

A Brief Survey of Multi-Processor Scheduling For Hard Real-Time Systems

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Abstract

In class, both of scheduling algorithms [1] and priority inheritance protocols [2] in the context of a single processor were examined in details. Nevertheless, the emergence and popularity of distributed computing system gave rise to the need to solve multi-processor scheduling and priority inheritance problems. As the supplementary study, this paper surveys existing scheduling algorithms in the context of multiple processors. The very first section outlines the background of multi-processor scheduling problems, as well as system models, terminology, and the metrics of scheduling algorithms. After that, partitioned scheduling and global scheduling, as the primary objects of our research, will be fully explored. Moreover, we will also give brief sketch to the hybrid approaches of partitioned scheduling and global scheduling.

Keywords: System, Scheduling Algorithm, Task Management

1. Introduction

1.1. Problem Defintion

1.2. Preview Of Related works

1.3. Paper Organization

0. Background and introduction

1. System Models

2. Partitioned Scheduling

3. Global Scheduling

4. Hybrid Approach

5. Conclusion and Discussion

11 **2. System Models**

12 *2.1.*

13 **3. Partitioned Scheduling**

14 In this section, we will review some partitioned approaches to multipro-
15 cessor real-time scheduling.

16 *3.1. Characteristic of Partitioned Scheduling*

17 *3.2. RMNF*

18 *3.3. RMFF*

19 *3.4. EDF-FF*

20 *3.5. EDF-BF*

21 *3.6. Comparision*

22 4. Global Scheduling

23 In this section, we will review some global approaches to multiprocessor
24 real-time scheduling.

25 4.1. Overview

26 The global scheduling paradigm has advantages over the partitioned ap-
27 proach. First of all, if tasks can join and leave the system at run-time,
28 then it may be necessary to reallocate tasks to processors in the partitioned
29 approach. In addition, the partitioned approach cannot produce optimal
30 real-time schedules – one that meets all task deadlines when task utiliza-
31 tion demand does not exceed the total processor capacity – for periodic task
32 sets, since the partitioning problem is analogous to the bin-packing problem
33 which is known to be NP-hard in the strong sense. On top of that, in some
34 embedded processor architectures with no cache and simpler structures, the
35 overhead of migration has a lower impact on the performance. Finally, global
36 scheduling can theoretically contribute to an increased understanding of the
37 properties and behaviors of real-time scheduling algorithms for multiproces-
38 sors.

39 The global scheduling paradigm has also several disadvantages, compared
40 with the partitioned approach. Firstly, global scheduling strategies are much
41 more complicated to implement than partitioned scheduling. In other words,
42 for the partitioned approach, once a set of tasks are allocated to proces-
43 sors, the multiprocessor real-time scheduling problem becomes a collection
44 of single processor real-time scheduling problems. The ease of programming
45 partitioned scheduling is obvious since the single processor scheduling prob-
46 lem has already been well-studied and optimal algorithms with easy imple-
47 mentations already exist. Secondly, migrating tasks at run-time means more
48 runtime overhead in that migrating tasks may suffer cache misses on the
49 newly assigned processor. If the task set is fixed and known in advanced, it
50 is obvious that the partitioned approach provides more appropriate solutions.

51 Although there are various categories of global scheduling algorithms,
52 the focus of this paper is on the Global Dynamic Priority Scheduling. In the
53 following subsection, it will be chacterized in details.

54 4.2. Global Dynamic Priority Scheduling

55 In this subsection, we will present our in-depth exploration to the track
56 of global dynamic priority scheduling algorithm. To the best of our knowl-
57 edge, a number of global dynamic priority scheduling algorithms are optimal

for periodic tasksets with explicit or implicit deadlines. For example, Proportionate Fairness algorithm and its variants including PD, PD², ERFair, BF, SA [3], and LLREF [4] as well, are all optimal for offline environment. Nevertheless, no algorithms until now are optimal to cope with online preemptive scheduling problem, where tasksets are sporadic and multi-processor environments are enforced. On the other hand, despite of its optimality and dominance in theory, the usage of global dynamic priority algorithms are limited in practice. This is because the existence of frequent preemption and migration between tasks gives rise to excessive overheads in potential.

The following part of this subsection will provide brief summary of three classic global dynamic priority scheduling algorithms. They are respectively Proportionate Fairness Algorithm (PFair), and Largest Local Remaining Execution First (LLREF).

4.2.1. *PFair*

Baruah et al [5] introduced Proportionate Fairness Algorithm. The Pfair class of algorithms that allow full migration and fully dynamic priorities have been shown to be theoretically optimal – i.e., they achieve a schedulable utilization bound (below which all tasks meet their deadlines) that equals the total capacity of all processors.

4.2.2. *LLREF*

LLREF was firstly introduced by Cho et al [4]. LLREF was designed based on a novel abstraction for reasoning over task execution behavior on multiprocessors, called Time and Local Execution Time Domain Plane (T-L Plane).

4.3. *Summary*

5. Hybrid Approaches

6. Conclusions

85 **References**

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