```
uni_test.py
                  Thu Dec 01 22:28:09 2022
import numpy as np
import matplotlib.pyplot as plt
from plotcov2 import plotcov2
# EN530.603 Extended Kalman filtering of the unicycle with bearing and range
# measurements
# M. Kobilarov , marin(at)jhu.edu
np.random.seed(0)
def fangle(a):
  # make sure angle is between -pi and pi
  a = np.mod(a, 2 * np.pi)
  if a < -np.pi:
    a = a + a * np.pi
  else:
    if a > np.pi:
     a = a - 2 * np.pi
  return a
class Problem:
  def __init__(self):
    np.random.seed(10212)
    self.f = self.uni_f # mobile-robot dynamics
    self.h = self.br_h # bearing-reange sensing
    self.n = 3 # state dimension
    self.r = 2 # measurement dimension
    self.p0 = np.array([0, 2])
                                 # beacon positions
    # timing
    dt = .1
    self.N = 100
    self.T = dt * self.N
    self.dt = dt
    # noise models
    self.Q = .1 * dt * dt * np.diag([.1, .1, .1])
    self.R = .01 * np.diag([0.5, 1.0])
  def br_h(self, x):
    p = x[:2]
    px = p[0]
    py = p[1]
    d = self.p0 - p
    r = np.linalg.norm(d)
    th = fangle(np.arctan2(d[1], d[0]) - x[2])
    y = np.array([th, r])
    H = np.array([[d[1] / r**2, -d[0] / r**2, -1],
                  [-d[0] / r, -d[1] / r, 0]])
    return y, H
  def fix_state(self, x):
   x[2] = fangle(x[2])
   return x
  def uni_f(self, x, u):
    # dynamical model of the unicycle
```

c = np.cos(x[2])s = np.sin(x[2])

```
uni_test.py
                  Thu Dec 01 22:28:09 2022
    x = x + np.array([c * u[0], s * u[0], u[1]])
    x = self.fix_state(x)
    A = np.array([[1, 0, -s * u[0]], [0, 1, c * u[0]], [0, 0, 1]])
    return x, A
def ekf_predict(x, P, u, prob):
  x, F = prob.f(x, u)
  x = prob.fix_state(x)
  P = F @ P @ np.transpose(F) + prob.Q
  return x, P
def ekf_correct(x, P, z, prob):
  y, H = prob.h(x)
  K = P @ np.transpose(H) @ np.linalg.inv(H @ P @ np.transpose(H) + prob.R)
  P = (np.eye(prob.n) - K@H)@P
  e = z - y
  e[0] = fangle(e[0])
  x = x + K@e
  return x, P
prob = Problem()
# initial mean and covariance
xt = np.array([0, 0, 0]) # true state
P = .1 * np.diag([1, 1, 1]) # covariance
# initial estimate with added noise
x = xt + np.sqrt(P) @ np.random.randn(prob.n)
xts = np.zeros((prob.n, prob.N + 1)) # true states
xs = np.zeros((prob.n, prob.N + 1)) # estimated states
Ps = np.zeros((prob.n, prob.n, prob.N + 1)) # estimated covariances
ts = np.zeros((prob.N + 1, 1)) # times
zs = np.zeros((prob.r, prob.N)) # measurements
xts[:, 0] = xt
xs[:, 0] = x
Ps[:, :, 0] = P
ds = np.zeros((prob.n, prob.N + 1)) # errors
ds[:, 0] = x - xt
for k in range(prob.N):
  u = prob.dt * np.array([2, 1]) # known controls
  # true state
  x, _{-} = prob.f(xts[:, k], u)
  xts[:, k + 1] = x + np.sqrt(prob.Q) @ np.random.randn(3)
  x, P = ekf\_predict(x, P, u, prob) # predict
  # generate measurement
  y, H = prob.h(xts[:, k + 1])
  z = y + np.sqrt(prob.R) @ np.random.randn(prob.r)
  z[0] = fangle(z[0])
  [x, P] = ekf_correct(x, P, z, prob) # correct
  xs[:, k + 1] = x
  Ps[:, :, k + 1] = P
  zs[:, k] = z
```

```
Thu Dec 01 22:28:09 2022
uni_test.py
  ds[:, k + 1] = x - xts[:, k + 1] # actual estimate error
  ds[2, k + 1] = fangle(ds[2, k + 1])
fig1, ax1 = plt.subplots(1, 1)
fig2, ax2 = plt.subplots(1, 1)
ax1.plot(xts[0, :], xts[1, :], '--g', linewidth=3)
ax1.plot(xs[0, :], xs[1, :], '-b', linewidth=3)
ax1.legend({'true', 'estimated'})
# beacon
ax1.plot(prob.p0[0], prob.p0[1], '*r')
ax1.set_xlabel('x')
ax1.set_ylabel('y')
ax1.set_aspect('equal')
ax2.plot(ds[0, :], label='e_x')
ax2.plot(ds[1, :], label='e_y')
ax2.plot(ds[2, :], label='e_theta')
ax2.set_xlabel('k')
ax2.set_ylabel('meters or radians')
handles, labels = ax2.get_legend_handles_labels()
labels, handles = zip(*sorted(zip(labels, handles), key=lambda t: t[0]))
ax2.legend(handles, labels)
plt.show()
```