Complex Lorentzian (From Lab Actor Program)

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In this paper, I will sepperate the complex Lorentzian equation used in the Lab Actor program into real and imaginary components.

General Equation

$$z(f) = \frac{Ae^{i\theta}}{f - f_0 + i\gamma}$$

Derivation

Mutltiple by complex conjugate.

$$\frac{Ae^{i\theta}}{f - f_0 + i\gamma} * \frac{(f - f_0) - i\gamma}{(f - f_0) - i\gamma} \tag{1}$$

Use Euler's identity in the numerator, and simplify the denominator.

$$\frac{A}{(f-f_0)^2 + \gamma^2} [\cos(\theta) + i\sin(\theta)] * ((f-f_0) - i\gamma)$$
(2)

Distribute factors in the numerator.

$$\frac{A}{(f - f_0)^2 + \gamma^2} [((f - f_0)\cos(\theta) + \gamma\sin(\theta)) + i((f - f_0)\sin(\theta) - \gamma(\cos(\theta)))]$$
(3)

$$Re(z(f)) = \frac{A}{(f - f_0)^2 + \gamma^2} ((f - f_0)\cos(\theta) + \gamma\sin(\theta))$$
$$Im(z(f)) = \frac{A}{(f - f_0)^2 + \gamma^2} ((f - f_0)\sin(\theta) - \gamma\cos(\theta))$$