

# Probabilistic Tracking of Multiple Rodent Whiskers In Monocular Video Sequences

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## Background

### The Problem

The interest in studying rodent whiskers has recently seen a significant increase, particularly in the field of neuro-physiology. As a result, there is a need for automatic tracking of whisker movements. Currently available commercial solutions either are extremely expensive, restrict the experiment setup<sup>1</sup>, or fail in *cluttered* environments or when whiskers occlude each other<sup>2</sup>. A cheap, reliable solution to the tracking problem is needed.

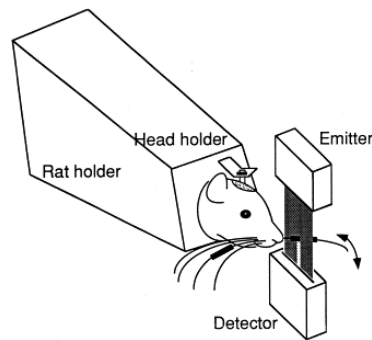


Figure 1: A very restrained experiment setup.

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<sup>1</sup>A method known as *optoelectronic monitoring* takes this to the extreme by having the rat locked in place by cranium-mounted screws [1]. See figure 1.

<sup>2</sup>A system developed by Volgts, Sakmann and Celikel manages to track  $\leq 8$  whiskers on each face side, but has difficulties tracking more whiskers than that [4].

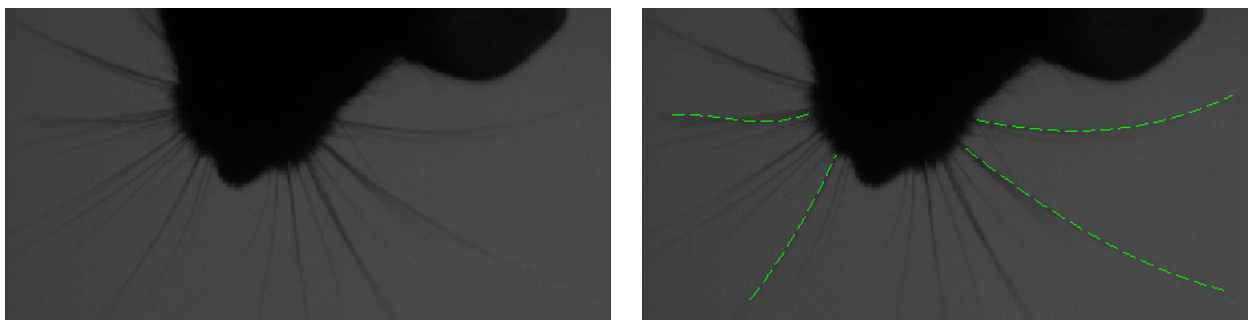


Figure 2: Left: Example image of a rat and its whiskers. Right: Least squares fitted third degree polynomials.

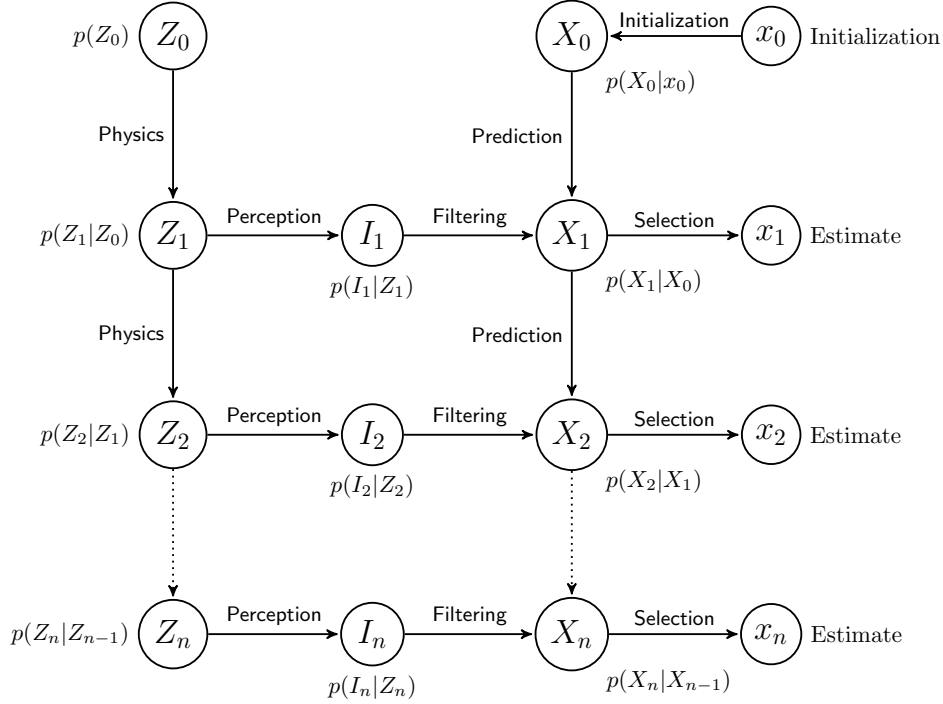


Figure 3: Schematic image of the Particle Filter working alongside a Hidden Markov Model.

## A Probabilistic Approach

We propose solving the problem by a probabilistic approach. We use a technique known as the *Particle Filter* to propagate a whisker model between frames of high speed video. In each frame, the next state of the model is predicted by searching a pre-trained database, and filtering the results through the Particle Filter. The main difference between this and existing solutions is that it maintains a model of the whiskers. This makes it easier to keep track of them even in the presence of clutter.

## The Probabilistic Framework

Our solution is based on *Markov processes*, which are a special case of stochastic processes. For a Markov process, the next state depends only on the present state and not on past states.

An example of a Markov process is that of throwing dice and summing the results: the possible states (sums) after the next throw depends only on the current state.

In mathematical terms, a Markov process satisfies the following:

$$p(Z_{n+1}|Z_n \wedge Z_{n-1} \wedge Z_{n-2} \wedge \dots \wedge Z_0) = p(Z_{n+1}|Z_n), \quad (1)$$

where  $Z_n$  is the system's *state* after step  $n$  and  $p(Z_{n+1}|Z_n, Z_{n-1}, Z_{n-2}, \dots, Z_0)$  is the probability that the system will have state  $Z_{n+1}$  in the next step, given that the previous states were  $Z_n, Z_{n-1}, Z_{n-2}, \dots, Z_0$ .

A *hidden Markov model* (HMM) describes a Markov process where one cannot measure the state  $Z$  of the system directly - it is "hidden"[2]. Instead we obtain an *observation*  $I^3$  of the state. This *perception* is generally non-deterministic, so we need to denote it as  $p(I_n|Z_n)$  which is the probability that we will observe  $I_n$  if the current state of the system is  $Z_n$ .

## The Particle Filter

The Particle Filter is a technique for tracking a process described by a HMM. It uses a finite set  $X_{n+1}$  of hypotheses to approximate the probability function  $p(Z_{n+1}|Z_n)$ . The hypotheses  $X_n$  are also known as *particles*, thereby the term "particle filter".

<sup>3</sup>In this project, the observation is a grayscale *image*, which is why we use the symbol  $I$ .

Figure 3 shows the working principle of the Particle Filter working alongside a Hidden Markov Model. The following is the core function of the Particle Filter:

*The particle filter attempts to approximate the probability density function  $p(Z_{n+1}|Z_n)$  as a set  $X_{n+1}$  of discrete hypotheses.*

More particles mean greater accuracy, since the PDF can then be approximated more closely. However, using many particles is also computationally expensive. Therefore the number of particles is an important quantity. The Particle Filter employs a few tricks to *filter* the hypotheses, keeping probable ones and throwing improbable ones away, in order to reduce the number of particles needed for a good approximation. The following is a quick run-down of how the Particle Filter does this. For brevity, we will commit some abuse of notation.

**Initialization:** Since the algorithm only does tracking, we need to initialize the algorithm with a start guess  $x_0$ . Using this we take a number of samples  $X_0 \sim \mathcal{N}(x_0, \Sigma)$  and let the set  $X_0$  be an approximation of  $p(Z_0)$ <sup>4</sup>.

**Prediction:** The hypotheses  $X_n$  are updated in the *prediction* step to an approximation of  $p(Z_{n+1}|Z_n)_{n+1}$ . This is done by drawing new samples  $\tilde{X}_{n+1} \sim p(X_{n+1}|X_n)$ .

**Perception:** By measuring the state of the system, we gain an *observation*  $I_{n+1} \sim p(I_{n+1}|Z_{n+1})$  of the state  $Z_{n+1}$ .

**Filtering:** The observation  $I_{n+1}$  of the system is then used for filtering bad hypotheses out of  $\tilde{X}_{n+1}$ . We draw samples  $X_{n+1}$  from  $\tilde{X}_{n+1}$  with probabilities given by  $p(I_{n+1}|\tilde{X}_{n+1})$ . As a result,  $X_{n+1}$  will be a subset of  $\tilde{X}_{n+1}$  where more probable hypotheses appear multiple times. For this reason, this is also known as the *resampling* step. The set  $X_{n+1}$  is the *belief*, our approximation of  $p(Z_{n+1}|Z_n)$ .

**Selection:** Finally, we produce a single hypothesis  $x_{n+1}$  from  $X_{n+1}$  as our *estimate* of the state  $Z_{n+1}$ . Supposing  $X_{n+1}$  is a good approximation of  $p(Z_{n+1}|Z_n)$ , and that  $p(Z_{n+1}|Z_n)$  is unimodal, the mean value of  $X_{n+1}$  is a good hypothesis since it approximates the expectation of  $p(Z_{n+1}|Z_n)$ .

## A Simple Whisker Model

Our simplest model of a whiskers is  $n$ -th degree polynomial curve attached at  $x = 0$  to a fixed point in space. This means our state parameters are the coefficients  $\{a_i\}_{i=0}^n$  of the polynomial  $\sum_{i=0}^n a_i x^i$ , and we can represent a whisker's state with the tuple of its coefficients. In this model we implicitly assume that the rat's head movements do not greatly affect the whiskers' movement. Possible improvements to this model may include:

- letting the whisker attach to a fixed point in a moving coordinate system (the "head system"),
- using some other function basis, such as a sine series.

So far we have only investigated the simplest polynomial model. Least squares fitting tests performed using MATLAB show that a third degree polynomial can represent any whisker in figure 2 with an error that is barely visible to the naked eye. Therefore a third degree polynomial was used as a first step. We omit the constant term since this information can instead be included in the position of the whisker base.

## Our implementation of the Particle Filter

An implementation of the Particle Filter consists mainly of designing the probability functions  $p(X_{n+1}|X_n)$  and  $p(I_n|X_n)$ , and providing the algorithm with a sensible initialization. This is what this project is all about. The rest just consists of taking samples from these functions.

### The prediction step: The Database

We investigate the plausibility of implementing  $p(X_{n+1}|X_n)$  as a search through a database of training data. We set up a database of known transitions between whisker shapes. A transition  $T$  consists of a "from" state  $f$  and a "to" state  $t$ . This denotes our *ground truth*<sup>5</sup> that "a whisker went from this shape to that shape in one time step". We then approximate  $p(X_{n+1}|X_n)$  as a weighted average of the database, where transitions are weighted by how much their "from" parts differ from the hypotheses in  $X_n$ .

What we do in practice when sampling is: for each hypothesis  $x_n^i \in X_n$ ,

<sup>4</sup>The problem of initialization is a tricky one[3], and is not covered in this project. In our testing implementation, we used  $\Sigma = 0$

<sup>5</sup>See [2]

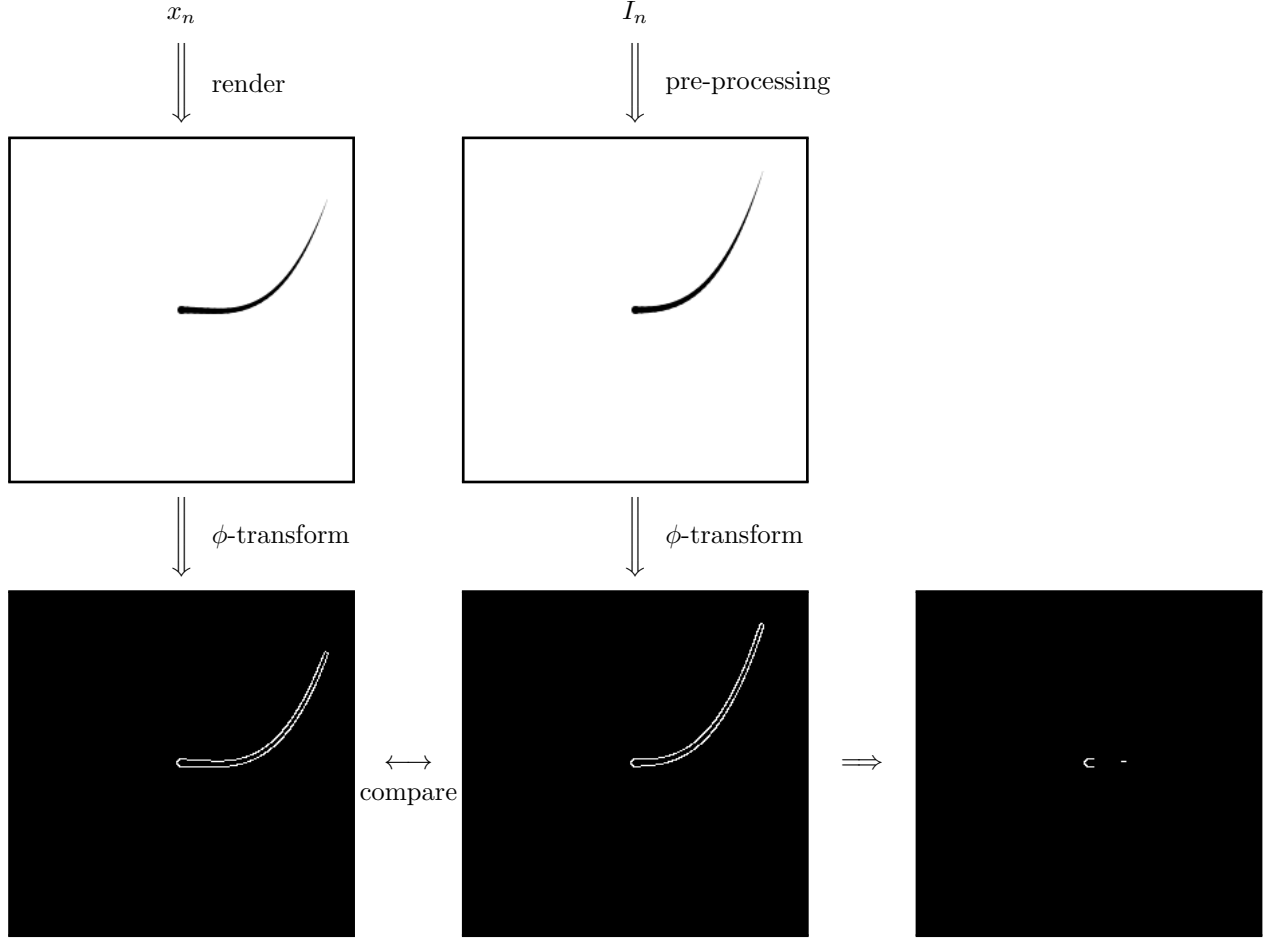


Figure 4: Schematic image of the process to evaluate the importance of a hypothesis. The transformation  $\phi$  in this case extracts an edge cue from the images.

1. For each transition  $T^j = (f^j, t^j)$  in the database, calculate the function  $d^{ij}$  that is the difference between the two functions described by  $x_n^i$  and  $f^j$ . In this case, both are polynomials and thus  $d^{ij}$  is the polynomial with coefficients given by the tuple  $x_n^i - f^j$ .
2. Let  $w^{ij} = \left( \frac{1}{\|d^{ij}\|_{L^p}} \right)^a$ , the reciprocal of the  $L^p$  norm of  $d^{ij}$  raised to a power  $a$ .
3. Return  $\frac{\sum_j t^j w^{ij}}{\sum_j w^{ij}}$ , the weighted average of the “to” states with weights  $w^{ij}$ .

Doing this for each hypothesis  $x_n^i$  yields the set  $\tilde{X}_n$ .

We have not yet thoroughly investigated which power  $a$  and which  $L^p$  space to use. We have run tests with  $L^2$ , and  $a = 4$  seems to be a good value. These will later be determined in a “bake-off”<sup>6</sup>.

### The filtering step: Image comparison

We implement the probability function  $p(I_n | X_n)$  as a comparison between  $I_n$  and the images corresponding to the hypotheses  $X_n$ . For each hypothesis  $\bar{x}_n^i \in \tilde{X}_n$  we create an image  $I_n^i$  that corresponds to the state described by  $\bar{x}_n^i$ .

We apply a transformation  $\phi$  to the images to get a sensory cue for evaluating the hypotheses. At the current stage in our testing, the images used are generated synthetic ones that are already easy to process. Therefore we let  $\phi$  be the identity transformation at the moment. Another feasible candidate for  $\phi$  would be a differentiation, in order to highlight edges in the image.

<sup>6</sup>See [2]

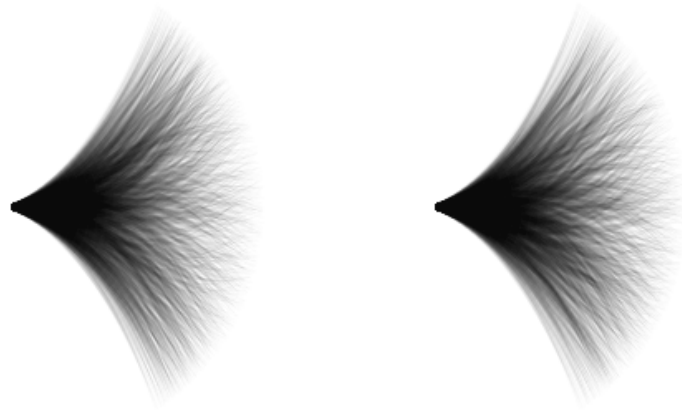


Figure 5: View of all whiskers in transition database. Left: from-states. Right: to-states.

We then let  $w^i = \sum_{\text{pixels}} \phi(I_n) \cdot \phi(I_n^i)$ , where the multiplication is done component-wise. We then let  $\{(\bar{x}_n^i, w^i)\}_{i=1}^N$  define a discrete probability function that returns  $\bar{x}_n^i$  with probability  $\frac{w^i}{\sum_{i=0}^N w^i}$ , and let this distribution be our approximation of  $p(I_N|X_n)$ .

### Example tracking image

Figure 6 shows an illustration of the three tracking steps. The blue lines are the hypotheses  $\bar{X}_n$  sampled from the database. The red lines are these same hypotheses, but after resampling,  $X_n$ . The green line is the estimate  $x_n$ , the mean of  $X_n$ . One can see how  $X_n$  is slightly more concentrated around the tracked whisker (white) than  $\bar{X}_n$  is.

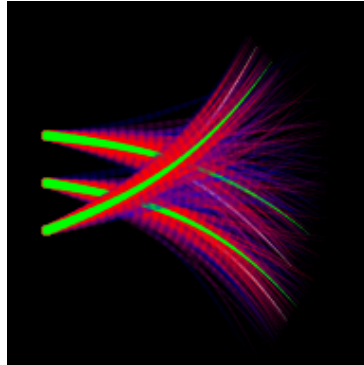


Figure 6: Tracking image with  $\bar{X}_n$  (blue) and  $X_n$  (blue) drawn along with the estimate  $x_n$  (green).

## Results

So far, we have run some tests on randomly generated video sequences of whisker-like objects. While the results are far from good enough for practical use, they are still quite promising.

Figure 7 shows the tracking result on a sequence of generated, synthetic whiskers. The estimate of the top and middle whiskers' positions are close to perfect, but the tracking of the bottom whisker fails much of the time. Still, this illustrates the power of the probabilistic approach. This was run using only 256 particles, which is a rather low amount. It took about 25 minutes to finish on a 2.83 GHz Intel® Core™ 2 Quad computer system with 3.8 GiB of RAM running Ubuntu 10.04, without multithreading the program at all.

## Conclusions

Our results so far lead us to believe that that it is indeed feasible to use this method for tracking whiskers.

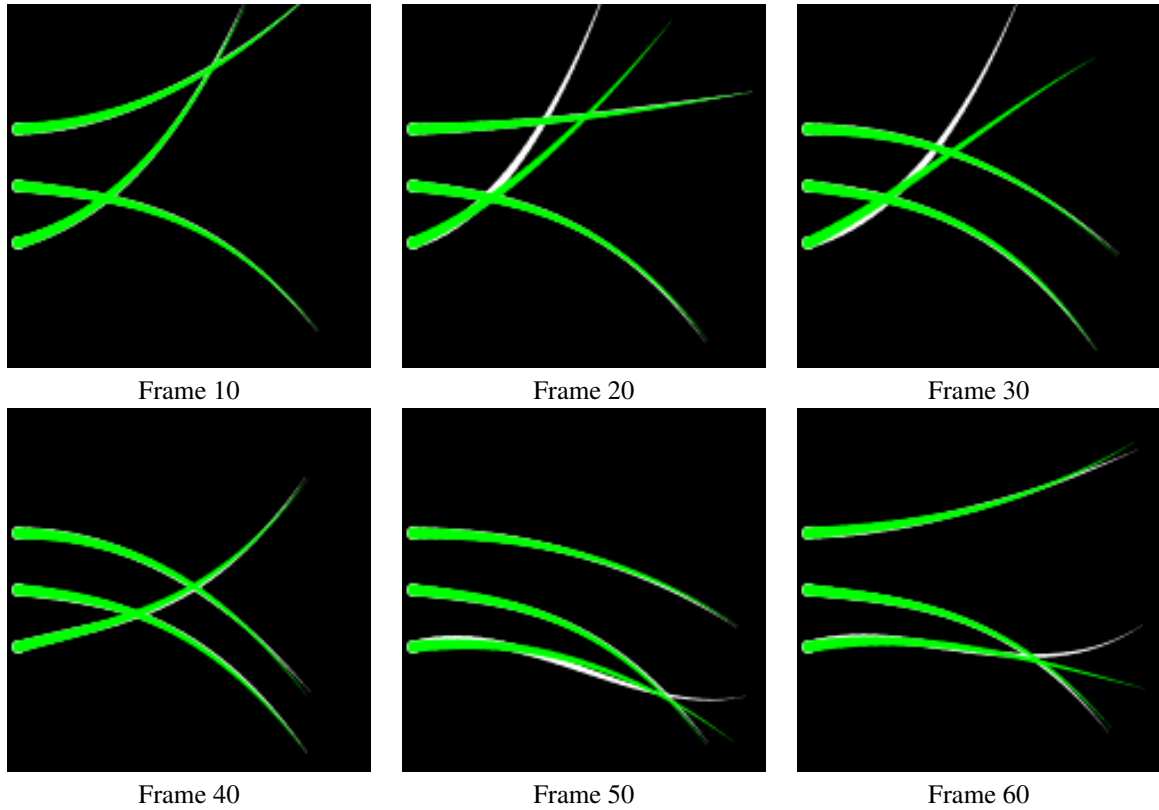


Figure 7: Tracking result using 256 particles on 64 frames of generated whiskers. White is the whisker being tracked, green is the estimate of its position.

## References

- [1] Bermejo R, D Houben, and H.Philip Zeigler. Optoelectronic monitoring of individual whisker movements in rats. *Journal of Neuroscience Methods*, 83, 1998.
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