Homework 1 Statistical Methods in Applied Computer Science DD2447

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Exercise 2.16 Mean, mode, variance for the beta distribution Suppose $\theta \sim Beta(a, b)$. Derive the mean, mode and variance.

Solution.

Exercise 3.6 MLE for the Poisson distribution

The Poisson pmf is defined as $Poi(x|\lambda) = e^{-\lambda} \frac{\lambda^x}{x!}$ for $x \in \{0, 1, 2, ...\}$ where $\lambda > 0$ is the rate parameter. Derive the MLE.

Solution.

Exercise 3.7 Bayesian analysis of the Poisson distribution

In exercise 3.6, we defined the Poisson distribution with rate λ and derived its MLE. Here we perform a conjugate Bayesian analysis.

- **a.** Derive the posterior $p(\lambda|D)$ assuming a conjugate prior $p(\lambda) = Ga(\lambda|a,b) \propto \lambda^{a-1}e^{-\lambda b}$. Hint: the posterior is also a Gamma distribution.
- **b.** What does the posterior mean tend to as $a \to 0$ and $b \to 0$? (Recall that the mean of a Ga(a,b) distribution is a/b.)

Solution.