





# **Abstract Data Type (ADT)**

- Definition: ADT is a set of objects together with a set of operations.
- Important points:
  - □ Nowhere in an ADT's definition is there any mention of how the set of operations is implemented.
  - □ Objects such as lists, sets, and graphs are **ADT**, just as integers, reals, and booleans are **data types**.
  - ☐ For the set ADT we might have such operations as add, remove, and contains. Alternatively, we might only want the two operations union and find.

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## The List ADT. Definition



- **List** <u>linear sequence</u> of an arbitrary number of items of the form  $A_0$ ,  $A_1$ ,  $A_2$ , ...,  $A_{N-1}$
- Important points:
  - ☐ The <u>size</u> of this list is *N*.
  - □ Empty list special list of size 0.
  - □ For any list (except the empty list)
    - $A_i$  follows (or succeeds)  $A_{i-1}$  (i < N)
    - $A_{i-1}$  precedes  $A_i$  (i > 0).
  - $\Box$  The <u>position</u> of element  $A_i$  in a list is i.



## The List ADT. Some Operations



- printList;
- makeEmpty;
- find returns the position of the <u>first occurrence</u> of an item;
- insert and remove generally insert and remove some element from some position in the list;
- **findKth** returns the element in some position (specified as an argument).

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Example: L = (34, 12, 52, 16, 12)
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\Box find(52) = 2
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- $\square$  insert(27, 2) returns L = (34,12, 27, 52, 16,12)
- □ remove(52) returns L = (34, 12, 27, 16, 12)
- $\Box$  findKth(3) = 16

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## The List ADT. Simple Array implementation



- We can implement a List ADT using an array.
- The most serious problem with using an array to estimate the maximum size of the list.
- This estimate is not needed in Java, or any modern programming language.
- Example code fragment:
  - (1) Classical version (re-define array):







- Example code fragment (cont...):
  - (2) After Java 1.5 (using an ArrayList):

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# The List ADT. Complexity of Operations



- Using Array implementation!
  - □ printList is O(N)
  - ☐ *find* is **O(N)** (worst case)
  - □ findKth is O(1)
  - □ *insert* and *remove* **O(N)** (worst case)



If **insertions** and **deletions** occur over the whole list, and in particular, <u>at the front of the list</u>, then the **array implementation** is not a good option.

Alternative - Linked List!







#### The Linked List. Definition

- Linked List consists of a collection of nodes, which are not necessarily adjacent in memory.
- Each **node** contains the <u>element (or data)</u> and a <u>link</u> to a node containing its successor (next link). The last cell's next link references null.



#### Important points:

- $\Box$  printList or find(x) is O(N) (start at the first node in the list and then traverse the list by following the next links);
- □ findKth is no longer quite as efficient as an array implementation;
- □ *findKth(i)* takes "O(i)" time and works by traversing down the list in the obvious manner.

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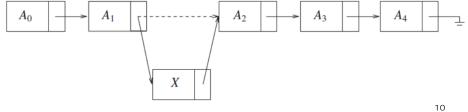
### The Linked List. Remove & Insert



■ The *remove* method can be executed in one next reference change.



The *insert* method requires obtaining a new node from the system by using a new call and then executing two reference movements.

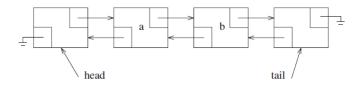




## The Linked List. Special cases.



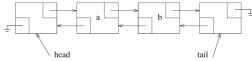
- Add to the front or Remove the first item O(1) time if a link to the front of the linked list is kept.
- Add at the end O(1) time if we maintain a link to the last node.
- Removing the last item is more complicated.
  - □ Solution: For every node maintains a link to its previous node in the list too. This is a **doubly linked list**.



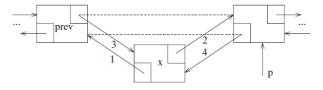
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# Insertion in a Doubly Linked List





add before: How a new node containing x is spliced in between a node referenced by p and p.prev



Node newNode = new Node( x, p.prev, p );
p.prev.next = newNode;
p.prev = newNode;

