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1. (Method-1). Algorithm Formula : $b_0 = a_0 + rb_1 + sb_2$
2. (Method-1). Example-1 $f(x) = x^4 - 3x^3 + 3x^2 - 3x + 2$ and $r = 0.1, s = 0.1$
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4. (Method-2). Algorithm Formula : $b_2 = a_2 - pb_1 - qb_0$
5. (Method-2). Example-1 $f(x) = x^3 + x^2 - x + 2$ and $r = -0.9, s = 0.9$
6. (Method-2). Example-2 $f(x) = x^4 + x^3 + 2x^2 + x + 1$ and $r = 0.5, s = 0.5$

1. (Method-1). Algorithm Formula : $b_0 = a_0 + rb_1 + sb_2$ 3. (Method-1). Example-2 $f(x) = x^4 - 2x^3 + 6x^2 - 2x + 5$ and $r = -1, s = -1$
 $b_0 = a_0 + rb_1 + sb_2$ $x^4 - 3x^3 + 3x^2 - 3x + 2 = 0$
(Previous example) (Next example)

2. (Method-1). Example-1 $f(x) = x^4 - 3x^3 + 3x^2 - 3x + 2$ and $r = 0.1, s = 0.1$

Algorithm**Example-1**

Find all roots of polynomial using Bairstow method

 $f(x) = x^4 - 3x^3 + 3x^2 - 3x + 2$ and $r = 0.1, s = 0.1$ **Solution:**

Let the initial approximation be and

Here $a_4 = 1, b_0 = a_0 + rb_1 + sb_2, a_3 = -3, f(x) = x^4 - 2x^3 + 6x^2 - 2x + 5, a_2 = 3, r = -1, s = -1, a_1 = -3, a_0 = 2$

Iteration=1

 $b_4 = a_4 = 1$ $b_3 = a_3 + rb_4 = -3 + 0.1 \cdot 1 = -2.9$ $b_2 = a_2 + rb_3 + sb_4 = 3 + 0.1 \cdot (-2.9) + 0.1 \cdot 1 = 2.81$ $b_1 = a_1 + rb_2 + sb_3 = -3 + 0.1 \cdot 2.81 + 0.1 \cdot (-2.9) = -3.009$ $b_0 = a_0 + rb_1 + sb_2 = 2 + 0.1 \cdot (-3.009) + 0.1 \cdot 2.81 = 1.9801$ ([Enter your problem](#))

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -2.9 + 0.1 \cdot 1 = -2.8$$

$$c_2 = b_2 + rc_3 + sc_4 = 2.81 + 0.1 \cdot (-2.8) + 0.1 \cdot 1 = 2.63$$

$$c_1 = b_1 + rc_2 + sc_3 = -3.009 + 0.1 \cdot 2.63 + 0.1 \cdot (-2.8) = -3.026$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$2.63 \Delta r - 2.8 \Delta s = 3.009 \text{ and } -3.026 \Delta r + 2.63 \Delta s = -1.9801$$

Solving equations using Cramer's rule method

$$D = c_2 \cdot c_2 - c_1 \cdot c_3 = 2.63 \cdot 2.63 - (-3.026) \cdot (-2.8) = -1.5559$$

$$D_1 = b_0 \cdot c_3 - b_1 \cdot c_2 = 1.9801 \cdot (-2.8) - (-3.009) \cdot 2.63 = 2.36939$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-3.009) \cdot (-3.026) - 1.9801 \cdot 2.63 = 3.89757$$

$$\Delta r = \frac{D_1}{D} = \frac{2.36939}{-1.5559} = -1.52284$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{3.89757}{-1.5559} = -2.50503$$

The new r and s are

$$r = r + \Delta r = 0.1 - 1.52284 = -1.42284$$

$$\text{and } s = s + \Delta s = 0.1 - 2.50503 = -2.40503$$

The approximate error in r and s

$$\left| \epsilon_{a,r} \right| = \left| \frac{\Delta r}{r} \right| \times 100 \% = \left| \frac{-1.52284}{-1.42284} \right| \times 100 \% = 107.02819$$

$$\left| \epsilon_{a,s} \right| = \left| \frac{\Delta s}{s} \right| \times 100 \% = \left| \frac{-2.50503}{-2.40503} \right| \times 100 \% = 104.15796$$

Iteration=2

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 - 1.42284 \cdot 1 = -4.42284$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 - 1.42284 \cdot (-4.42284) - 2.40503 \cdot 1 = 6.88798$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 - 1.42284 \cdot 6.88798 - 2.40503 \cdot (-4.42284) = -2.16345$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 - 1.42284 \cdot (-2.16345) - 2.40503 \cdot 6.88798 = -11.48752$$

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -4.42284 - 1.42284 \cdot 1 = -5.84568$$

$$c_2 = b_2 + rc_3 + sc_4 = 6.88798 - 1.42284 \cdot (-5.84568) - 2.40503 \cdot 1 = 12.80044$$

$$c_1 = b_1 + rc_2 + sc_3 = -2.16345 - 1.42284 \cdot 12.80044 - 2.40503 \cdot (-5.84568) = -6.31743$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$12.80044 \Delta r - 5.84568 \Delta s = 2.16345 \text{ and } -6.31743 \Delta r + 12.80044 \Delta s = 11.48752$$

Solving equations using Cramer's rule method

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$$D = c_2 \cdot c_2 - c_1 \cdot c_3 = 12.80044 \cdot 12.80044 - (-6.31743) \cdot (-5.84568) = 126.92152$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-2.16345) \cdot (-6.31743) - (-11.48752) \cdot 12.80044 = 160.71276$$

$$\Delta r = \frac{D_1}{D} = \frac{94.84557}{126.92152} = 0.74728$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{160.71276}{126.92152} = 1.26624$$

The new r and s are

$$r = r + \Delta r = -1.42284 + 0.74728 = -0.67556$$

$$\text{and } s = s + \Delta s = -2.40503 + 1.26624 = -1.13879$$

The approximate error in r and s

$$\left| \varepsilon_{a,r} \right| = \left| \frac{\Delta r}{r} \right| \times 100\% = \left| \frac{0.74728}{-0.67556} \right| \times 100\% = 110.6152$$

$$\left| \varepsilon_{a,s} \right| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{1.26624}{-1.13879} \right| \times 100\% = 111.19153$$

Iteration=3

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 - 0.67556 \cdot 1 = -3.67556$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 - 0.67556 \cdot (-3.67556) - 1.13879 \cdot 1 = 4.34429$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 - 0.67556 \cdot 4.34429 - 1.13879 \cdot (-3.67556) = -1.74916$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 - 0.67556 \cdot (-1.74916) - 1.13879 \cdot 4.34429 = -1.76557$$

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -3.67556 - 0.67556 \cdot 1 = -4.35113$$

$$c_2 = b_2 + rc_3 + sc_4 = 4.34429 - 0.67556 \cdot (-4.35113) - 1.13879 \cdot 1 = 6.14497$$

$$c_1 = b_1 + rc_2 + sc_3 = -1.74916 - 0.67556 \cdot 6.14497 - 1.13879 \cdot (-4.35113) = -0.94546$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$6.14497 \Delta r - 4.35113 \Delta s = 1.74916 \text{ and } -0.94546 \Delta r + 6.14497 \Delta s = 1.76557$$

Solving equations using Cramer's rule method

$$D = c_2 \cdot c_2 - c_1 \cdot c_3 = 6.14497 \cdot 6.14497 - (-0.94546) \cdot (-4.35113) = 33.64686$$

$$D_1 = b_0 \cdot c_3 - b_1 \cdot c_2 = (-1.76557) \cdot (-4.35113) - (-1.74916) \cdot 6.14497 = 18.43073$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-1.74916) \cdot (-0.94546) - (-1.76557) \cdot 6.14497 = 12.50312$$

$$\Delta r = \frac{D_1}{D} = \frac{18.43073}{33.64686} = 0.54777$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{12.50312}{33.64686} = 0.3716$$

The new r and s are

$$r = r + \Delta r = -0.67556 + 0.54777 = -0.1278$$

$$\text{and } s = s + \Delta s = -1.13879 + 0.3716 = -0.76719$$

The approximate error in r and s

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$$|e_{a,s}| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{0.3716}{-0.76719} \right| \times 100\% = 48.43623$$

Iteration=4

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 - 0.1278 \cdot 1 = -3.1278$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 - 0.1278 \cdot (-3.1278) - 0.76719 \cdot 1 = 2.63253$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 - 0.1278 \cdot 2.63253 - 0.76719 \cdot (-3.1278) = -0.93681$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 - 0.1278 \cdot (-0.93681) - 0.76719 \cdot 2.63253 = 0.10007$$

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -3.1278 - 0.1278 \cdot 1 = -3.25559$$

$$c_2 = b_2 + rc_3 + sc_4 = 2.63253 - 0.1278 \cdot (-3.25559) - 0.76719 \cdot 1 = 2.28138$$

$$c_1 = b_1 + rc_2 + sc_3 = -0.93681 - 0.1278 \cdot 2.28138 - 0.76719 \cdot (-3.25559) = 1.2693$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$2.28138 \Delta r - 3.25559 \Delta s = 0.93681 \text{ and } 1.2693 \Delta r + 2.28138 \Delta s = -0.10007$$

Solving equations using Cramer's rule method

$$D = c_2 \cdot c_2 - c_1 \cdot c_3 = 2.28138 \cdot 2.28138 - 1.2693 \cdot (-3.25559) = 9.33704$$

$$D_1 = b_0 \cdot c_3 - b_1 \cdot c_2 = 0.10007 \cdot (-3.25559) - (-0.93681) \cdot 2.28138 = 1.81143$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-0.93681) \cdot 1.2693 - 0.10007 \cdot 2.28138 = -1.41739$$

$$\Delta r = \frac{D_1}{D} = \frac{1.81143}{9.33704} = 0.19401$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{-1.41739}{9.33704} = -0.1518$$

The new r and s are

$$r = r + \Delta r = -0.1278 + 0.19401 = 0.06621$$

$$\text{and } s = s + \Delta s = -0.76719 - 0.1518 = -0.91899$$

The approximate error in r and s

$$|e_{a,r}| = \left| \frac{\Delta r}{r} \right| \times 100\% = \left| \frac{0.19401}{0.06621} \right| \times 100\% = 293.01478$$

$$|e_{a,s}| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{-0.1518}{-0.91899} \right| \times 100\% = 16.51837$$

Iteration=5

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 + 0.06621 \cdot 1 = -2.93379$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 + 0.06621 \cdot (-2.93379) - 0.91899 \cdot 1 = 1.88676$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 + 0.06621 \cdot 1.88676 - 0.91899 \cdot (-2.93379) = -0.17894$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 + 0.06621 \cdot (-0.17894) - 0.91899 \cdot 1.88676 = 0.25423$$

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$$c_0 = a_0 + rb_1 + sb_2 = 2 - 0.00944 + (-0.17894) \cdot 0.91899 - 1.00192 \cdot 0.27658$$

$$c_3 = b_3 + rc_4 = -2.93379 + 0.06621 \cdot 1 = -2.86758$$

$$c_2 = b_2 + rc_3 + sc_4 = 1.88676 + 0.06621 \cdot (-2.86758) - 0.91899 \cdot 1 = 0.7779$$

$$c_1 = b_1 + rc_2 + sc_3 = -0.17894 + 0.06621 \cdot 0.7779 - 0.91899 \cdot (-2.86758) = 2.50785$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$0.7779 \Delta r - 2.86758 \Delta s = 0.17894 \text{ and } 2.50785 \Delta r + 0.7779 \Delta s = -0.25423$$

Solving equations using Cramer's rule method

$$D = c_2 \cdot c_3 - c_1 \cdot c_2 = 0.7779 \cdot 0.7779 - 2.50785 \cdot (-2.86758) = 7.7966$$

$$D_1 = b_0 \cdot c_3 - b_1 \cdot c_2 = 0.25423 \cdot (-2.86758) - (-0.17894) \cdot 0.7779 = -0.58983$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-0.17894) \cdot 2.50785 - 0.25423 \cdot 0.7779 = -0.64653$$

$$\Delta r = \frac{D_1}{D} = \frac{-0.58983}{7.7966} = -0.07565$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{-0.64653}{7.7966} = -0.08292$$

The new r and s are

$$r = r + \Delta r = 0.06621 - 0.07565 = -0.00944$$

$$\text{and } s = s + \Delta s = -0.91899 - 0.08292 = -1.00192$$

The approximate error in r and s

$$\left| \varepsilon_{a,r} \right| = \left| \frac{\Delta r}{r} \right| \times 100\% = \left| \frac{-0.07565}{-0.00944} \right| \times 100\% = 801.22073$$

$$\left| \varepsilon_{a,s} \right| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{-0.08292}{-1.00192} \right| \times 100\% = 8.27658$$

Iteration=6

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 - 0.00944 \cdot 1 = -3.00944$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 - 0.00944 \cdot (-3.00944) - 1.00192 \cdot 1 = 2.0265$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 - 0.00944 \cdot 2.0265 - 1.00192 \cdot (-3.00944) = -0.00392$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 - 0.00944 \cdot (-0.00392) - 1.00192 \cdot 2.0265 = -0.03035$$

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -3.00944 - 0.00944 \cdot 1 = -3.01888$$

$$c_2 = b_2 + rc_3 + sc_4 = 2.0265 - 0.00944 \cdot (-3.01888) - 1.00192 \cdot 1 = 1.05308$$

$$c_1 = b_1 + rc_2 + sc_3 = -0.00392 - 0.00944 \cdot 1.05308 - 1.00192 \cdot (-3.01888) = 3.01081$$

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The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$1.05308 \Delta r - 3.01888 \Delta s = 0.00392 \text{ and } 3.01081 \Delta r + 1.05308 \Delta s = 0.03035$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-0.00392) \cdot 3.01081 - (-0.03035) \cdot 1.05308 = 0.02016$$

$$\Delta r = \frac{D_1}{D} = \frac{0.09574}{10.19828} = 0.00939$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{0.02016}{10.19828} = 0.00198$$

The new r and s are

$$r = r + \Delta r = -0.00944 + 0.00939 = -0.00005$$

$$\text{and } s = s + \Delta s = -1.00192 + 0.00198 = -0.99994$$

The approximate error in r and s

$$\left| e_{a,r} \right| = \left| \frac{\Delta r}{r} \right| \times 100\% = \left| \frac{0.00939}{-0.00005} \right| \times 100\% = 17406.4444$$

$$\left| e_{a,s} \right| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{0.00198}{-0.99994} \right| \times 100\% = 0.19768$$

Iteration=7

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 + 0 \cdot 1 = -3.00005$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 + 0 \cdot (-3.00005) - 0.99994 \cdot 1 = 2.00022$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 + 0 \cdot 2.00022 - 0.99994 \cdot (-3.00005) = -0.00023$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 + 0 \cdot (-0.00023) - 0.99994 \cdot 2.00022 = -0.0001$$

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -3.00005 + 0 \cdot 1 = -3.00011$$

$$c_2 = b_2 + rc_3 + sc_4 = 2.00022 + 0 \cdot (-3.00011) - 0.99994 \cdot 1 = 1.00044$$

$$c_1 = b_1 + rc_2 + sc_3 = -0.00023 + 0 \cdot 1.00044 - 0.99994 \cdot (-3.00011) = 2.99965$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$1.00044 \Delta r - 3.00011 \Delta s = 0.00023 \text{ and } 2.99965 \Delta r + 1.00044 \Delta s = 0.0001$$

Solving equations using Cramer's rule method

$$D = c_2 \cdot c_2 - c_1 \cdot c_3 = 1.00044 \cdot 1.00044 - 2.99965 \cdot (-3.00011) = 10.00015$$

$$D_1 = b_0 \cdot c_3 - b_1 \cdot c_2 = (-0.0001) \cdot (-3.00011) - (-0.00023) \cdot 1.00044 = 0.00054$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (-0.00023) \cdot 2.99965 - (-0.0001) \cdot 1.00044 = -0.00058$$

$$\Delta r = \frac{D_1}{D} = \frac{0.00054}{10.00015} = 0.00005$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{-0.00058}{10.00015} = -0.00006$$

The new r and s are

$$r = r + \Delta r = -0.00005 = 0$$

$$\text{and } s = s + \Delta s = -0.99994 = -1$$

The approximate error in r and s

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The approximate error in r and s

$$\left| \varepsilon_{a,r} \right| = \left| \frac{\Delta r}{r} \right| \times 100\% = \left| \frac{0}{0} \right| \times 100\% = 0$$

$$\left| \varepsilon_{a,s} \right| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{-0.00006}{-1} \right| \times 100\% = 0.00583$$

Iteration=8

$$b_4 = a_4 = 1$$

$$b_3 = a_3 + rb_4 = -3 + 0 \cdot 1 = -3$$

$$b_2 = a_2 + rb_3 + sb_4 = 3 + 0 \cdot (-3) - 1 \cdot 1 = 2$$

$$b_1 = a_1 + rb_2 + sb_3 = -3 + 0 \cdot 2 - 1 \cdot (-3) = 0$$

$$b_0 = a_0 + rb_1 + sb_2 = 2 + 0 \cdot (0) - 1 \cdot 2 = 0$$

$$c_4 = b_4 = 1$$

$$c_3 = b_3 + rc_4 = -3 + 0 \cdot 1 = -3$$

$$c_2 = b_2 + rc_3 + sc_4 = 2 + 0 \cdot (-3) - 1 \cdot 1 = 1$$

$$c_1 = b_1 + rc_2 + sc_3 = 0 + 0 \cdot 1 - 1 \cdot (-3) = 3$$

The simultaneous equations for Δr and Δs are

$$c_2 \Delta r + c_3 \Delta s = -b_1 \text{ and } c_1 \Delta r + c_2 \Delta s = -b_0$$

Substitute values of c_1, c_2, c_3 and b_0, b_1

$$\Delta r - 3\Delta s = 0 \text{ and } 3\Delta r + \Delta s = 0$$

Solving equations using Cramer's rule method

$$D = c_2 \cdot c_2 - c_1 \cdot c_3 = 1 \cdot 1 - 3 \cdot (-3) = 10$$

$$D_1 = b_0 \cdot c_3 - b_1 \cdot c_2 = 0 \cdot (-3) - (0) \cdot 1 = 0$$

$$D_2 = b_1 \cdot c_1 - b_0 \cdot c_2 = (0) \cdot 3 - 0 \cdot 1 = 0$$

$$\Delta r = \frac{D_1}{D} = \frac{0}{10} = 0$$

$$\text{and } \Delta s = \frac{D_2}{D} = \frac{0}{10} = 0$$

The new r and s are

$$r = r + \Delta r = 0 = 0$$

$$\text{and } s = s + \Delta s = -1 = -1$$

The approximate error in r and s

$$\left| \varepsilon_{a,r} \right| = \left| \frac{\Delta r}{r} \right| \times 100\% = \left| \frac{0}{0} \right| \times 100\% = 3262152642.45229$$

$$\left| \varepsilon_{a,s} \right| = \left| \frac{\Delta s}{s} \right| \times 100\% = \left| \frac{0}{-1} \right| \times 100\% = 0$$

Now determine roots using r and s

$$x_{1,2} = \frac{r \pm \sqrt{r^2 + 4s}}{2}$$

$$x_{1,2} = \frac{0 \pm \sqrt{0 + 4 \cdot (-1)}}{2}$$

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Now, divide the polynomial

$$\frac{x^4 - 3x^3 + 3x^2 - 3x + 2}{x^2 + 1}$$

$$= x^2 - 3x + 2 \text{ (This is nothing but the first 3 elements of b)}$$

This quotient polynomial is a quadratic polynomial, so roots can be found using quadratic formula

$$x_{3,4} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x_{3,4} = \frac{3 \pm \sqrt{9 - 4 \cdot 1 \cdot 2}}{2 \cdot 1}$$

$$x_{3,4} = \frac{3 \pm \sqrt{1}}{2}$$

$$x_{3,4} = \frac{3 \pm 1}{2}$$

$$x_3 = 2, x_4 = 1$$

So the roots of the equation are $+i, -i, 2, 1$

Iteration	$a_{i,n}$	$b_{i,n}$	$c_{i,n}$	Δr	Δs	r	s
1	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -2.9$ $b_2 = 2.81$ $b_1 = -3.009$ $b_0 = 1.9801$	$c_4 = 1$ $c_3 = -2.8$ $c_2 = 2.63$ $c_1 = -3.026$	-1.52284	-2.50503	-1.42284	-2.40503
2	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -4.42284$ $b_2 = 6.88798$ $b_1 = -2.16345$ $b_0 = -11.48752$	$c_4 = 1$ $c_3 = -5.84568$ $c_2 = 12.80044$ $c_1 = -6.31743$	0.74728	1.26624	-0.67556	-1.13879
3	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -3.67556$ $b_2 = 4.34429$ $b_1 = -1.74916$ $b_0 = -1.76557$	$c_4 = 1$ $c_3 = -4.35113$ $c_2 = 6.14497$ $c_1 = -0.94546$	0.54777	0.3716	-0.1278	-0.76719
4	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -3.1278$ $b_2 = 2.63253$ $b_1 = -0.93681$ $b_0 = 0.10007$	$c_4 = 1$ $c_3 = -3.25559$ $c_2 = 2.28138$ $c_1 = 1.2693$	0.19401	-0.1518	0.06621	-0.91899
5	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -2.93379$ $b_2 = 1.88676$ $b_1 = -0.17894$ $b_0 = 0.25423$	$c_4 = 1$ $c_3 = -2.86758$ $c_2 = 0.7779$ $c_1 = 2.50785$	-0.07565	-0.08292	-0.00944	-1.00192
6	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -3.00944$ $b_2 = 2.0265$ $b_1 = -0.00392$ $b_0 = -0.03035$	$c_4 = 1$ $c_3 = -3.01888$ $c_2 = 1.05308$ $c_1 = 3.01081$	0.00939	0.00198	-0.00005	-0.99994
7	$a_4 = 1$ $a_3 = -3$ $a_2 = 3$ $a_1 = -3$ $a_0 = 2$	$b_4 = 1$ $b_3 = -3.00005$ $b_2 = 2.00022$ $b_1 = -0.00023$ $b_0 = -0.0001$	$c_4 = 1$ $c_3 = -3.00011$ $c_2 = 1.00044$ $c_1 = 2.99965$	0.00005	-0.00006	0	-1
	$a_{\infty} = 1$	$b_{\infty} = 1$	$c_{\infty} = 1$				

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8	$\tilde{a}_2 = 2$	$\tilde{b}_2 = 0$	$\tilde{c}_2 = 3$	0	0	0	-1
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$a_0 = 2$	$b_0 = 0$	$c_1 = 3$				
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This material is intended as a summary. Use your textbook for detail explanation.
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[1. \(Method-1\). Algorithm Formula :](#)
 (Previous example)

[3. \(Method-1\). Example-2 and](#)
 (Next example)






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