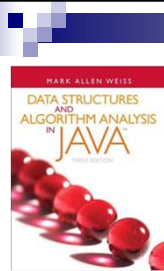


Algorithm Analysis (I)

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Note: The most of the information of these slides was extracted and adapted from Weiss's book, "*Data Structures and Algorithm Analysis in Java*". They are provided for COP3530 students only. Not to be published or publicly distributed without permission by the publisher.



COP-3530 - Data Structures



Module #1: Algorithm Analysis (part I)

Outline:

- What is algorithm?
- How efficient is an algorithm?
- Performance vs Complexity
- $T(n)$ - the relation of the number of operations to the problem size

The first claim of this course...



“**Bad** programmers worry about the code. **Good** programmers worry about data structures and their relationships.”

(by Linus Trovals, creator of **Linux** kernel)

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Some Terminology



■ **Algorithm**

- A high-level description of a piece-by-piece or step-by-step process.

■ **Abstract Data Type (ADT)**

- Formal (Mathematical) description/model of components of the data and the set of operations that are allowed.

■ **Data structure**

- A specific organization of data for implementing an ADT

■ **Implementation**

- A specific implementation of a data structure in a specific programming language.

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The Definition of an Algorithm



- Brief and concise definition:

An **algorithm** is a clearly specified set of simple instructions to be followed to solve a problem.

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The Definition of an Algorithm



- A more complete definition:

An **algorithm** is a well-ordered collection of clear and effectively computable operations that when executed produces a result and halts in a finite amount of time*.

*Schneider, M. and J. Gersting (1995), *An Invitation to Computer Science*, West Publishing Company, New York, NY, p. 9.

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The Definition of an Algorithm



- Some **relevant** points of this definition:
 - An algorithm is a **well-ordered** collection...
 - An algorithm has **clear** operations...
 - An algorithm has **effectively computable** operations...
 - An algorithm **produces a result**...
 - An algorithm **halt in a finite amount of time**

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Algorithm Efficiency



- How efficient is an algorithm?
 - **Efficiency** covers lots of resources, including:
 - **CPU** (running time) usage
 - **Memory** (internal) usage
 - **Disk** (external memory) usage
 - **Network** usage
 - All are important but we will mostly talk about the **time complexity** (**CPU** usage).

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Algorithm CPU Efficiency



■ Performance vs Complexity?

□ Performance:

- How much time is used when a program is executed.
- Please note that this depends on the computer, operating system, compiler, etc.

□ Complexity:

- What happens as the **size** of the problem being solved gets larger?
- We want to evaluate the “quality” of the algorithms independent of their implementation.

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Algorithm Analysis



■ In this module we shall discuss:

- How to **estimate** the **running time** required for an **algorithm**.
- How to **reduce the running time** of an algorithm (from days or years to fractions of a second).
- The results of careless use of **recursion**.
- Some examples of **efficient algorithms**.

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Algorithm Analysis



■ Very Important!

- When we are trying to find the **complexity** of an algorithm, **we are not interested in the exact number of operations** that are necessary to solve the problem.
- We are interested in **the relation of the number of operations to the problem size**
- We are usually interested in the **worst case** - the maximum number of operations that are necessary to be performed for a given problem size.

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Algorithm Analysis



- Most of the problems we will study have an **input size**.
- Example:
 - For the problem of sorting, the size of the input is the number of elements to be sorted.
- The **CPU** time and **space** (internal **memory**) used by an algorithm will in general be a function of this **input size**.
- For a given input size **n** we often express the time **T** to execute the algorithm as a **function of n**, written as **$T(n)$** .
- We will always assume **$T(n)$ is a non-negative value function.**

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Algorithm Analysis



■ Example:

- Consider a simple algorithm to solve the problem of **finding the largest (max) value in an array of n integers**.
- The algorithm looks at each integer in turn, saving the position of the largest value seen so far.
- The **total time** to run this algorithm is approximately **cn** , because we must make **n** comparisons, with each comparison costing **c** time.
- Then for this algorithm **$T(n) = cn$**

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Algorithm Analysis



■ Example:

- An algorithm with running time **$T(n) = n^2$** requires **$1024 \times 1024 = 1,048,576$** time steps for an input of size **$n = 1024$** .
- An algorithm with running time **$T(n) = n \log n$** requires **$1024 \times 10 = 10,240$** time steps for an input of size **$n = 1024$** .
- It's easy to verify that **$n^2 > 10n \log n$** when **$n > 58$** .



You would be **much better off changing algorithms** instead of **buying a computer ten times faster**.

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