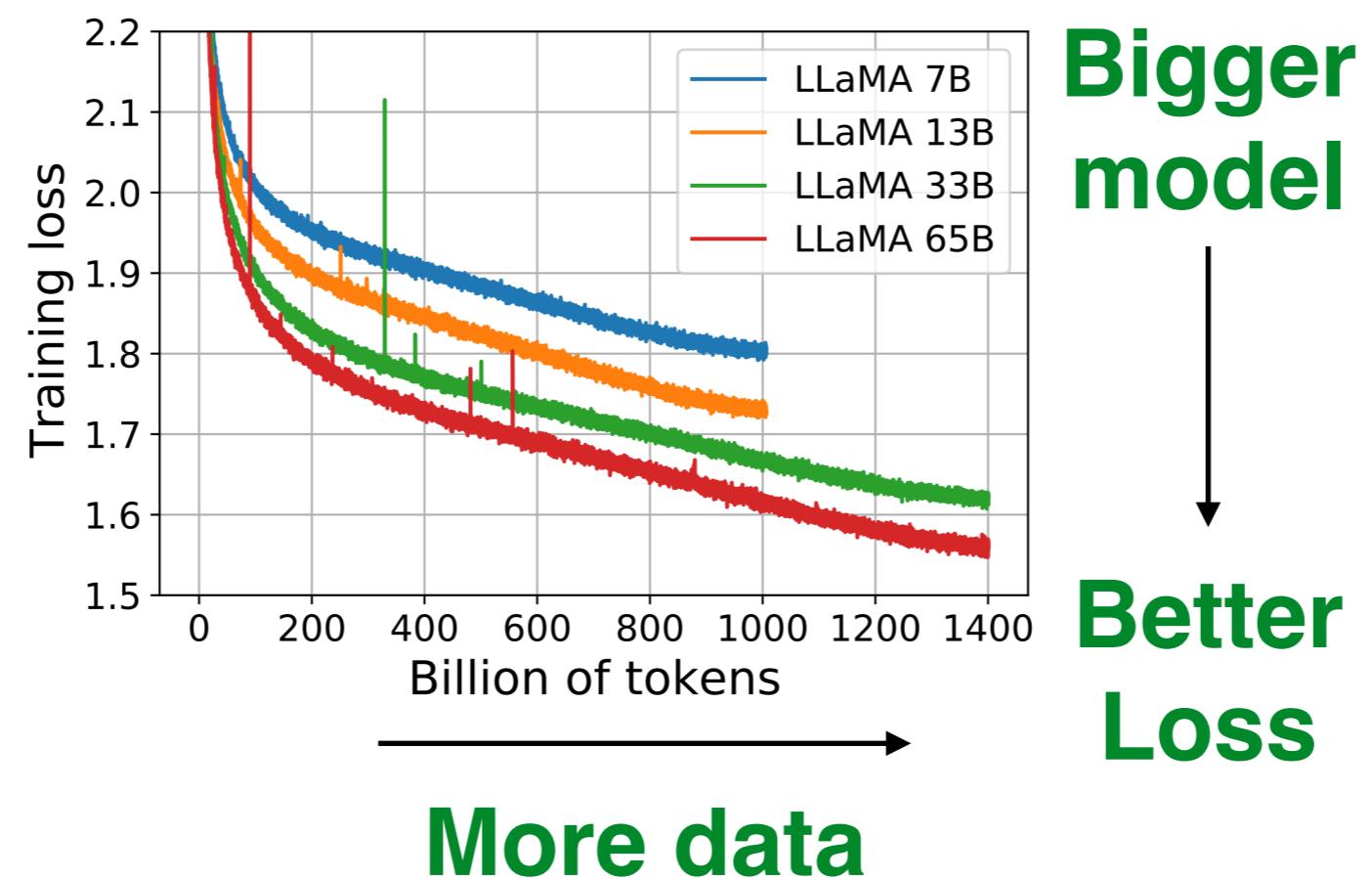
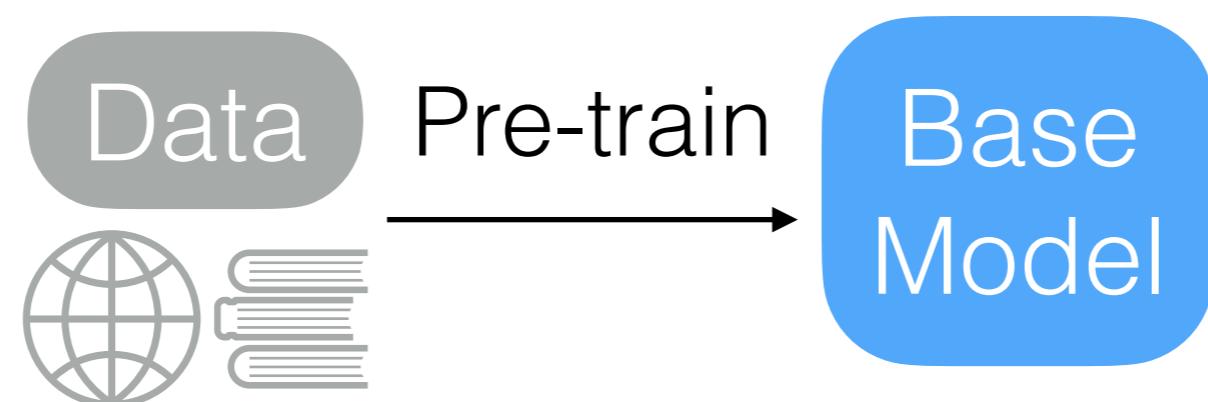


# Scaling and Parallelism

James Mooney

Slides from [Sean Welleck](#)

# Recap: pre-training



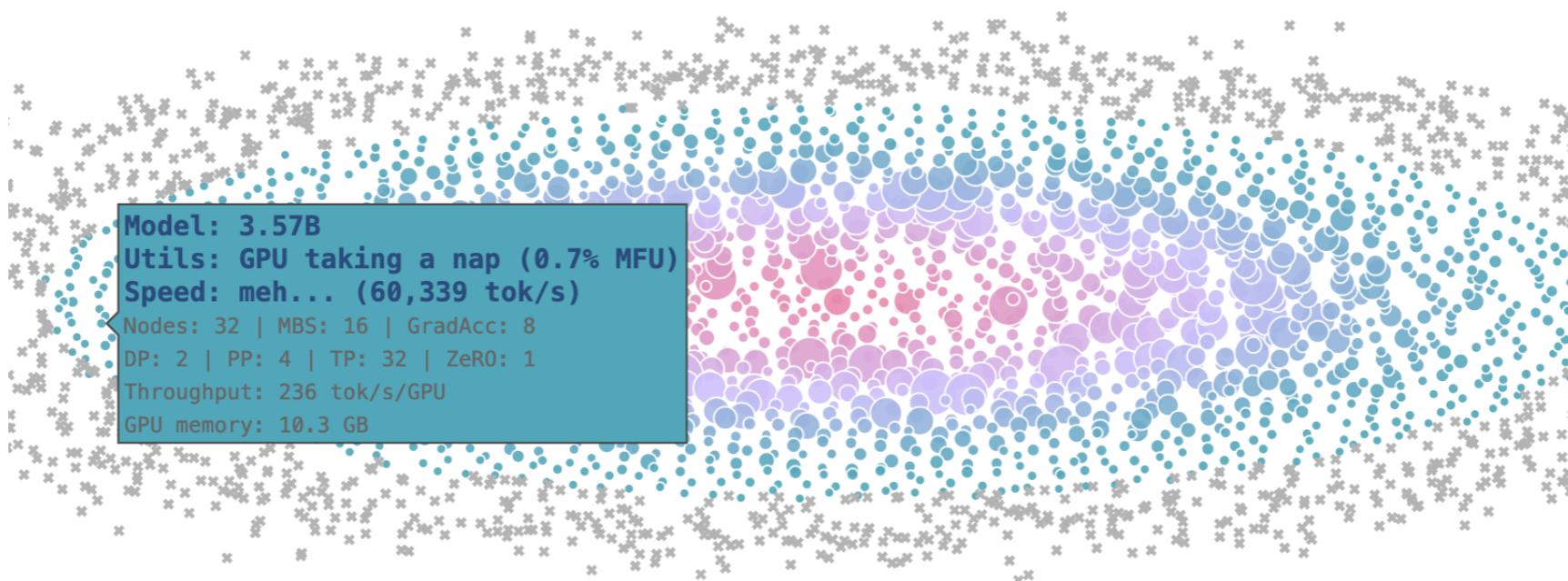
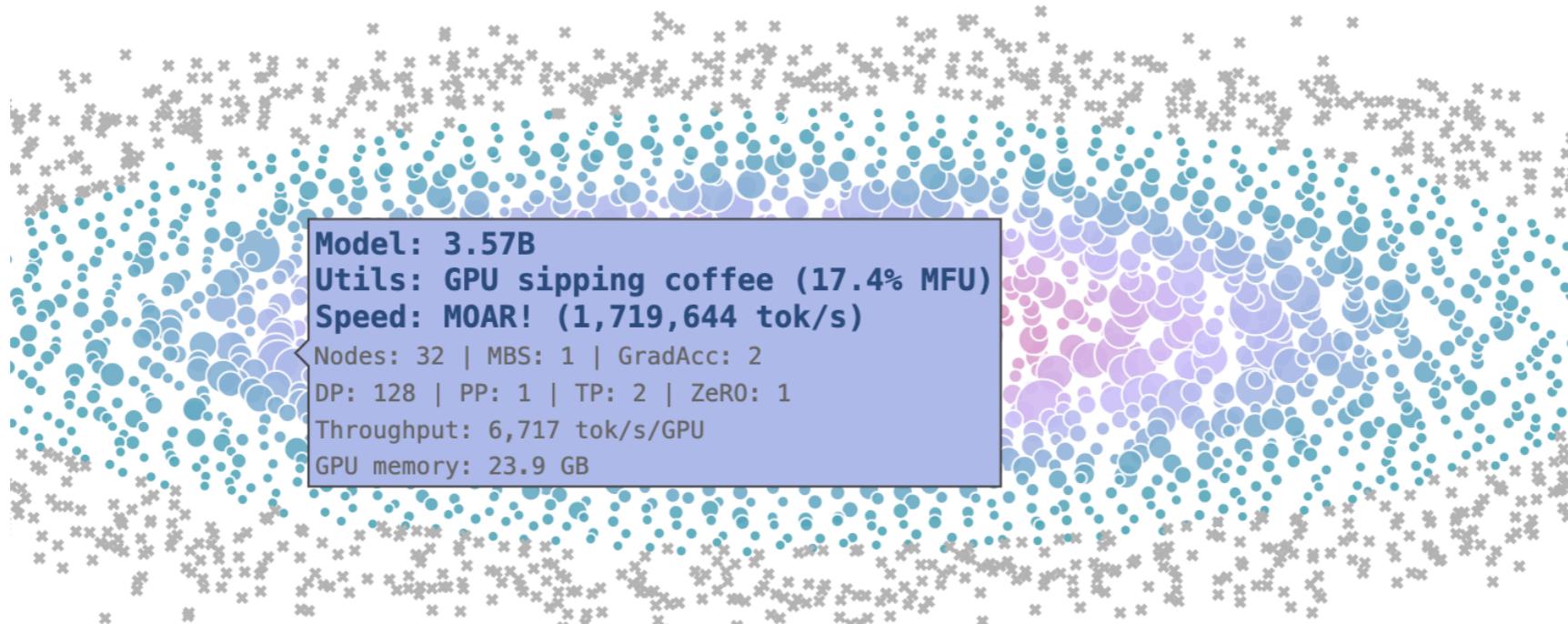
# Scale the training of LLMs

- Key problem: take advantage of multiple devices (e.g., GPUs)
  - Train larger models
  - Process more tokens in a given amount of time

# Scale the training of LLMs

- **Memory usage:** training steps need to fit in memory
- **Compute efficiency:** we want our hardware to spend most time computing
- **Communication overhead:** minimize since it keeps GPUs idle

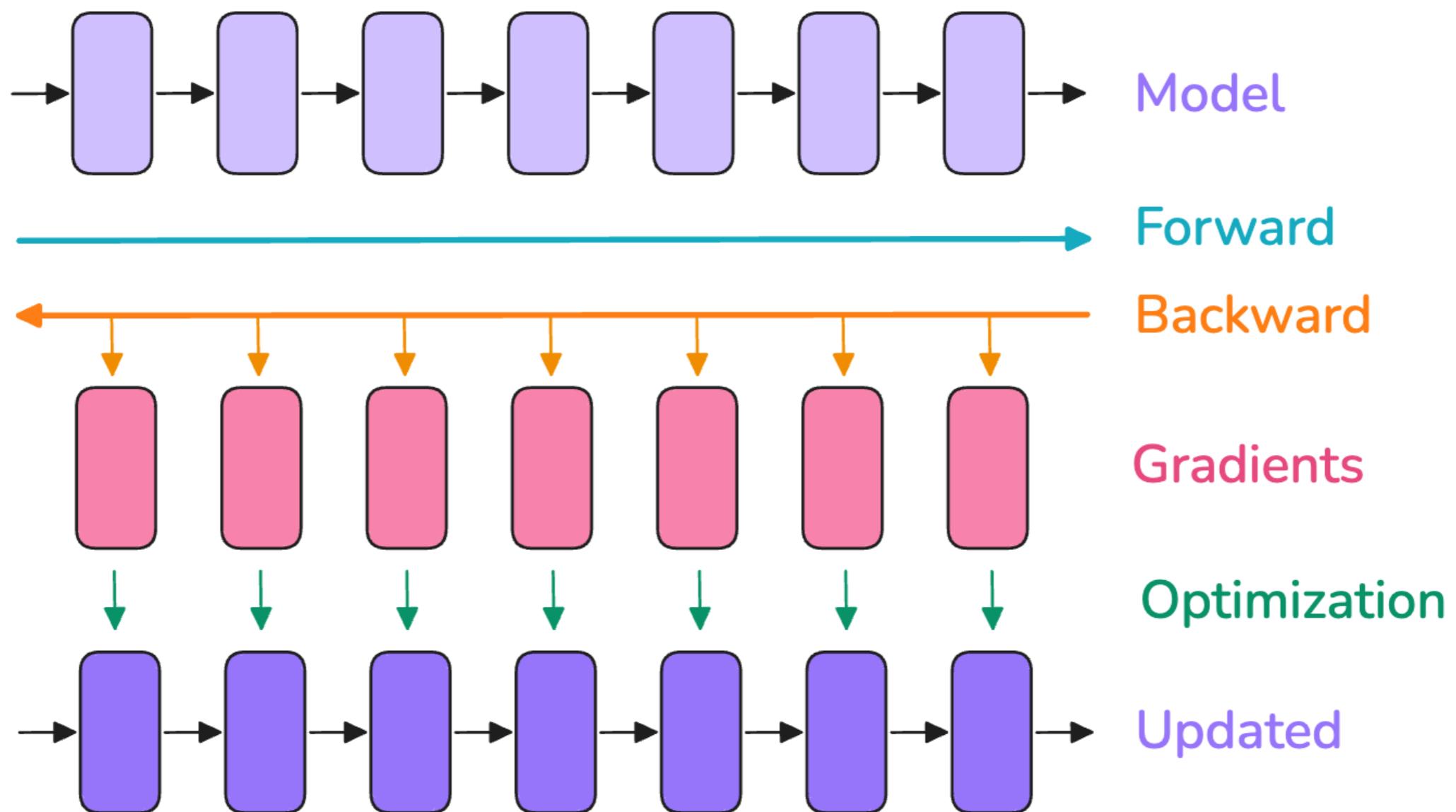
# Large impact



# Today's lecture

- Basics of training on one GPU
- Parallelization on multiple GPUs
  - Data, tensor, pipeline parallelism, ZeRO
- Choosing and comparing strategies

# Training on one GPU



# Training basics

- Compute
- Memory
  - Activation recomputation
  - Gradient accumulation

# Compute

- Compute: floating point operations (FLOP)
  - Forward and backward pass:  
 $6 \times \text{model\_parameters} \times \text{token\_batch\_size}$
  - FLOPS: floating point operations per second

# Compute

- **Model FLOP Utilization (MFU)** measures how effectively available compute is used for training

$$\text{MFU} = \frac{\text{Achieved FLOPS}}{\text{Theoretical Peak FLOPS}}$$

- Theoretical peak (H100):

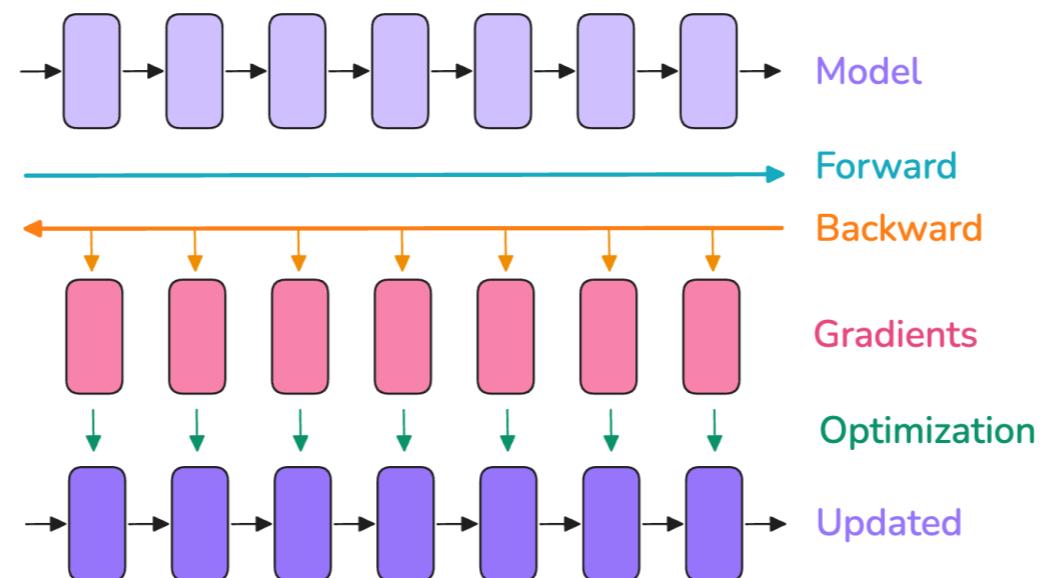
## Technical Specifications

H100 SXM	
<b>FP64</b>	34 teraFLOPS
<b>FP64 Tensor Core</b>	67 teraFLOPS
<b>FP32</b>	67 teraFLOPS
<b>TF32 Tensor Core*</b>	989 teraFLOPS
<b>BFLOAT16 Tensor Core*</b>	1,979 teraFLOPS

- Inefficiencies: communication, memory bandwidth, idle time (discussed later!)

# Memory usage

- Weights, gradients, optimizer states, activations
  - Tensors with shapes and precisions



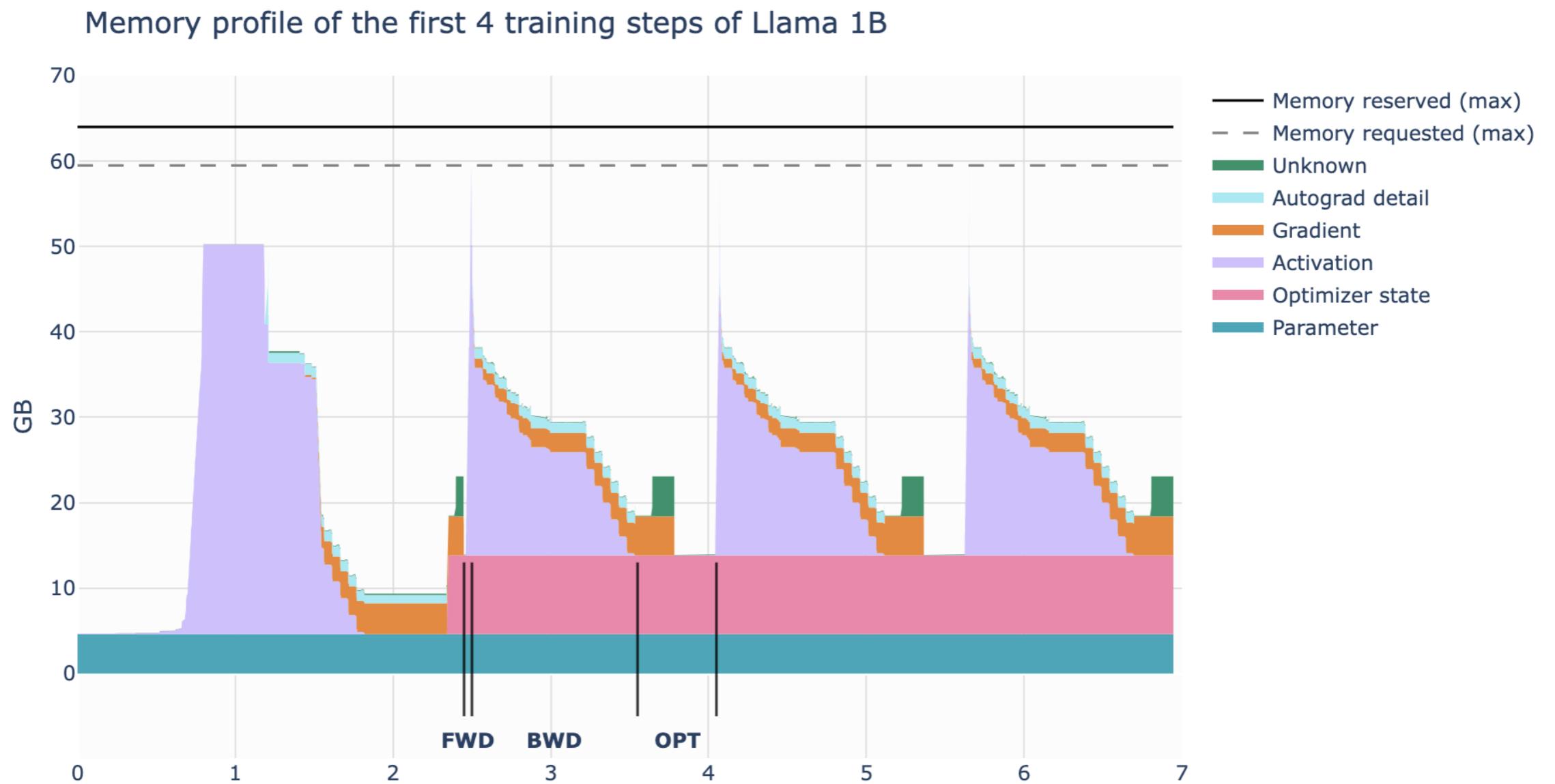
# Memory usage

- A rough approximation for a training step:

`peak_memory = model_bf16 + model_fp32 + grads_fp32 + optim_states + activations`

- BF16 model:  $2 * \text{num\_parameters}$
- FP32 model/grads:  $4 * \text{num\_parameters}$
- FP32 optimizer states:  $(4 + 4) * \text{num\_parameters}$ 
  - Adam momentum and variance

# Memory usage



# Memory usage

<b>Model parameters</b>	<b>FP32 or BF16 w/o FP32 grad acc</b>	<b>BF16 w/ FP32 grad acc</b>
1B	16 GB	20 GB
7B	112 GB	140 GB
70B	1120 GB	1400 GB
405B	6480 GB	8100 GB

H100 GPU: 80 GB

# Batch size

- **Small**: adjust parameters quickly but noisily
- **Large**: adjust parameters accurately, fewer steps to train on a given dataset

$$bst = bs * seq$$

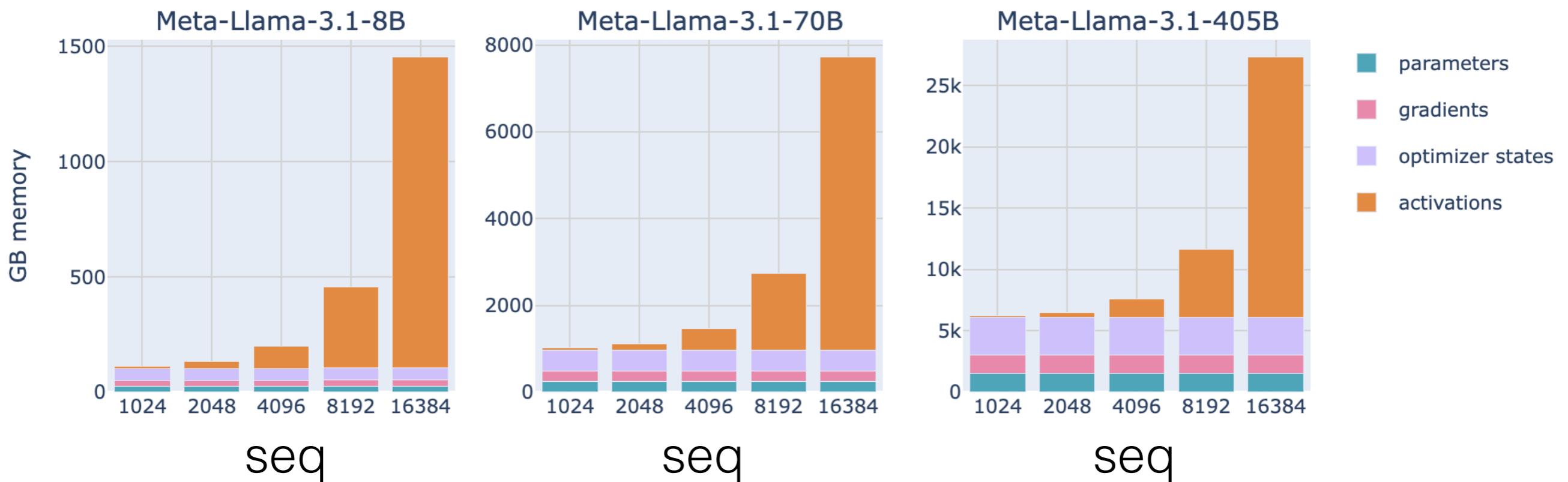
Typically ~4-60 million tokens per batch

- **Too large**: out of memory due to large activations!

# Memory usage: activations

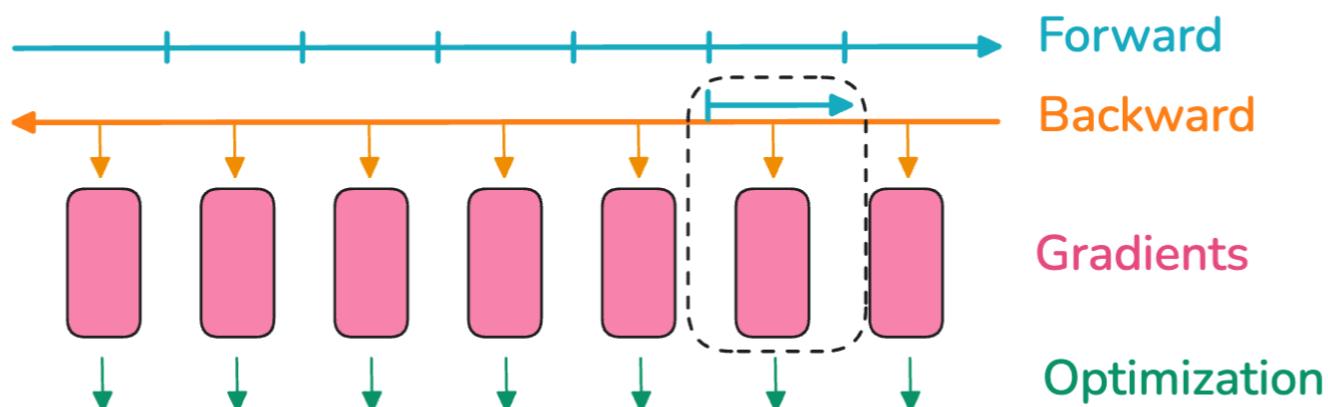
$$m_{act} = L \cdot seq \cdot bs \cdot h \cdot \left( 34 + \frac{5 \cdot n_{heads} \cdot seq}{h} \right)$$

- Linear with batch size, quadratic sequence length



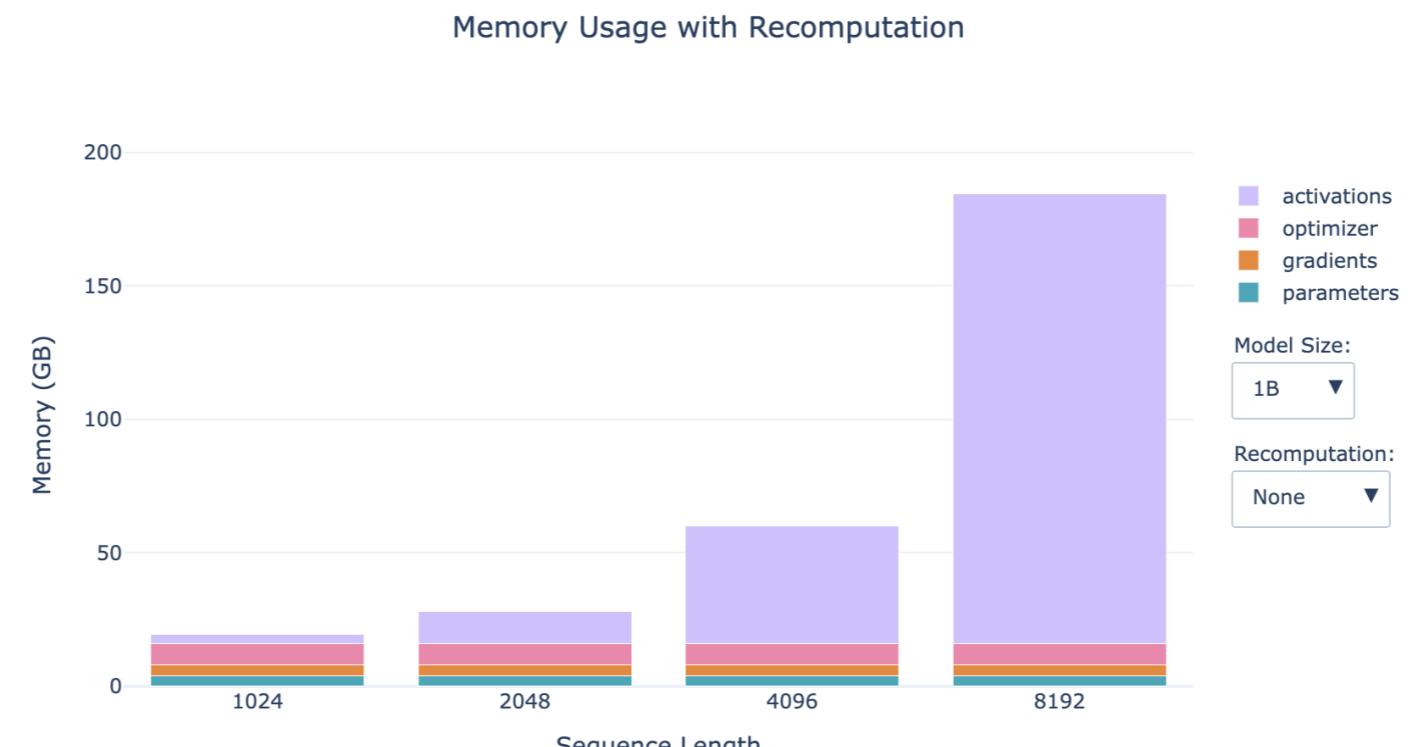
# Activation recomputation

- Recompute some activations during the backward pass
  - Store some activations during the forward pass as “checkpoints”
  - Discard other activations and recompute them during the backward pass
- Increases compute, reduces activation memory requirements

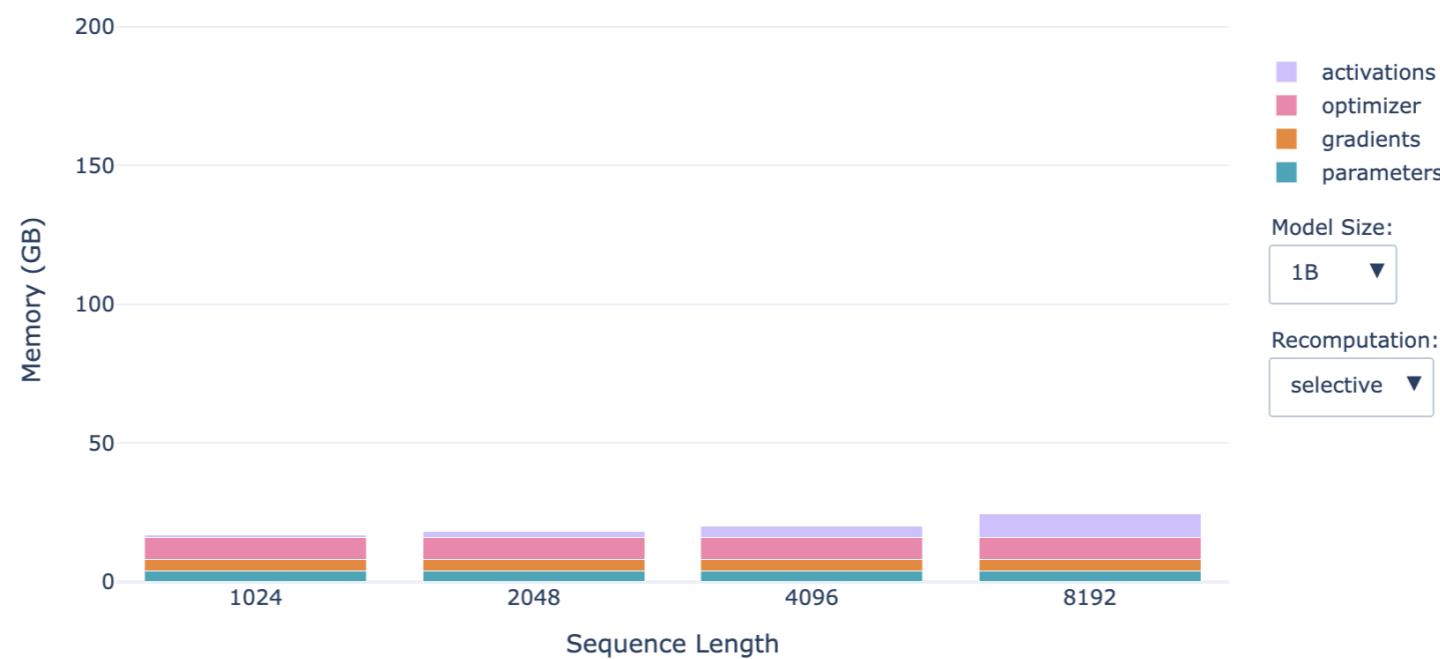


# Activation recomputation

Without  
recomputation



With  
recomputation

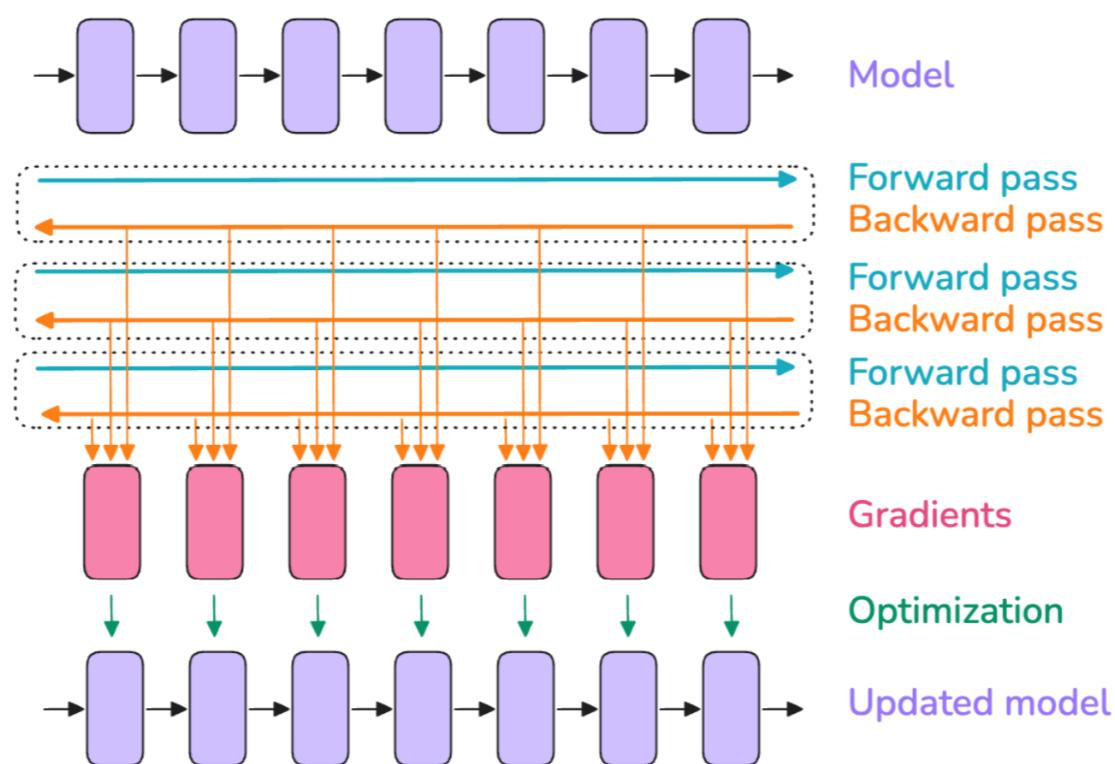


# Gradient accumulation

- Split batch into micro-batches, do forward/backward passes on each micro-batch, average the gradients

$$bs = gbs = mbs \cdot grad\_acc$$

- Lets you increase batch size with constant memory



# Recap: basics (single GPU)

- **Compute**: FLOPS and MFU
- **Memory**: parameters, gradients, optimizer states, activations
- **Activation recomputation**: save memory, add compute
- **Gradient accumulation**: save memory, add compute
- Use of memory savings: larger batch size and/or larger model

# Multiple GPUs: Parallelism

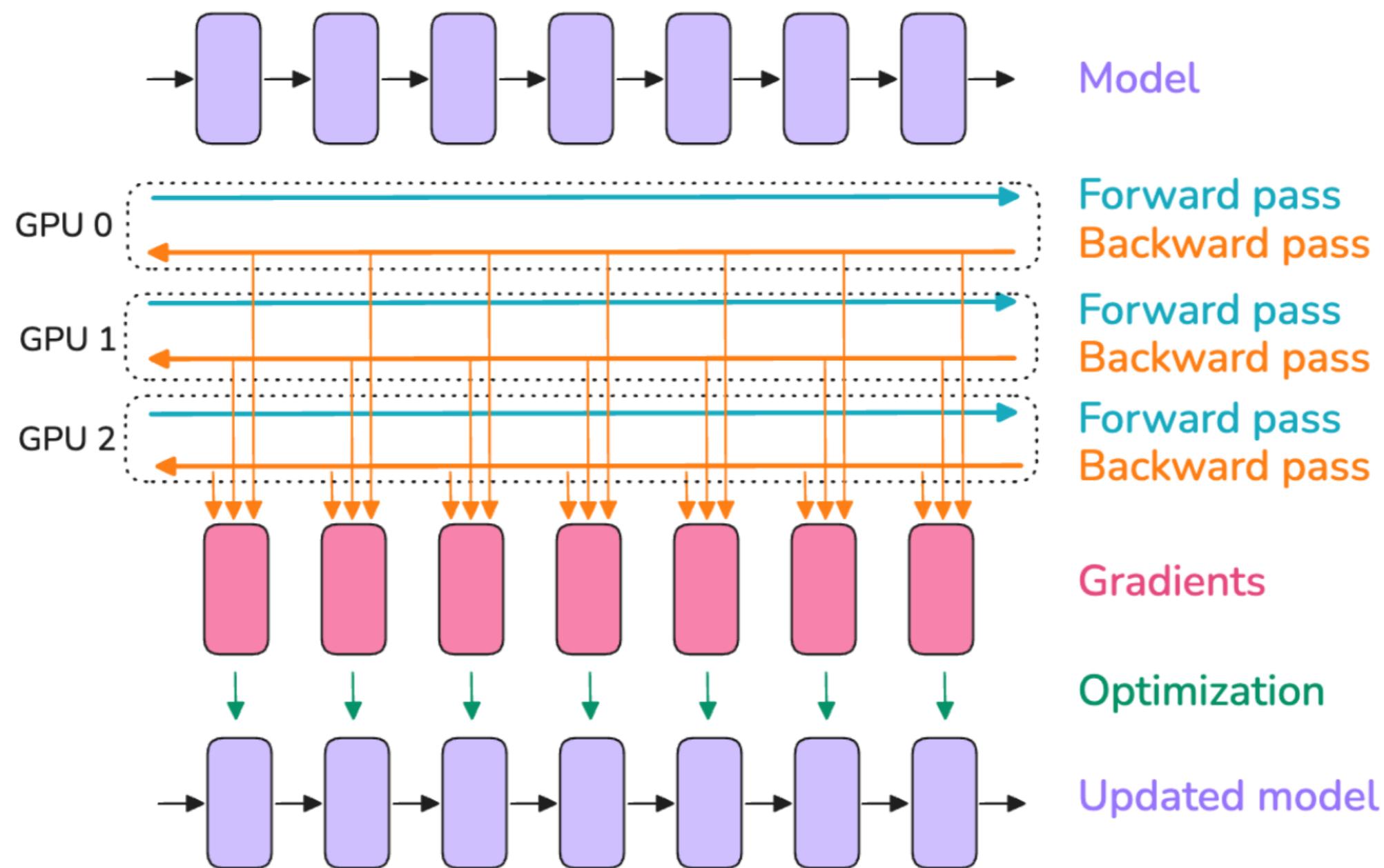
# Parallelism

- Techniques for leveraging computation and memory from multiple GPUs
  - Data parallelism
  - Tensor parallelism
  - Pipeline parallelism
  - Memory optimization
  - Choosing parallelism strategies

# Data Parallelism

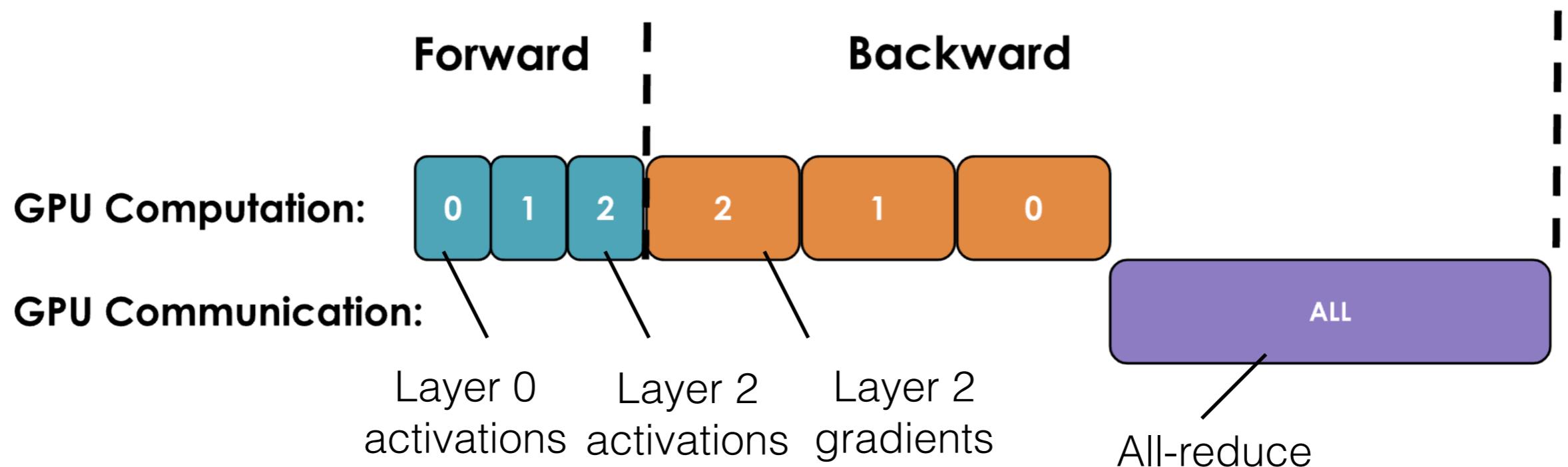
- Replicate model on several GPUs
- Run forward / backward passes on different micro-batches in parallel for each GPU
- Average the gradients across the GPUs

# Data Parallelism



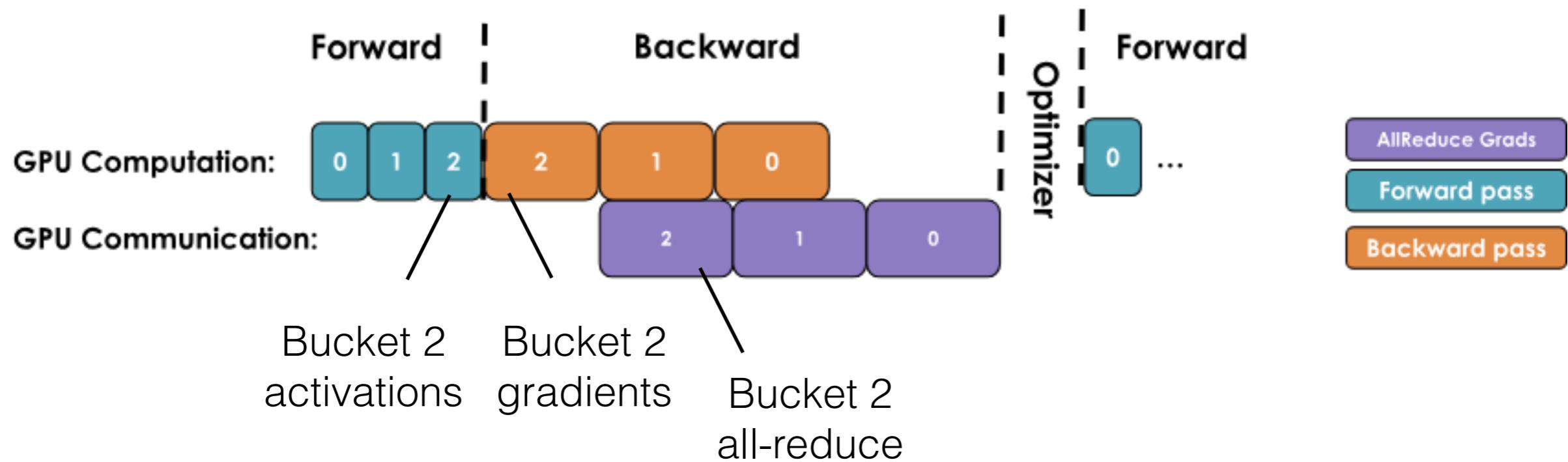
# Data Parallelism: Naive

- Wait for all backward passes to finish, trigger an all-reduce over all GPUs



# Overlap + bucketing

- Start all-reduce as soon as gradients are ready
- Group gradients into buckets and launch a single all-reduce for all the gradients in the same bucket



# Data Parallelism: + bucketing

```
59     class BucketManager:
60         def __init__(self, params: List[torch.nn.Parameter], process_group: torch.distributed.ProcessGroup, bucket_size:
61
62             cur_bucket_size = 0
63             cur_bucket_idx = 0
64
65             # Assign parameters to buckets.
66             for param in self.params:
67                 if not param.requires_grad:
68                     continue
69
70                 # If the bucket is empty, add the parameter to the bucket.
71                 if cur_bucket_size == 0:
72                     self.params_to_bucket_location[param] = (0, param.numel(), cur_bucket_idx)
73                     cur_bucket_size = param.numel()
74                     continue
75
76                 # If the parameter cannot fit in the current bucket, create a new bucket
77                 if cur_bucket_size + param.numel() > self.bucket_size:
78                     cur_bucket_idx += 1
79                     self.params_to_bucket_location[param] = (0, param.numel(), cur_bucket_idx)
80                     cur_bucket_size = param.numel()
81                 else:
82                     self.params_to_bucket_location[param] = (cur_bucket_size, cur_bucket_size + param.numel(), cur_bucket_idx)
83
84             self.params_to_bucket_location = {param: loc for param, loc in self.params_to_bucket_location.items() if loc[0] != 0}
```

# Batch size summary

$$\text{global batch size} = mbs \cdot grad\_acc \cdot dp$$

- mbs: micro batch size
- grad\_acc: gradient accumulation steps
- dp: number of parallel instances

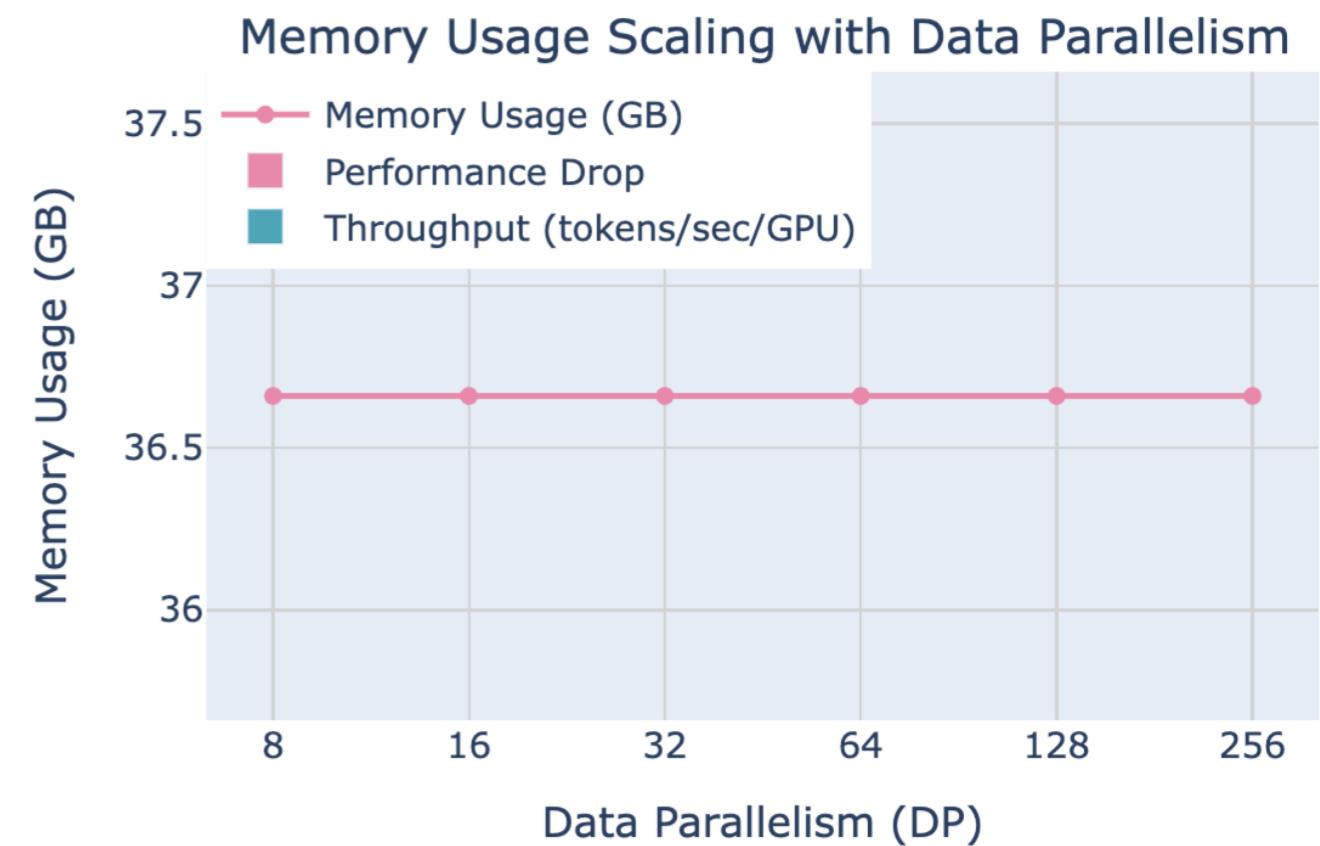
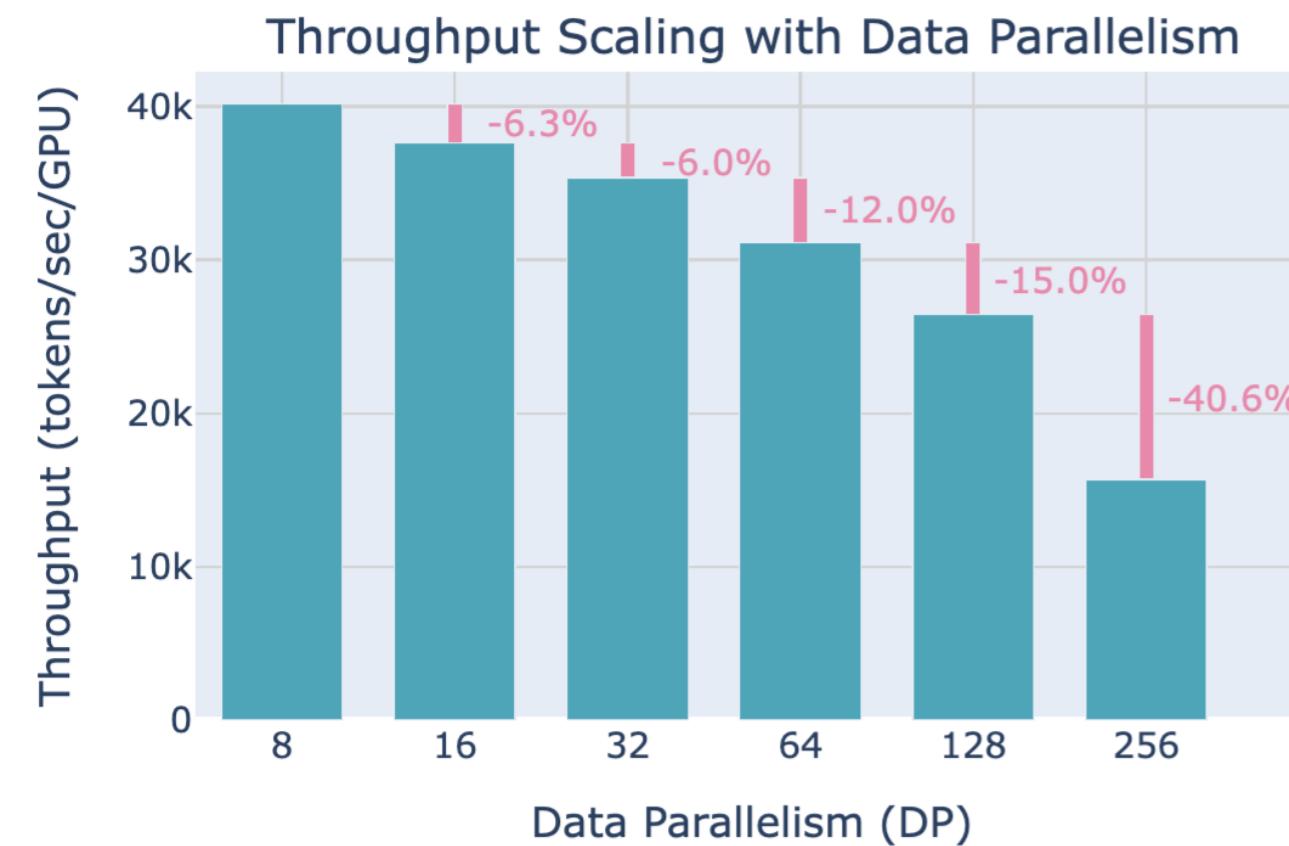
# Putting it all together

- Global batch size: 4 million tokens
- Sequence length: 4,000 tokens
  - $\Rightarrow$  batch size: 1024 sequences
- mbs: Suppose 1 GPU fits 2 sequences
- dp: 128 GPUs:  $2 * 128 = 256$
- grad\_acc of 4:  $256 * 4 = 1024$

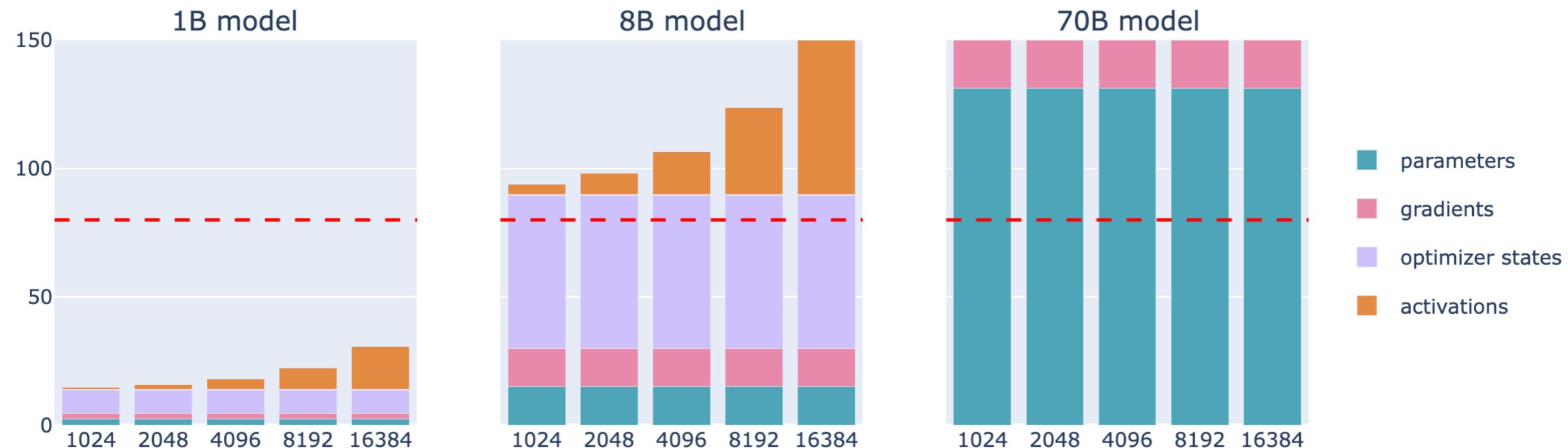
Quiz: what if we had 512 GPUs?

# Data Parallelism scaling

- More GPUs means more coordination (e.g., all-reduce, network communication, stragglers)



# What if the model is too large?



- Split tensors:
  - Parallelism (e.g., tensor, pipeline)
  - Sharding (DeepSpeed ZeRO or PyTorch FSDP)

# Parallelism

- Techniques for leveraging computation and memory from multiple GPUs
  - Data parallelism
  - **Tensor parallelism**
  - Pipeline parallelism
  - Memory optimization
  - Choosing parallelism strategies

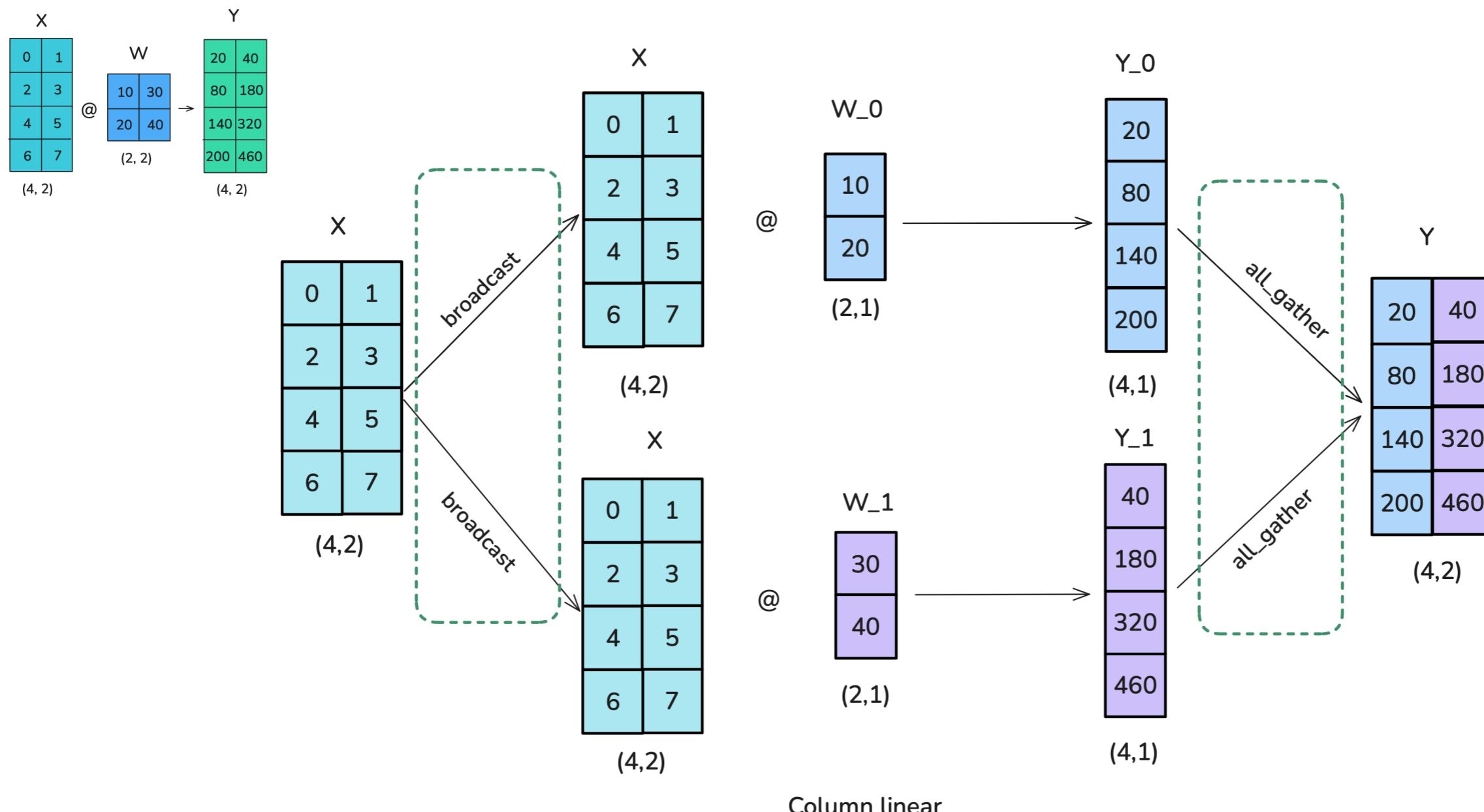
# Tensor Parallelism

- Basic idea: take advantage of the structure of matrix multiplication to distribute computation across multiple GPUs.

$$\begin{array}{c} \mathbf{X} \\ \begin{array}{|c|c|} \hline 0 & 1 \\ \hline 2 & 3 \\ \hline 4 & 5 \\ \hline 6 & 7 \\ \hline \end{array} \\ (4, 2) \end{array} @ \begin{array}{c} \mathbf{W} \\ \begin{array}{|c|c|} \hline 10 & 30 \\ \hline 20 & 40 \\ \hline \end{array} \\ (2, 2) \end{array} \rightarrow \begin{array}{c} \mathbf{Y} \\ \begin{array}{|c|c|} \hline 20 & 40 \\ \hline 80 & 180 \\ \hline 140 & 320 \\ \hline 200 & 460 \\ \hline \end{array} \\ (4, 2) \end{array}$$

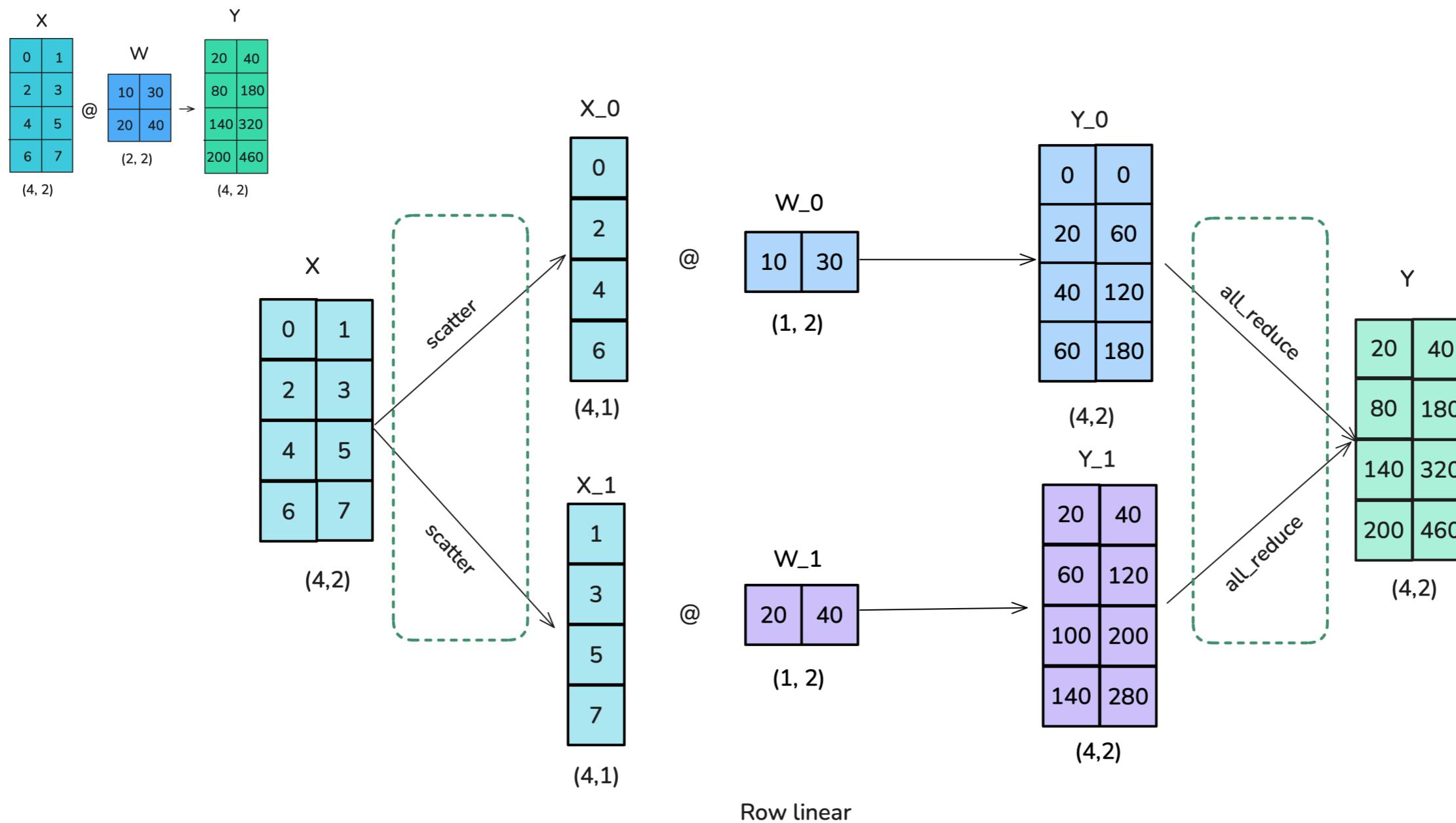
# Column-wise

- Split weight matrix into columns, each GPU handles a column chunk



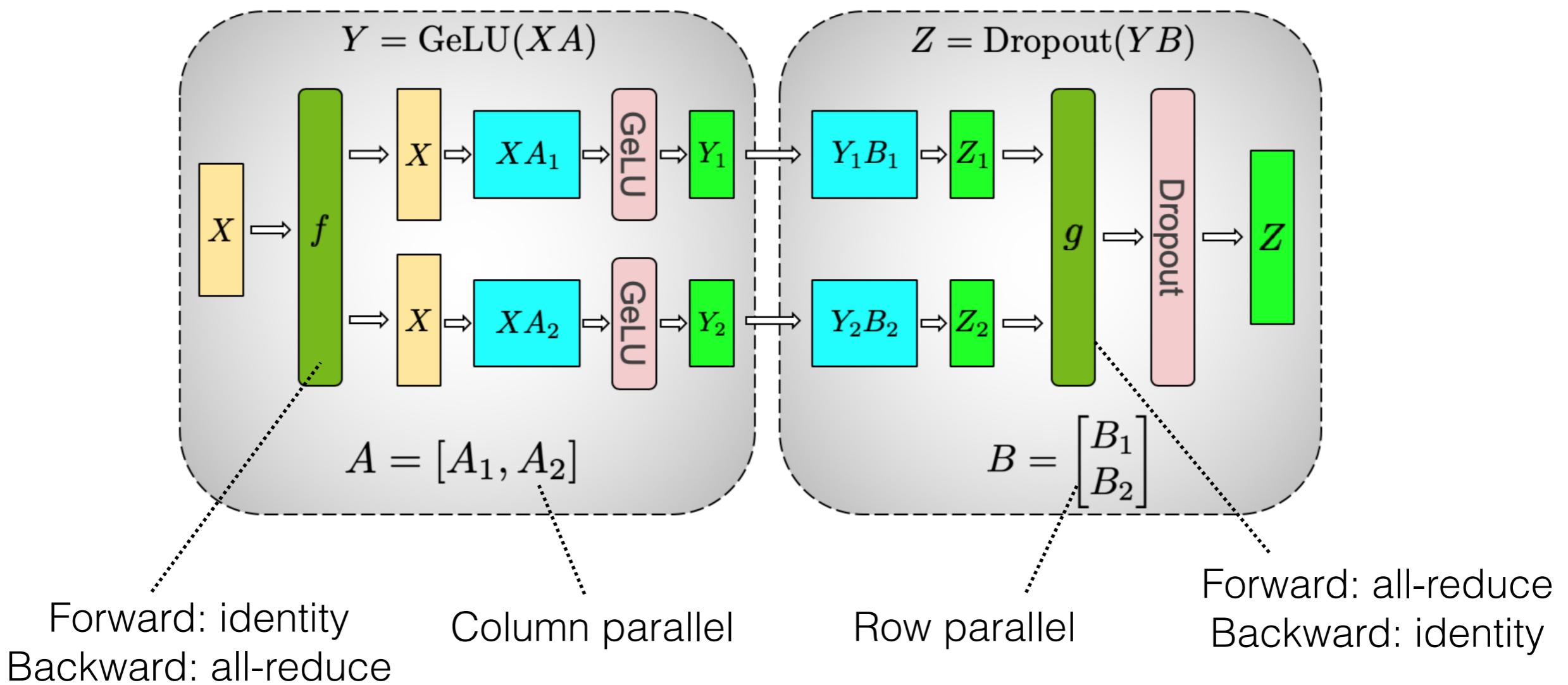
# Row-wise

- Split weight matrix into rows (and split inputs into columns), then sum



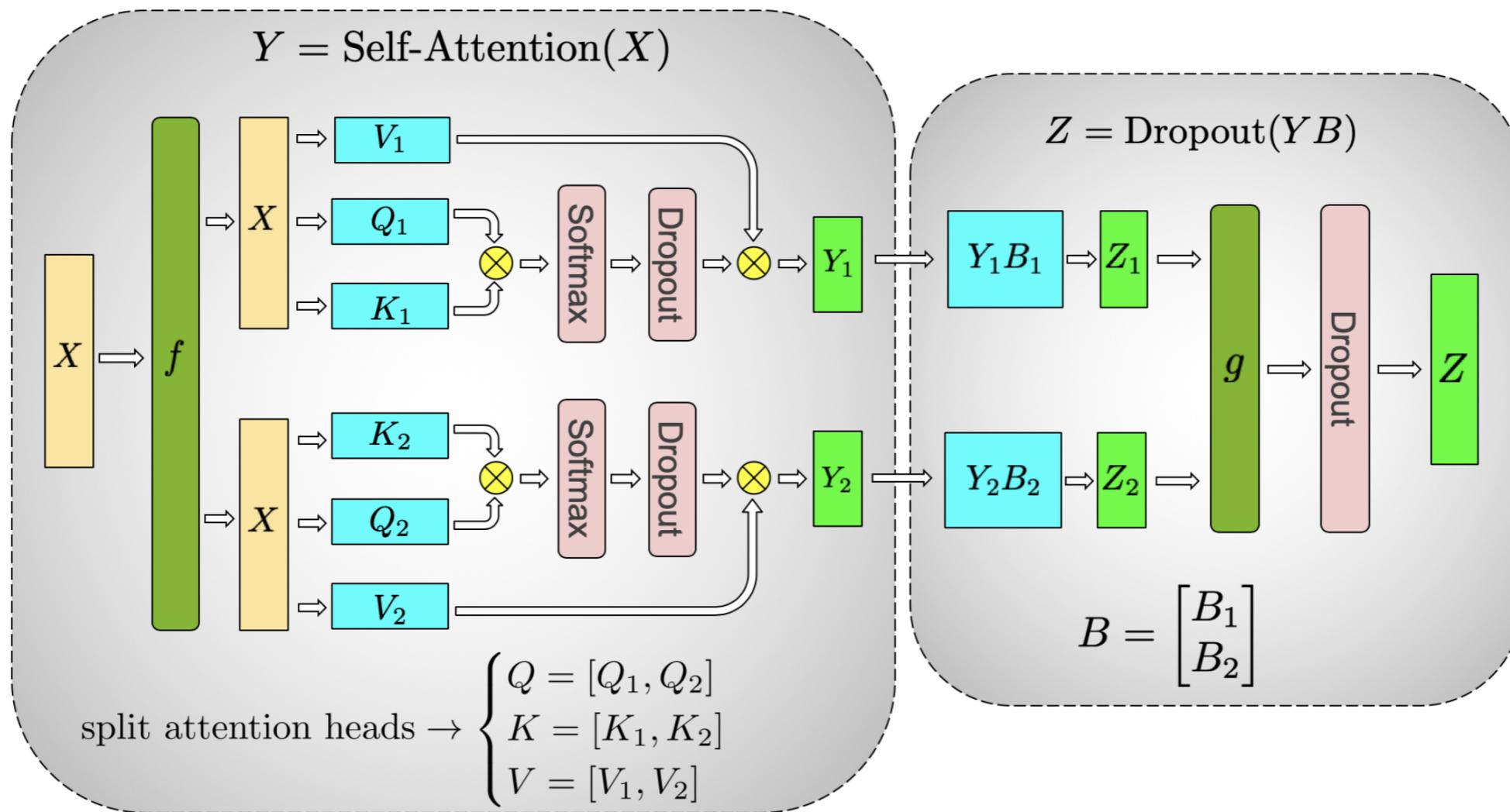
# Example: feedforward

- Use column parallel, then row parallel  
(benefit: no intermediate all-reduce/gather)



# Example: attention

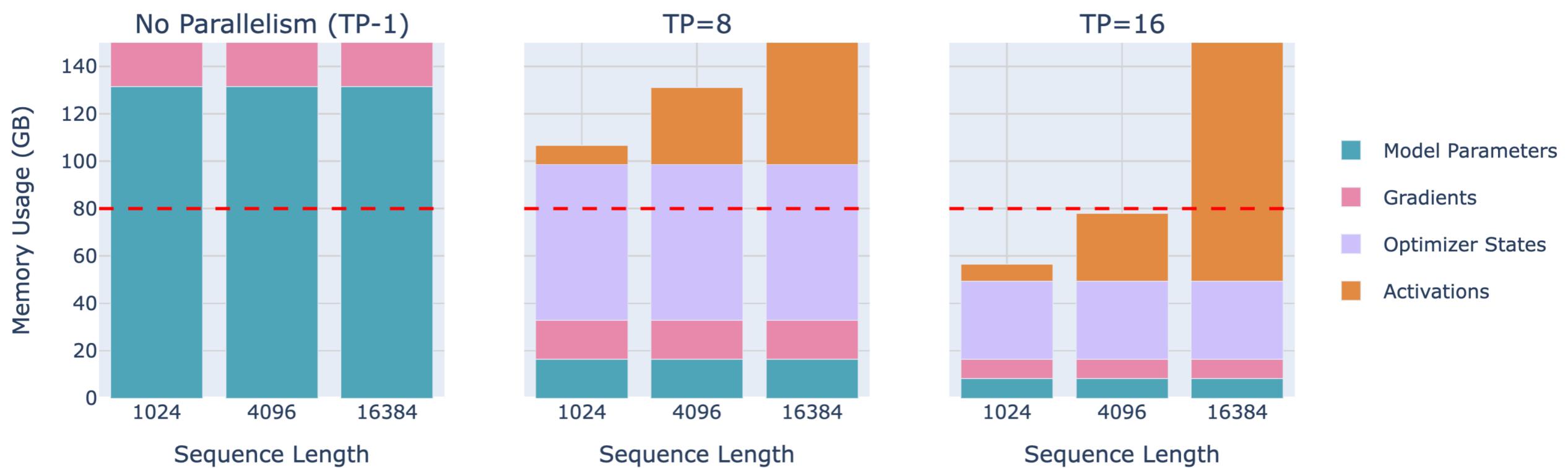
- Each GPU handles a subset of attention heads



# Tensor Parallelism

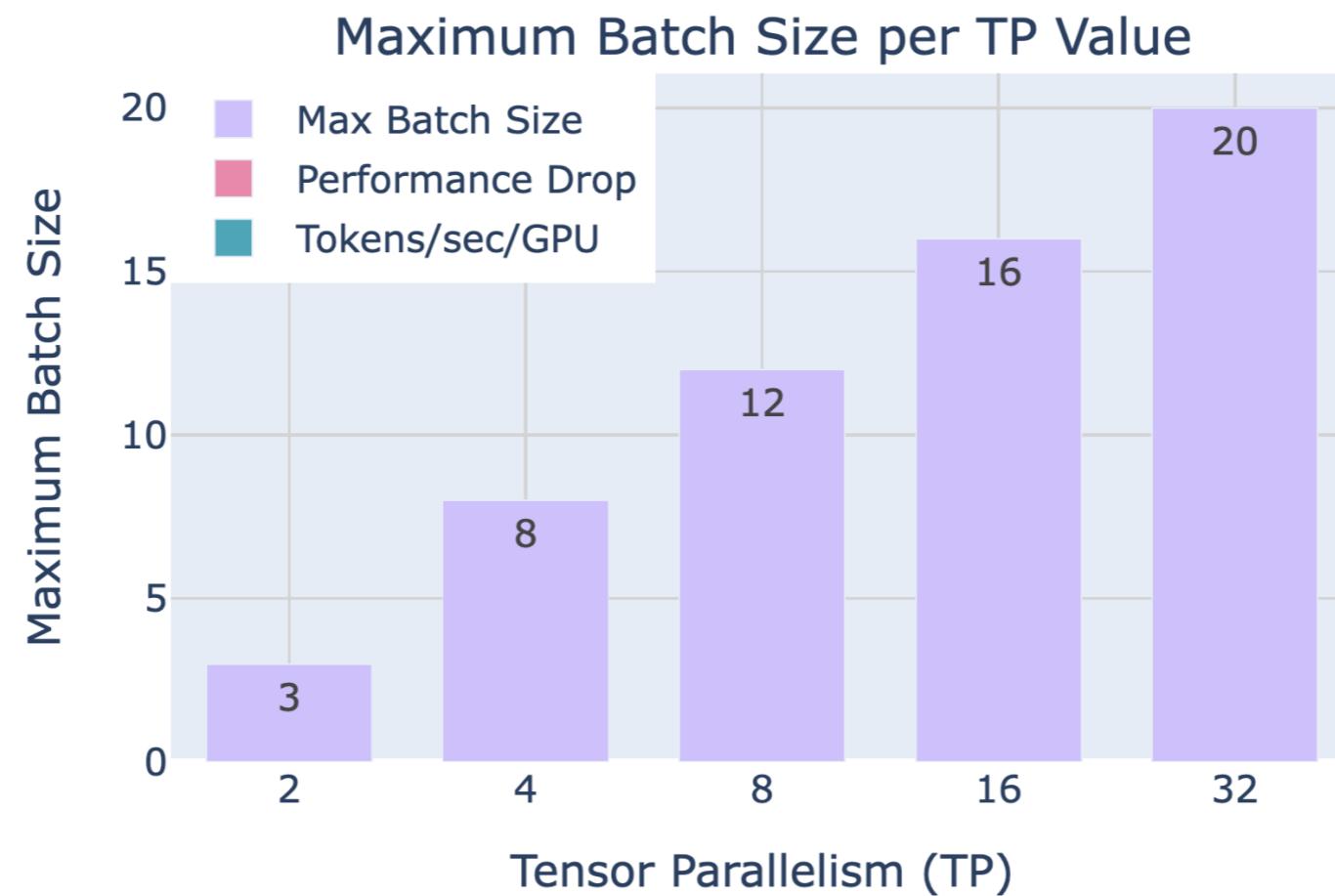
- Benefit: reduce memory requirements

Memory Usage for 70B Model



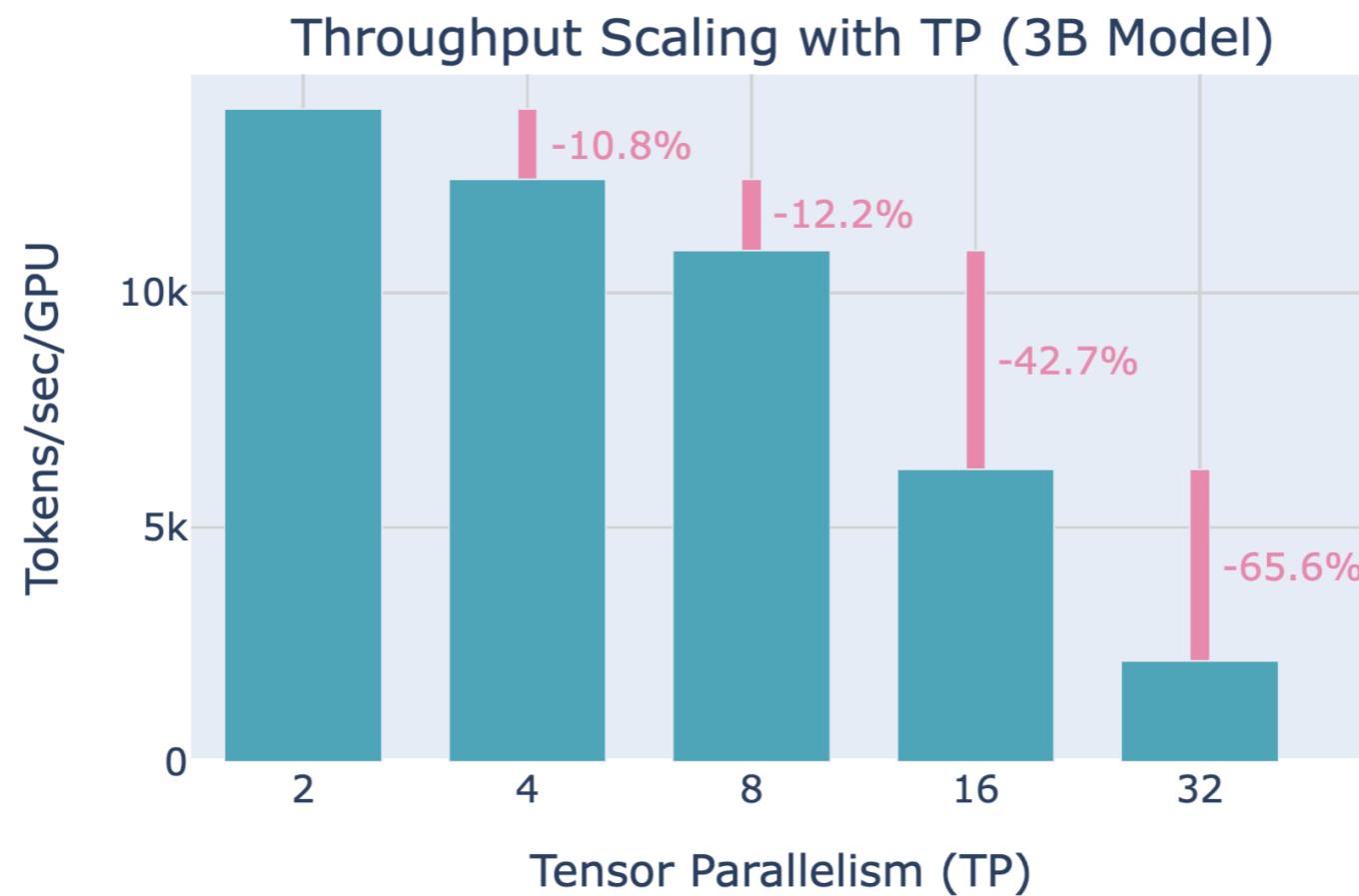
# Tensor Parallelism

- Benefit: reduce memory requirements



# Tensor Parallelism

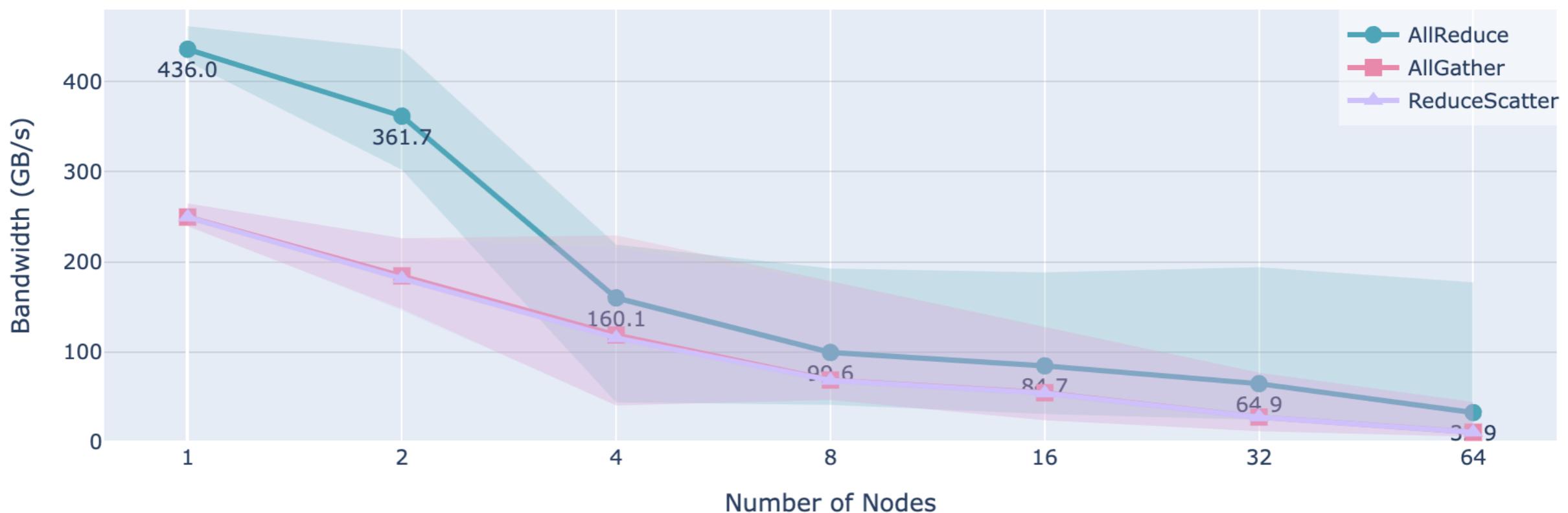
- Tradeoff: communication costs (e.g., all-reduce)



# Tensor Parallelism

- Tradeoff: communication costs (e.g., all-reduce)
  - Cross-node connections particularly slow

Communication Bandwidth by Number of Nodes (size=256MB)



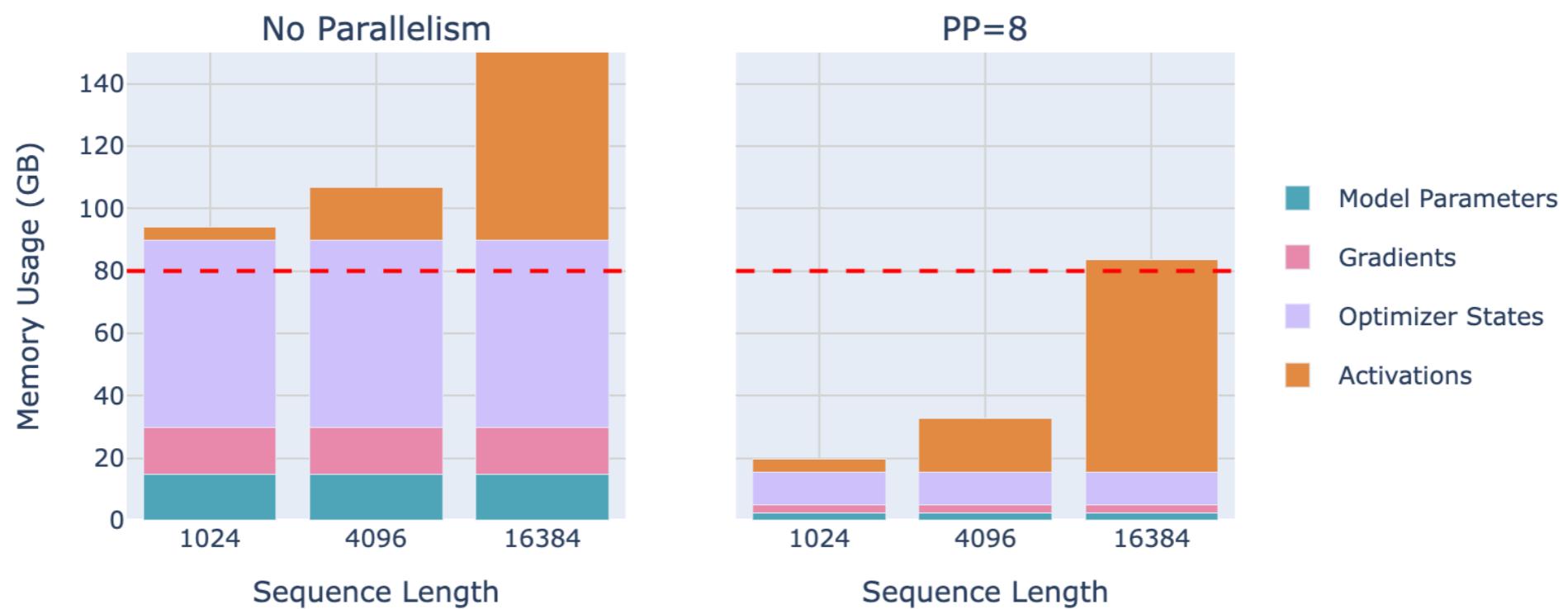
# Parallelism

- Techniques for leveraging computation and memory from multiple GPUs
  - Data parallelism
  - Tensor parallelism
  - **Pipeline parallelism**
  - Memory optimization
  - Choosing parallelism strategies

# Pipeline Parallelism

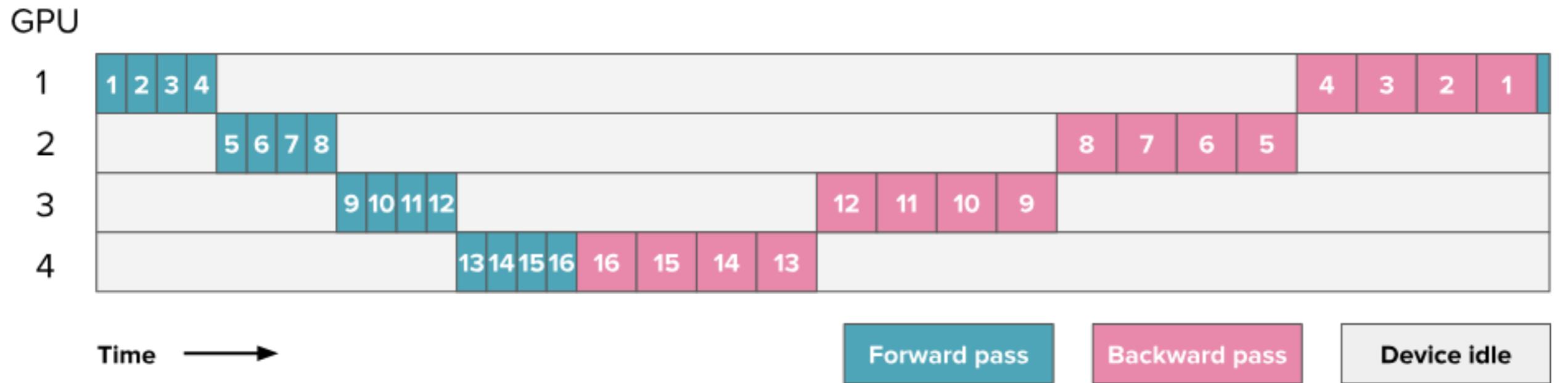
- Basic idea: split *layers* across multiple GPUs
  - E.g., layers 1-4 on GPU 1, layers 5-8 on GPU 2

Memory Usage for 8B Model



# Pipeline Parallelism

- Basic idea: split layers across multiple GPUs

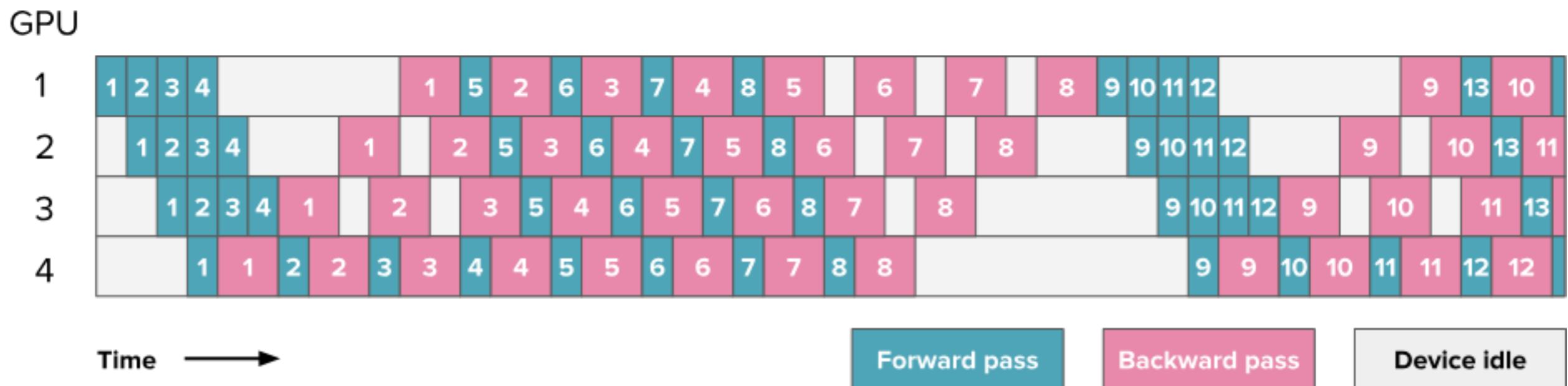


An example of Pipeline parallelism for a model with 16 layers distributed across 4 GPUs. The numbers correspond to the layer IDs.

Key challenge: reducing time lost due to the “bubble” (grey)

# One-forward one-backward

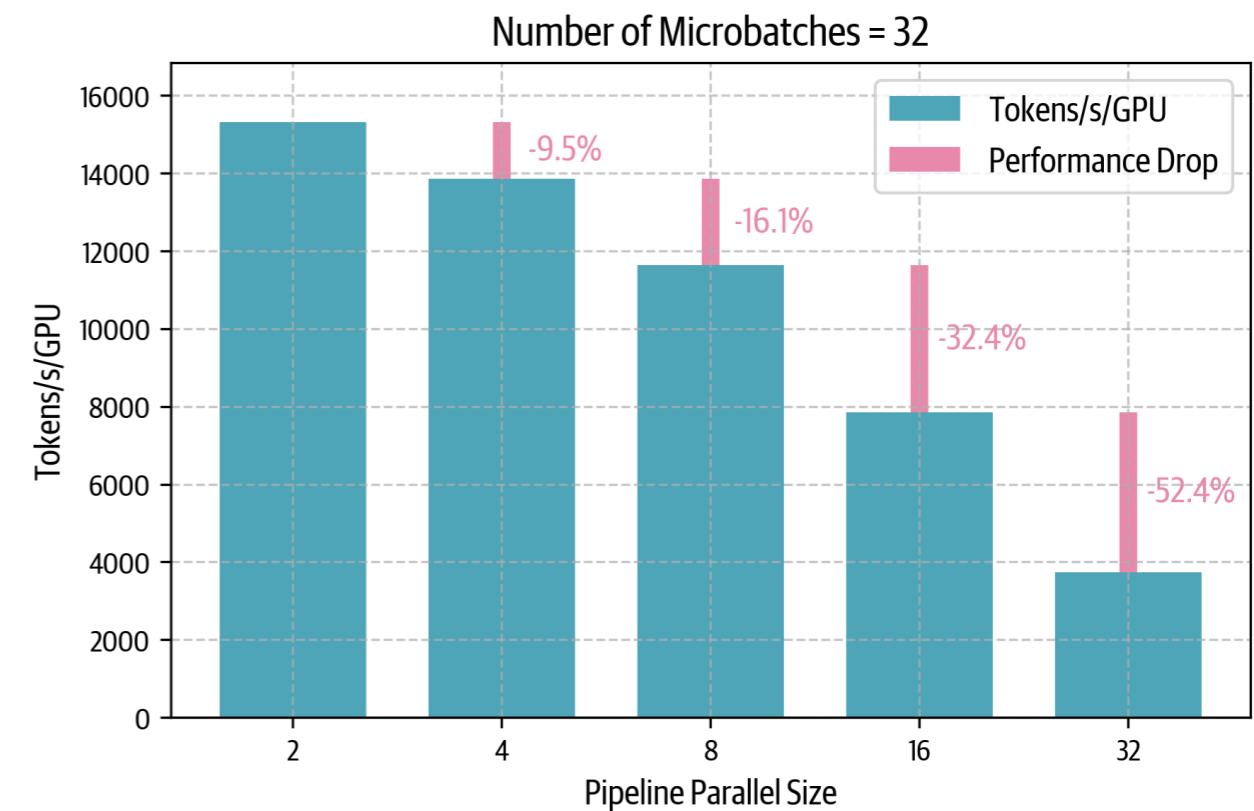
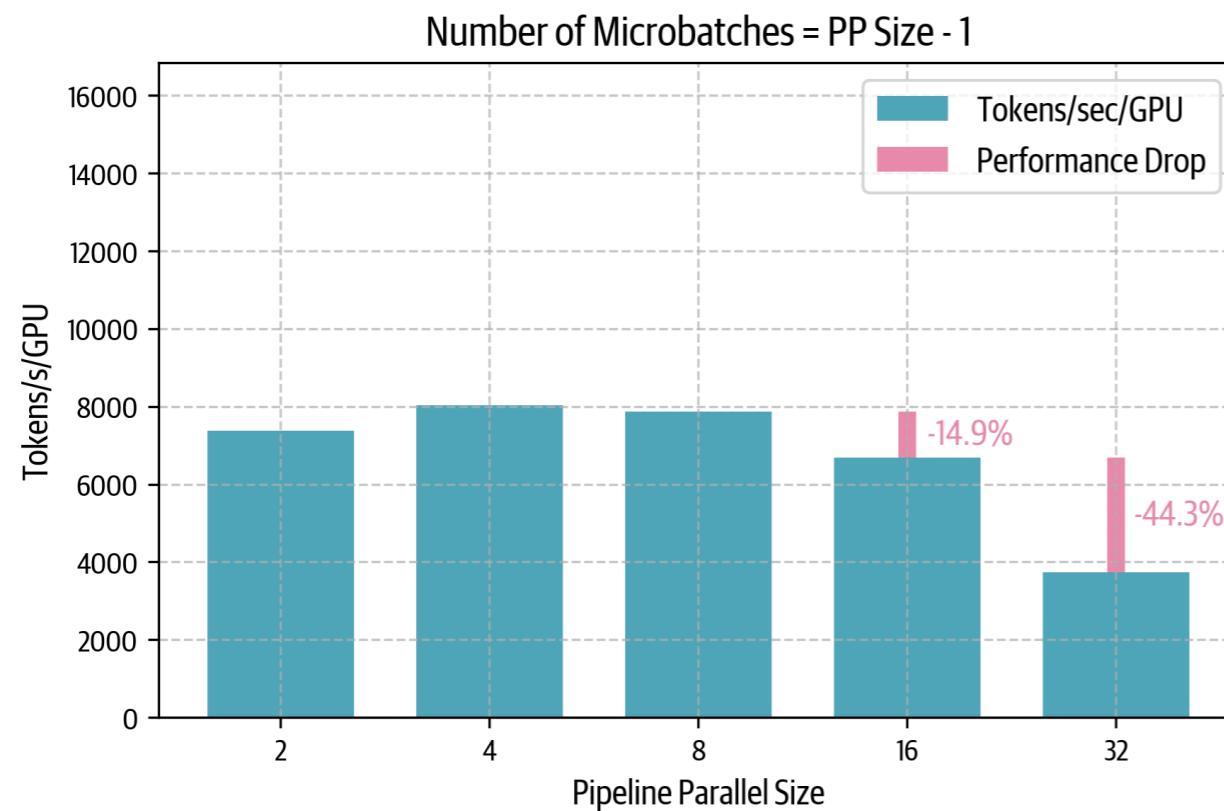
- Start performing backward pass as soon as possible



Numbers: microbatch

# One-forward one-backward

Throughput Scaling with Pipeline Parallelism (1F1B schedule)



Small # of microbatches:  
inefficient due to bubble

Better scaling with  
a larger # of microbatches

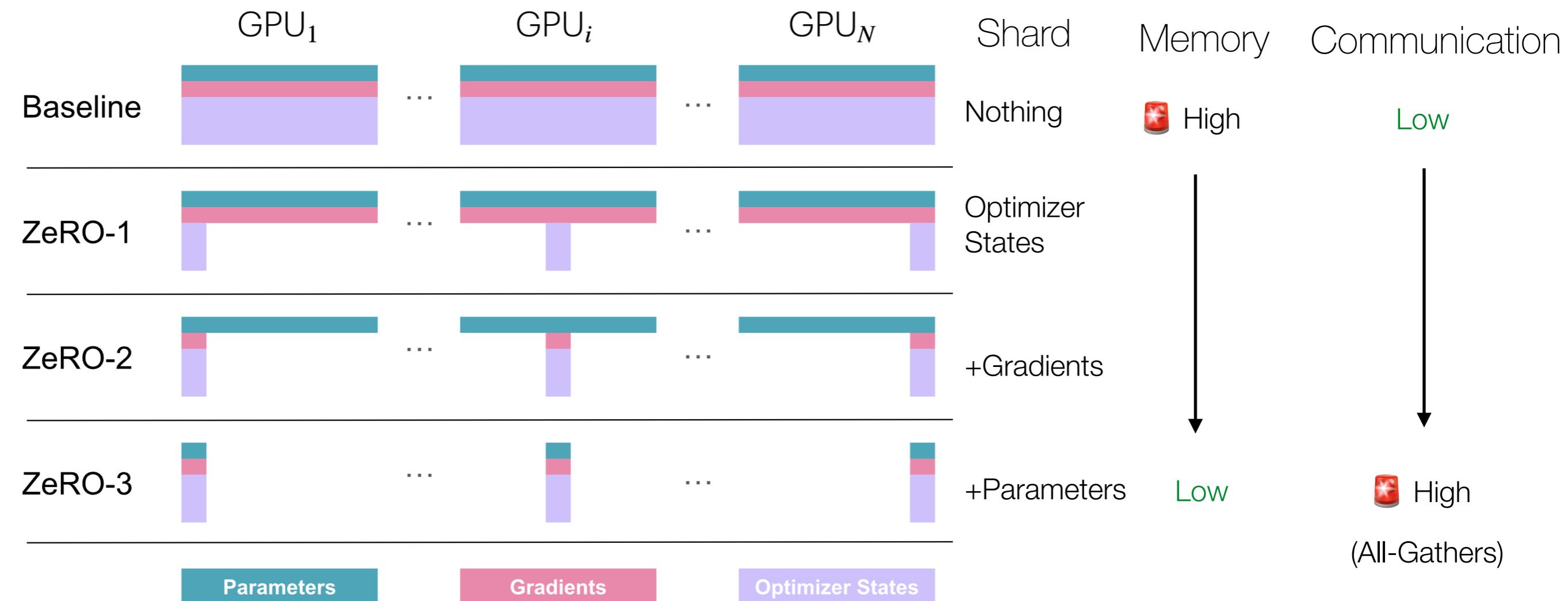
# Scaling training

- Parallelism
  - Data parallelism
  - Tensor parallelism
  - Pipeline parallelism
- **Memory optimization**
- Choosing strategies

# Memory optimization: ZeRO

- In standard Data Parallelism, each GPU replicates:
  - Model parameters
  - Gradients
  - Optimizer states
- Zero Redundancy Optimizer (ZeRO) partitions these across GPUs

# Memory optimization: ZeRO



# Memory optimization: ZeRO

- Key idea: load parameters just-in-time. Example:
  - Model: 1B parameters
  - 4 GPUs, each storing 250M parameters
  - At each layer  $\ell$ :
    - GPU uses all-gather to fetch parameters for layer  $\ell$ , computes activations
    - Free fetched parameter memory and continue to next layer
- Different than TP / PP! Only memory sharding, not sharding the computation

# Recap of strategies

	Key Idea	Tradeoffs	Use Case
<b>Data Parallelism (DP)</b>	Parallelize on batch dimension	Redundancy. Need to fit model on GPU.	Standard models that fit in GPU memory
<b>Tensor Parallelism (TP)</b>	Parallelize on hidden dimension	Fine-grained => high communication costs.	Large layers (e.g. MLP). Parallelize within a node.
<b>Pipeline Parallelism (PP)</b>	Parallelize on model dimension	Pipeline bubbles	Large deep models. Parallelize across nodes.
<b>ZeRO</b>	Sharding model, optimizer, gradients in DP	High communication costs (all-gather)	Big models that don't fit in GPU memory

Often combined for efficient training (next)!

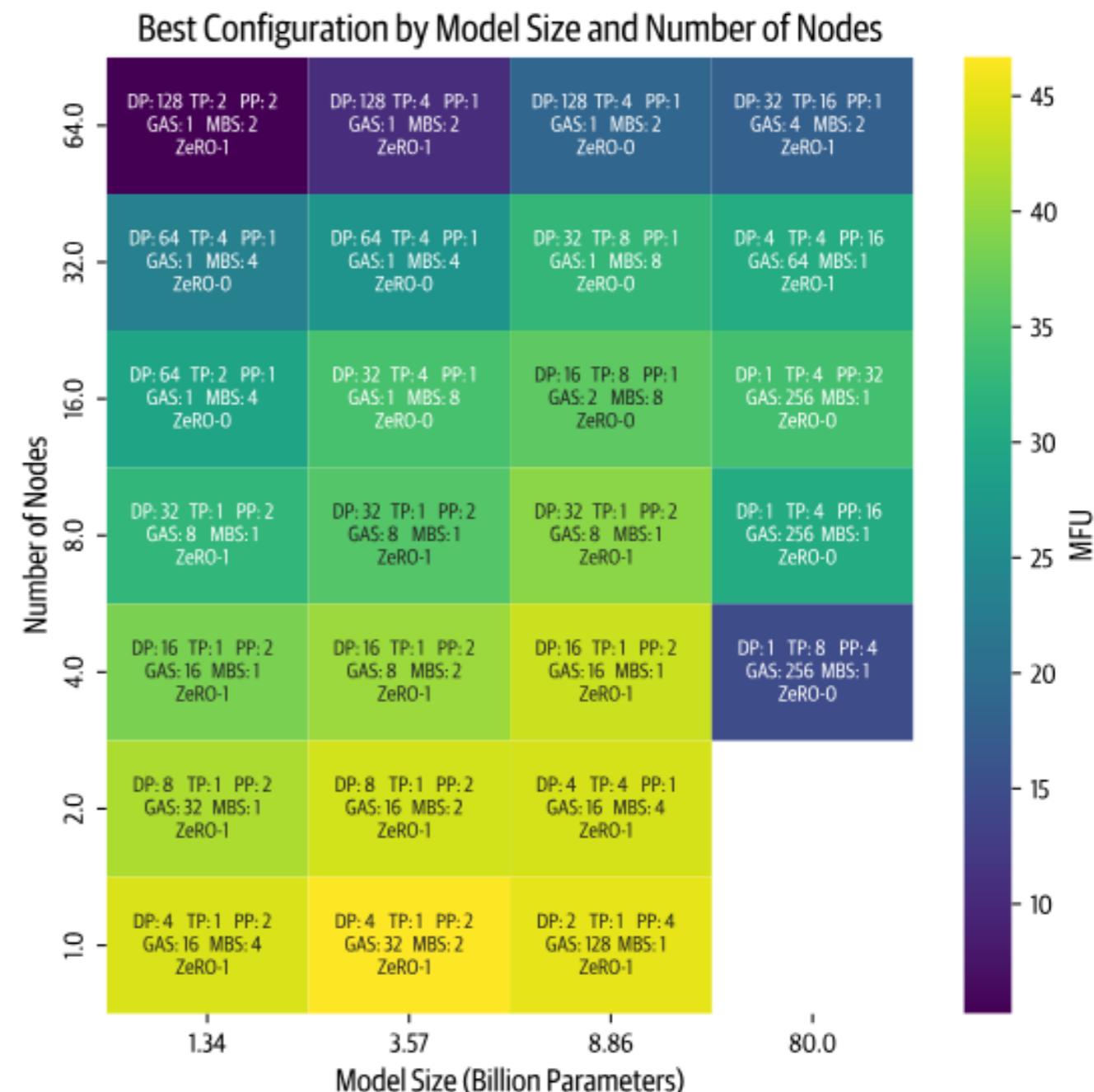
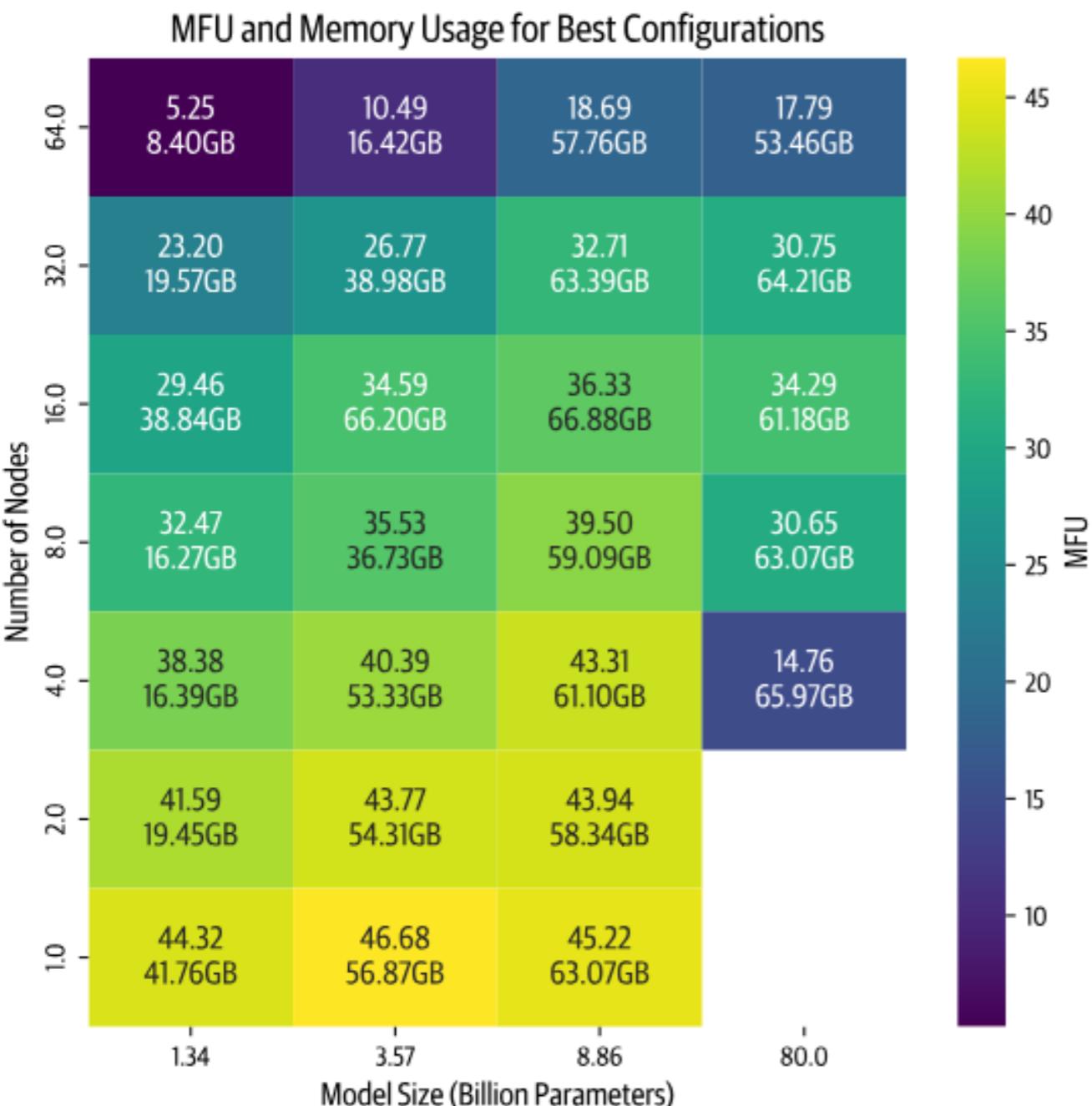
# Scaling training

- Parallelism
  - Data parallelism
  - Tensor parallelism
  - Pipeline parallelism
- Memory optimization
- **Choosing strategies**

# Choosing strategies

- Fit model into memory
- Satisfy target global batch size
- Optimize training throughput

# Best configuration experiment



GBS 1M tokens, sequence length 4096, 1-64 8xH100 nodes

# Scaling training

- Parallelism
  - Data parallelism
  - Tensor parallelism
  - Pipeline parallelism
- Memory optimization
- Choosing strategies