AF-vapeR Manual v0.2.1

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Allele Frequency Vector Analysis of Parallel Evolutionary Responses

The aim of this software is to quantify and compare parallel genotype change based on allele frequency changes between population pairs. The software produces a series of allele frequency matrices with n (number of snps per window) columns and m (number of population pairs) rows. Within each matrix, we perform eigen analysis to quantify skew in the underlying eigenvalue distributions across the genome. An eigenvalue distribution with elevated eigenvalues on the first eigenvector is indicative of a common trajectory through multivariate space for more than one population pair (ie. parallel or antiparallel genotype change in multiple populations). Multiple eigenvectors with elevated eigenvalues is indicative of multiple parallel/antiparallel axes within a genomic region, highlighting nonparallelism.

It is highly recommended to read the accompanying manuscript before applying this method. The manuscript is published in Methods in Ecology and Evolution (https://doi.org/10.1111/2041-210X.13952)

Citation

Whiting, James R., Josephine R. Paris, Mijke J. van der Zee, and Bonnie A. Fraser. 2022.

"AF-vapeR: A Multivariate Genome Scan for Detecting Parallel Evolution Using Allele Frequency Change V Methods in Ecology and Evolution / British Ecological Society, August. https://doi.org/10.1111/2041-210

Installation

```
# install.packages("remotes",repos = "http://cran.us.r-project.org")
# remotes::install_github("JimWhiting91/afvaper")
library(afvaper,verbose = F)
```

Parallelism Definitions:

- Parallel Change along the same axis in the same direction.
- Antiparallel Change along the same axis in the opposite direction.
- Nonparallel Change along an alternative axis.
- Multi-parallel Parallelism along multiple non-parallel axes, for e.g. 2 of 4 pops are parallel on eigenvector 1, and the other 2 pops are parallel on eigenvector 2.

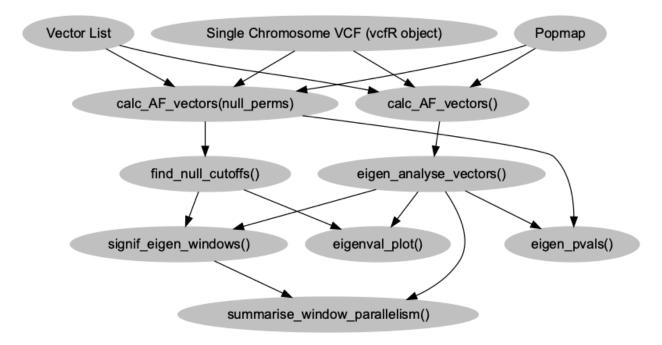


Figure 1: AFvapeR

Workflow Summary

Demo

Make the inputs

The software runs in R and requires the following inputs:

• A vcfR object of a chromosome (here we are using simulated data), eg:

```
library(vcfR, verbose = F)
##
##
                        vcfR
##
      This is vcfR 1.13.0
        browseVignettes('vcfR') # Documentation
##
        citation('vcfR') # Citation
                                          ****
vcf_in <- read.vcfR(system.file("full_parallel.vcf.gz",package="afvaper"),verbose = F)</pre>
vcf_in
## ***** Object of Class vcfR ****
## 100 samples
## 1 CHROMs
## 169,184 variants
## Object size: 150.4 Mb
## 0 percent missing data
## ****
                ****
                               ****
```

```
# For your own data:
# vcf_in <- read.vcfR("/path/to/chromosome-vcf/")</pre>
```

• As of v0.2 we can alternatively provide as input a matrix of population-level allele frequencies. This matrix should be in the form of a row for each SNP, where columns 1 and 2 have the chromosome and bp position of each SNP. Each column from 3 onwards should include the population allele frequency for a population included in the vectors. The pop names used in column headers must match the pop IDs in the vectors, e.g.

```
## chr pos pop1 pop2 pop3 pop4 pop5
## 1 chr1 1 0.2 0.1 0.6 0.2 0.4
## 2 chr1 10 0.5 0.1 0.1 0.4 0.8
## 3 chr1 50 0.7 0.3 0.2 0.0 1.0
```

• A popmap, with individuals in column 1 and population/habitat/ecotype in column 2, eg. (Note, if using an AF frequency table, a popmap is not required)

```
popmap <- read.table(system.file("full_parallel.popmap",package="afvaper"))
# Show popmap
head(popmap)</pre>
```

```
## V1 V2
## 1 msp_207 pop1
## 2 msp_223 pop1
## 3 msp_1390 pop1
## 4 msp_1426 pop1
## 5 msp_2045 pop1
## 6 msp_2268 pop1
```

• A list of vectors describing parallel replicates. These are based on population identifiers in the popmap, and in all cases the first and second population should be in the same direction, i.e. for Ecotype1 vs Ecotype2, all first populations should be Ecotype1 and all second populations should be Ecotype2. Here for example, pop1 represents Ecotype 1, and pop2-5 represent Ecotype 2. In this data, we are interested in the change in allele frequencies from pop1 to each of pops 2-5, as in these simulations pop1 is the founding/ancestral population from which pops 2-5 have diverged from. To build the vector list:

```
# View populations in the popmap
unique(popmap[,2])
```

```
## [1] "pop1" "pop2" "pop3" "pop4" "pop5"
```

```
## $pop2
## [1] "pop1" "pop2"
##
## $pop3
## [1] "pop1" "pop3"
##
## $pop4
## [1] "pop1" "pop4"
##
## $pop5
## [1] "pop1" "pop5"
```

Calculate Allele Frequency Change Vectors

In order to analyse our VCF, we need to transform the inputs into a list of allele frequency change matrices, where each row is the normalised allele frequency change vector (AFV) for one of our replicates, for N SNPs (where N is our window size). This is handled with the calc_AF_vectors() function:

```
## Calculating AF vectors for 845 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
```

```
# Show features of input...
print(paste0("Number of windows = ",length(AF_input)))
```

```
## [1] "Number of windows = 845"
```

```
print(paste0("Number of SNPs per window = ",ncol(AF_input[[1]])))
## [1] "Number of SNPs per window = 200"
print(paste0("Number of vectors per window = ",nrow(AF_input[[1]])))
## [1] "Number of vectors per window = 4"
Note, if we are using a matrix of allele frequencies, we set data_type="freq"
We also want to build a set of null vectors, in which the observed allele frequencies are shuffled among
populations and new vectors are calculated using the same vector structure as the originals. We do this
using the same function, but pass a null perms value to describe how many random vectors to calculate:
# How many permutations to run
null_perm_N = 1000
# Calculate Allele Frequency Change Vector Matrices
null_input <- calc_AF_vectors(vcf = vcf_in,</pre>
                               window_size = window_snps,
                               popmap = popmap,
                               vectors = vector_list,
                               n_{cores} = 4,
                               null_perms = null_perm_N,
                               data_type = "vcf")
## Calculating NULL AF vectors for 1000 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
# Show features of input...
print(paste0("Number of null windows = ",length(null_input)))
## [1] "Number of null windows = 1000"
print(paste0("Number of SNPs per window = ",ncol(null_input[[1]])))
## [1] "Number of SNPs per window = 200"
print(paste0("Number of vectors per window = ",nrow(null_input[[1]])))
```

Note here that 1000 null permutations is on the low side, and a value closer to 10,000+ would be better. In practice, given it is easiest to run these functions over separate chromosomes, we can aim for a total of 10,000 null vectors from across all chromosomes and combine null vectors calculated on individual chromosomes. The easiest way to do this is to divide the desired total of 10,000 (or more) up between chromosomes based on the relative sizes (this info is available in a genome fasta index for e.g.).

[1] "Number of vectors per window = 4"

```
# How many permutations do we want in total?
total_perms <- 10000
# Imagine a hypothetical fasta index with three chromosomes
genome_fai <- data.frame(chr=c("chr1","chr2","chr3"),</pre>
                          size=c(2e7,4e7,3e7))
# Fetch proportional size of all chromosomes
chr_props <- genome_fai$size/sum(genome_fai$size)</pre>
chr_perms <- data.frame(chr=genome_fai$chr,</pre>
                        perms=round(chr_props * total_perms))
# This gives us approximately 10000 null perms in total, distributed across the genome according to rel
chr_perms
##
      chr perms
## 1 chr1 2222
## 2 chr2 4444
## 3 chr3 3333
```

If we store each per-chromosome set of null_input vectors to a list, we can easily merge these into a single list with: merged_null_input <- unlist(all_chr_null_input_list,recursive=FALSE). This merged_null_input can then be used as detailed below.

Example of splitting analysis over chromosomes

#chr_vcf <- read.vcfR(/path/to/vcf)</pre>

Let's say we have three chromosomes, and each chromosome is currently stored as a VCF. We can loop over each VCF and perform the analysis, saving results as we go. Here I'll make two identical copies of the simulated chromosome VCF for demonstration purposes:

```
# Make our VCF copies, give them new chromosome identifiers, and save as a list to loop over.
# Note: In practice, if VCFs are stored somewhere on the system, we can just read them in within the lo
vcf_in3 <- vcf_in2 <- vcf_in</pre>
vcf_in2@fix[,1] <- "chr2"</pre>
vcf_in3@fix[,1] <- "chr3"</pre>
vcf_list <- list(vcf_in,vcf_in2,vcf_in3)</pre>
# Assume we have already calculated our per-chrom permutation count as chr_perms (see above)
chr_perms
      chr perms
## 1 chr1 2222
## 2 chr2 4444
## 3 chr3 3333
# We can now loop over our chromosome VCFs.
# Here I will just output each per-chrom results to a full list, but we could save the results to .rds
all_chr_res <- lapply(1:3,function(i){</pre>
  # First read in the VCF
```

```
chr_vcf <- vcf_list[[i]]</pre>
  # Calculate AFV
  chr_AF_input <- calc_AF_vectors(vcf = chr_vcf,</pre>
                                  window_size = window_snps,
                                  popmap = popmap,
                                  vectors = vector_list,
                                  n cores = 4)
  # Calculate null AFV
  chr_null_input <- calc_AF_vectors(vcf = chr_vcf,</pre>
                                    window_size = window_snps,
                                    popmap = popmap,
                                    vectors = vector_list,
                                    n_{cores} = 4,
                                    null_perms = chr_perms$perms[i])
  ## We could save these to some temporary file, e.g.
  # saveRDS(list(chr_AF_input,chr_null_input),paste0("chr",i,"_AFV.rds"))
  # Return our results
  return(list(chr_AF_input,chr_null_input))
})
## Calculating AF vectors for 845 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
## Calculating NULL AF vectors for 2222 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
## Calculating AF vectors for 845 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
## Calculating NULL AF vectors for 4444 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
## Calculating AF vectors for 845 windows with 200 SNPs each
```

```
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
## Calculating NULL AF vectors for 3333 windows with 200 SNPs each
## Popmap check passed, all popmap inds are in VCF
## VCF check passed, all VCF inds are in popmap
## If saved as .rds, we can read these back in and merge to single lists
#all_chr_res <- lapply(1:3,function(i) readRDS(pasteO("chr",i,"_AFV.rds")))</pre>
# To fetch all of chr AFV, we take the first element of each list element
# Note: the merge_eigen_res() func is the same as unlist(,recursive=F)
AF_input <- merge_eigen_res(lapply(all_chr_res, '[[',1))
# All null, we take the second element of each list element
null_input <- merge_eigen_res(lapply(all_chr_res,'[[',2))</pre>
# We now have our whole (3 chr) genome's worth of AFV matrices and null matrices in a single input
c(head(names(AF_input)),tail(names(AF_input)))
   [1] "chr1:15-18166"
                                 "chr1:18718-48277"
                                                           "chr1:48287-74923"
##
   [4] "chr1:75219-95836"
                                 "chr1:96020-119073"
                                                           "chr1:119085-144327"
## [7] "chr3:19808619-19838830" "chr3:19838918-19877336" "chr3:19877527-19907262"
## [10] "chr3:19907433-19932368" "chr3:19932509-19954790" "chr3:19954865-19983084"
```

Perform Eigen Analysis Over Allele Frequency Matrices

Taking the AF_input data, we can perform eigen analyses over all matrices with a single command. This can be run over the AFV from all chromosomes as it is not computationally expensive:

```
# Perform eigen analysis
eigen_res <- lapply(AF_input,eigen_analyse_vectors)</pre>
```

The eigen_res output is a list containing, for each matrix, the eigenvalue distribution, the eigenvector loadings, and the projected A matrix that shows per-SNP scores for each eigenvector. The chromosomal regions are stored in names(eigen_res):

```
# View chromosomal regions:
head(names(eigen_res))

## [1] "chr1:15-18166" "chr1:18718-48277" "chr1:48287-74923"

## [4] "chr1:75219-95836" "chr1:96020-119073" "chr1:119085-144327"

# View eigenvalue distribution of first matrix
eigen_res[[1]]$eigenvals

## Eigenvector_1 Eigenvector_2 Eigenvector_3 Eigenvector_4

## 3.76064811 0.16154864 0.04904462 0.02875863
```

```
# View eigenvector loadings of first matrix
eigen_res[[1]]$eigenvecs
```

```
##
        Eigenvector_1 Eigenvector_2 Eigenvector_3 Eigenvector_4
## pop2
           -0.4972237
                           0.5445576
                                         0.6742875
                                                      -0.03952282
           -0.5046727
                           0.3187280
                                        -0.5982165
                                                       0.53465398
## pop3
## pop4
           -0.5091357
                          -0.1106599
                                        -0.3321564
                                                      -0.78626165
## pop5
           -0.4887279
                          -0.7678697
                                         0.2777508
                                                       0.30720625
```

```
# View head of SNP scores
head(eigen_res[[1]]$A_matrix)
```

Find Null Cutoffs

Using our null_input, we can output a matrix containing the cutoff expectations from the null distribution for each eigenvector for various significance thresholds:

```
# Get cutoffs for 95%, 99% and 99.9%
null_cutoffs <- find_null_cutoff(null_input,cutoffs = c(0.95,0.99,0.999))
null_cutoffs</pre>
```

```
## Eigenvector 1 3.478392 3.741727 3.948183
## Eigenvector 2 3.836957 3.916202 3.983822
## Eigenvector 3 3.958875 3.980533 3.995407
## Eigenvector 4 4.000000 4.000000 4.000000
```

Here, the values are summed through eigenvalues, such that the value for Eigenvector 2 is the sum of Eigenvalues 1 + 2, and the maximum value is equivalent to the number of replicates (length(vector_list)).

Calculate empirical p-values

We can also calculate one-tailed empirical p-values (empPvalues) by comparing our observed eigenvalues to the null distribution. These are conceptually similar to using cutoffs, i.e. anything above the 95% cutoff outlined above will have an empPvalue < 0.05, however they can be useful for removing noise and highlighting peaks for visualisation. These are calculated using the eigen_res results and the null_input vectors, and as output we get p-values for each eigenvector and window.

```
# Calculate p-vals
pvals <- eigen_pvals(eigen_res,null_input)

# Showpvals
head(pvals)</pre>
```

```
##
                      Eigenvalue_1 Eigenvalue_2 Eigenvalue_3 Eigenvalue_4
                         0.00920092
                                      0.00870087
                                                   0.02360236
                                                                  0.5468547
## chr1:15-18166
## chr1:18718-48277
                         0.81208121
                                                                  0.8721872
                                      0.57885789
                                                   0.71047105
## chr1:48287-74923
                         0.25062506
                                      0.47394739
                                                   0.45534553
                                                                  0.6136614
## chr1:75219-95836
                         0.93439344
                                      0.97589759
                                                   0.94839484
                                                                  0.1287129
## chr1:96020-119073
                                      0.30843084
                                                   0.25622562
                                                                  0.6814681
                         0.27362736
## chr1:119085-144327
                                      0.08520852
                                                   0.11021102
                                                                  0.2080208
                         0.12651265
```

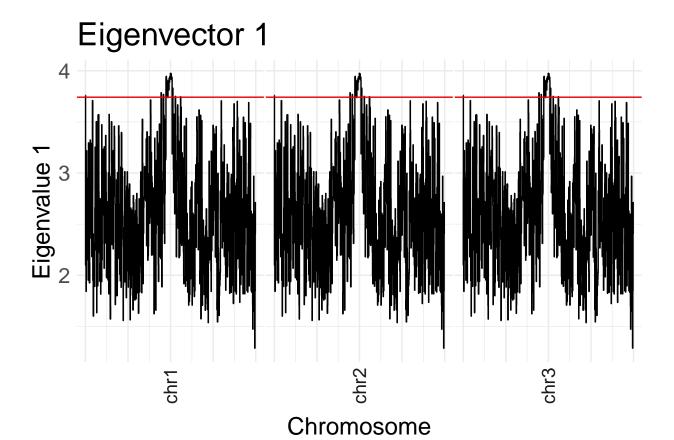
Note: Because these empPvalues are calculated by comparing to the null distribution, they are bounded by the number of permutations. For e.g. if you run 1000 permutations, the lowest possible p-value for an observed value that exceeds all 1000 of the null values is simply (0+1/1000+1) which is ~ 0.001 . If we ran 10,000 permutations and again had an observed eigenvalue greater than all 10,000 null values, this would be ~ 0.0001 e.t.c.

Consider this when interpreting empPvalues, as they are not a true statistic test!

Plot Eigenvalues Along Chromosomes

We can plot the eigenvalues for each chromosome, either plotting the raw eigenvalues or the associated p-values. The output of eigenval_plot() gives a figure for each eigenvector. Each facet panel on the horizontal gives the results for a separate chromosome (recall here that chr2+3 are copies of chr1 as above):

```
# Plot the raw eigenvalues, and visualise the cutoff of 99%
all_plots <- eigenval_plot(eigen_res,cutoffs = null_cutoffs[,"99%"])
# Show the plots for eigenvalue 1
all_plots[[1]]</pre>
```

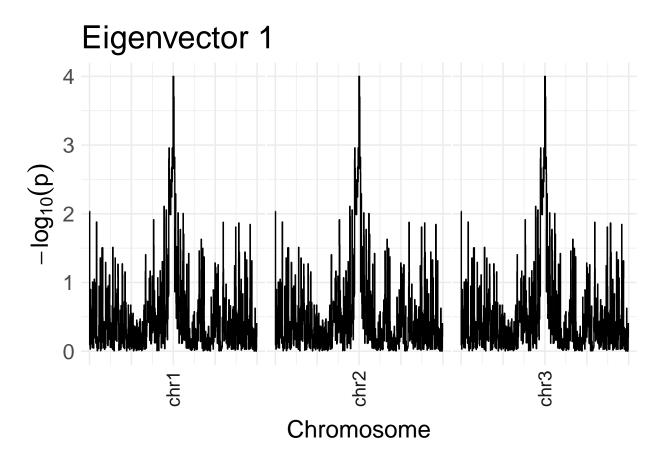


Alternatively, we can plot the empPvalues:

```
# Plot empirical p-values, -log10(p) of 2 ~ p=0.01, 3 ~ p=0.001 etc.
all_plots_p <- eigenval_plot(eigen_res,null_vectors = null_input,plot.pvalues = T)</pre>
```

Calculating empirical p-values for plotting...

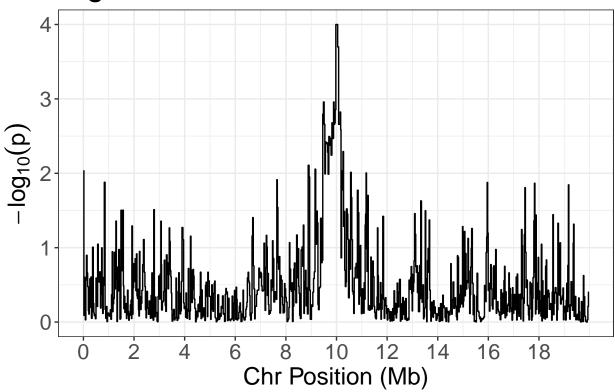
```
# Show the plots for eigenvalue 1
all_plots_p[[1]]
```



We can also exploit that all windows are named in the format chr:start-end to plot specific chromosomes using grep():

```
# Plot empirical p-values, -log10(p) of 2 ~ p=0.01, 3 ~ p=0.001 etc.
chr1_windows <- grep("chr1",names(eigen_res))
all_plots_p_chr1 <- eigenval_plot(eigen_res[chr1_windows],null_vectors = null_input,plot.pvalues = T)
## Calculating empirical p-values for plotting...
# Show the plots for eigenvalue 1
all_plots_p_chr1[[1]]</pre>
```

Eigenvector 1

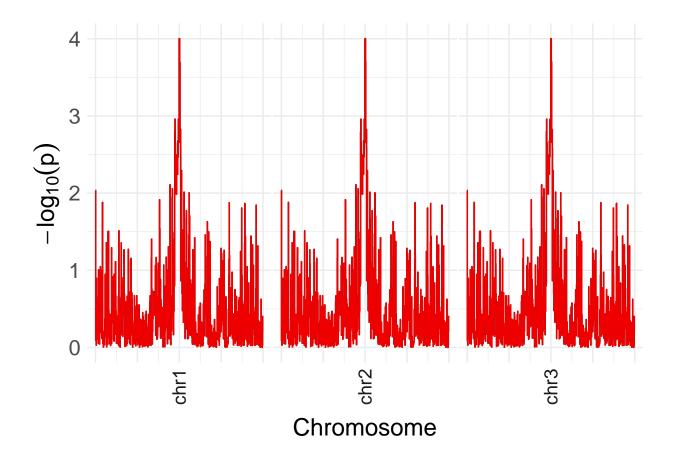


Note here, each of the plots is a ggplot object that can be extracted and edited however you like, for e.g. we can remove the title and change the colour using standard ggplot syntax:

```
library(ggplot2,verbose = F)

# Pull the figure
eig1_pval_fig <- all_plots_p[[1]]

# Edit
eig1_pval_fig + theme(title = element_blank()) + geom_step(colour="red2")</pre>
```



Pull Significant Windows

##

Using the eigen_res() results and null_cutoffs(), we can identify windows that exceed the null cutoffs and return a list of genome windows.

IMPORTANT: Because we summing eigenvalues, regions with a very large eigenvalue 1 may exceed the null cutoffs for several of our eigenvectors (e.g eigenvector 1, 2 and 3). The function signif_eigen_windows() is aware of this, and only returns windows on the first eigenvector for which they exceed a cutoff. This prevents windows being marked as significant on multiple eigenvectors. These window however may still appear as peaks when plotting, so bear this in mind.

```
# Recall the use of find_null_cutoffs() to fetch a matrix of cutoffs...

# null_cutoffs

# Find significant windows above 99.9% null permutation
significant_windows <- signif_eigen_windows(eigen_res,null_cutoffs[,"99.9%"])

# Display 'outliers'
significant_windows

## $'Eigenvector 1'
## [1] "chr1:9973948-10015463" "chr1:10015604-10045407" "chr1:10045553-10083818"
## [4] "chr2:9973948-10015463" "chr2:10015604-10045407" "chr2:10045553-10083818"
## [7] "chr3:9973948-10015463" "chr3:10015604-10045407" "chr3:10045553-10083818"
```

```
## $'Eigenvector 2'
## [1] "chr1:9883146-9904934" "chr1:9925507-9947330" "chr2:9883146-9904934"
## [4] "chr2:9925507-9947330" "chr3:9883146-9904934" "chr3:9925507-9947330"
##
## $'Eigenvector 3'
## [1] "chr1:9904984-9925507" "chr2:9904984-9925507" "chr3:9904984-9925507"
##
## $'Eigenvector 4'
## [1] "chr1:2174583-2191154" "chr2:2174583-2191154" "chr3:2174583-2191154"
```

Summarise Outliers

To make sense of outliers, we want to summarise various information within candidate windows. This includes: which of our replicate vectors are associated with the relevant eigenvector (i.e. which vectors load above a certain threshold onto the focal eigenvector); and whether vectors are associated in the same (parallel) or different (antiparallel) direction.

We also want to know for genome regions that exhibited elevated eigenvalues on eigenvectors 2+, what is happening on all preceding eigenvectors. This is because we are always summing the eigenvalues, and as such a large eigenvalue 2 sum reflects that most allele frequency variance is captured by the first 2 eigenvectors. This could mean a large eigenvalue 1 and small eigenvalue 2, or a more balanced eigenvalue 1+2. Interpreting this is important for classifying multi-parallelism.

The summarise_window_parallelism() function takes this into account, and returns all of this information into an output table for interpretation. The user defines the loading cutoff (which is an absolute value):

```
##
                  window_id eigenvector eigenvalue parallel_lineages
## 1
     chr1:9973948-10015463
                                    Eig1
                                           3.974657
## 2 chr1:10015604-10045407
                                                                     4
                                    Eig1
                                           3.972499
## 3 chr1:10045553-10083818
                                    Eig1
                                           3.968457
                                                                     4
     chr2:9973948-10015463
                                                                     4
                                    Eig1
                                           3.974657
## 5 chr2:10015604-10045407
                                    Eig1
                                           3.972499
                                                                     4
## 6 chr2:10045553-10083818
                                    Eig1
                                           3.968457
##
           parallel_pops antiparallel_pops
## 1 pop2,pop3,pop4,pop5
## 2 pop2,pop3,pop4,pop5
## 3 pop2,pop3,pop4,pop5
## 4 pop2,pop3,pop4,pop5
## 5 pop2,pop3,pop4,pop5
## 6 pop2,pop3,pop4,pop5
```

This output therefore tells us how many replicates are associated with the first eigenvector at this genomic region (using the names(vector_list) provided earlier), and lists which of these are parallel or anti-parallel.

For outliers on eigenvectors 2+ we have an additional eigenvalue_sum column that describes the sum of eigenvalues 1+2, as well as the individual eigenvalue 1 and eigenvalue 2 scores for every window. These

tell us that most of these windows are exhibiting a signature closer to full-parallelism (large eigenvalue 1) rather than multi-parallelism (more balanced eigenvalue 1 + 2), which is expected for this simulation (these regions are around the focal 10 Mb fully parallel sweep).

```
##
                window_id eigenvector eigenvalue eigenvalue_sum parallel_lineages
                                  Eig1 3.94129971
## 1 chr1:9883146-9904934
                                                         3.985715
## 2 chr1:9883146-9904934
                                  Eig2 0.04441480
                                                         3.985715
                                                                                   2
## 3 chr1:9925507-9947330
                                  Eig1 3.92085336
                                                         3.984427
                                                                                   4
## 4 chr1:9925507-9947330
                                  Eig2 0.06357374
                                                         3.984427
                                                                                   2
## 5 chr2:9883146-9904934
                                  Eig1 3.94129971
                                                         3.985715
                                                                                   4
## 6 chr2:9883146-9904934
                                  Eig2 0.04441480
                                                         3.985715
                                                                                   2
##
           parallel_pops antiparallel_pops
## 1 pop2,pop3,pop4,pop5
## 2
                    pop5
                                       pop2
## 3 pop2,pop3,pop4,pop5
## 4
                                       pop5
## 5 pop2,pop3,pop4,pop5
## 6
                    pop5
                                       pop2
```

Interpreting these tables, the eigenvalues, and the distribution of parallel/antiparallel lineages, is key to filtering out regions that may be of most interest to particular study questions. For instance, windows with very large eigenvalues but a mix of parallel and antiparallel lineages may not be good candidates if the hypothesis is that all replicate lineages should be evolving using the same alleles...

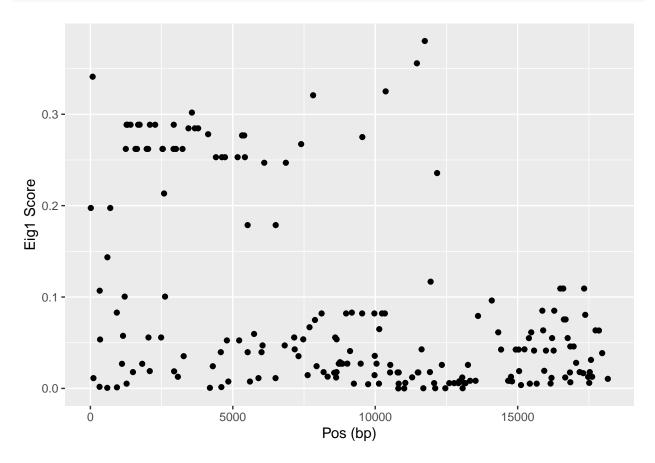
For more information on interpreting eigenvalue tables, see the preprint.

Explore candidate regions

Given a focal candidate region, we may be interested in the genes within that region, and whether our signal is localised around these genes. To do this, we can use the per-SNP scores stored within the A_matrix slot of each window's entry in eigen_res. This a matrix with a row per SNP and a column per eigenvector, given the per-SNP per-eigenvector score of association:

```
# Fetch an A matrix
A_mat <- eigen_res[[1]]$A_matrix
head(A_mat)</pre>
```

These can be plotted by separating out the chr and pos values stored in rownames(A_mat). Note that here we have not polarised the allele frequencies in any way, by default the analysis just tracks the REF allele as labelled in the VCF, so both positive and negative scores of association are of interest. Here then we can just plot the absolute score:



Version History

- v0.2.1 Minor bug fixes and documentation fixes.
- v0.2 Major update, includes the addition of the data_type parameter for calc_AF_vectors(), and modification of permutation process to shuffle observed frequencies rather than shuffle population IDs for individual and recalculate new allele frequencies. As such, results based on this permutation approach will differ from those of v0.1! Generally this updated permutation approach is more conservative than the previous approach.
- v0.1 Initial release alongside preprint.