

Statistical Analysis Empirical Exercise

Min Jiang; F2

1.1 Find the sample size.

```
vlhh <- read.csv("C:/studydata/Statistical Analysis/R/vlhh.csv")##insert data
View(vlhh)
##1.1 Find the sample size
n <- length(vlhh$mpid_hh)
```

n	6163L
---	-------

We get the sample size is 6163.

1.2 Find the mean and standard deviation for the following variables:

templecompany_hh

lendmoney_hh

keroricego_hh

```
> summary(vlhh)
      X      mpid_hh      pid_hh
Min.   : 1      Min.   :1002      Min.   : 1001
1st Qu.:1542      1st Qu.:1048      1st Qu.: 1048
Median :3082      Median :1089      Median : 1089
Mean   :3082      Mean   :1091      Mean   : 1677
3rd Qu.:4622      3rd Qu.:1140      3rd Qu.: 1140
Max.   :6163      Max.   :1174      Max.   :77777
keroricego_hh      templecompany_hh      keroricecome_hh
Min.   :0.00000      Min.   :0.00000      Min.   :0.0000
1st Qu.:0.00000      1st Qu.:0.00000      1st Qu.:0.0000
Median :0.00000      Median :0.00000      Median :0.0000
Mean   :0.04056      Mean   :0.01136      Mean   :0.0404
3rd Qu.:0.00000      3rd Qu.:0.00000      3rd Qu.:0.0000
Max.   :1.00000      Max.   :1.00000      Max.   :1.0000
lendmoney_hh      borrowmoney_hh      samecaste_hh
Min.   :0.00000      Min.   :0.00000      Min.   :0.000
1st Qu.:0.00000      1st Qu.:0.00000      1st Qu.:0.000
Median :0.00000      Median :0.00000      Median :1.000
Mean   :0.04024      Mean   :0.04511      Mean   :0.656
3rd Qu.:0.00000      3rd Qu.:0.00000      3rd Qu.:1.000
Max.   :1.00000      Max.   :1.00000      Max.   :1.000
sameoccupation_hh
Min.   :0.0000
1st Qu.:0.0000
Median :1.0000
Mean   :0.5694
3rd Qu.:1.0000
Max.   :1.0000
> sd(vlhh$templecompany_hh)
[1] 0.105976
> sd(vlhh$lendmoney_hh)
[1] 0.1965379
> sd(vlhh$keroricego_hh)
[1] 0.1972954
```

So templecompany_hh's mean is 0.01136, standard deviation is 0.105976.

lendmoney_hh's mean is 0.04024, standard deviation is 0.1965379.

keroricego_hh's mean is 0.0404, standard deviation is 0.1972954.

1.3 Find the correlation coefficient between keroricego_hh and samecaste_hh

```
> cor(v1hh$keroricego_hh, v1hh$samecaste_hh)
[1] -0.09176947
```

The correlation coefficient between keroricego_hh and samecaste_hh is -0.09176947.

1.4 How many pairs (in total) have the relation "lendmoney_hh" in this village?

```
> sum(v1hh$lendmoney_hh)
[1] 248
```

There are 248 pairs (in total) have the relation "lendmoney_hh" in this village.

We can also calculate it through 1.1 and 1.2 questions. We can get the mean of lendmoney_hh is 0.0404 and the sample size is 6163. So there are $0.0404 \times 6163 = 248$ pairs (in total) have the relation "lendmoney_hh" in this village

1.5 Is the average number relation "lendmoney_hh" greater than 0.035 at 5% significance level?

Run the t-test below and report/interpret what you find.

```
> t.test(v1hh$lendmoney_hh, mu = 0.035, alternative = c("greater"))
```

```
One Sample t-test

data:  v1hh$lendmoney_hh
t = 2.0931, df = 6162, p-value = 0.01819
alternative hypothesis: true mean is greater than 0.035
95 percent confidence interval:
 0.03612161      Inf
sample estimates:
mean of x
0.04024014
```

We can get p-value is $0.01819 < 0.05$, so we reject H_0 and get the conclusion that the average number relation "lendmoney_hh" is greater than 0.035 at 5% significance level.

Or 95 percent confidence interval = $0.03612161 < \text{mean of } x = 0.04024014$, so we reject H_0 and get the same conclusion that the average number relation "lendmoney_hh" is greater than 0.035 at 5% significance level.

1.6. Construct a confidence level for the population mean for lendmoney_hh, at confidence level 95%.

```
meanlendmoney <- mean(v1hh$lendmoney_hh)
n <- length(v1hh$lendmoney_hh)
s <- sd(v1hh$lendmoney_hh)
se <- s/sqrt(n)
c <- qt(0.975, n-2)
CI <- c(meanlendmoney-c*se, meanlendmoney+c*se)
```

CI

num [1:2] 0.0353 0.0451

So we get a confidence level for the population mean for lendmoney_hh, at confidence level 95% is (0.0353, 0.0451).

2. Simple linear regressions

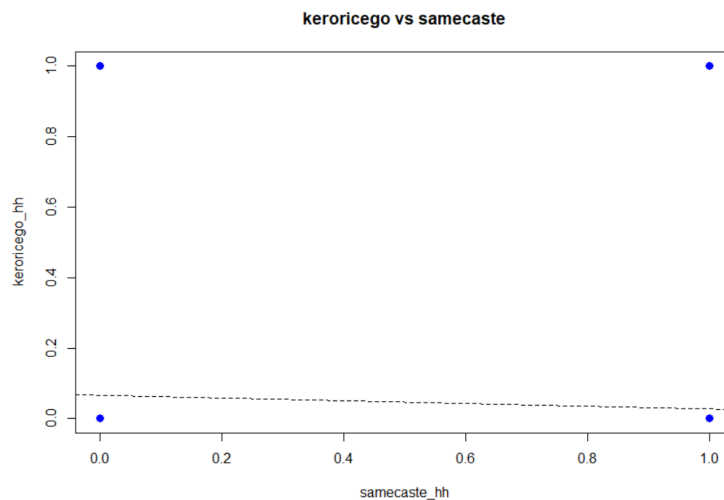
```
lm1 <- lm(keroricego_hh ~ samecaste_hh, data = vlhh)
summary(lm1)
plot(keroricego_hh ~ samecaste_hh, data = vlhh, pch = 16, cex = 1.3, col = "blue", main = "keroricego vs samecaste", xlab = "samecaste_hh", ylab = "keroricego_hh")
abline(lm1, lty=2)
```

```
Call:
lm(formula = keroricego_hh ~ samecaste_hh, data = vlhh)

Residuals:
    Min       1Q   Median       3Q      Max
-0.06557 -0.06557 -0.02745 -0.02745  0.97255

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  0.065566   0.004267  15.365 < 2e-16 ***
samecaste_hh -0.038111   0.005269  -7.234 5.27e-13 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1965 on 6161 degrees of freedom
Multiple R-squared:  0.008422, Adjusted R-squared:  0.008261
F-statistic: 52.33 on 1 and 6161 DF, p-value: 5.271e-13
```



2.1 Find the intercept and slope. Find the p-values for both. How do you interpret the slope (together with its p-value)?

Compare your answer here to your answer to question 1.3, what can you find?

Plot the regression line, what can you find?

Intercept is 0.065566, its P-value is $< 2e-16$ ***. Intercept is significantly different from 0 at 0.1% level. Slope is -0.038111, its P-value is $5.27e-13$ ***. Slope is significantly different from 0 at 0.1% level.

On average, the likelihood of having the relationship of borrowing/lending rice is 6.6% if the two hh's do not belong to the same caste. Belonging to same caste decreases that likelihood by 3.8%, to 6.6- 3.8= 2.8%. The effect of same caste is very significant (extremely small p-value)

The correlation coefficient, denoted by r , tells us how closely data in a scatterplot falls along a straight line. The closer that the absolute value of r is to 1, the closer that the data is described by a linear equation. In this condition, the correlation coefficient is -0.09176947, which shows the data cannot be described by a linear equation suitably. We can also find Multiple R-squared is 0.008422, which also shows the data cannot be described by a linear equation suitably. But in question 2.1 shows “keroricego_hh” and “samecaste_hh” are related, so we had better find other function to fit the data.

The correlation coefficient of keroricego_hh and samecaste_hh is so low that it seems to show there are not relationship between. But in question 2.1, the P-value of the slop show they are related at a 0.1% significance level.

Plot the regression line, we can see keroricego_hh and samecaste_hh are negative correlated. The line very close to the samecastes_hh line, which means whether the two hh's belong to the same caste, the first hh does not tend to lend rice to the second hh.

2.2 Repeat what you did in 2.1, with “templecompany_hh” being the new dependent variable (instead of “keroricego_hh”).

```
lm2 <- lm(templecompany_hh ~ samecaste_hh, data = v1hh)
summary(lm2)
plot(templecompany_hh ~ samecaste_hh, data = v1hh, pch = 16, cex = 1.3, col = "blue", main = "templecompany vs samecaste", xlab = "samecaste_hh", ylab = "templecompany_hh")
abline(lm2, lty=2)
```

Call:

```
lm(formula = templecompany_hh ~ samecaste_hh, data = v1hh)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.01410	-0.01410	-0.01410	-0.00613	0.99387

Coefficients:

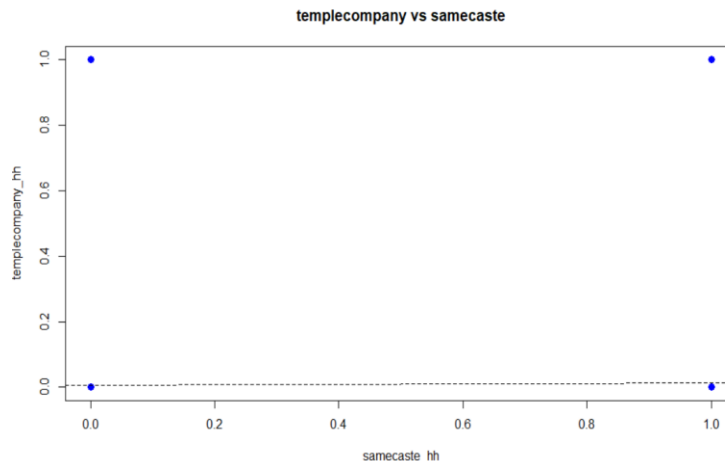
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	0.006132	0.002300	2.666	0.00770 **
samecaste_hh	0.007966	0.002840	2.805	0.00505 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1059 on 6161 degrees of freedom

Multiple R-squared: 0.001275, Adjusted R-squared: 0.001113

F-statistic: 7.867 on 1 and 6161 DF, p-value: 0.005049



Intercept is 0.006132, its P-value is 0.00770 **. Intercept is significantly different from 0 at 1% level, but not at 0.1% level.

Slop is 0.007966, its P-value is 0.00505 **. Slop is significantly differed from 0 at 1% level, but not at 0.1% level.

On average, the likelihood of having the relationship of going to temple together is 0.61% if the two hh's do not belong to the same caste. Belonging to same caste increases that likelihood by 0.80%, to 0.61+0.80= 1.41%. The effect of same caste is very significant (extremely small p-value)

```
> cor(v1hh$templecompany_hh, v1hh$samecaste_hh)
[1] 0.03571211
```

In this condition, the correlation coefficient is 0.03571211, which shows the data cannot be described by a linear equation suitably. We can also find Multiple R-squared is 0.001275, which also shows the data cannot be described by a linear equation suitably. But in question 2.2 shows “templecompany_hh” and “samecaste_hh” are related, so we had better find other function to fit the data.

The correlation coefficient of templecompany_hh and samecaste_hh is so low that it seems to show there are not relationship between. But in question 2.2, the P-value of the slop show they are related at a 1% significance level.

Plot the regression line, we can see templecompany_hh and samecaste_hh are positive correlated. The line very close to the samecastes_hh line, which means whether the two hh's belong to the same caste, the two hh's don't tend to go to temple together.

2.3 Is there any difference(s) between what you found in 2.1 and 2.2? (e.g., in terms of slope, p-value, etc.)

If you found any differences, can you tell some story/intuition to justify those?

1)

Belonging to same caste decreases the likelihood of having the relationship of borrowing/lending rice by 3.8%. Probably because it two households are in the same social class, then they may have the same economic difficulties. They may tend to borrow rice from higher caste.

Belonging to same caste increases the likelihood of having the relationship of going to temple by 0.80%. Probably because if two household are in the same caste, then they may have the common topics and the same affordable vehicles to go to the temple.

2)

The P-value of slop in 2.1 is $5.27e-13$ ***. The P-value of slop in 2.2 is 0.00505 **. $5.27e-13$ is much smaller than 0.00505 . It means Belonging to same caste is more likely to affect the relationship of borrowing/lending rice than the relationship of going to temple. Probably because the problem of survival is the most important problem. People can participate in other recreational and religious activities only when they have enough to eat.

3. Multiple linear regressions

3.1 Report the following information:

**Coefficients of the two explanatory variables,
Corresponding p-values,
(Adjusted) R-squared,**

```
> lm3 <- lm(keroricego_hh ~ templecompany_hh + lendmoney_hh, data = vlhh)
> summary(lm3)

Call:
lm(formula = keroricego_hh ~ templecompany_hh + lendmoney_hh,
    data = vlhh)

Residuals:
    Min       1Q   Median       3Q      Max
-0.64132 -0.01911 -0.01911 -0.01911  0.98089

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  0.019112   0.002221   8.605  < 2e-16 ***
templecompany_hh 0.124130   0.020533   6.045 1.58e-09 ***
lendmoney_hh    0.498074   0.011072  44.987 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1702 on 6160 degrees of freedom
Multiple R-squared:  0.2564,    Adjusted R-squared:  0.2561
F-statistic: 1062 on 2 and 6160 DF,  p-value: < 2.2e-16
```

Slop of templecompany_hh: 0.124130; Corresponding p-values: $1.58e-09$ ***;
Slop of lendmoney_hh: 0.498074; Corresponding p-values: $< 2e-16$ ***;
(Adjusted) R-squared: 0.2561

3.2 Interpret your result based on coefficients and p-values you found in 3.1.

Intercept is 0.019112, which means on average, the likelihood of having the relationship of borrowing/lending rice is 1.9% if the two hh's neither go to temple together nor having the relationship of borrowing/lending money.

Slop of templecompany_hh is 0.124130; Corresponding p-values is $1.58e-09$ ***; Slop is significantly differed from 0 at 0.1% level. Going to temple together increases the likelihood of having the relationship of borrowing/lending rice by 12.4%, to $1.9+12.4=14.3\%$. (Still don't have the relationship of borrowing/lending money)

Slop of lendmoney_hh is 0.498074; Corresponding p-values is $< 2e-16$ ***; Slop is significantly differed from 0 at 0.1% level. having the relationship of borrowing/lending money increases the likelihood of having the relationship of borrowing/lending rice by 49.8%; to $1.9+49.8=51.7\%$. (Still don't go the temple together)

3.3 For a pair of households such that “templecompany_hh = 1” and “lendmoney_hh = 1”, what is the predicted/fitted value (probability) that they also have the relation “keroricego_hh_fit”?

(a) First calculate the fitted value based on what you answered in 3.1.

(b) Verify your answer using the following code in R:

```
keroricego_hh_fit <- predict(lm3)
which(v1hh$templecompany_hh == 1 & v1hh$lendmoney_hh == 1)
keroricego_hh_fit[XXX]
```

(a) When templecompany_hh = 1 and lendmoney_hh = 1, we plug them into the formula:

```
keroricego_hh= 0.019+0.124 templecompan
y_hh+ 0.498 lendmoney_hh
```

Then we get: keroricego_hh= 0.019+0.124+0.498=0.641

So the predicted/fitted value (probability) that they also have the relation “keroricego_hh_fit” is 64.1%.

(b)

```
> keroricego_hh_fit <- predict(lm3)
> which(v1hh$templecompany_hh == 1 & v1hh$lendmoney_hh == 1)
[1] 245 2003 3543 4144 4165 4185 4743 4759 5093 5170 5173 5413 5418
[14] 5512

> keroricego_hh_fit[245]
      245
0.6413163
> keroricego_hh_fit[2003]
     2003
0.6413163
> keroricego_hh_fit[4185]
     4185
0.6413163
> keroricego_hh_fit[5512]
     5512
0.6413163
```

We get when mpid_hh=245 2003 3543 4144 4165 4185 4743 4759 5093 5170 5173 5413 5418 5512, “templecompany_hh = 1” and “lendmoney_hh = 1”, the probability of each one is 64.1%, which fits the answer in 3.2 question.