CSCI 5451: Introduction to Parallel Computing

Lecture 13: MPI Examples



Announcements (10/15)

- HW1 → Due later today (<u>Canvas</u>)
- ☐ HW 2 released on Monday, Oct 20
- ☐ Group Formation due Sunday, Oct 19 (Canvas)

- Leftover MPI Functions from (10/13)
 - MPI_Alltoallv
 - MPI_Comm_split & MPI_Cart_sub
- MPI Examples (Whiteboard walkthrough)
 - Row-Wise Matrix-Vector Multiplication
 - Column-Wise Matrix-Vector Multiplication
 - 2-D Matrix-Vector Multiplication
 - o Djikstra's Single Source Shortest Path
 - Sample Sort



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MPI_Alltoallv

Each process sends variable-sized data to all others and receives variable-sized data from all others.

- sendbuf: Starting address of send buffer.
- sendcounts: Array specifying number of elements sent to each rank.
- sdispls: Array of offsets in sendbuf.
- sendtype: Type of send data.
- recvbuf: Starting address of receive buffer.
- recvcounts: Array specifying number of elements received from each rank.
- rdispls: Array of offsets in recvbuf.
- recvtype: Type of receive data.
- comm: Communicator handle.



MPI_Alltoallv

Each process sends variable-sized data to all others and receives variable-sized data from all others.

```
int sendbuf[10];
for (int i=0; i<10; i++) sendbuf[i] = rank*10 + i;
int sendcounts[4] = \{1,2,3,4\};
int sdispls[4] = \{0,1,3,6\};
int recvcounts[4] = {rank+1, rank+1, rank+1};
int rdispls[4] = \{0, (rank+1), (rank+1)^2, (rank+1)^3\};
int recvbuf[16];
MPI Alltoally(sendbuf, sendcounts, sdispls, MPI INT, recybuf,
              recvcounts, rdispls, MPI INT, MPI COMM WORLD);
printf("Rank %d received:", rank);
for (int i=0; i<(rank+1)*4; i++)
  printf(" %d", recvbuf[i]);
printf("\n");
```



MPI_Alltoallv

Each process sends variable-sized data to all others and receives variable-sized data from all others.

```
int sendbuf[10];
for (int i=0; i<10; i++) sendbuf[i] = rank*10 + i;
int sendcounts[4] = \{1,2,3,4\};
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int recvcounts[4] = {rank+1, rank+1, rank+1};
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int recvbuf[16];
MPI Alltoally(sendbuf, sendcounts, sdispls, MPI INT, recybuf,
              recvcounts, rdispls, MPI INT, MPI COMM WORLD);
printf("Rank %d received:", rank);
for (int i=0; i<(rank+1)*4; i++)
  printf(" %d", recvbuf[i]);
printf("\n");
```

Rank 0 received: 0 10 20 30

Rank 1 received: 1 2 11 12 21 22 31 32

Rank 2 received: 3 4 5 13 14 15 23 24 25 33 34 35

Rank 3 received: 6 7 8 9 16 17 18 19 26 27 28 29 36 37 38 39



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```
int MPI_Comm_split(MPI_Comm comm,
    int color, int key,
    MPI_Comm *newcomm);
```

Creates new communicator by splitting an existing communicator into subgroups based on color.

Processes with the same color are grouped together; within each group, ranks are ordered by key



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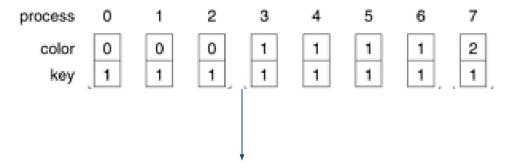
- comm: Existing communicator to be split (e.g., MPI_COMM_WORLD).
- color: Integer identifier for subgroup membership.
 - All processes with the same color form a new communicator.
 - A process can set color =
 MPI_UNDEFINED to be excluded entirely.
- key: Determines ordering of ranks within the new communicator.
 - Lower keys get lower ranks.
 - Equal keys are ordered according to ordering in previous communicator
- newcomm: Output handle to the newly created communicator.



```
int MPI_Comm_split(MPI_Comm comm,
    int color, int key,
    MPI_Comm *newcomm);
```



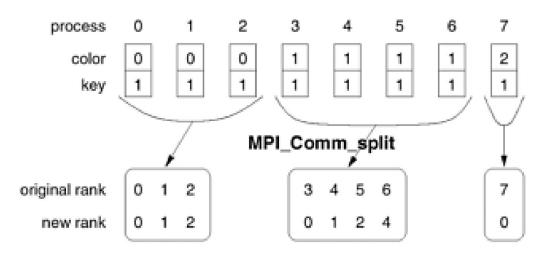
```
int MPI_Comm_split(MPI_Comm comm,
    int color, int key,
    MPI_Comm *newcomm);
```



Which processes will be grouped together?



```
int MPI_Comm_split(MPI_Comm comm,
    int color, int key,
    MPI_Comm *newcomm);
```





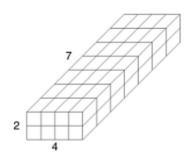
Creates a lower-dimensional subcommunicator from an existing Cartesian topology communicator by selecting which dimensions to keep.



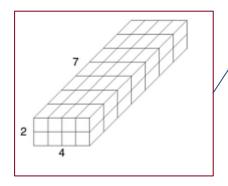
Creates a lower-dimensional subcommunicator from an existing Cartesian topology communicator by selecting which dimensions to keep.

- comm: Input communicator with Cartesian topology (created via MPI_Cart_create).
- remain_dims: Logical array of length equal to the number of dimensions.
 - remain_dims[i] = 1 → keep this dimension.
 - remain_dims[i] = 0 → collapse (drop) this dimension.
- newcomm: Output communicator corresponding to the subgrid of the original topology.



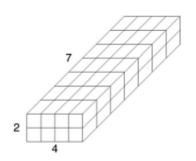


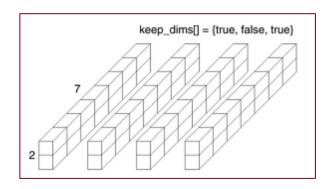




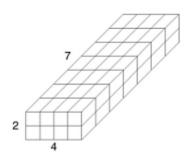
```
int dims[3] = \{2, 4, 7\}; // grid dimensions
int periods[3] = \{0, 0, 0\};
                        // non-periodic in all dimensions
int reorder = 0:
                        // keep original ranks
MPI Comm cart comm;
MPI Cart create(MPI COMM WORLD, 3, dims, periods,
     reorder, &cart comm);
int keep dims[3] = \{1, 0, 1\};
MPI Comm sub comm;
MPI Cart_sub(cart_comm, keep_dims, &sub_comm);
```



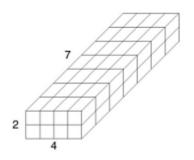


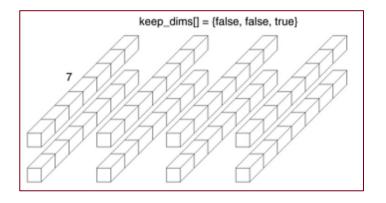














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Row-Wise Matrix-Vector Multiplication

```
void RowMatrixVectorMultiply(int n, double *a, double *b, double *x, MPI Comm comm)
  int i, j;
  int nlocal; /* Number of locally stored rows of A */
  double *fb; /* Buffer that stores the entire vector b */
  int npes, myrank;
  MPI Status status;
  /* Get information about the communicator */
  MPI Comm size(comm, &npes);
  MPI Comm rank(comm, &myrank);
  /* Allocate memory to store the entire vector b */
  fb = (double *)malloc(n * sizeof(double));
  nlocal = n / npes;
```



Row-Wise Matrix-Vector Multiplication

```
/* Gather the entire vector b on each processor using MPI's ALLGATHER operation */
    MPI_Allgather(b, nlocal, MPI_DOUBLE, fb, nlocal, MPI_DOUBLE, comm);

/* Perform the matrix-vector multiplication involving the locally stored submatrix */
    for (i = 0; i < nlocal; i++) {
        x[i] = 0.0;
        for (j = 0; j < n; j++)
            x[i] += a[i * n + j] * fb[j];
    }

    free(fb);
}</pre>
```



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Column-Wise Matrix-Vector Multiplication

```
void ColMatrixVectorMultiply(int n, double *a, double *b, double *x, MPI Comm comm)
  int i, j;
  int nlocal;
  double *px;
  double *fx;
  int npes, myrank;
  MPI Status status;
  /* Get identity and size information from the communicator */
  MPI Comm size(comm, &npes);
  MPI Comm rank(comm, &myrank);
  nlocal = n / npes;
```



Column-Wise Matrix-Vector Multiplication

```
/* Allocate memory for arrays storing intermediate results. */
  px = (double *)malloc(n * sizeof(double));
  fx = (double *)malloc(n * sizeof(double));
  /* Compute the partial dot products that correspond to the local columns of A. */
  for (i = 0; i < n; i++) {
     px[i] = 0.0;
     for (j = 0; j < nlocal; j++)
       px[i] += a[i * nlocal + i] * b[i];
  /* Sum up the results by performing an element-wise reduction operation */
  MPI Reduce(px, fx, n, MPI DOUBLE, MPI SUM, 0, comm);
  /* Redistribute fx in a fashion similar to that of vector b */
  MPI Scatter(fx, nlocal, MPI DOUBLE, x, nlocal, MPI DOUBLE, 0, comm);
  free(px);
  free(fx);
```



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2-D Matrix-Vector Multiplication

```
void MatrixVectorMultiply_2D(int n, double *a, double *b, double *x, MPI_Comm comm)
  int ROW = 0, COL = 1;
  int i, j, nlocal;
  double *px;
  int npes, dims[2], periods[2], keep_dims[2];
  int myrank, my2drank, mycoords[2];
  int other rank, coords[2];
  MPI Status status;
  MPI Comm comm 2d, comm row, comm col;
  MPI Comm size(comm, &npes);
  MPI Comm rank(comm, &myrank);
  dims[ROW] = dims[COL] = sqrt(npes);
  nlocal = n / dims[ROW];
  px = malloc(nlocal * sizeof(double));
```



```
periods[ROW] = periods[COL] = 1;
MPI Cart create(MPI COMM WORLD, 2, dims, periods, 1, &comm 2d);
MPI Comm rank(comm 2d, &my2drank);
MPI Cart coords(comm_2d, my2drank, 2, mycoords);
keep dims[ROW] = 0; keep dims[COL] = 1;
MPI Cart sub(comm 2d, keep dims, &comm row);
keep dims[ROW] = 1; keep dims[COL] = 0;
MPI Cart sub(comm 2d, keep dims, &comm col);
if (mycoords[COL] == 0 && mycoords[ROW] != 0) {
  coords[ROW] = mycoords[ROW];
  coords[COL] = mycoords[ROW];
  MPI Cart rank(comm 2d, coords, &other rank);
  MPI Send(b, nlocal, MPI DOUBLE, other rank, 1, comm 2d);
if (mycoords[ROW] == mycoords[COL] && mycoords[ROW] != 0) {
  coords[ROW] = mycoords[ROW];
  coords[COL] = 0;
  MPI Cart rank(comm 2d, coords, &other rank);
  MPI Recv(b, nlocal, MPI DOUBLE, other rank, 1, comm 2d, &status);
```



2-D Matrix-Vector Multiplication

```
coords[0] = mycoords[COL];
MPI Cart rank(comm col, coords, &other rank);
MPI Bcast(b, nlocal, MPI DOUBLE, other rank, comm col);
for (i = 0; i < nlocal; i++) {
  px[i] = 0.0;
  for (j = 0; j < nlocal; j++)
    px[i] += a[i * nlocal + i] * b[i];
coords[0] = 0;
MPI Cart rank(comm row, coords, &other rank);
MPI Reduce(px, x, nlocal, MPI DOUBLE, MPI SUM, other rank, comm row);
MPI Comm free(&comm 2d);
MPI Comm free(&comm row);
MPI Comm free(&comm col);
free(px);
```

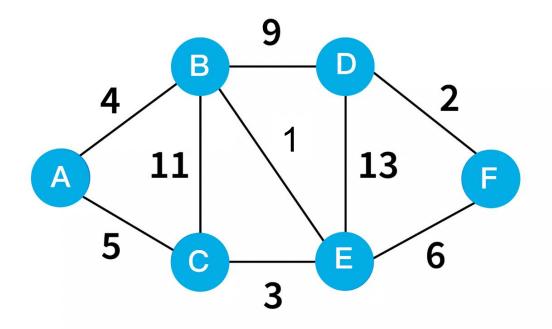


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Djikstra's Single-Source Shortest Path (Review)

- ☐ Find the shortest path from a single node in a graph to all other nodes in a graph
- Serial ExampleWalkthrough



Djikstra's Single-Source Shortest Path

```
void SingleSource(int n, int source, int *wgt, int *lengths, MPI Comm comm)
  int i, j;
  int nlocal; /* The number of vertices stored locally */
  int *marker; /* Used to mark the vertices belonging to Vo */
  int firstvtx; /* The index number of the first vertex that is stored locally */
  int lastvtx; /* The index number of the last vertex that is stored locally */
  int u, udist;
  int lminpair[2], gminpair[2];
  int npes, myrank;
  MPI Status status;
  MPI Comm size(comm, &npes);
  MPI Comm rank(comm, &myrank);
  nlocal = n / npes;
  firstvtx = myrank * nlocal;
  lastvtx = firstvtx + nlocal - 1;
```



Djikstra's Single-Source Shortest Path

```
/* Set the initial distances from source to all the other vertices */
for (j = 0; j < nlocal; j++)
    lengths[j] = wgt[source * nlocal + j];

/* This array is used to indicate if the shortest path to a vertex has been found */
marker = (int *)malloc(nlocal * sizeof(int));
for (j = 0; j < nlocal; j++)
    marker[j] = 1;

/* The process that stores the source vertex marks it as seen */
if (source >= firstvtx && source <= lastvtx)
    marker[source - firstvtx] = 0;</pre>
```

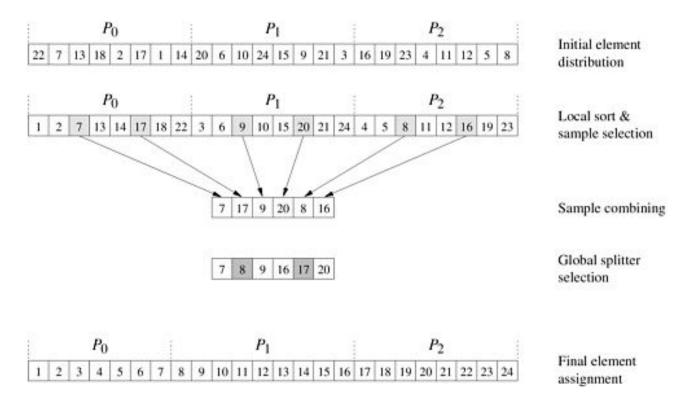


```
/* The main loop of Dijkstra's algorithm */
for (i = 1; i < n; i++) {
  /* Step 1: Find the local vertex at the smallest distance from source */
  Iminpair[0] = MAXINT; /* architecture dependent large number */
  Iminpair[1] = -1;
  for (j = 0; j < nlocal; j++) {
     if (marker[i] && lengths[i] < lminpair[0]) {</pre>
       lminpair[0] = lengths[j];
        lminpair[1] = firstvtx + j;
  /* Step 2: Compute the global minimum vertex and insert it into Vc */
  MPI Allreduce(Iminpair, gminpair, 1, MPI 2INT, MPI MINLOC, comm);
  udist = gminpair[0];
  u = gminpair[1];
  /* The process that stores the minimum vertex marks it as seen */
  if (u == Iminpair[1])
     marker[u - firstvtx] = 0;
  /* Step 3: Update the distances given that u got inserted */
  for (j = 0; j < nlocal; j++) {
     if (marker[j] && udist + wgt[u * nlocal + j] < lengths[j])
        lengths[j] = udist + wgt[u * nlocal + j];
free(marker);
```



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```
int *SampleSort(int n, int *elmnts, int *nsorted, MPI Comm comm)
  int i, j, nlocal, npes, myrank;
  int *sorted elmnts, *splitters, *allpicks;
  int *scounts, *sdispls, *rcounts, *rdispls;
  /* Get communicator-related information */
  MPI Comm size(comm, &npes);
  MPI Comm rank(comm, &myrank);
  nlocal = n / npes;
  /* Allocate memory for the arrays that will store the splitters */
  splitters = (int *)malloc(npes * sizeof(int));
  allpicks = (int *)malloc(npes * (npes - 1) * sizeof(int));
  /* Sort local array */
  gsort(elmnts, nlocal, sizeof(int), IncOrder);
```



```
/* Select local npes-1 equally spaced elements */
for (i = 1; i < npes; i++)
  splitters[i - 1] = elmnts[i * nlocal / npes];
/* Gather the samples in the processors */
MPI Allgather(splitters, npes - 1, MPI INT, allpicks, npes - 1, MPI INT, comm);
/* Sort these samples */
gsort(allpicks, npes * (npes - 1), sizeof(int), IncOrder);
/* Select splitters */
for (i = 1; i < npes; i++)
  splitters[i - 1] = allpicks[i * npes - (int)ceil((double)npes/2)];
splitters[npes - 1] = MAXINT;
/* Compute the number of elements that belong to each bucket */
scounts = (int *)malloc(npes * sizeof(int));
for (i = 0; i < npes; i++)
  scounts[i] = 0;
for (i = i = 0; i < nlocal; i++) {
  if (elmnts[i] < splitters[j])</pre>
     scounts[i]++;
  else
     scounts[++i]++;
```



```
/* Determine starting locations of each bucket's elements */
  sdispls = (int *)malloc(npes * sizeof(int));
  sdisp[s[0] = 0:
  for (i = 1; i < npes; i++)
     sdispls[i] = sdispls[i - 1] + scounts[i - 1];
  /* Inform all processes about receive counts */
  rcounts = (int *)malloc(npes * sizeof(int));
  MPI Alltoall(scounts, 1, MPI INT, rounts, 1, MPI INT, comm);
  /* Compute receive displacements */
  rdispls = (int *)malloc(npes * sizeof(int));
  rdispls[0] = 0;
  for (i = 1; i < npes; i++)
     rdispls[i] = rdispls[i - 1] + rcounts[i - 1];
  *nsorted = rdispls[npes - 1] + rcounts[npes - 1];
  sorted elmnts = (int *)malloc((*nsorted) * sizeof(int));
  /* Exchange elements between processors */
  MPI Alltoally(elmnts, scounts, sdispls, MPI INT,
           sorted elmnts, rcounts, rdispls, MPI INT, comm);
  /* Final local sort */
  gsort(sorted elmnts, *nsorted, sizeof(int), IncOrder);
```



```
free(splitters);
free(allpicks);
free(scounts);
free(sdispls);
free(rcounts);
free(rdispls);

return sorted_elmnts;
}
```

