stop, Stop
TAG, Stop, Stop, Stop
TGT, Cys, C, Cysteine
TGC, Cys, C, Cysteine
TGA, Stop, Stop, Stop
TGG, Trp, W, Tryptophan
CTT, Leu, L, Leucine
CTC, Leu, L, Leucine
CTA, Leu, L, Leucine
CTG, Leu, L, Leucine
CCT, Pro, P, Proline
CCC, Pro, P, Proline
CCA, Pro, P, Proline
CCG, Pro, P, Proline
CAT, His, H, Histidine
CAC, His, H, Histidine
CAA, Gln, Q, Glutamine
CAG, Gln, Q, Glutamine
CGT, Arg, R, Arginine
CGC, Arg, R, Arginine
```

Dictionary lookup

Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

Ex 3. Class list.



% more classlist.csv 13, Berl, Ethan Michael, P01, eberl 12, Cao, Phillips Minghua, P01, pcao 11, Chehoud, Christel, P01, cchehoud 10, Douglas, Malia Morioka, P01, malia 12, Haddock, Sara Lynn, P01, shaddock 12, Hantman, Nicole Samantha, P01, nhantman 11, Hesterberg, Adam Classen, PO1, ahesterb 13, Hwang, Roland Lee, P01, rhwang 13, Hyde, Gregory Thomas, P01, ghyde 13, Kim, Hyunmoon, P01, hktwo 12, Korac, Damjan, P01, dkorac 11, MacDonald, Graham David, P01, gmacdona 10, Michal, Brian Thomas, P01, bmichal 12, Nam, Seung Hyeon, P01, seungnam 11, Nastasescu, Maria Monica, PO1, mnastase 11, Pan, Di, PO1, dpan 12, Partridge, Brenton Alan, P01, bpartrid 13, Rilee, Alexander, P01, arilee 13, Roopakalu, Ajay, P01, aroopaka 11, Sheng, Ben C, P01, bsheng 12, Webb, Natalie Sue, P01, nwebb

Dictionary lookup: Java implementation

```
public class LookupCSV
   public static void main(String[] args)
      In in = new In(args[0]);
                                                                         process input file
      int keyField = Integer.parseInt(args[1]);
      int valField = Integer.parseInt(args[2]);
      ST<String, String> st = new ST<String, String>();
      while (!in.isEmpty())
         String line = in.readLine();
         String[] tokens = line.split(",");
                                                                         build symbol table
         String key = tokens[keyField];
         String val = tokens[valField];
         st.put(key, val);
      while (!StdIn.isEmpty())
                                                                         process lookups
         String s = StdIn.readString();
                                                                         with standard I/O
         if (!st.contains(s)) StdOut.println("Not found");
                               StdOut.println(st.get(s));
         else
   }
```

- dictionary clients
- indexing clients
- sparse vectors

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Algorithms

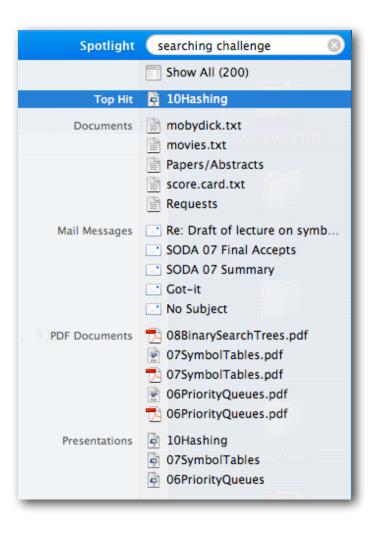
- sets
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Algorithms

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File indexing

Goal. Index a PC (or the web).



File indexing

Goal. Given a list of files specified, create an index so that you can efficiently find all files containing a given query string.

```
% ls *.txt
aesop.txt magna.txt moby.txt
sawyer.txt tale.txt

% java FileIndex *.txt

freedom
magna.txt moby.txt tale.txt

whale
moby.txt

lamb
sawyer.txt aesop.txt
```

```
% ls *.java
BlackList.java Concordance.java
DeDup.java FileIndex.java ST.java
SET.java WhiteList.java

% java FileIndex *.java

import
FileIndex.java SET.java ST.java

Comparator
null
```

Solution. Key = query string; value = set of files containing that string.

File indexing

```
import java.io.File;
public class FileIndex
   public static void main(String[] args)
                                                                           symbol table
      ST<String, SET<File>> st = new ST<String, SET<File>>();
      for (String filename : args) {
                                                                           list of file names
         File file = new File(filename);
                                                                           from command line
         In in = new In(file);
         while (!in.isEmpty())
                                                                           for each word in file,
             String key = in.readString();
                                                                           add file to
             if (!st.contains(key))
                                                                           corresponding set
                st.put(key, new SET<File>());
             SET<File> set = st.get(key);
             set.add(file);
      while (!StdIn.isEmpty())
         String query = StdIn.readString();
                                                                           process queries
         StdOut.println(st.get(query));
   }
```

Book index

Goal. Index for an e-book.

Index

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Concordance

Goal. Preprocess a text corpus to support concordance queries: given a word, find all occurrences with their immediate contexts.

% java Concordance tale.txt cities tongues of the two *cities* that were blended in majesty their turnkeys and the *majesty* of the law fired me treason against the *majesty* of the people in of his most gracious *majesty* king george the third princeton no matches

Concordance

```
public class Concordance
   public static void main(String[] args)
      In in = new In(args[0]);
      String[] words = in.readAllStrings();
      ST<String, SET<Integer>> st = new ST<String, SET<Integer>>();
      for (int i = 0; i < words.length; <math>i++)
                                                                               read text and
      {
                                                                               build index
         String s = words[i];
         if (!st.contains(s))
            st.put(s, new SET<Integer>());
         SET<Integer> set = st.get(s);
         set.add(i);
      while (!StdIn.isEmpty())
                                                                             process queries
         String query = StdIn.readString();
                                                                               and print
         SET<Integer> set = st.get(query);
                                                                              concordances
         for (int k : set)
             // print words[k-4] to words[k+4]
```

- sets
- dictionary clients
- indexing clients
- sparse vectors

Algorithms

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sets

dictionary clients

indexing clients

sparse vectors

Algorithms

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Matrix-vector multiplication (standard implementation)

```
      a[][]
      x[]
      b[]

      0 .90 0 0 0 0
      .05
      .036

      0 0 .36 .36 .18
      .04
      .297

      0 0 0 .90 0
      .36
      =
      .333

      .90 0 0 0 0
      .37
      .045

      .47 0 .47 0 0
      .19
      .1927
```

```
double[][] a = new double[N][N];
double[] x = new double[N];
double[] b = new double[N];
...

// initialize a[][] and x[]
...

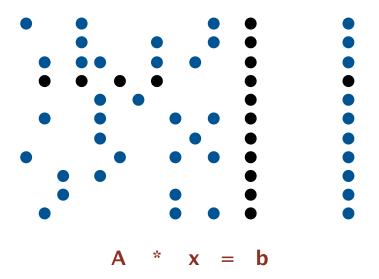
for (int i = 0; i < N; i++)

    sum = 0.0;
    for (int j = 0; j < N; j++)
        sum += a[i][j]*x[j];
    b[i] = sum;
}</pre>
```

Sparse matrix-vector multiplication

Problem. Sparse matrix-vector multiplication.

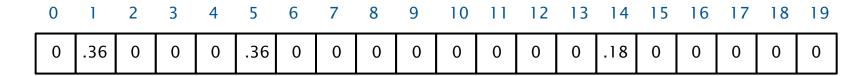
Assumptions. Matrix dimension is 10,000; average nonzeros per row ~ 10.



Vector representations

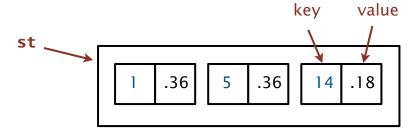
1d array (standard) representation.

- Constant time access to elements.
- Space proportional to N.



Symbol table representation.

- Key = index, value = entry.
- Efficient iterator.
- Space proportional to number of nonzeros.



Sparse vector data type

```
public class SparseVector
                                                       HashST because order not important
   private HashST<Integer, Double> v;
   public SparseVector()
                                                       empty ST represents all 0s vector
   { v = new HashST<Integer, Double>();
   public void put(int i, double x)
                                                       a[i] = value
   { v.put(i, x); }
   public double get(int i)
      if (!v.contains(i)) return 0.0;
                                                       return a[i]
      else return v.get(i);
   public Iterable<Integer> indices()
      return v.keys(); }
   public double dot(double[] that)
                                                        dot product is constant
                                                        time for sparse vectors
       double sum = 0.0;
       for (int i : indices())
           sum += that[i]*this.get(i);
       return sum;
```

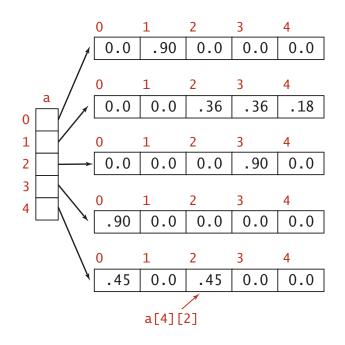
Matrix representations

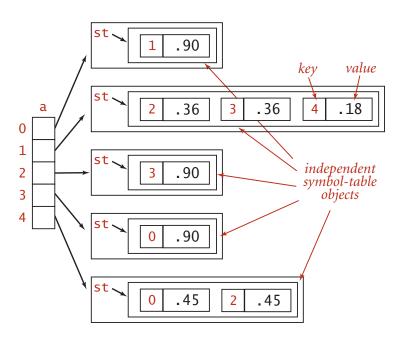
2D array (standard) matrix representation: Each row of matrix is an array.

- Constant time access to elements.
- Space proportional to N².

Sparse matrix representation: Each row of matrix is a sparse vector.

- Efficient access to elements.
- Space proportional to number of nonzeros (plus N).





Sparse matrix-vector multiplication

```
      a[][]
      x[]
      b[]

      0 .90 0 0 0 0
      0.05
      .036

      0 0 .36 .36 .18
      .04
      .297

      0 0 0 .90 0
      .36
      .333

      .90 0 0 0 0 0
      .37
      .045

      .47 0 .47 0 0
      .19
      .1927
```

```
SparseVector[] a = new SparseVector[N];
double[] x = new double[N];
double[] b = new double[N];
...
// Initialize a[] and x[]
...
for (int i = 0; i < N; i++)
    b[i] = a[i].dot(x);

linear running time
for sparse matrix</pre>
```

sets

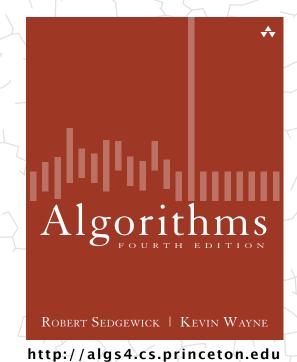
dictionary clients

indexing clients

sparse vectors

Algorithms

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