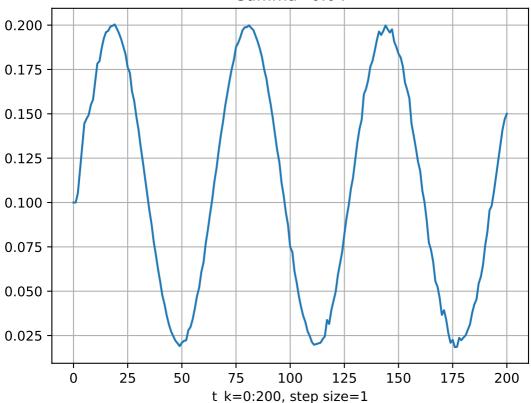
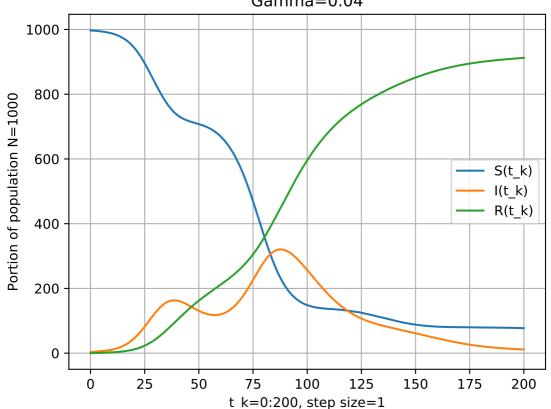
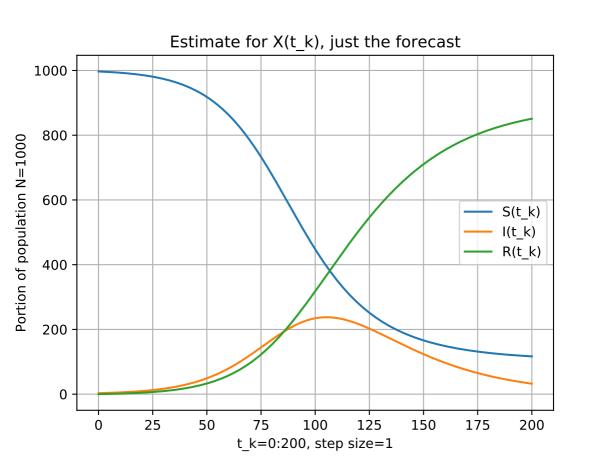
## Estimate for Beta(t\_k) Gamma=0.04



Estimate for  $X(t_k)$  after filter, X=[S,I,R]Gamma=0.04





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```
JimVargas5 Did hw3, will format a single pdf nicely

3c74d71 5 minutes ago

1 contributor
```

```
\Box
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        Blame
                History
 Raw
160 lines (120 sloc) 3.53 KB
      # Jim Vargas
      # MTH 610
  4
      # Remember that vectors are actually 2D at least, nx1 or 1xn matrices
  6
  8
      import numpy as np
  9
      from matplotlib import pyplot as plt
 10
      from matplotlib.backends.backend_pdf import PdfPages
      pdf=PdfPages('raw_graphs_n_such.pdf')
 14
      ''' constants '''
 16
      h=1
 18
      t0=0
      tf=200
 20
      N=1000
      t=np.linspace(t0, tf, int(tf/h)+1)
      Gamma=0.04
 24
      stand_dev=0.001
      Q=np.diag(np.array([0.01, 0.01, 0.01, 0.04]))
 26
      DATA=np.loadtxt('obsdata_txt.txt')
 28
 29
 30
      ''' data structures and models '''
      Xa_0=np.array([[997, 3, 0, 0.1]]) # [S I R Beta]
 34
      Xa_0=Xa_0.transpose() # [S I R Beta]^T
 36
      Xa_storage=np.zeros((4, tf+1))
      Xa_storage[:,0]=Xa.reshape(4)
      Xf_just_forecast=Xa
 38
      Xf_storage=np.zeros((4, tf+1))
 39
 40
      Xf_storage[:,0]=Xa.reshape(4)
 41
 42
      Pa_0=np.diag(np.array([10, 10, 0.01, 0.04]))
 43
      Pa=np.array(Pa_0)
 44
      def Mf(X): # 4x1
 45
 46
          'input is augmented analysis Xa_k-1'
 47
          'output is forecast Xf_k'
 48
          S=X[0]
 49
          I=X[1]
          R=X[2]
          Beta=X[3]
```

```
c=h/N
 54
          S next= S - c*Beta*S*I
          I_next= I + c*Beta*S*I - h*Gamma*I
          R_next= R + h*Gamma*I
          Beta_next= Beta
 58
          return np.array([S_next, I_next, R_next, Beta_next]).reshape((4,1))
 59
      def Ma(X): # 4x4
          'input is augmented analysis Xa_k-1'
          'output is \{dMf/dXa\}_k-1, for decluttering code'
 63
          S=X[0]
 64
          I=X[1]
 65
          Beta=X[3]
 66
          c=h/N
          return np.array([
              [1-c*Beta*I, -1*c*Beta*S, 0, -1*c*S*I],
              [c*Beta*I, 1+c*Beta*S-h*Gamma, 0, c*S*I],
 70
              [0, h*Gamma, 1, 0],
              [0, 0, 0, 1]
          ])
 74
      def Pf(P, X):
          'input is augmented analysis Pa_k-1, augmented analysis Xa_k-1'
 76
          'output is forecast covariance Pf_k'
          return np.matmul(
 78
              Ma(X), np.matmul( P, Ma(X).transpose() )
 79
 80
 81
      H=np.array([[0,0,1,0]]) # observe R only
 82
      r_constant=stand_dev**2
 83
 84
      def Xa_k(X, P, K, y):
 85
          'input is forecast Xf_k, forecast covariance Pf_k'
          'output is augmented analysis Xa_k'
 86
          return X + K*(y - np.matmul(H,X))
 87
 88
 89
      def Pa_k(P,K):
 90
          'input is forecast covariance Pf_k'
 91
          'output is analysis covariance Pa_k'
          return np.matmul(
              (np.identity(4) - np.matmul(K,H)), P
 94
 96
 97
 98
      ''' main loop '''
      for k in range(1, tf+1):
         Xf_just_forecast=Mf(Xf_just_forecast)
102
          Xf_k=Mf(Xa)
103
          Pf_k=Pf(Pa, Xa)
104
105
          K=np.matmul( Pf_k, H.transpose() )
          c=np.matmul(
              H, np.matmul( Pf_k, H.transpose() )
108
109
          K=((c+r_constant)**(-1))*K
110
          y=DATA[k-1]
          Xa=Xa_k(Xf_k, Pf_k, K, y)
          Pa=Pa_k(Pf_k, K)
114
          Xf_storage[:,k]=Xf_just_forecast.reshape(4)
116
          Xa_storage[:,k]=Xa.reshape(4)
```

```
118
120
      ''' plots '''
      fig_Beta=plt.figure()
      plt.plot(t, Xa_storage[3,:], label='Beta(t_k)')
124
      plt.title("Estimate for Beta(t_k)"+'\n'+"Gamma="+str(Gamma))
      plt.xlabel("t_k=0:"+str(tf)+", step size="+str(h))
      plt.grid(True)
      plt.close()
128
     pdf.savefig(fig_Beta)
129
130
     fig_state=plt.figure()
     plt.plot(t, Xa_storage[0,:], label='S(t_k)')
     plt.plot(t, Xa_storage[1,:], label='I(t_k)')
     plt.plot(t, Xa_storage[2,:], label='R(t_k)')
134
     plt.title("Estimate for X(t_k) after filter, X=[S,I,R]"+'\n'+"Gamma="+str(Gamma))
     plt.xlabel("t_k=0:"+str(tf)+", step size="+str(h))
136
      plt.ylabel("Portion of population N="+str(N))
      plt.legend(loc='best')
138
     plt.grid(True)
      plt.close()
140
     pdf.savefig(fig_state)
141
142
     fig_forecasted=plt.figure()
143
     plt.plot(t, Xf_storage[0,:], label='S(t_k)')
144
     plt.plot(t, Xf_storage[1,:], label='I(t_k)')
     plt.plot(t, Xf_storage[2,:], label='R(t_k)')
     plt.title("Estimate for X(t_k), just the forecast")
146
     plt.xlabel("t_k=0:"+str(tf)+", step size="+str(h))
147
      plt.ylabel("Portion of population N="+str(N))
148
149
      plt.legend(loc='best')
150
      plt.grid(True)
      plt.close()
      pdf.savefig(fig_forecasted)
154
      pdf.close()
156
158
      \# My function names are confusing, maybe change them to 'compute_Xa_k' or something...
```