

STUDY GUIDE FOR THE FINAL EXAM LINEAR ALGEBRA (MATH 115A)

1. CHAPTER 1: VECTOR SPACES

- (1) Definition of vector space and examples.
- (2) Exercises: Section 1.2: 12 – 15, 18.
- (3) Definition of subspace and Theorem 1.3 for testing subspace.
- (4) Exercises: Section 1.3: 8, 10, 11, 17 – 20.
- (5) Definition of span and generating set.
- (6) Exercises: Section 1.4: 5, 9, 12, 13.
- (7) Linear dependence and independence.
- (8) Theorem 1.7 and its applications.
- (9) Exercises: Section 1.5: 2(a) – (f), 9, 13.
- (10) Basis and dimension.
- (11) Theorem 1.9, Replacement Theorem (1.10) and Corollary 2 and their applications.
- (12) Theorem 1.11 and its Corollary, and their applications.
- (13) Exercises: Section 1.6: 4 – 9, 11 – 17, 26.

2. CHAPTER 2: LINEAR TRANSFORMATION AND MATRICES

- (1) Definition of linear transformation, null space $N(T)$, range $R(T)$, nullity and rank.
- (2) Theorem 2.3, 2.4, 2.5, 2.6 and their applications.
- (3) Exercises: Section 2.1: 2 – 6, 9 – 14, 17.
- (4) Ordered basis, coordinate vector and matrix representation.
- (5) Exercises: Section 2.2: 3 – 5.
- (6) Invertible linear transformation and isomorphism. A linear transformation is invertible if and only if it is *one-to-one* and *onto*.
- (7) Theorem 2.18 and 2.19 and their applications.
- (8) Exercises: Section 2.4: 2, 3, 14, 15, 17, 22.
- (9) Change of coordinate matrix, Theorem 2.23 and its applications.
- (10) Exercises: Section 2.5: 3 – 5.

3. CHAPTER 5: DIAGONALIZATION

- (1) Definition of diagonalizability, characteristic polynomial, eigenvalue and eigenvector, Theorem 5.1.
- (2) Exercises: Section 5.1: 2, 3, 8(a) – (b), 8 – 11, 15.
- (3) Theorem 5.9, test for diagonalization and applications.
- (4) Exercises: Section 5.2: 2, 3, 8.

4. CHAPTER 6: INNER PRODUCT SPACE

- (1) Definition of inner product, norm of a vector and their examples.
- (2) Exercises: Section 6.1: 2 – 5, 8, 9.
- (3) Definition of orthogonal set and orthonormal set of vectors and their examples.
- (4) Orthonormal basis, Theorem 6.3, Corollary 2 and their applications.
- (5) Gram-Schmidt Process (Theorem 6.4) and its applications.
- (6) Exercises: Section 6.2: 2, 4 – 8, 17.