Datatypes and functions

Haskell and Cryptocurrencies

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Goals

- Introduce Bool, Maybe, [a], binary trees, and one or two other types.
- Introduce the standard design pattern (catamorphism) by example for all these types.

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Bool

Booleans

data Bool = False | True

Booleans

```
data Bool = False | True
```

Constructors:

False :: Bool

True :: Bool

Booleans

```
data Bool = False | True
```

Constructors:

```
False :: Bool
True :: Bool
```

Functions on Booleans:

```
fun :: Bool -> ...
fun False = ...
fun True = ...
```

Patterns

Allowed patterns are:

- · Saturated constructor applications to other patterns.
- Variables (match anything).
- · Underscore / wildcard pattern (matches anything).
- · Literals (numbers, characters, strings, lists).

Exhaustive patterns and overlap

- · Patterns are matched in order.
- In particular, catch-all cases must come last.
- Best practice: split programming problems by expanding variables into all possible constructors for the type of the variable.
- For non-overlapping cases, the order does not matter.

```
not :: Bool -> Bool
not = _
```

Start with the type signature. Use typed holes.

Type of hole: **Bool** -> **Bool**.

```
not :: Bool -> Bool
not x = _
```

Introduce function arguments.

Type of hole: Bool .

Available locally: x :: Bool .

```
not :: Bool -> Bool
not False = _
not True = _
```

Split cases (if you cannot solve directly).

Type of holes: **Bool** and **Bool**.

```
not :: Bool -> Bool
not False = True
not True = False
```

Solve. Easy in this case.

```
not :: Bool -> Bool
not False = True
not True = False
```

Reflect. Everything looks good.

```
(||) :: Bool -> Bool -> Bool
(||) = _
```

Start with the type signature.

Type of hole: Bool -> Bool -> Bool.

```
(||) :: Bool -> Bool -> Bool
(||) x y = _
```

Introduce function arguments.

```
Type of hole: Bool .
```

Available locally: x :: Bool and y :: Bool.

```
(||) :: Bool -> Bool -> Bool
x || y = _
(If preferred, we can use infix notation.)

Type of hole: Bool .
Available locally: x :: Bool and y :: Bool .
```

```
(||) :: Bool -> Bool -> Bool

False || y = _

True || y = _
```

Split on a suitable argument (let's take the first).

```
Type of holes: Bool and Bool. Available locally: y :: Bool (in each case).
```

```
(||) :: Bool -> Bool -> Bool

False || y = y

True || y = True
```

We actually can solve at this point.

```
(||) :: Bool -> Bool -> Bool

False || y = y

True || y = True
```

Reflect. Everything looks good.

Different options

```
(||) :: Bool -> Bool -> Bool
False | | v = v
True || y = True
(||) :: Bool -> Bool -> Bool
False | | False = False
False | | True = True
True || False = True
True | | True = True
```

Different options

```
(||) :: Bool -> Bool -> Bool
False | | v = v
True || v = True
(||) :: Bool -> Bool -> Bool
False || False = False
False | | True = True
True || False = True
True | | True = True
```

```
loop :: a
loop = loop
```

What about True | | loop?

Undefined / run-time crashes

Haskell does not prevent looping or crashing:

```
undefined :: a
error :: String -> a
```

Undefined / run-time crashes

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```

First (library) version:

```
GHCi> GHCi > True || undefined
True
```

Second (fully expanded) version:

```
GHCi> GHCi > True || undefined
*** Exception: Prelude.undefined
```

Undefined / run-time crashes

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```
undefined :: a
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Second (fully expanded) version:

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GHCi> GHCi > True || undefined

*** Exception: Prelude.undefined
```

Also relevant for possibly infinite or just very large terms.

If-then-else

```
ifthenelse :: Bool -> a -> a
ifthenelse False t e = e
ifthenelse True t e = t
```

Works as expected: only one branch is evaluated.

Syntax for if-then-else

```
ifthenelse :: Bool -> a -> a -> a
ifthenelse c t e = if c then t else e
```

Guards

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- Guards are tried one by one.
- Conditions all of type Bool.
- First guard that evaluates to **True** is chosen.

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```
otherwise :: Bool
otherwise = True
```

Maybe

Optional values

data Maybe a = Nothing | Just a

Optional values

```
data Maybe a = Nothing | Just a
```

Constructors:

```
Nothing :: Maybe a
```

Just :: a -> Maybe a

Optional values

```
data Maybe a = Nothing | Just a
```

Constructors:

```
Nothing :: Maybe a

Just :: a -> Maybe a
```

Functions on Maybe:

```
fun :: Maybe a -> ...
fun Nothing = ...
fun (Just x) = ...
```

Using a default Value

```
fromMaybe :: a -> Maybe a -> a
fromMaybe def Nothing = def
fromMaybe _ (Just x) = x
```

Using a default Value

```
fromMaybe :: a -> Maybe a -> a
fromMaybe def Nothing = def
fromMaybe _ (Just x) = x
```

```
GHCi> fromMaybe 3 Nothing
3
GHCi> fromMaybe 3 (Just 5)
5
```

Chaining optional values

```
orelse :: Maybe a -> Maybe a
orelse Nothing y = y
orelse (Just x) _ = Just x
```

Chaining optional values

```
orelse :: Maybe a -> Maybe a
orelse Nothing y = y
orelse (Just x) _ = Just x
```

```
GHCi> Nothing `orelse` Just 5

Just 5

GHCi> Just 3 `orelse` Just 5

Just 3

GHCi> Just 3 `orelse` Nothing

Just 3

GHCi> Nothing `orelse` Nothing

Nothing
```

Modifying an optional value

```
mapMaybe :: (a -> b) -> Maybe a -> Maybe b
mapMaybe f Nothing = Nothing
mapMaybe f (Just x) = Just (f x)
```

Modifying an optional value

```
mapMaybe :: (a -> b) -> Maybe a -> Maybe b
mapMaybe f Nothing = Nothing
mapMaybe f (Just x) = Just (f x)
GHCi> mapMaybe (+ 1) Nothing
Nothing
GHCi> mapMaybe (+ 1) (Just 5)
Just 6
GHCi> mapMaybe not (Just True)
Just False
```

Adding two optional values

```
addMaybes :: Maybe Int -> Maybe Int -> Maybe Int addMaybes (Just x) (Just y) = Just (x + y) addMaybes _ = Nothing
```

Adding two optional values

```
addMaybes :: Maybe Int -> Maybe Int -> Maybe Int addMaybes (Just x) (Just y) = Just (x + y) addMaybes _ _ = Nothing
```

```
liftMaybe ::
  (a -> b -> c)
  -> Maybe a -> Maybe b -> Maybe c
liftMaybe f (Just x) (Just y) = Just (f x y)
liftMaybe _ _ = Nothing
```

Constructor:

Constructor:

Functions on pairs:

```
fun :: (a, b) -> ...
fun (a, b) = ...
```

Extracting components

```
fst :: (a, b) -> a
fst (a, b) = a
```

```
snd :: (a, b) -> b
snd (a, b) = b
```

Swapping components

```
swap :: (a, b) -> (b, a)
swap (a, b) = (b, a)
```

Currying and uncurrying

```
curry :: ((a, b) -> c) -> a -> b -> c
curry f a b = f (a, b)
```

Currying and uncurrying

```
curry :: ((a, b) -> c) -> a -> b -> c
curry f a b = f (a, b)
```

```
uncurry :: (a -> b -> c) -> (a, b) -> c
uncurry f (a, b) = f a b
```

Lists

Lists

```
data [a] = [] | a : [a] -- special syntax
```

Lists

```
data [a] = [] | a : [a] -- special syntax
```

Constructors:

```
[] :: [a]
(:) :: a -> [a] -> [a]
```

```
data [a] = [] | a : [a] -- special syntax
```

Constructors:

```
[] :: [a]
(:) :: a -> [a] -> [a]
```

Functions on lists:

```
fun :: [a] -> ...

fun [] = ...

fun (x : xs) = ... fun xs ...
```

Recursion in types and functions are connected!

Length of a list

```
length :: [a] -> Int
length [] = 0
length (x : xs) = 1 + length xs
```

Finding an element in a list

```
elem :: Eq a => a -> [a] -> Bool
elem x [] = False
elem x (y : ys) = x == y || elem x ys
```

Appending two lists

```
(++):: [a] -> [a] -> [a]
[] ++ ys = ys
(x:xs) ++ ys = x:(xs ++ ys)
```

Reversing a list

```
reverse :: [a] -> [a]
reverse [] = []
reverse (x : xs) = reverse xs ++ [x]
```

Filtering a list

Simple look-up tables

Modelling a look-up table

```
type Table k v = [(k, v)]
```

Modelling a look-up table

```
type Table k v = [(k, v)]
```

Interface:

```
empty :: Table k v
insert :: k -> v -> Table k v -> Table k v
delete :: Eq k => k -> Table k v -> Table k v
lookup :: Eq k => k -> Table k v -> Maybe v
```

Note: functional data structures are persistent!

An empty table

```
empty :: Table k v
empty = []
```

Inserting a new key-value pair

```
insert :: k -> v -> Table k v -> Table k v
insert k v t = (k, v) : t
```

Deleting a key

Deleting a key

```
delete :: Eq k \Rightarrow k \Rightarrow Table k v \Rightarrow Table k v delete k = filter (\((k', _) \Rightarrow not (k == k'))
```

Finding a value for a given key

A new datatype for tables

```
newtype Table k v = Table [(k, v)]
```

Constructor:

```
Table :: [(k, v)] \rightarrow Table k v
```

Functions on tables:

```
fun :: Table k v -> ...
fun (Table table) = ...
```

newtype vs. data

newtype:

- · restricted to one constructor with one argument,
- · otherwise like data,
- guaranteed to have the same representation as the wrapped type.

data:

- arbitrary number of constructors and argument,
- introduces an additional indirection.

Making tables abstract

- Functions on tables have to be adapted to (un)wrap the **Table** constructor applications.
- The Table constructor can then be hidden from the module exports.
- Pattern matching and accessing the internal representation becomes unavailable outside of the defining module, only the interface defined by the functions remains.

Transactions

Modelling a transaction

```
data Transaction =
  Transaction Amount Account Account
  deriving (Eq, Show)

type Amount = Int
type Account = String
```

Modelling a transaction

```
data Transaction =
  Transaction Amount Account Account
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type Amount = Int
  type Account = String
```

Constructor (same name as type):

```
Transaction ::
Amount -> Account -> Transaction
```

Functions on transactions:

```
fun :: Transaction -> ...
fun (Transaction amount from to) = ...
```

Accessing components

```
trAmount :: Transaction -> Amount
trAmount (Transaction a _ _) = a

trFrom :: Transaction -> Account
trFrom (Transaction _ f _) = f

trTo :: Transaction -> Account
trTo (Transaction _ _ t) = t
```

Record syntax

```
data Transaction =
  Transaction
    {trAmount :: Amount
    , trFrom :: Account
    , trTo :: Account
    }
  deriving (Eq, Show)
```

- · Constructor can still be used with positional arguments.
- · Provides selector functions for free.
- Also provides record construction and update syntax, and record patterns.

Updating an account table with a transaction

```
type Accounts = Table Account Amount
processTransaction ::
 Transaction -> Accounts -> Accounts
processTransaction (Transaction amount f t) as =
 let
   fOld = fromMaybe 0 (lookup f as)
   tOld = fromMaybe 0 (lookup t as)
 in
   insert f (fOld - amount)
     (insert t (tOld + amount) as)
```

(It would be better to define a dedicated update on tables.)

Binary trees

Binary trees

```
data Tree a = Leaf a | Node (Tree a) (Tree a)
```

Constructors:

```
Leaf :: a -> Tree a
Node :: Tree a -> Tree a
```

Functions on trees:

```
fun :: Tree a -> ...
fun (Leaf x) = ...
fun (Node l r) = ... fun l ... fun r ...
```

Functions usually recurse twice!

Flattening a tree into a list

```
flatten :: Tree a -> [a]
flatten (Leaf x) = [x]
flatten (Node l r) = flatten l ++ flatten r
```

Computing the height of a tree

```
height :: Tree a -> Int
height (Leaf x) = 0
height (Node l r) = 1 + max (height l) (height r)
```

Expressions

Abstract syntax trees of an expression language

```
data Expr =
    Lit Int
   | Add Expr Expr
  | Neg Expr
   | IfZero Expr Expr Expr
```

Constructors:

```
Lit :: Int -> Expr
Add :: Expr -> Expr -> Expr
Neg :: Expr
IfZero :: Expr -> Expr -> Expr -> Expr
```

Functions on expressions

Evaluating an expression