

A Brief Survey of Multi-Processor Scheduling For Hard Real-Time Systems

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Abstract

In class, both of scheduling algorithms [1] and priority inheritance protocols [2] in the context of a single processor were examined in details. Nevertheless, the emergence and popularity of distributed computing system gave rise to the need to solve multi-processor scheduling and priority inheritance problems. As the supplementary study, this paper surveys existing scheduling algorithms in the context of multiple processors. The very first section outlines the background of multi-processor scheduling problems, as well as system models, terminology, and the metrics of scheduling algorithms. After that, partitioned scheduling and global scheduling, as the primary objects of our research, will be fully explored. Moreover, we will also give brief sketch to the hybrid approaches of partitioned scheduling and global scheduling.

Keywords: System, Scheduling Algorithm, Task Management

1. Introduction

1.1. Problem Defintion

1.2. Preview Of Related works

1.3. Paper Organization

0. Background and introduction

1. System Models

2. Partitioned Scheduling

3. Global Scheduling

4. Hybrid Approach

5. Conclusion and Discussion

11 **2. System Models**

12 *2.1.*

13 **3. Partitioned Scheduling**

14 In this section, we will review some partitioned approaches to multipro-
15 cessor real-time scheduling.

16 *3.1. Characteristic of Partitioned Scheduling*

17 *3.2. RMNF*

18 *3.3. RMFF*

19 *3.4. EDF-FF*

20 *3.5. EDF-BF*

21 *3.6. Comparision*

22 4. Global Scheduling

23 In this section, we will dive into another branch of scheduling strategies
24 – global approaches to multiprocessor real-time scheduling.

25 4.1. Overview

26 Global scheduling algorithms, as its name suggests, globally schedules
27 any feasible periodic task set. In contrast to partitioned scheduling, global
28 scheduling schedules jobs and tasks in one single shared queue instead of
29 multiple local, dedicated queues. By this means, the automatic load balancing
30 and lower average response time can be achieved by global approaches.
31 In addition to this, global approaches also take advantages of the simpler
32 implementations and the existence of optimal schedulers.

33 Global scheduling strategies include Global Fixed-Job-Priority Scheduling,
34 Global Fixed-Task-Priority Scheduling, and Global Dynamic Priority
35 Scheduling. Although there are various categories of global scheduling algorithms,
36 the focus of this paper is on the Global Dynamic Priority Scheduling.
37 In the following subsection, it will be characterized in details.

38 4.2. Global Dynamic Priority Scheduling

39 In this subsection, we will present our in-depth exploration to the track
40 of global dynamic priority scheduling algorithm. To the best of our knowledge,
41 a number of global dynamic priority scheduling algorithms are optimal
42 for periodic tasksets with explicit or implicit deadlines. For example, Proportionate
43 Fairness algorithm and its variants including PD, PD², ERFair,
44 BF, SA [3], and LLREF [4] as well, are all optimal for offline environment.
45 Nevertheless, no algorithms until now are optimal to cope with online preemptive
46 scheduling problem, where tasksets are sporadic and multi-processor environments
47 are enforced. On the other hand, despite of its optimality and dominance in theory,
48 the usage of global dynamic priority algorithms are limited in practice. This is
49 because the existence of frequent preemption and migration between tasks gives
50 rise to excessive overheads in potential.

51 The following part of this subsection will provide brief summary of three
52 classic global dynamic priority scheduling algorithms. They are respectively
53 Proportionate Fairness Algorithm (PFair), and Largest Local Remaining Execution
54 First (LLREF).

4.2.1. PFair

Baruah et al [5] introduced Proportionate Fairness Algorithm. The Pfair class of algorithms that allow full migration and fully dynamic priorities have been shown to be theoretically optimal – i.e., they achieve a schedulable utilization bound (below which all tasks meet their deadlines) that equals the total capacity of all processors. Here are some fundamental principles of Proportionate Fairness algorithms:

1. Timeline is divided into equal length slots.
2. Task period and execution time are multiples of the slot size.
3. Each task receives amount of slots proportional to its task utilization.

The essential part of PFair algorithms is the quantum-based optimization defined over the lag of each task $lag(\tau_i, t)$, with the goal of minimizing the maximum lags of all tasks $\max_t |lag(\tau_i, t)|$.

$$\underbrace{lag(\tau_i, t)}_{error} = \underbrace{t \cdot \left(\frac{c_i}{T_i}\right)}_{fluid\ execution\ in[0,t)} - \underbrace{allocated(\tau_i, t)}_{real\ execution\ in[0,t)} \quad (1)$$

The generation of an optimal schedule is based on the above definition of lag . PFair algorithm does execute all urgent tasks with $lag(\tau_i, t) > 0$ and $lag(\tau_i, t + 1) \geq 0$ if τ_i executes. On top of that, PFair algorithm does not execute tnegru tasks, for which $lag(\tau_i, t) < 0$ and $lag(\tau_i, t + 1) \leq 0$ if τ_i does not execute. Besides, for other tasks, only those that have the least t such that $lag(\tau_i, t) > 0$ are executed.

The PFair algorithm will assign priorities to tasks at every time slot, which indicated itself as one of job-level dynamic priority scheduling policies. However, this characteristic gives rise to some issues, for example, frequent preemptions and frequent migrations.

Proportionate Fairness algorithm, as a strong candidate for solving resource allocation problems, has wide variety of interesting applications and powerful theoretical support. For instances, Kelly et al [6] presented its application on the problem of rate control for communication networks. Application of PFair algorithm on LANs and hoc networks was fulfilled by Jiang et al [7]. Besides, Bonald’s paper [8] provides in-depth queueing analysis over proportionate fairness as well as max-min fairness and balanced fairness.

85 4.2.2. *LLREF*

86 LLREF was firstly introduced by Cho et al [4]. Similar to PFair class
87 of algorithms, LLREF is also based on the fluid scheduling model, where
88 each task executes at a constant rate at all times. The principal idea of
89 LLREF is that given M processors, M largest local remaining execution
90 time tasks are selected first for every secondary event. This is also called
91 the LLREF scheduling policy. To reason over task execution behavior on
92 multiprocessors, a novel abstraction called Time and Local Execution Time
93 Domain Plane (T-L Plane) was developed.

94 This algorithm divides the schedule into Time and Local execution time
95 planes (TL-planes), which are determined by task deadlines. The algorithm
96 schedules tasks by creating smaller local jobs within each TL-plane. The
97 only parameters considered by the algorithm during a TL-plane are the pa-
98 rameters of the local jobs. When a TL-plane completes, the next TL-plane
99 is started. The duration of each TL-plane is the amount of time between
100 consecutive deadlines.

101 4.3. *Summary*

102 The global scheduling paradigm has advantages over the partitioned ap-
103 proach. First of all, if tasks can join and leave the system at run-time,
104 then it may be necessary to reallocate tasks to processors in the partitioned
105 approach. In addition, the partitioned approach cannot produce optimal
106 real-time schedules – one that meets all task deadlines when task utiliza-
107 tion demand does not exceed the total processor capacity – for periodic task
108 sets, since the partitioning problem is analogous to the bin-packing problem
109 which is known to be NP-hard in the strong sense. On top of that, in some
110 embedded processor architectures with no cache and simpler structures, the
111 overhead of migration has a lower impact on the performance. Finally, global
112 scheduling can theoretically contribute to an increased understanding of the
113 properties and behaviors of real-time scheduling algorithms for multiproces-
114 sors.

115 However, the global scheduling paradigm has also several disadvantages.
116 Firstly, global scheduling strategies are much more complicated to implement
117 than partitioned scheduling. In other words, for the partitioned approach,
118 once a set of tasks are allocated to processors, the multiprocessor real-time
119 scheduling problem becomes a collection of single processor real-time schedul-
120 ing problems. The ease of programming partitioned scheduling is obvious
121 since the single processor scheduling problem has already been well-studied

122 and optimal algorithms with easy implementations already exist. Secondly,
123 migrating tasks at run-time means more runtime overhead in that migrating
124 tasks may suffer cache misses on the newly assigned processor. If the task set
125 is fixed and known in advanced, it is obvious that the partitioned approach
126 provides more appropriate solutions.

127 **5. Hybrid Approaches**

128 **6. Conclusions**

129 References

- 130 [1] C. L. Liu, J. W. Layland, Scheduling algorithms for multiprogramming
131 in a hard-real-time environment, *Journal of the ACM (JACM)* 20 (1973)
132 46–61.
- 133 [2] L. Sha, R. Rajkumar, J. P. Lehoczky, Priority inheritance protocols: An
134 approach to real-time synchronization, *Computers, IEEE Transactions*
135 on 39 (1990) 1175–1185.
- 136 [3] A. Khemka, R. Shyamasundar, An optimal multiprocessor real-time
137 scheduling algorithm, *Journal of parallel and distributed computing* 43
138 (1997) 37–45.
- 139 [4] H. Cho, B. Ravindran, E. D. Jensen, An optimal real-time scheduling
140 algorithm for multiprocessors, in: *Real-Time Systems Symposium, 2006.*
141 *RTSS’06. 27th IEEE International*, IEEE, pp. 101–110.
- 142 [5] S. K. Baruah, N. K. Cohen, C. G. Plaxton, D. A. Varvel, Proportionate
143 progress: A notion of fairness in resource allocation, *Algorithmica* 15
144 (1996) 600–625.
- 145 [6] F. P. Kelly, A. K. Maulloo, D. K. Tan, Rate control for communication
146 networks: shadow prices, proportional fairness and stability, *Journal of*
147 *the Operational Research society* (1998) 237–252.
- 148 [7] L. B. Jiang, S. C. Liew, Proportional fairness in wireless lans and ad
149 hoc networks, in: *Wireless Communications and Networking Conference,*
150 *2005 IEEE*, volume 3, IEEE, pp. 1551–1556.
- 151 [8] T. Bonald, L. Massoulié, A. Proutiere, J. Virtamo, A queueing analysis of
152 max-min fairness, proportional fairness and balanced fairness, *Queueing*
153 *systems* 53 (2006) 65–84.