

Intrinsic backbone preferences are fully present in blocked amino acids

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The preferences of amino acid residues for ϕ, ψ backbone angles vary strikingly among the amino acids, as shown by the backbone angle ϕ found from the $^3J(H_{\alpha}, H_N)$ coupling constant for short peptides in water. New data for the $^3J(H_{\alpha}, H_N)$ values of blocked amino acids (dipeptides) are given here. Dipeptides exhibit the full range of coupling constants shown by longer peptides such as GGXGG and dipeptides present the simplest system for analyzing backbone preferences. The dipeptide coupling constants are surprisingly close to values computed from the coil library (conformations of residues not in helices and not in sheets). Published coupling constants for GGXGG peptides agree closely with dipeptide values for all nonpolar residues and for some polar residues but not for X = D, N, T, and Y, which are probably affected by polar side chain–backbone interactions in GGXGG peptides. Thus, intrinsic backbone preferences are already determined at the dipeptide level and remain almost unchanged in GGXGG peptides and are strikingly similar in the coil library of conformations from protein structures. The simplest explanation for the backbone preferences is that backbone conformations are strongly affected by electrostatic dipole–dipole interactions in the peptide backbone and by screening of these interactions with water, which depends on nearby side chains. Strong backbone electrostatic interactions occur in dipeptides. This is shown by calculations both of backbone electrostatic energy for different conformers of the alanine dipeptide in the gas phase and by electrostatic solvation free energies of amino acid dipeptides.

amino acid conformations | dipeptides | electrostatic screening

The origin of the differences among the intrinsic backbone preferences of the 20 aa is an unsolved puzzle, and these intrinsic preferences (1–6) are an important part of the local structure (7, 8) in unfolded peptide chains that may be used to guide the folding process at early stages of folding. The “intrinsic” conformational preferences are specified by the backbone ϕ, ψ angles found in short peptides and in the “coil library” (1–6) of Protein Data Bank residue conformations for residues outside repetitive secondary structures (helices, sheets). The existence of different backbone preferences in short peptides in water is demonstrated by values of the backbone angle ϕ , which can be measured by NMR from the $^3J(H_{\alpha}, H_N)$ coupling constant (vicinal coupling constant between $C_{\alpha}H$ and NH protons) by using the Karplus relation (9). These coupling constants are averaged over all backbone conformations that are present. Individual ϕ -values are obtained for residues in the coil library of the Protein Data Bank, and corresponding values of $^3J(H_{\alpha}, H_N)$ are found from the Karplus relation and then averaged. In the coil library of Smith *et al.* (3), average values of $^3J(H_{\alpha}, H_N)$ range from 5.9 Hz for Gly and 6.1 Hz for Ala to 7.7 Hz for Val. In addition to the different intrinsic backbone preferences, there is a substantial neighboring residue effect: ϕ angles are shifted toward more negative values if the neighboring residues are aromatic or β -branched (FHITVWY) than if they are not (10, 11). Any attempt to explain the different intrinsic backbone preferences of the amino acids should also give an explanation for the neighboring residue effect. The electrostatic

screening model (see below) has been shown to give a plausible explanation for the neighboring residue effect (11).

The purpose of this article is to present data for the $^3J(H_{\alpha}, H_N)$ coupling constants of the amino acid residues in dipeptides (blocked amino acids) and to consider the meaning of this result for different hypotheses regarding the origin of the different backbone preferences. Disfavored backbone conformations that arise from steric clash between neighboring side chains (12, 13) have been suggested as a main source of local structure in unfolded peptides. More recently steric hindrance to the formation of H-bonds between peptide groups and water molecules has been found to be a major cause of disfavored backbone conformations (14) in Protein Data Bank structures. The disfavored backbone conformations are uncommon in tripeptide segments but become increasingly frequent in tetra and higher peptide segments (14), which suggests that this type of disfavored backbone conformations (over and above those found in the Ramachandran plots for dipeptides) are rare in dipeptides. Pairwise attractive interactions between side chains, which are well known in α -helices (15), have been proposed as a significant source of local structure in unfolded peptides (8). H-bonds between polar side chains and especially backbone $-NH$ groups occur commonly in helix capping (16) and may occur in short peptides. Amino-aromatic, or “pseudo-H-bond,” interaction (17) between a tyrosine ring and the peptide $-NH$ of a nearby glycyl residue was reported for peptides containing the sequence Tyr-Xaa-Gly (18).

The alternative to side chain interactions as an explanation for diverse backbone preferences is electrostatic dipole–dipole interactions in the peptide backbone and side chain-dependent screening of these interactions by water (5, 11, 19–22). We demonstrate that this explanation is plausible for peptides as short as dipeptides by computing values of the backbone electrostatic energy for different conformers of the alanine dipeptide in the gas phase, with the aid of four published *ab initio* studies (23–26), and also by using DELPHI (27) to compute the electrostatic solvation free energies (ESF values) in water of the various amino acid dipeptides. The electrostatic screening model (5, 20), which can explain the backbone conformations in highly unstructured peptides, is based on a 1995 proposal by Avbelj and Moult (21) that was developed further by Avbelj (20). The electrostatic screening model proposes that three physical factors are dominant in determining backbone conformations in highly unstructured peptides. The three factors are (i) the local electrostatic energy (E_{local}) at a given site within the backbone; (ii) the ESF at that site, which depends on the screening interaction of water dipoles with the polar peptide group; and

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Abbreviations: ESF, electrostatic solvation free energy; GdmCl, guanidinium chloride; J-dipep, pH 4.9 dipeptide coupling constant; P_{II}, polyproline II; uls, upper left strip of ϕ, ψ map.

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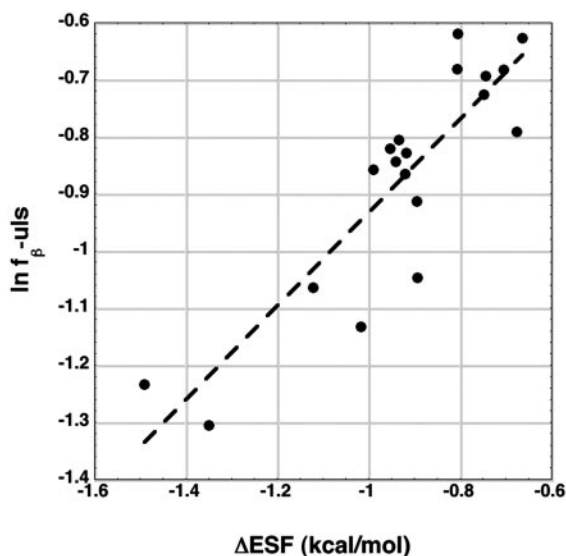


Fig. 4. The y axis refers to the fraction of residues in the coil library β basin, which is divided by the number of residues in the upper left strip of the ϕ, ψ map. The logarithm of this fraction is plotted against the difference in ESF between the P_{II} and β backbone conformations, $ESF(P_{II}) - ESF(\beta)$, for dipeptides ($R = 0.88$).

adjacent peptide groups. A small residue like alanine provides better access to water and therefore has a larger negative ESF value than a β -branched residue like valine (20, 21). The ESF varies in an approximately linear manner with E_{local} (20) (the local backbone electrostatic energy), and the slope of the plot of ESF versus E_{local} , denoted here by $k(ESF)$, is amino acid-specific and linearly related (20) to the “screening coefficient” of the amino acid residue defined earlier (21). The plot of $k(ESF)$ versus J-dipep (Fig. 3) shows a clear linear correlation ($R = 0.80$), indicating that the backbone preferences expressed in the J-dipep values are related to those predicted by the electrostatic screening model (5, 20–22). The J-dipep values for Asp, Glu, and His are omitted in Fig. 3 because the J-dipep values were measured for the partly or fully ionized forms whereas the ESF values were calculated for the neutral forms. Table 1 shows a strong dependence of J-dipep on the extent of ionization for Asp and Glu, whose charged groups are near the backbone, and a similar effect is expected for His; the charged groups of Lys and Arg are more remote. Values of $k(ESF)$ are taken from table 2 of ref. 20, for the central residues of a large number of randomly generated tripeptides. Different sets of assumed values of the partial charges on the peptide group were examined (20), and the $k(ESF)$ results shown here (Fig. 3) refer to the PARSE partial charges that are used in DELPHI (27).

As noted above, the J-dipep values may be determined chiefly by residues in just the upper left strip of the ϕ, ψ map, and a significant dependence of J-dipep on $f_{\beta-uls}$ is observed. Earlier studies of the relation between the electrostatic screening model and the coil library (5, 11) indicated that $f_{\beta-uls}$ should depend on ΔESF , the difference between $ESF(P_{II})$ and $ESF(\beta)$, and specifically that $\ln f_{\beta-uls}$ should show a nearly linear dependence on ΔESF . The data given here for $f_{\beta-uls}$ (Table 1) allow this proposal to be tested for the coil library. Fig. 4 shows a good linear plot ($R = 0.88$) of $\ln f_{\beta-uls}$ versus ΔESF , using the dipeptide ESF values. This result supports the earlier proposal (5, 20–22) that the electrostatic screening model can predict how an amino acid is distributed between the P_{II} and β -basins of the coil library.

Earlier Studies of Backbone Preferences. From the 1960s onward, it was evident that some data for backbone preferences of the amino acids clash with the prevailing random coil model for unfolded proteins. Flory’s (35) 1969 definition of a random coil polymer states that a random coil has no strongly preferred backbone conformation and “differences in energy between alternative rotational configurations about a given bond are usually of the order of RT.” Tanford’s (36) 1968 summary of his influential work on the properties of denatured proteins was interpreted by a random coil model. Nevertheless, Schellman and Schellman (37) had earlier (1964) pointed out that denatured proteins are not likely to be random coil molecules because of their distinctive optical rotatory dispersion (the forerunner of the modern CD spectrum), which suggests that at most a few backbone conformations are well populated. In 1970, Madison and Schellman (38) reported that both the optical rotatory dispersion and CD spectrum of a proline diamide are closely related to those of P_{II} , indicating that this dipeptide has a well defined backbone preference and therefore that dipeptides might be good models for the backbone preferences of the amino acid residues in proteins. The Schellman laboratory then explored the possibility that the CD spectra of dipeptides with closed-ring side chains (39) might be used to relate CD spectra to ϕ, ψ maps. In 1973, Tiffany and Krimm (40) pointed out that the typical CD spectrum of denatured proteins closely resembles that of P_{II} , and three decades later this subject became a lively research field [see review by Shi, Woody, and Kallenbach (41)].

Modern work on backbone preferences is better known and is reviewed here only briefly. In 1995, Swindells, MacArthur, and Thornton (1) found that the “coil” segments of Protein Data Bank structures give backbone preferences (1) that are related to the Chou–Fasman statistical frequencies of amino acids in α -helices and β -sheets. Serrano (2) then reported that $^3J(H_{\alpha}, H_N)$ coupling constants measured in peptides give similar values as those computed from the coil library. In this period, the “extended- β ” ($-120^\circ, 120^\circ$) and P_{II} ($-75^\circ, 145^\circ$) conformational basins were often not analyzed separately but rather included together within a broad distribution of β conformations (3). Interest in the P_{II} conformation as a major backbone conformation of short peptides and denatured proteins grew rapidly after 2000 (for review, see ref. 41).

Comparison Between Electrostatic Energy and *ab Initio* Energy for Conformers of the Alanine Dipeptide. The backbone electrostatic energy of the alanine dipeptide ($E_{dipeptide}$) has been computed for various conformers in the gas phase by taking the conformer geometry determined in an *ab initio* study and using Coulomb’s law with atom-centered partial charges (see *Materials and Methods*). Fig. 5A compares the difference in $E_{dipeptide}$ between stable gas phase conformers of the alanine dipeptide with the difference in conformational energy ($E_{ab initio}$) for six conformers (25). The conformer coordinates were not published (25), and the geometries of the conformers were built by using bond angles and distances from DISCOVER LIBRARY (Accelrys, Inc., San Diego). Fig. 5B shows corresponding data for a study (24) in which the conformer coordinates were published but which has only four conformers that can be shown here. The data points for the $C7_{eq}$ and $C7_{ax}$ conformers are omitted because they have internal H-bonds and Coulomb’s law does not represent these H-bond energies satisfactorily in the calculation of $E_{dipeptide}$.

Surprisingly, the difference in $E_{dipeptide}$ is proportional to, and approximately as large as, the difference in $E_{ab initio}$, which includes other energetic contributions such as torsional energy from rotation about the ϕ and ψ backbone bonds. Similar results, showing a proportionality between $E_{dipeptide}$ and $E_{ab initio}$, were obtained from two other *ab initio* studies (23, 26) of the alanine dipeptide. The slope of the line in Fig. 5A is 1.22, with a correlation coefficient of 0.93, and the slope of the line in Fig.

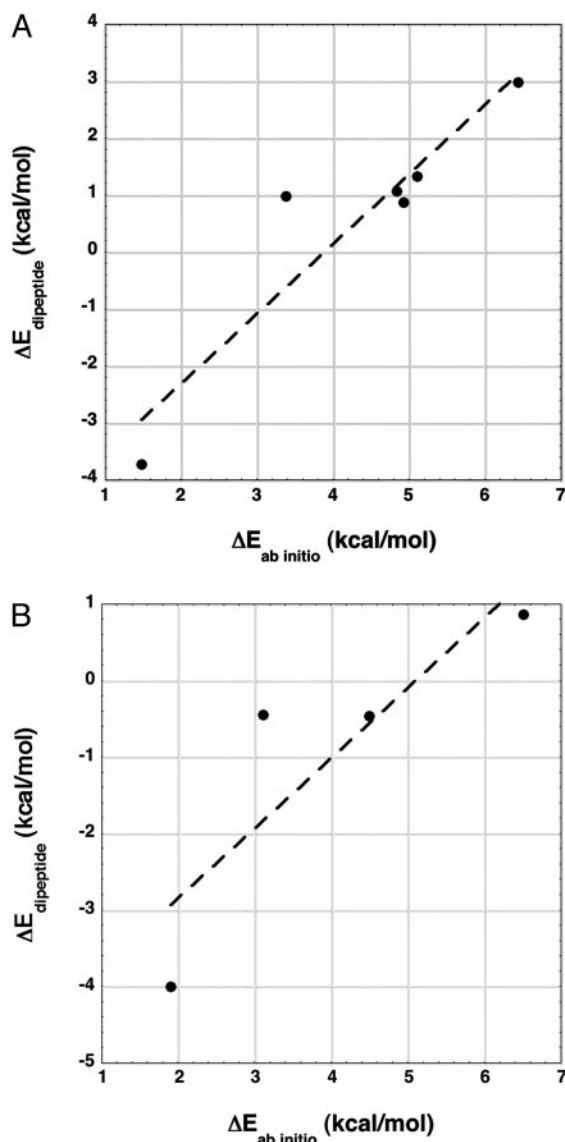


Fig. 5. The calculated backbone electrostatic energy difference ($\Delta E_{\text{dipeptide}}$, see *Materials and Methods*) is plotted against the *ab initio* conformational energy difference ($\Delta E_{\text{ab initio}}$) for various gas phase conformers of the alanine dipeptide, taken from *ab initio* studies in the literature. The geometry of each conformer, which is used in calculating $E_{\text{dipeptide}}$, is taken from the *ab initio* study. Similar results are obtained for two other *ab initio* studies of the alanine dipeptide (data not shown; see text). The data points for the $C7_{\text{eq}}$ and $C7_{\text{ax}}$ conformers are omitted because these conformers have an internal H-bond, whose energy is not well represented by using Coulomb's law. (A) In this study (25), data for six conformers could be shown here. The conformer coordinates were not published, and their geometries were built by using bond angles and distances from DISCOVER LIBRARY. The slope of the line is 1.22 ($R = 0.93$). (B) In this study (24), data for four conformers could be shown here, and the published conformer coordinates could be used to give the conformer geometry. The slope of the line is 0.92 ($R = 0.87$).

5B is 0.92, with a correlation coefficient of 0.87. In the other two studies, which have data for four conformers when $C7_{\text{eq}}$ and $C7_{\text{ax}}$ are excluded, the slope ranges from 1.54 (23) to 1.86 (26). All four *ab initio* studies indicate that $E_{\text{dipeptide}}$ is proportional to $E_{\text{ab initio}}$ and the backbone electrostatic energy is large, accounting for a large part of the variation in $E_{\text{ab initio}}$ among conformers of the alanine dipeptide. In some cases, the slope is larger than 1 (23, 25, 26), which is unexpected; further work is needed to find the explanation. Note that a dielectric constant of 1 is used in calculating $E_{\text{dipeptide}}$.

In aqueous solution, the electrostatics are very different from the gas phase because the backbone electrostatic energy is screened by water, like the screening described by the Born equation (42) for an ion in water. Solvation of the alanine dipeptide has been studied *ab initio* in the presence of four water molecules (43) or with the polarizable continuum model (44) or with a hybrid quantum mechanics/molecular mechanics model (45). The Born equation considers the case when a spherical ion is fully exposed to solvent and water is treated as a continuum solvent. The Born equation gives the fractional extent of screening by water as $[1 - (1/D)] = 0.987$ at 25°C ($D = 78.5$). Screening of backbone electrostatic energy in aqueous solution can be evaluated from the screening coefficients computed by Avbelj (20), whose results show that the electrostatic energy of the peptide backbone is screened much less by water than for the ions considered in the Born equation (20).

Conclusions

The intrinsic backbone preferences of the amino acid residues are fully present in blocked amino acids, according to new measurements of $^3J(\text{H}_\alpha, \text{H}_\text{N})$ for dipeptides, and dipeptides provide the simplest system for analyzing intrinsic backbone preferences. Because pairwise side chain interactions are eliminated and polar side chain-backbone interactions are made improbable as possible explanations for the backbone preferences, the electrostatic screening model becomes the probable explanation. Calculations show that this model is applicable to peptides as short as dipeptides. There are large differences in backbone electrostatic energy between conformers of the alanine dipeptide in the gas phase and the electrostatic dipole-dipole interactions are screened by water in a side chain-dependent manner, giving dipeptide ESF values that differ substantially among the amino acids. The dipeptide coupling constants are correlated with ESF values calculated earlier (20) for randomly generated backbone conformations.

Materials and Methods

Materials and Sample Preparation. Blocked amino acids (e.g., acetyl-Ala-*N*-methylamide) were purchased from Bachem or Biosyn or otherwise were synthesized from the corresponding methylester by using methylamine at 0°C. NMR samples had 20 mM peptide in 90% H_2O /10% D_2O and either 0.005 M citric acid (pH 2.9) or 0.03 M Na citrate/0.02 M citric acid (pH 4.9). Samples in 1,4-dioxane- d_8 had 20 mM Ala dipeptide or 10 mM Val dipeptide. Samples in CCl_4 had <1 mM peptide because of poor solubility, and external locking was used with a CDCl_3 stem coaxial insert. Concentration dependence was studied between 1 and 20 mM peptide.

NMR Spectroscopy. Coupling constants $^3J(\text{H}_\alpha, \text{H}_\text{N})$ were measured from 1D- ^1H spectra at 30°C in a Varian INOVA 600-MHz spectrometer. The spectral width was 6,000 Hz with 64,000 data points, zero filling to 128,000 data points and 32 scans. Except for glycine dipeptide, coupling constants were measured from H_N resonances, and a band-fitting algorithm was used to calculate the peak frequency of the broad H_N doublet. NMR spectra were processed without filter function to allow selection of the pure Lorentzian lineshape in the fitting procedure (GRAMS program, Thermo Electron, San Jose, CA). Band frequencies, bandwidths, and intensities were allowed to vary simultaneously with no restrictions. The parameters determined in this way were tested by the fitting program based on the maximum entropy algorithm. The coupling constants of the Ala and Val dipeptides were cross-checked by determining them by a second method, based on the well resolved H_α doublets found by decoupling the H_β resonances. The accuracy of the coupling constants is believed to be ± 0.05 Hz.

Backbone Electrostatic Energy and ESF. There are several *ab initio* studies in the literature of conformational energies of stable

conformers of the alanine dipeptide in the gas phase. We compare the *ab initio* energy difference between two conformers with the corresponding difference in backbone electrostatic energy, calculated by Coulomb's law using fixed, atom-centered partial charges and a dielectric constant of 1. To demonstrate generality, we selected four studies with the following levels of theory: MP4/cc-pVTZ(-f) (23), MP2/aug-cc-pVDZ (24), MP2/aug-cc-pVTZ (25), and MP2/6-311++G** (26). The backbone electrostatic energy, which is the total electrostatic energy ($E_{\text{dipeptide}}$) of the dipeptide, was calculated for various conformations of the alanine dipeptide in the gas phase by using the conformer geometries determined in various *ab initio* calculations of conformational energy. When the conformer coordinates were not published, the conformer geometries were built by using standard bond angles and distances from DISCOVER LIBRARY. The point atomic charges for the main chain atoms N, H_N, C, and O were equal to -0.28, +0.28, +0.38, and -0.38, respectively, electron

charge. Interactions between point charges within a single peptide group were omitted.

The ESF of the two peptide groups in the different amino acid dipeptides was calculated as discussed by Avbelj (5, 20), using the DELPHI (27) algorithm with water treated as a continuum solvent. The partial charges on the side chains were set = 0 ["PARSE neutral" calculations (20)], and only the ESF values of the peptide groups were calculated.

Coil Library. The coil library used here is described in refs. 5 and 11. Average coupling constants computed from the coil library were found as described in ref. 5.

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