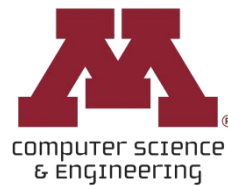


CSCI 5451: Introduction to Parallel Computing

Lecture 4: Parallel Algorithm Design



UNIVERSITY OF MINNESOTA
Driven to Discover®

Announcement (09/15)

- ❑ Office Hours are posted to the course site
- ❑ Homework Testing
 - We will be using two clusters ([plate and cuda](#)) for all homework assignments in this course
 - Examine [this pdf](#) and [corresponding code](#) to test that you are able to use these machines going forward (these are simple 'hello world' style tests)
 - Doing this in advance gives us the chance to fix any problems you may have with connecting/running programs before we get closer to homework deadlines



Lecture Overview

- ❑ Recap
- ❑ Task Decomposition
 - Background
 - MatVec Example Decompositions
 - Metrics & Definitions
- ❑ Decompositions (Recursive, Exploratory, Data, Speculative, Hybrid)
- ❑ Classifying Task Interaction & Generation



Lecture Overview

❑ **Recap**

❑ Task Decomposition

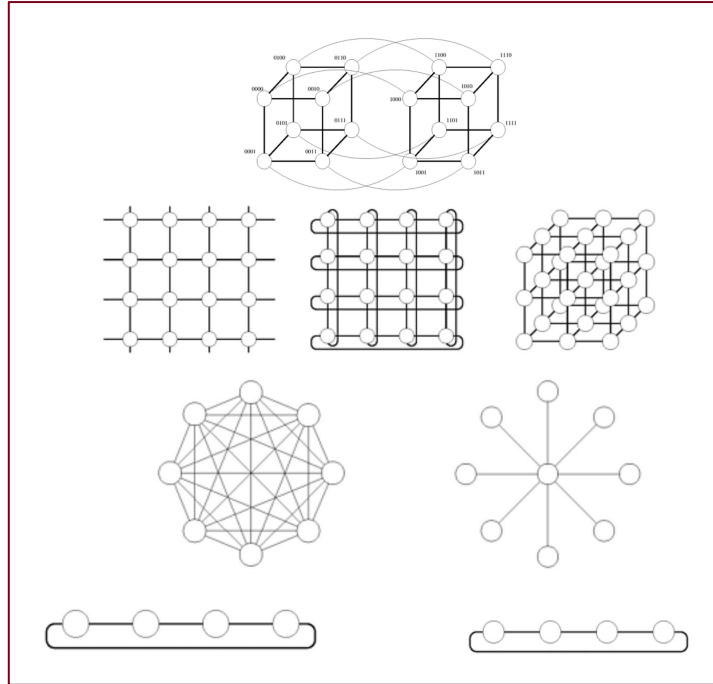
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❑ Decompositions (Recursive, Exploratory, Data, Speculative, Hybrid)

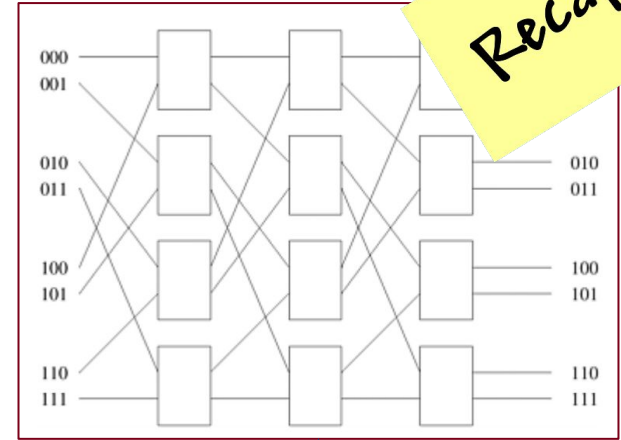
❑ Classifying Task Interaction & Generation



Recap



Topologies



Omega
Networks

Recap



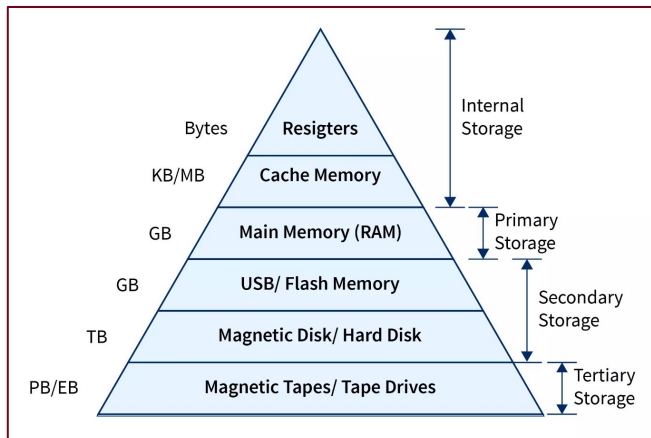
Recap

Recap

Topology Metrics

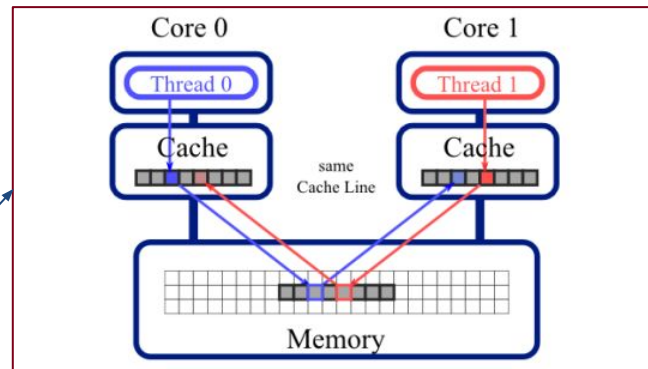
Table 2.1 A summary of the characteristics of various static network topologies.

Network	Diameter	Bisection Width	Arc Connectivity	(No. of links)
Completely-connected	1	$p^2/4$	$p - 1$	$p(p - 1)/2$
Star	2	1	1	$p - 1$
Complete binary tree	$2 \log((p + 1)/2)$	1	1	$p - 1$
Linear array	$p - 1$	1	1	$p - 1$
2-D mesh, no wraparound	$2(\sqrt{p} - 1)$	\sqrt{p}	2	$2(p - \sqrt{p})$
2-D wraparound mesh	$2\lfloor\sqrt{p}/2\rfloor$	$2\sqrt{p}$	4	$2p$
Hypercube	$\log p$	$p/2$	$\log p$	$(p \log p)/2$
Wraparound k -ary d -cube	$d\lfloor k/2\rfloor$	$2k^{d-1}$	$2d$	dp



Memory Basics

False Sharing



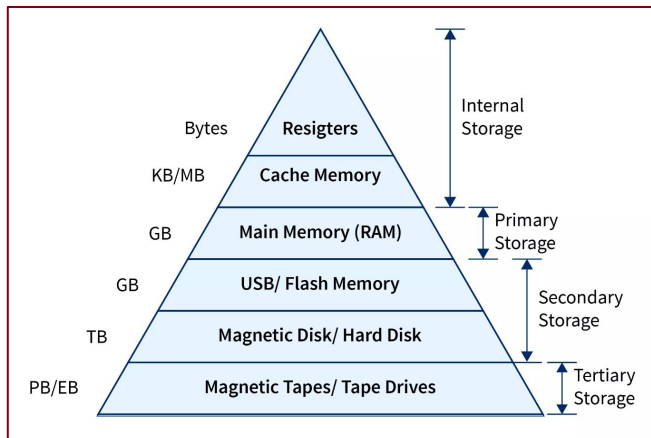
Recap

Recap

Topology Metrics

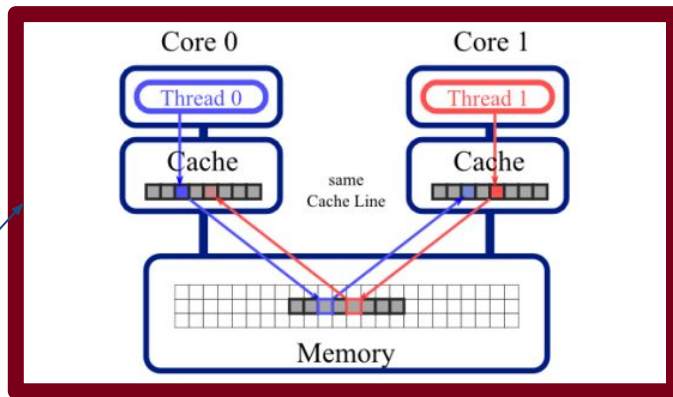
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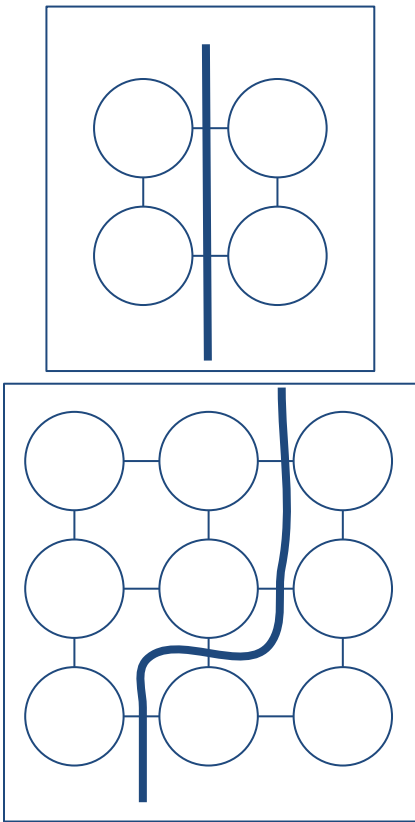


Memory Basics

False Sharing



Recap (Revisiting Mesh Bisection Width)



General Case

- $(\sqrt{p}) \bmod 2 == 0$
 - Bisection width = \sqrt{p}
- $(\sqrt{p}) \bmod 2 == 1$
 - Bisection width = $\sqrt{p} + 1$



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❑ Recap

❑ **Task Decomposition**

- **Background**

- MatVec Example Decompositions

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❑ Decompositions (Recursive, Exploratory, Data, Speculative, Hybrid)

❑ Classifying Task Interaction & Generation



How do we map from a serial program into some parallel program?



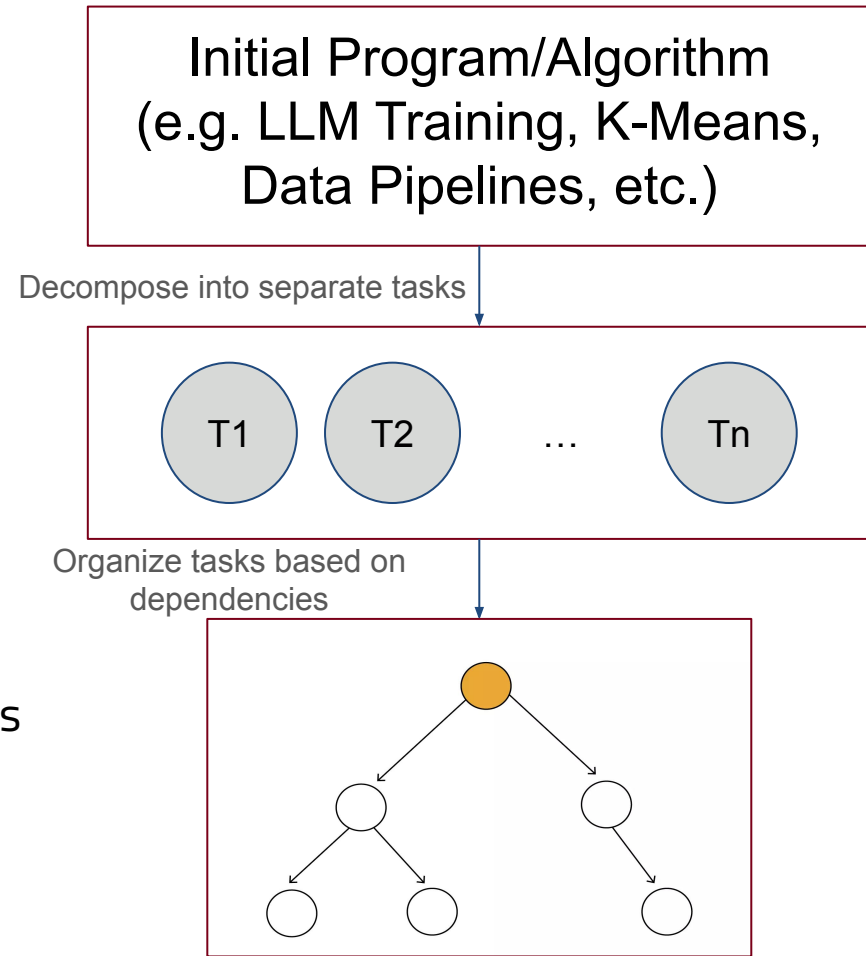
How do we map from a serial program into some parallel program?

Decompose the program into smaller tasks, then find out how to organize them.



Task Decomposition

- ❑ We have to break down the tasks individually and determine their dependencies
- ❑ What are tasks?
 - Atomic units of computation within our program
 - We as programmers decide what these tasks are
 - Once we define a task, we assume that it is both serial and indivisible



Lecture Overview

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Matrix Vector Multiplication

$$A * x = b$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$



Matrix Vector Multiplication

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Simplest decomposition: Don't decompose any tasks at all. This is the same as serial execution. No parallel speedups = bad task decomposition.



Matrix Vector Multiplication

$$A * x = b$$

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Other Decomposition Ideas?



Matrix Vector Multiplication

$$A * x = b$$

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Task 1

Task 2

Task 3



Matrix Vector Multiplication

Most Granular*

$$A * x = b$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$



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Tasks 1-3

Tasks 7-9

Tasks 4-6



Task Dependency Graph (TDG)

- ❑ Once we break things down into smaller tasks, we need to build out how we should execute them
- ❑ There can be *more than one* way to combine the tasks
- ❑ Each node is a task, arrows represent dependencies
- ❑ Each node will oftentimes have the amount of work required attached to them (typically represented by the number of atomic operations performed within that task - add, subtract, multiply, divide)
- ❑ We assume, within each task, that work is serial



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Why might this be a poor way of measuring work?



Task Dependency Graph (TDG)

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- ❑ We assume, within each task, that work is serial

For our purposes, we will assume all work is equal until later on in the course.



Matrix Vector Multiplication (TDG)

$$A * x = b$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$

How to
represent this
decomposition
as a TDG?



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Task 1
(15)

Amount of Work



Matrix Vector Multiplication (TDG)

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$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$

Task 1

Task 2

Task 3

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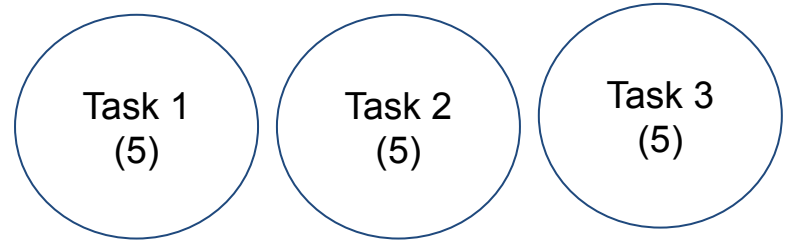
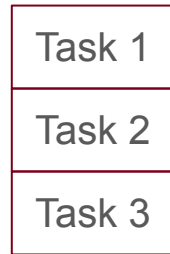


Matrix Vector Multiplication (TDG)

No edges
because there
are no
dependencies
between tasks

$$A * x = b$$

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} ax + by + cz \\ dx + ey + fz \\ gx + hy + iz \end{bmatrix}$$



Matrix Vector Multiplication

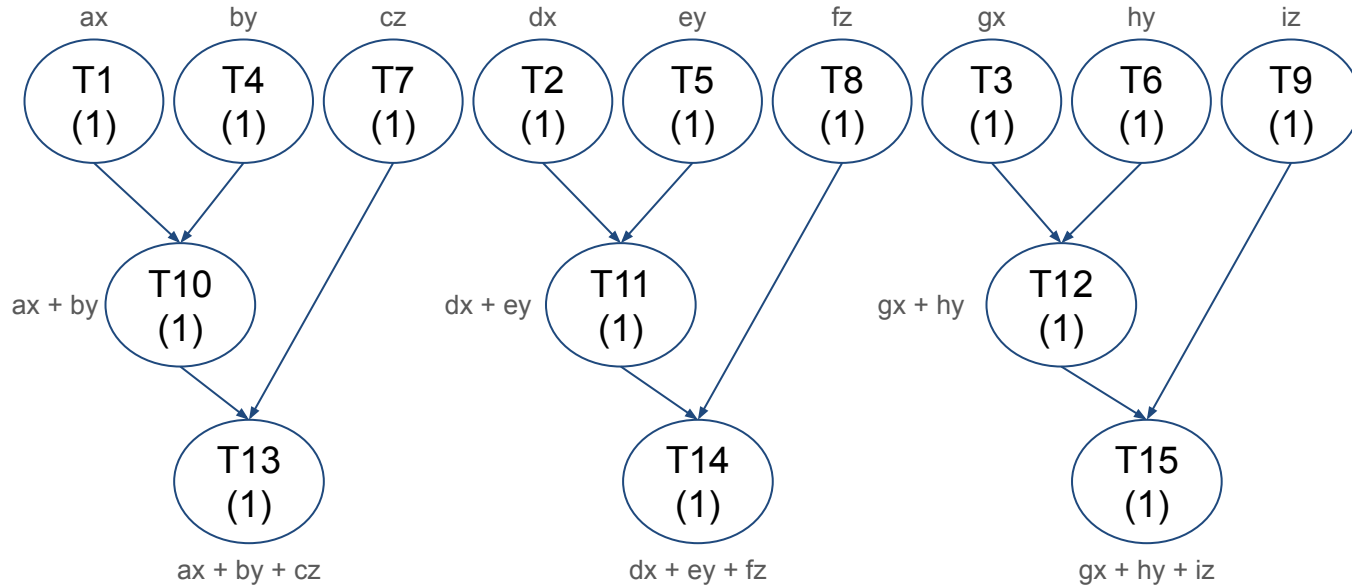
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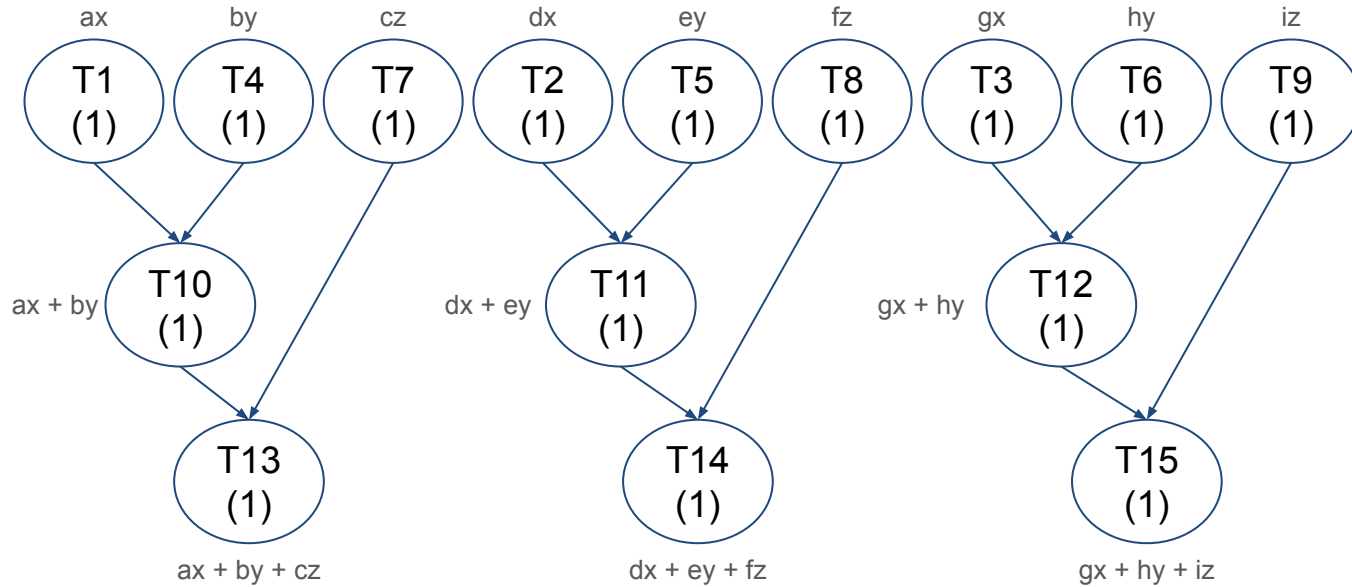
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Matrix Vector Multiplication



Matrix Vector Multiplication



Alternative
Decompositions?

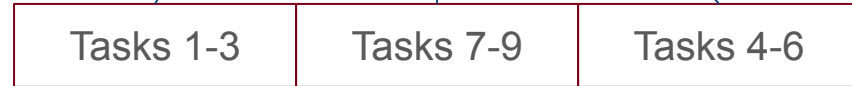


Matrix Vector Multiplication

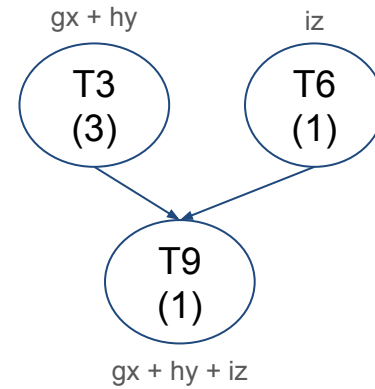
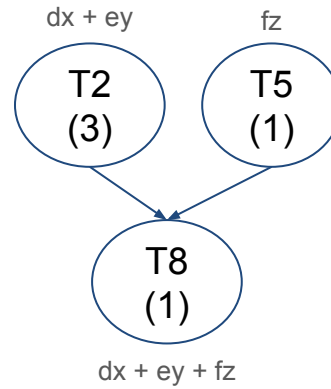
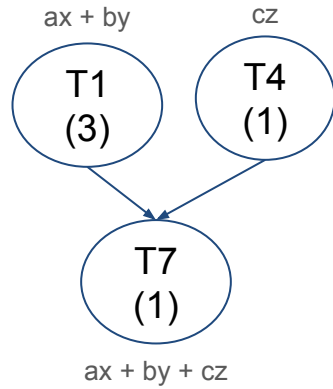
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How to
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Matrix Vector Multiplication



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- MatVec Example Decompositions
- **Metrics & Definitions**

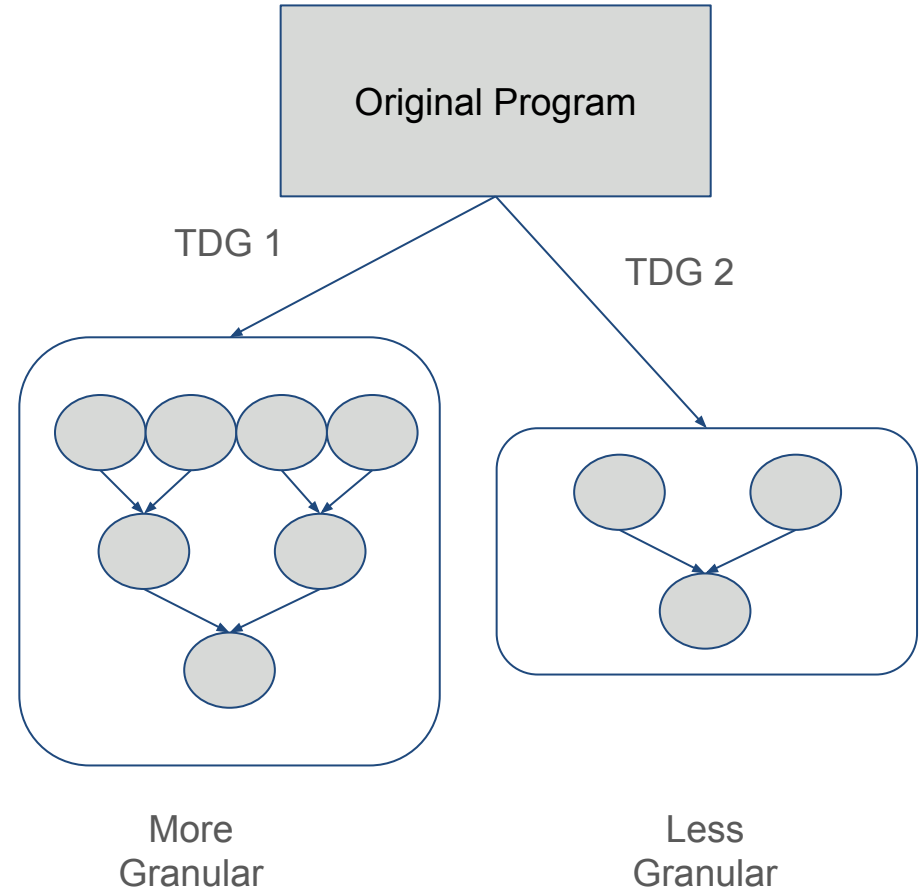
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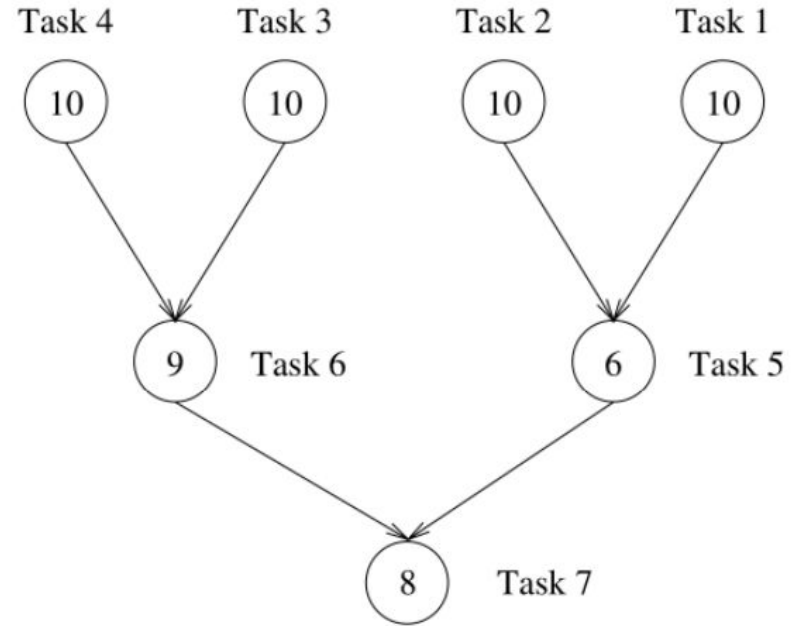
Granularity

- ❑ Defines how fine-grain the parallel program has been decomposed
- ❑ More granular = smaller tasks with less work per task
- ❑ Less granular = larger tasks with more work per task



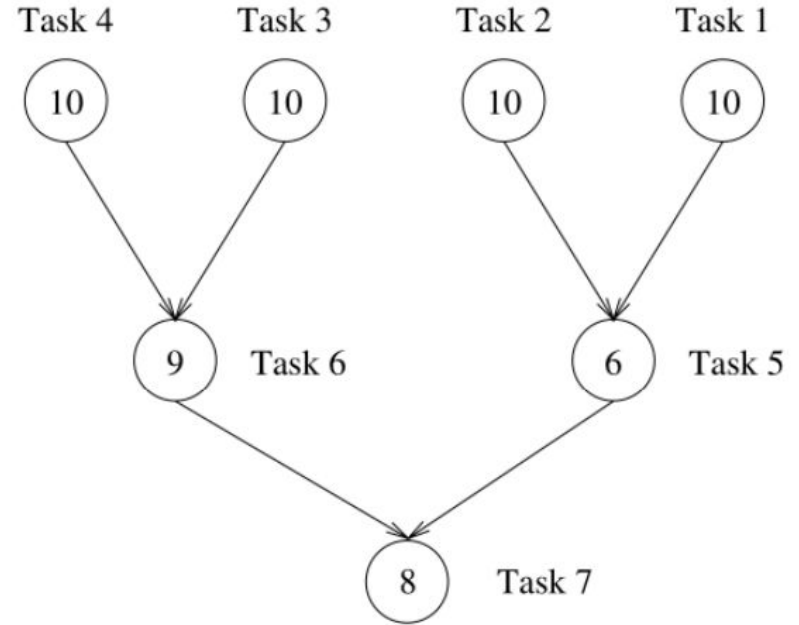
Total Work

Sum of all work completed over all tasks



Total Work

Sum of all work completed over all tasks

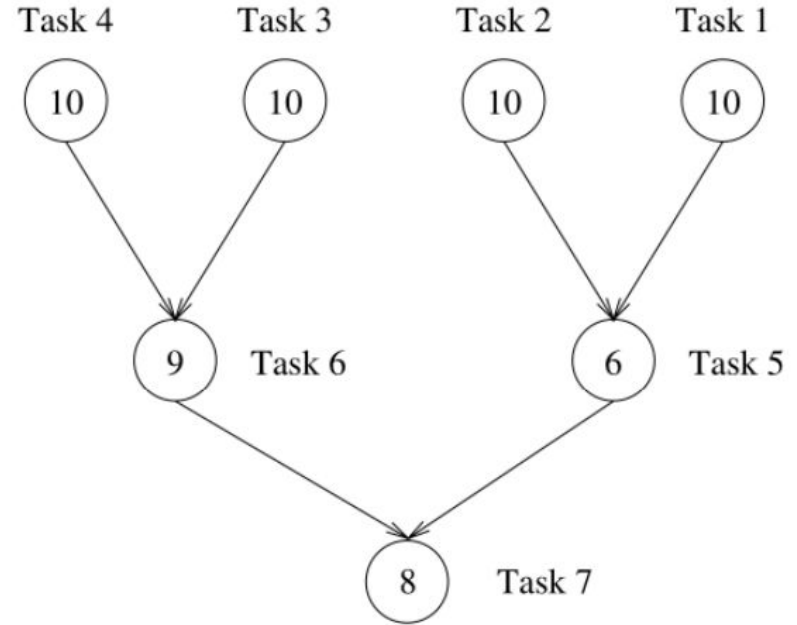


Total Work = 63



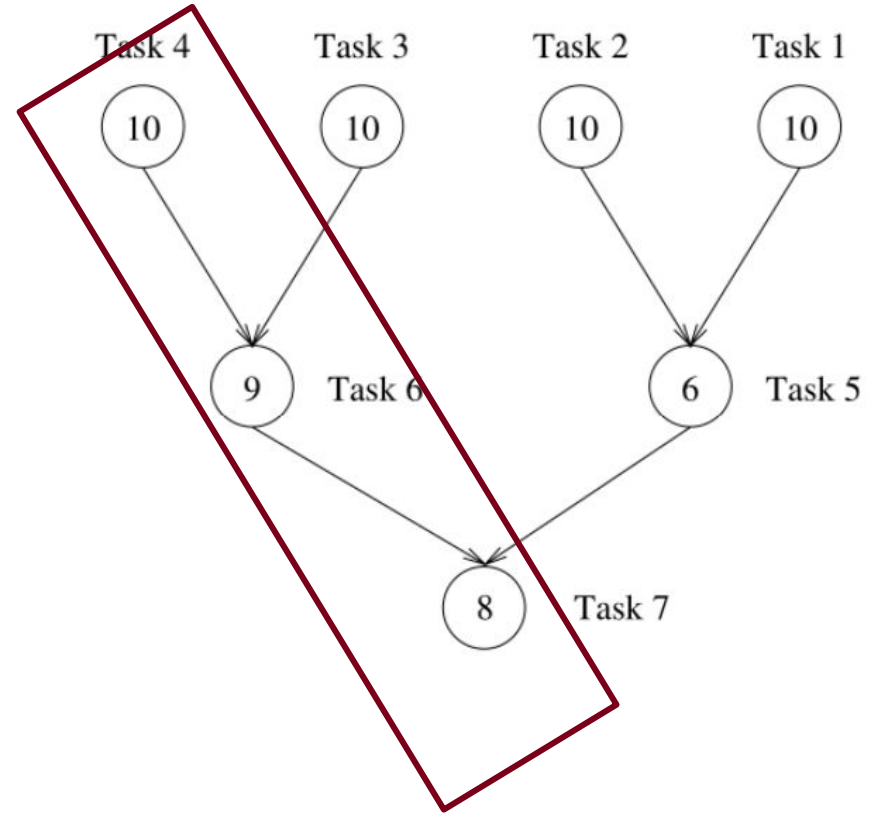
Critical Path Length

Largest amount of *sequential* work which must be performed in order to complete program execution



Critical Path Length

Largest amount of *sequential* work which must be performed in order to complete program execution



Critical Path Length = 27



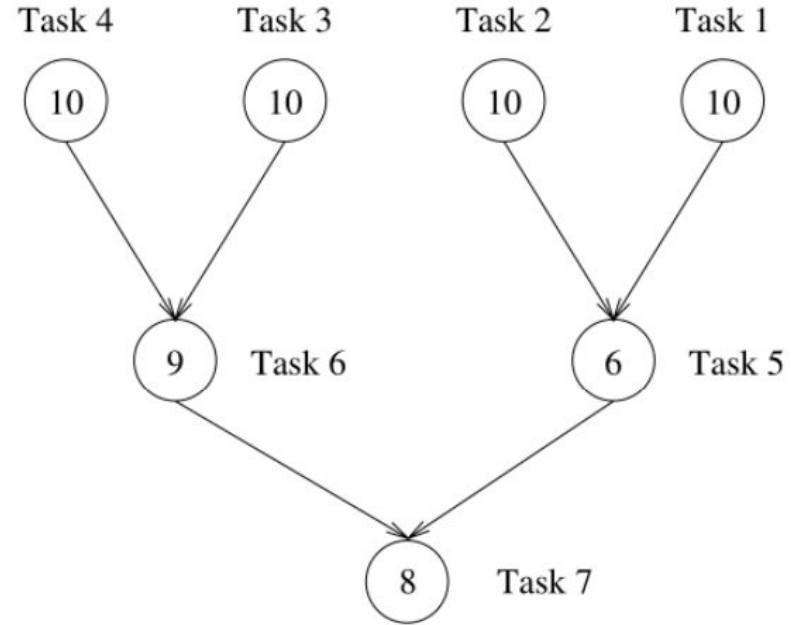
Concurrency

Maximum Concurrency

- Largest number of tasks which can be completed concurrently
- The largest *width* of the TDG

Average Concurrency

- Total Work/Critical Path Length
- This term usually sets an upper bound on parallel speedups



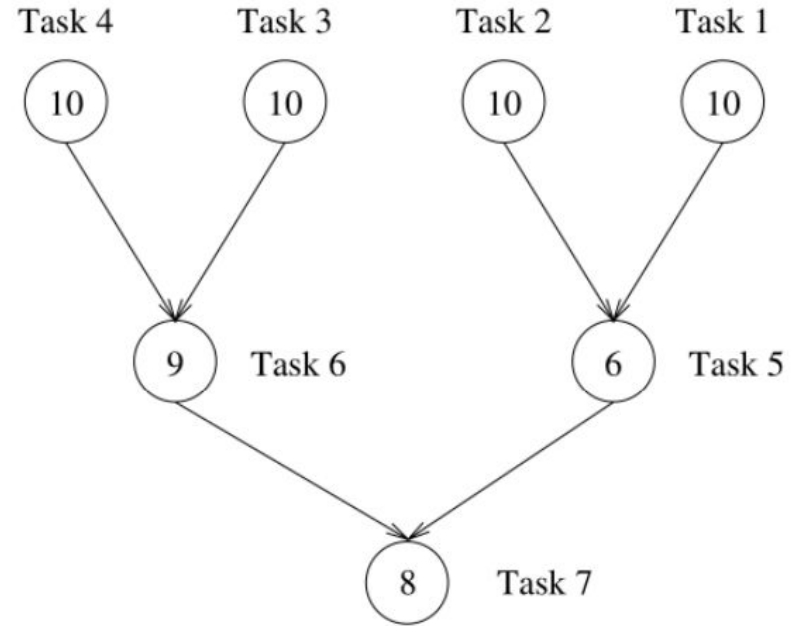
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Average Concurrency

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Maximum Concurrency = 4
Average Concurrency = 2.33



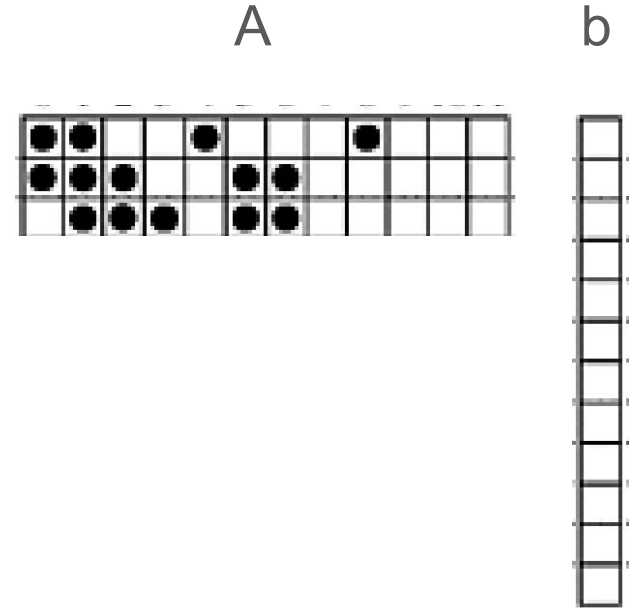
Sparse MatVec Example TDG + Metrics

□ Assume

- A is sparse
- b is dense

□ In Class Example

- Decompose this into tasks
- Create a Task Decomposition Graph (TDG) for these tasks
- Define the following metrics for this TDG
 - ✓ Total Work
 - ✓ Critical Path Length
 - ✓ Average + Maximum Currency



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What are some general strategies we can use for decomposing algorithms?



Recursive Decomposition

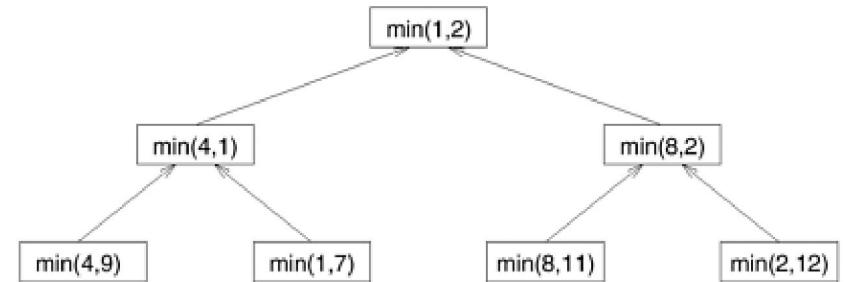
- ❑ Problems which can be solved via some divide + conquer strategies
- ❑ Subproblems can be recursively parallelized
- ❑ Partition tasks to each recursive call
- ❑ Examples
 - Finding the minimum element of an array
 - Quicksort Example



Recursive Decomposition

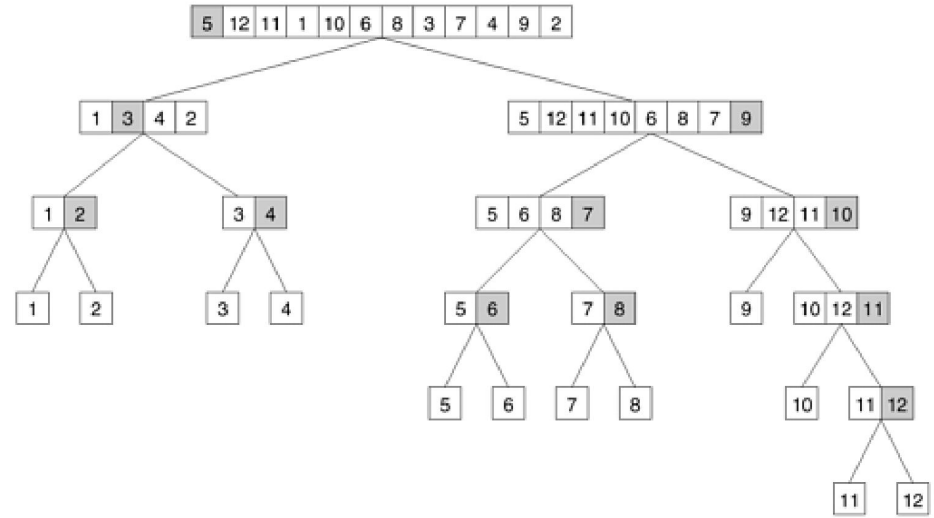
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{4, 9, 1, 7, 8, 11, 2, 12}



Recursive Decomposition

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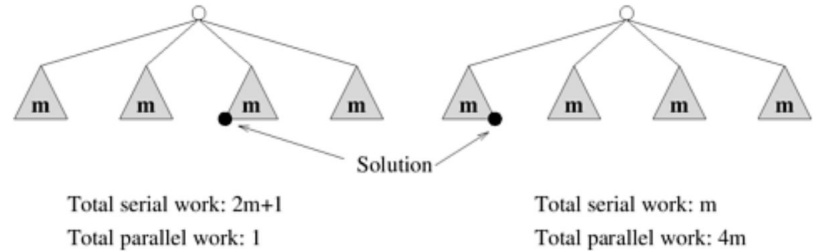
Exploratory Decomposition

- ❑ Use this for problems involving some kind of search
- ❑ Partition the search space among different processes
- ❑ Can lead to much anomalous speedups (slower or faster)
- ❑ Example
 - 15-puzzle search



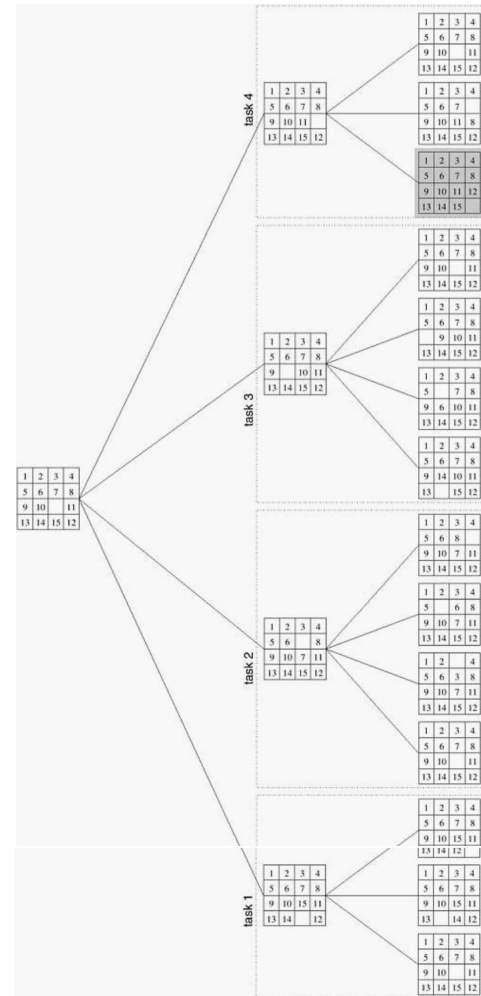
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Exploratory Decomposition

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- ❑ Example
 - 15-puzzle search



Data Decomposition (Output)

- ❑ Take the expected outputs of your program, then split them among your processes
- ❑ Assign tasks to each of these output elements

$$\text{Task 1: } C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1}$$

$$\text{Task 2: } C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2}$$

$$\text{Task 3: } C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1}$$

$$\text{Task 4: } C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2}$$

$$\begin{pmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{pmatrix} \cdot \begin{pmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{pmatrix} \rightarrow \begin{pmatrix} \boxed{C_{1,1}} & \boxed{C_{1,2}} \\ \boxed{C_{2,1}} & \boxed{C_{2,2}} \end{pmatrix}$$



Data Decomposition (Intermediate)

- ❑ Many algorithms have multiple, sequential stages of computation
- ❑ First partition the problem into these intermediate computations
- ❑ Then assign tasks based on which processes *own* which computation

Stage I

$$\begin{pmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{pmatrix} \cdot \begin{pmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{pmatrix} \rightarrow \begin{pmatrix} \begin{pmatrix} D_{1,1,1} & D_{1,1,2} \\ D_{1,2,1} & D_{1,2,2} \end{pmatrix} \\ \begin{pmatrix} D_{2,1,1} & D_{2,1,2} \\ D_{2,2,1} & D_{2,2,2} \end{pmatrix} \end{pmatrix}$$

Stage II

$$\begin{pmatrix} D_{1,1,1} & D_{1,1,2} \\ D_{1,2,1} & D_{1,2,2} \end{pmatrix} + \begin{pmatrix} D_{2,1,1} & D_{2,1,2} \\ D_{2,2,1} & D_{2,2,2} \end{pmatrix} \rightarrow \begin{pmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{pmatrix}$$

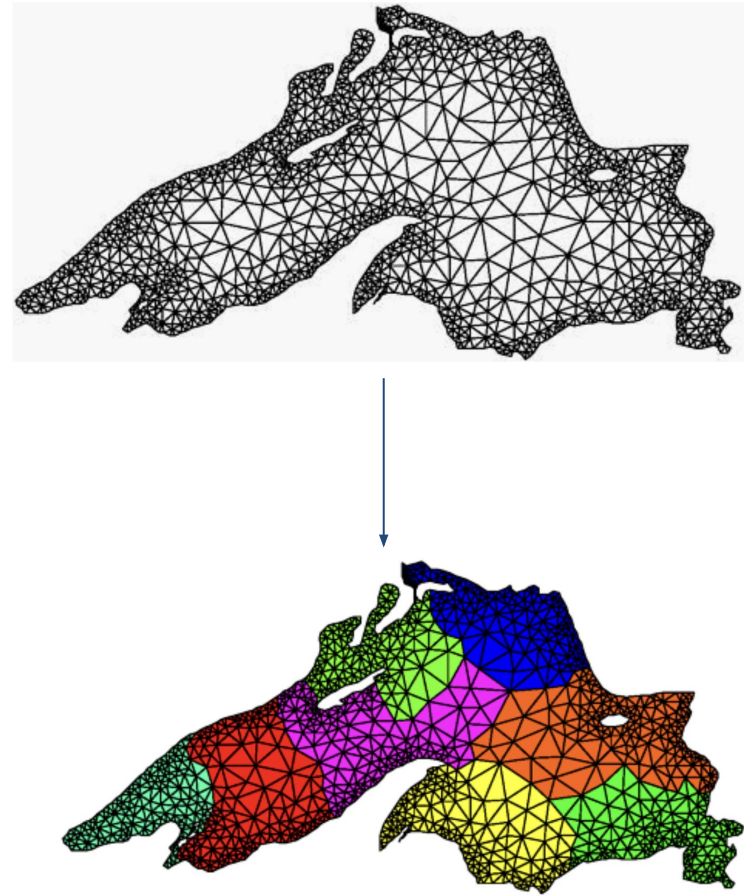
A decomposition induced by a partitioning of D

- Task 01: $D_{1,1,1} = A_{1,1} B_{1,1}$
- Task 02: $D_{2,1,1} = A_{1,2} B_{2,1}$
- Task 03: $D_{1,1,2} = A_{1,1} B_{1,2}$
- Task 04: $D_{2,1,2} = A_{1,2} B_{2,2}$
- Task 05: $D_{1,2,1} = A_{2,1} B_{1,1}$
- Task 06: $D_{2,2,1} = A_{2,2} B_{2,1}$
- Task 07: $D_{1,2,2} = A_{2,1} B_{1,2}$
- Task 08: $D_{2,2,2} = A_{2,2} B_{2,2}$
- Task 09: $C_{1,1} = D_{1,1,1} + D_{2,1,1}$
- Task 10: $C_{1,2} = D_{1,1,2} + D_{2,1,2}$
- Task 11: $C_{2,1} = D_{1,2,1} + D_{2,2,1}$
- Task 12: $C_{2,2} = D_{1,2,2} + D_{2,2,2}$



Data Decomposition (Input)

- ❑ First split the inputs of the problem into separate pieces so that each process will only have some subset of data
- ❑ Then assign tasks based on what data each of your processes stores
- ❑ Example:
 - Measuring temperatures at various positions in Lake Superior
 - Want to predict temperatures in the future



Speculative Decomposition

- Useful when a program has many conditional branches & computationally intensive statements to execute to determine the appropriate branch

- Examples

- Simple Switch Statement
- Discrete Event Simulation

```
int main() {  
    int choice = long_running_program();  
  
    switch (choice) {  
        case 1:  
            f_1();  
            break;  
        case 2:  
            f_2();  
            break;  
        case 3:  
            f_3();  
            break;  
        case 4:  
            f_4();  
            break;  
        default:  
            printf("Invalid choice.\n");  
    }  
}
```

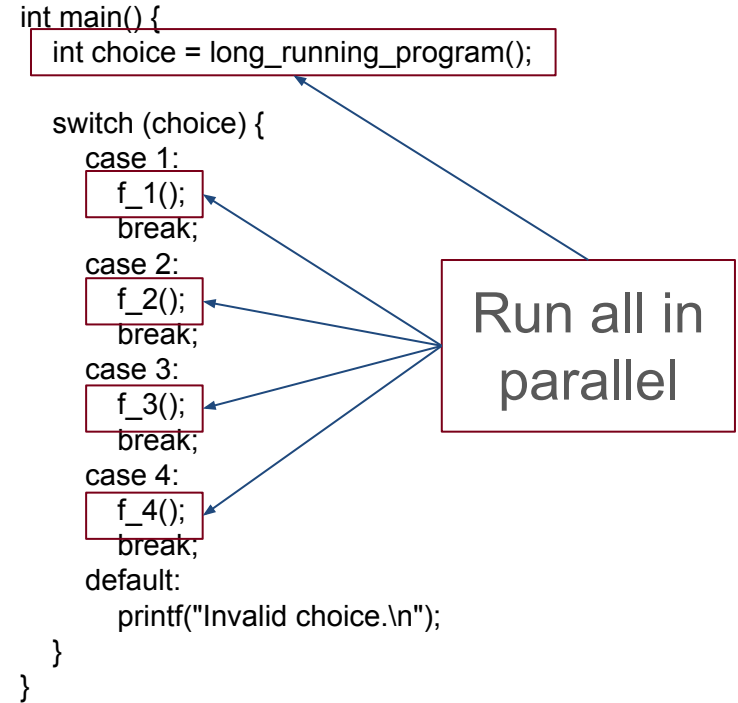


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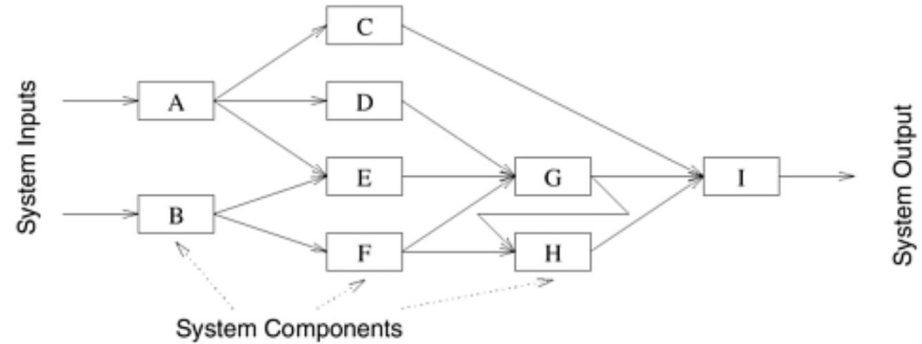


Speculative Decomposition

❑ Useful when a program has many conditional branches & computationally intensive statements to execute to determine the appropriate branch

❑ Examples

- Simple Switch Statement
- Discrete Event Simulation



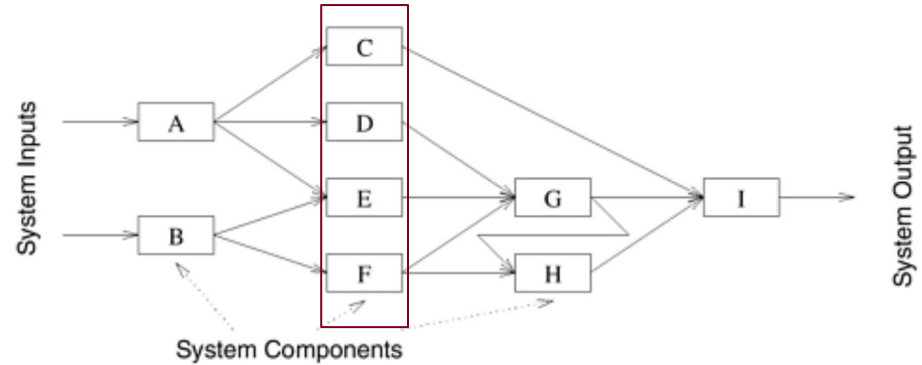
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Run multiple conditional branches at a time



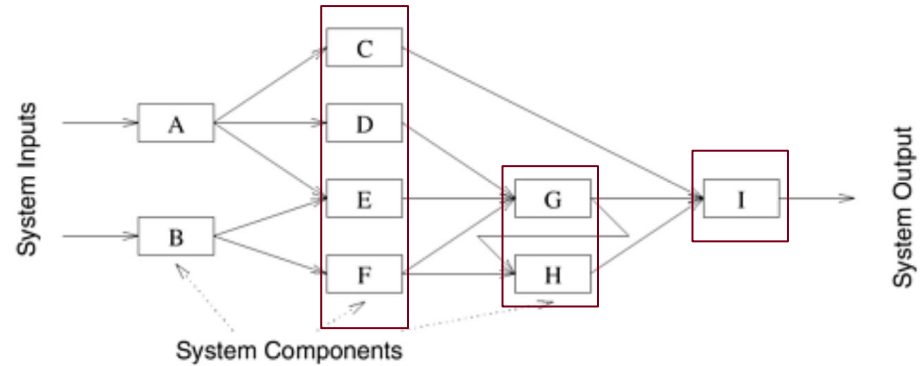
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❑ Examples

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...we can also run computations at greater depth in parallel



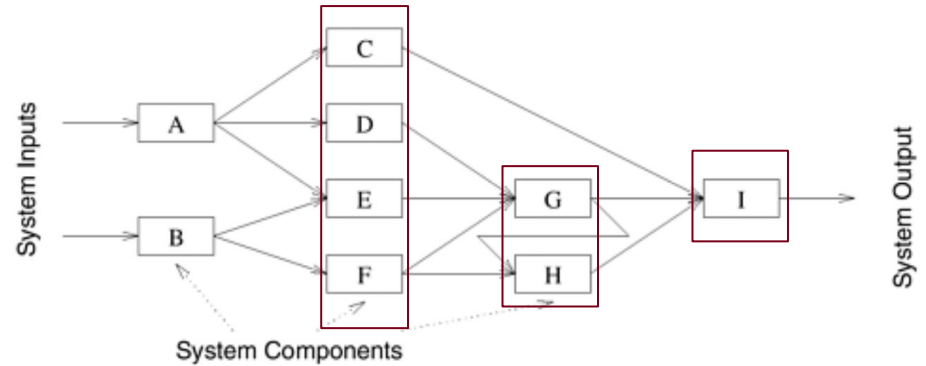
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Under what conditions, can we not run each of the following tasks at the same time?



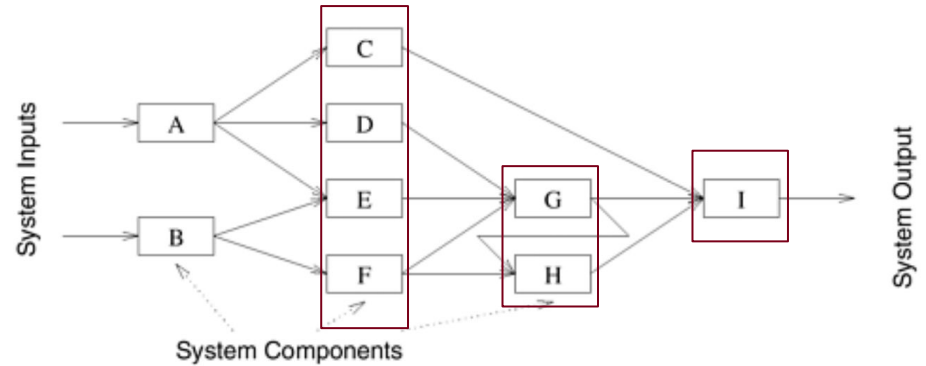
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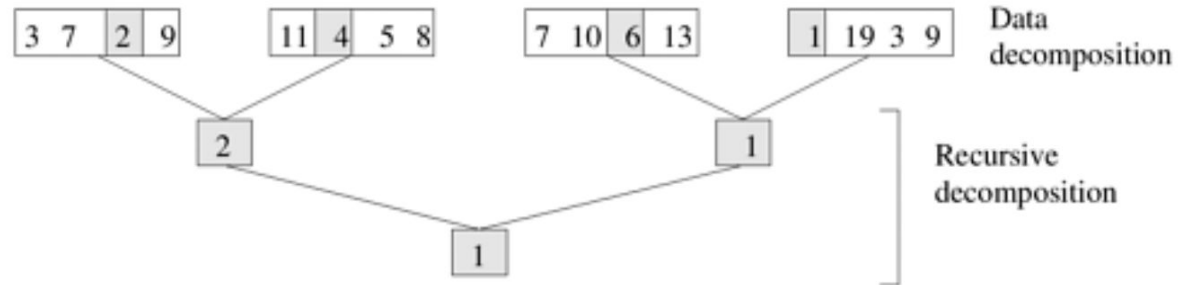
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...when the data produced from earlier tasks is required for later ones (i.e. computing **G** is dependent on **A**)

Hybrid Decomposition

- ❑ Combine multiple decomposition techniques at the same time
- ❑ More typical in practical settings
- ❑ Example (Min-Array)



Lecture Overview

- ❑ Recap
- ❑ Task Decomposition
 - Background
 - MatVec Example Decompositions
 - Metrics & Definitions
- ❑ Decompositions (Recursive, Exploratory, Data, Speculative, Hybrid)
- ❑ **Classifying Task Interaction & Generation**



How can we classify task generation & interaction?



Static vs. Dynamic Task Generation

- ❑ Static Task Generation: All tasks are known *exactly* before program execution
- ❑ Dynamic Task Generation: Tasks and the Task Dependency Graph are not known exactly before program execution



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(a)

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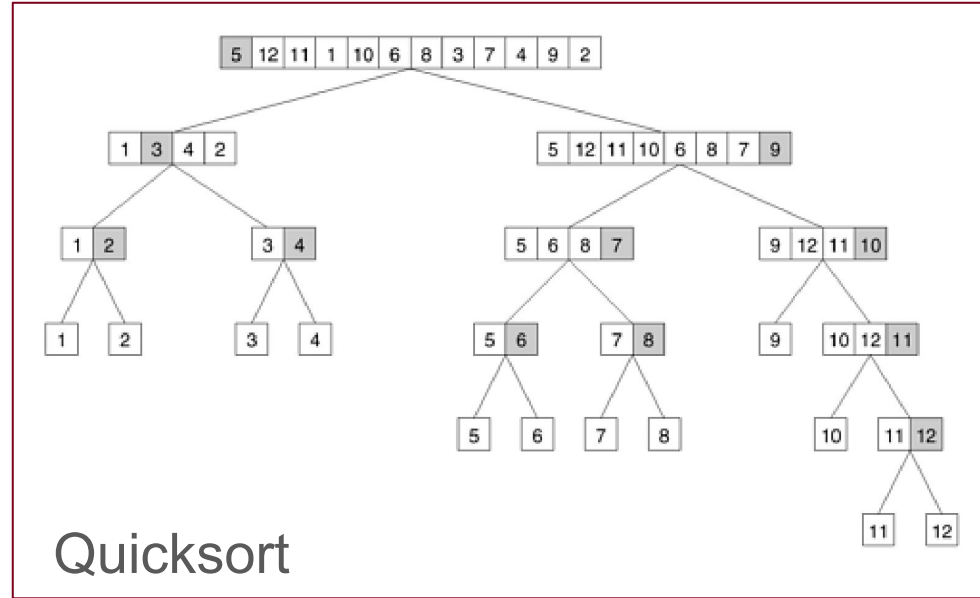
$$\text{Task 3: } C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1}$$

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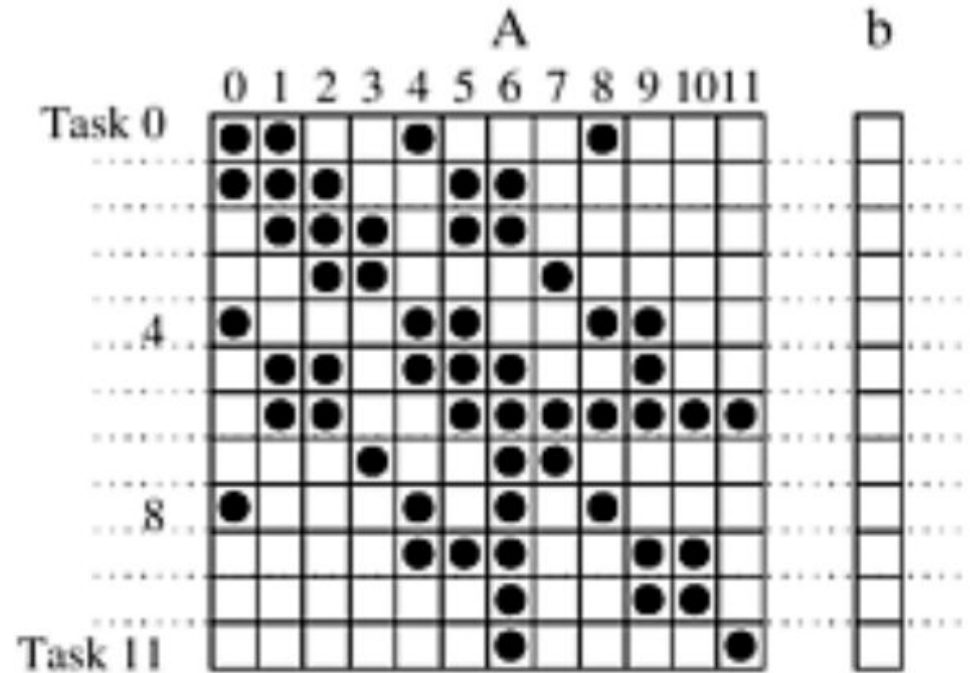
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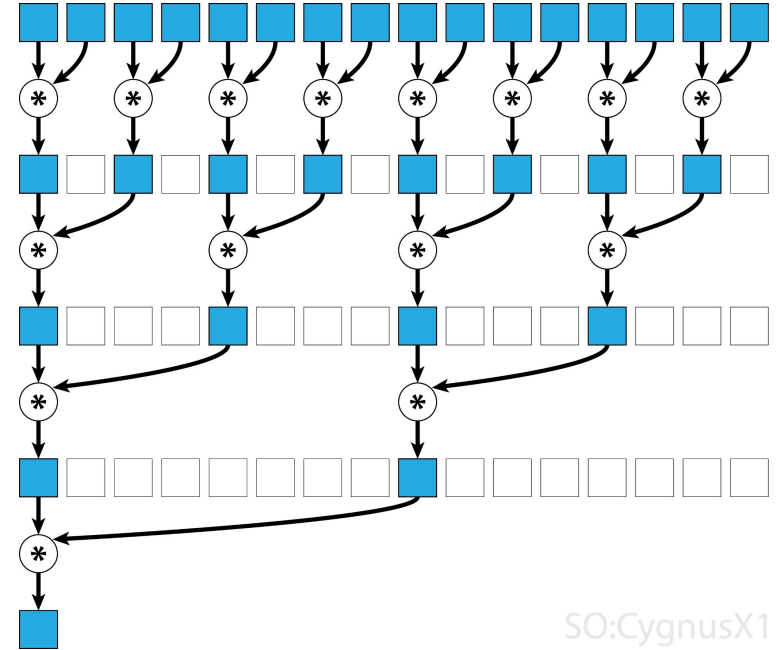
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SO: CygnusX1

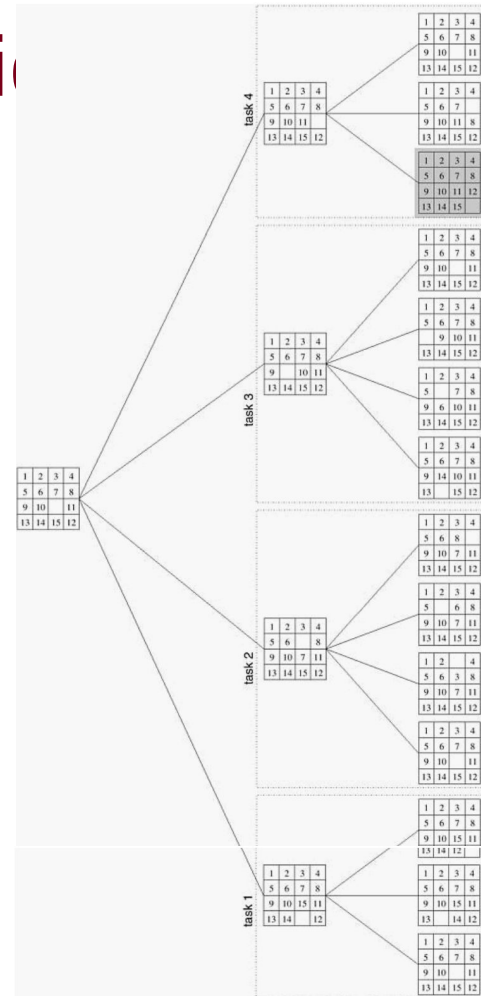
Parallel Array Sum
Interactions are fixed



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Search Problems require communication to prevent redundant rollouts



Regular vs. Irregular Task Interactions

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